

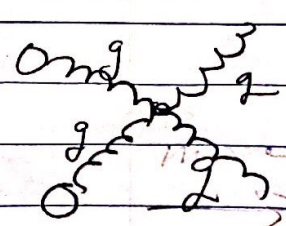
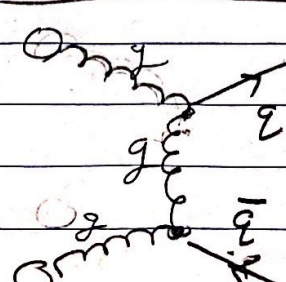
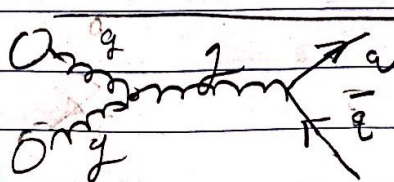
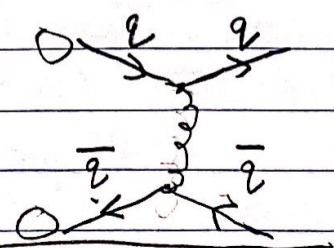
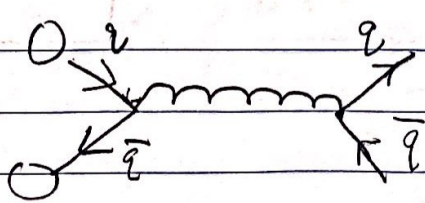
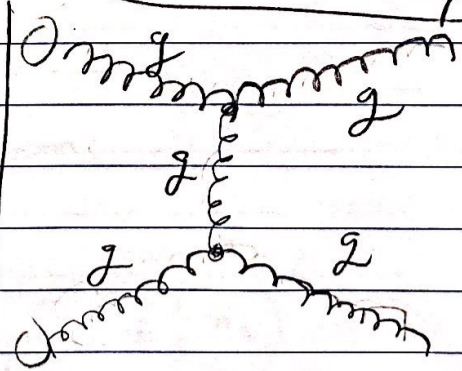
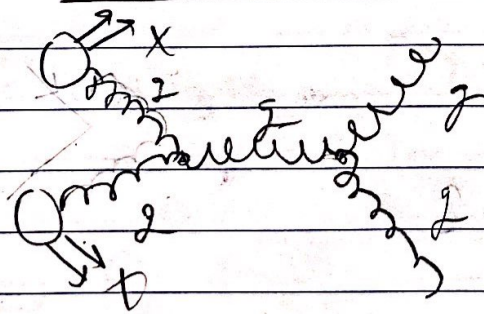
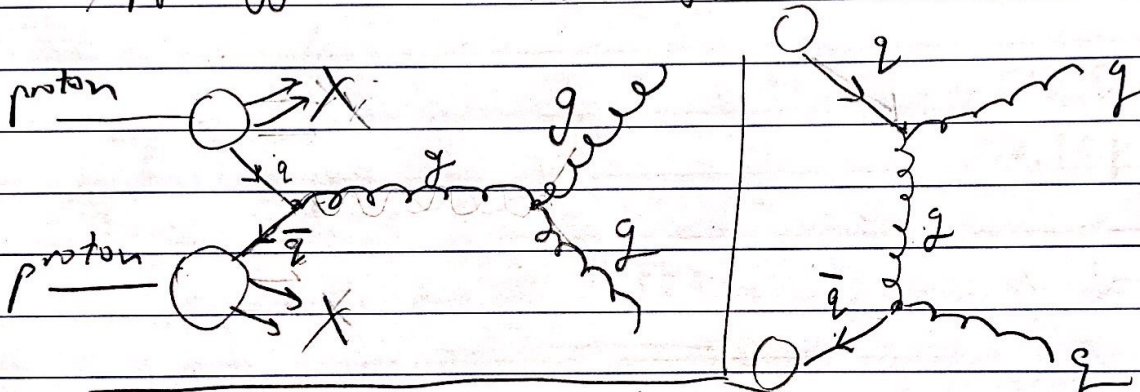
1) $pp \rightarrow \mu^+ \mu^- X$, em interaction

↳ cross section prop. to α^2

$pp \rightarrow jj X$: strong interaction, $\sigma \propto \alpha_s^2$ (lowest order)

Draw all Feynman Diagrams that contribute to lowest order
 ↳ quark from 1 proton and 1 antiquark from other term

$$pp \rightarrow jj X \Leftrightarrow q\bar{q} \rightarrow jj X$$



$$2) \Gamma(2\gamma) = \frac{\alpha^5 m_e}{2}, \quad \Gamma(3\gamma) = \frac{2(\pi^2 - 9)}{9\pi} \alpha^6 m_e$$

a) J/ψ decays through 3 gluons.

$$\Gamma = 87 \text{ keV} \quad \alpha \rightarrow \frac{4}{3} \alpha_s$$

$$\Gamma(3g) = \frac{2(\pi^2 - 9)}{9\pi} \left(\frac{4}{3} \alpha_s\right)^6 m_e = 87 \text{ keV}$$

$$\alpha_s^6 = \left(\frac{3}{4}\right)^6 \frac{9\pi}{2(\pi^2 - 9)m_e} \cdot 87 \text{ keV}$$

$$\alpha_s^6 = 0.4923$$

$$\hookrightarrow m_e = 0.510998 \text{ MeV} \\ = 510.998 \text{ KeV}$$

$$\therefore \boxed{\alpha_s \approx 0.889} \quad (\text{unitless}) \checkmark$$

b) estimate $\frac{J/\psi \rightarrow \gamma + \text{hadrons}}{J/\psi \rightarrow \text{hadrons}}$

$$\begin{aligned} \rightarrow \frac{\Gamma_{\alpha_s}(3\gamma)}{\Gamma_{\alpha_s}(2\gamma)} &= \frac{2(\pi^2 - 9)}{9\pi} \left(\frac{4}{3} \alpha_s\right)^6 m_e \left(\frac{2}{\left(\frac{4}{3} \alpha_s\right)^5 m_e} \right) \\ &= \frac{4}{9\pi} (\pi^2 - 9) \left(\frac{4}{3} \alpha_s\right) \end{aligned}$$

$$= \boxed{0.14577}$$