

"a **proposition** is a statement"
 Conjunction (\wedge): And, but, plus, as well, too : TFFF

Disjunction (\vee): or : TTTF

Conditional implication (\rightarrow): if, in the case that, given that, provided that, so long as, when, where, whenever, should : TFFT

"if": "We will contact you if there is an issue with the payment" is $I \rightarrow P$

"only if": "We will contact you only if the case that there is an issue with the payment" is $C \rightarrow I$

Biconditional Implication (\leftrightarrow): if and only if : TFFT

"Sufficient": "Matching fingerprints are a sufficient condition to establish the presence of the suspect in the room." is $F \rightarrow R$

"Necessary": "Being plugged in is a necessary condition for the device to be on." $O \rightarrow P$

"Necessary and Sufficient": \leftrightarrow

A formula of propositional logic is a **contradiction** if and only if no truth assignment satisfies it.
 A formula of propositional logic is **satisfiable** if and only if there is at least one truth assignment that satisfies it.
 A formula of propositional logic is a **tautology** if and only if it is satisfied by every truth assignment. To prove that a formula is a tautology using tables, you must give every row of the table.
 A formula of propositional logic that has at least one satisfying assignment and at least one non-satisfying assignment is called a **contingency**. To prove that a formula is a contingency, you must give two truth assignments: one satisfying, and one not satisfying. To prove that a formula is not a contingency using tables, you must give an entire table, showing either that every assignment satisfies the formula or no assignment does.

A set of formulas is **consistent** if and only if there exists at least one truth assignment that satisfies all of the formulas in the set. An argument is **valid** if and only if every truth assignment that satisfies all the premises also satisfies the conclusion.

Commutative Laws
 $p \wedge q \equiv q \wedge p$ (\wedge -Commutative)
 $p \vee q \equiv q \vee p$ (\vee -Commutative)

Association Laws
 $p \wedge (q \wedge r) \equiv (p \wedge q) \wedge r$
 $p \vee (q \vee r) \equiv (p \vee q) \vee r$

DeMorgan's Laws
 $\neg(p \wedge q) \equiv \neg p \vee \neg q$
 $\neg(p \vee q) \equiv \neg p \wedge \neg q$

Distributive Laws
 $p \wedge (q \vee r) \equiv (p \wedge q) \vee (p \wedge r)$
 $p \vee (q \wedge r) \equiv (p \vee q) \wedge (p \vee r)$

Idempotence Laws
 $p \wedge p \equiv p$
 $p \vee p \equiv p$

Absorption
 $p \wedge (q \vee p) \equiv p$

Implication or Material Implication
 $p \rightarrow q \equiv \neg p \vee q$

Bi-Implication
 $p \leftrightarrow q \equiv (p \wedge q) \vee (\neg p \wedge \neg q)$

Exclusive Disjunction
 $p \oplus q \equiv (p \wedge \neg q) \vee (\neg p \wedge q)$

Setlist Notation
 $A = \{0, 1, 2, 3\}$

Set builder notation
 $S = \{n^2 \mid n \text{ is an integer} \wedge n \geq 20 \wedge n \leq 500\}$

Special Sets of Numbers

Natural Numbers: $\mathbb{N} = \{0, 1, 2, 3, \dots\}$

Integers: $\mathbb{Z} = \{\dots, -2, -1, 0, 1, 2, \dots\}$

Rational Numbers: $\mathbb{Q} = \{\frac{p}{q} \mid p \in \mathbb{Z} \wedge q \in \mathbb{Z} \wedge q \neq 0\}$
 = any # that can be written as a ratio/fraction/quotient of integers

The universal set (or the universe) is the set of all the things we currently care about. We often use a cursive capital \mathbb{U} for the universe.