Strassen's Algorithm Solution

$$T(n) = 7T\left(\frac{n}{2}\right) + n^{2}$$

$$= 7\left(7T\left(\frac{n}{2^{2}}\right) + \left(\frac{n}{2}\right)^{2}\right) + n^{2}$$

$$= 7\left(7^{m}T\left(\frac{n}{2^{m}}\right) + \sum_{k=1}^{m} \left(\frac{n}{2^{k}}\right)^{2}\right) + n^{2}$$

$$\in \Theta\left(7^{\log_{2} n} + n^{2}\right)$$

$$= \Theta\left(\left(2^{\log_{2} 7}\right)^{\log_{2} n} + n^{2}\right)$$

$$= \Theta\left(n^{\log_{2} 7} + n^{2}\right)$$

$$\approx \Theta(n^{2.8})$$

Note: log₂7 approximately 2.8.