Mini-Homework 3

Will Boland

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Claim: This is valid $\neg \neg A \land \neg B, \, A \to C \vdash C \land \neg B$

Proof

Assume $\neg\neg A \land \neg B$ and $A \to C$. Since $\neg\neg A \land \neg B$,we know $\neg\neg A$ and $\neg B$ (\land -elimination) From $\neg\neg A$, we get A (Double negation) Applying $A \to C$ to A gives us C (Application, or \rightarrow -elim) Because C and $\neg B$, C $\land \neg B$. (\land -introduction) \square