

Homework 1  
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01/10/2019

Question 1

- A) not a proposition
- B) proposition: false. The lottery, while usually requires a purchased ticket, could be won by having a special sort of promotion not requiring purchase.
- C) not a proposition
- D) not a proposition
- E) not a proposition
- F) proposition: false. We can measure the height of humans and we have demonstrated that there exist some that are greater than six feet tall.
- G) proposition: false. This is false because questions are not propositions due to the fact they aren't stating an opinion but inquiring about a topic.
- H) not a proposition
- I) proposition: false. Six multiplied by nine is fifty four.
- J) not a proposition
- K) proposition: true. It is true because  $1 + 1 = 2$ , which makes the greater than or equal to equality true as well.
- L) proposition: false.  $1 + 1$  is equal to 2, and not 5.

Question 2

- A) I am allergic to penicillin; therefore, taking penicillin may cause a rash. (a note I wrote during a Philmont trip in 2016, for medical records)
- B) I don't know if I left my keys at home. (My mom) - She was looking for her keys and couldn't find them.

Question 3

- A)  $R \wedge \neg Q$
- B)  $Q \rightarrow R$
- C)  $R \rightarrow Q$
- D)  $R \leftrightarrow Q$
- E)  $R \leftrightarrow (Q \vee P)$
- F)  $P \wedge Q \wedge R$
- G)  $R \rightarrow P$
- H)  $R \rightarrow P$
- I)  $((P \wedge \neg Q)) \wedge R$

Question 4

A) R: The suspect wore gloves. P: He didn't touch it

$$R \oplus \neg P$$

B) R: Eat my tie. P: Cubs win the World Series.

$$P \rightarrow R$$

C) R: it smelled funny. P: Ate it.

$$R \wedge P$$

D) R: The people gave up their arms. P: Tyrant resigns. Q: Get money back money back.

$$R \rightarrow (P \wedge Q)$$

E) R: Prizes awarded. P: sufficient number of entries received.

$$P \rightarrow R$$

F) R: absence of antibodies in body. P: are susceptible to infection.

$$R \rightarrow \neg P$$

G) R: Participants were timed on this task. P: finished in less than 8 minutes.

$$\neg R \wedge P$$

H) R: Holds black ink cartridge. P: Holds color cartridge.

$$R \oplus P$$

I) R: person has a real desire to want to change. P: Puts forth real effort to make those changes. X: Changes come about.

$$(R \wedge P) \rightarrow X$$

J) R: Lyapunov function exists. P: the system is stable.

$$R \leftrightarrow P$$

K) R: Regulation applies. P: both houses vote to impose regulation.

$$\neg P \vee \neg R$$

#### Question 5

A) I entered the lottery or I won the jackpot.

IB) f I won the jackpot then I entered the lottery.

C) I won the jackpot if and only if I entered the lottery.

D) If I didn't enter the lottery then I didn't win the jackpot.

E) I did not enter the lottery and I did not win the jackpot.

F) I did not enter the lottery, or I entered the lottery and won the jackpot.

Question 6

- A) I would first prove that either  $p$  is true or  $q$  is true, or that both  $p$  and  $q$  is true.
- B) I would first prove that  $p$  is true then prove that  $q$  is also true, or I could simply prove that  $p$  is true and that  $q$  is not true, which would leave the only conditional claim that is false. From that, we know all other possibilities lead to true.
- C) I would prove that not  $p$  is true and demonstrate that  $p$  is false, or vice versa.
- D) I would prove that  $p$  is true and  $q$  is true, or that  $p$  is false and  $q$  is false, and demonstrate that all other condition for  $p$  and  $q$  is not true.
- E) I would prove that  $p$  is true and  $q$  is false, or that  $p$  is false and  $q$  is true, or that  $p$  is false and  $q$  is false.

Question 7 (Bonus)

The TV was on, and the TV was plugged in.