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Problem Set 12 problems

Question 1: Feynman diagrams with $\gamma,\,W$ and Z bosons (30 points)

Learning objectives

In this question you will:

• Apply knowlege of Feynman diagrams involved electroweak bosons to various physical processes

Draw the lowest order Feynman diagram or diagrams for each of the following processes

1a.

$$e^+e^-
ightarrow
u_ au \overline{
u}_ au$$

Write your answer here

1b.

$$\mu^+\mu^- o u\overline{u}$$
 where u is an up quark

Write your answer here

1c.

$$\overline{
u}_{\mu} + e^{-}
ightarrow \overline{
u}_{\mu} + e^{-}$$

Problem Set 12 problems

Write your answer here

1d.

$$\overline{
u}_e + e^-
ightarrow \overline{
u}_e + e^-$$

Write your answer here

1e.

 $p\overline{p} o W^+W^-$ (consider only the valence quarks in the proton and anti-proton)

Write your answer here

Question 2: Mixing in the K and B systems (30 points)

Learning objectives

In this question you will:

ullet Review the formulae for flavor mixing and see how the mixing phenomenology depends on $\Delta\Gamma$ and Δm

The phenomenon if K^0 - \overline{K}^0 mixing was discussed in Lecture 22 and in Thomson Section 14.5. If a K^0 is produced via the strong interactions at t=0 the probabilities of the state being observed as a K^0 or as a \overline{K}^0 at a later time t are giving by the expressions

$$egin{array}{lll} P(K^0_{t=0} o K^0) &=& rac{1}{4}ig[e^{-\Gamma_1 t} + e^{-\Gamma_2 t} + 2e^{-(\Gamma_1 + \Gamma_2)t/2}\cos(\Delta m t)ig] \ P(K^0_{t=0} o \overline{K}^0) &=& rac{1}{4}ig[e^{-\Gamma_1 t} + e^{-\Gamma_2 t} - 2e^{-(\Gamma_1 + \Gamma_2)t/2}\cos(\Delta m t)ig] \end{array}$$

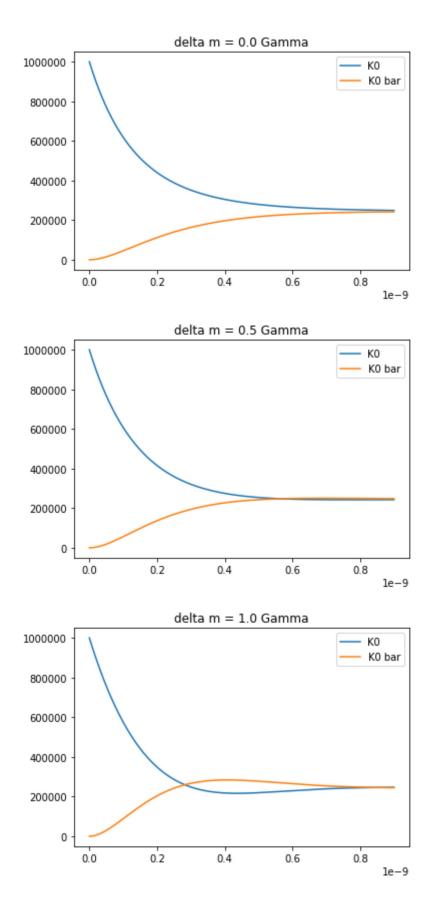
where Γ_1 and Γ_2 are the inverse lifetimes of the K_S and K_L states and Δm is the mass difference between the states. Note: for this problem we will ignore CP violation so that $|K_S>\equiv |K_1>$ and $|K_L>\equiv |K_2>$

2a.

If a beam of 1 million K^0 is produced, using the measured values of the K_S and K_L lifetimes plot the predicted number of K^0 and of \overline{K}^0 that would be present in the beam as a function of time for $0 < t < \frac{10}{\Gamma_1}$ if the value of Δm were 0, 0.5Γ or Γ .

```
In [8]: import numpy as np
import matplotlib.pyplot as plt
```

```
In [9]: num K0 = 10**6
        #from slides:
        tau s = 0.9*10**(-10) #sec
        tau p = 0.5*10**(-7) #sec
        gamma1 = 1/tau s
        gamma2 = 1/tau p
        gamma = (gamma1 + gamma2)/2
        deltam = np.array([0, 0.5, 1])*gamma
        times = np.linspace(0, 10/gamma1, 1000)
        def KtoK(t, g1, g2, dm, bar = False):
            a = np.exp(-1*g1*t)
            b = np.exp(-1*g2*t)
            c = 2*np.exp(-1*(g1 + g2)*t/2)*np.cos(dm*t)
            if bar == True:
                c *= -1
            return (1/4) * (a + b + c)
        for i in range(len(deltam)):
            KOs = KtoK(times, gamma1, gamma2, deltam[i])*num KO
            K0bars = KtoK(times, gamma1, gamma2, deltam[i], bar = True)*num K0
            titlestr = str(i*0.5) + " Gamma"
            plt.figure()
            plt.title("delta m = " + titlestr)
            plt.plot(times, KOs, label = "KO")
            plt.plot(times, K0bars, label = "K0 bar")
            plt.legend()
        plt.show()
```



2b.

Remake the plot above but plotting the predicted number of K_1 and K_2 in the beam instead of K_0 and \overline{K}_0

```
In [10]: # by definition:

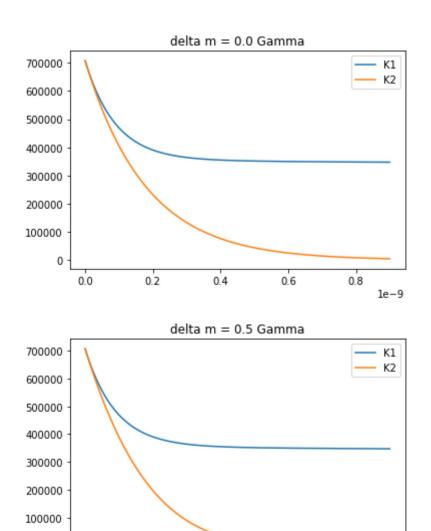
for i in range(len(deltam)):
    K0s = KtoK(times, gamma1, gamma2, deltam[i])*num_K0
    K0bars = KtoK(times, gamma1, gamma2, deltam[i], bar = True)*num_K0

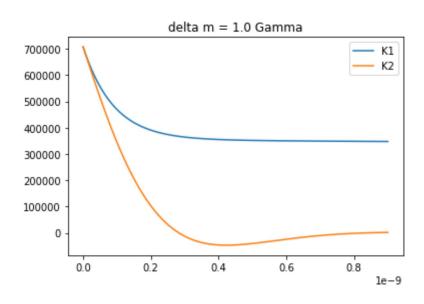
    K1s = (1/np.sqrt(2))*(K0s + K0bars)
    K2s = (1/np.sqrt(2))*(K0s - K0bars)

    titlestr = str(i*0.5) + " Gamma"

    plt.figure()
    plt.title("delta m = " + titlestr)
    plt.plot(times, K1s, label = "K1")
    plt.plot(times, K2s, label = "K2")
    plt.legend()

plt.show()
```





0.4

0.6

0.8

le-9

0.2

2c.

0

0.0

The measured value of the mass difference is

$$\Delta m = 3.383 imes 10^{-15} \; \mathrm{GeV}$$

remake the plots above for this value

```
In [20]: given_dm = 3.383*(10**(-15)) # Gev

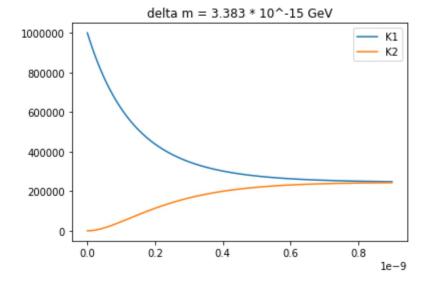
### convert to freq
h = 4.135*(10**(-15)) #eV*s
hGeV = h*(10**(-9)) # GeV*s

converted_dm = given_dm/hGeV #s

K1s = KtoK(times, gamma1, gamma2, converted_dm)*num_K0
K2s = KtoK(times, gamma1, gamma2, converted_dm, bar = True)*num_K0

titlestr = "3.383 * 10^-15 GeV"

plt.figure()
plt.title("delta m = " + titlestr)
plt.plot(times, K1s, label = "K1")
plt.plot(times, K2s, label = "K2")
plt.legend()
plt.show()
```

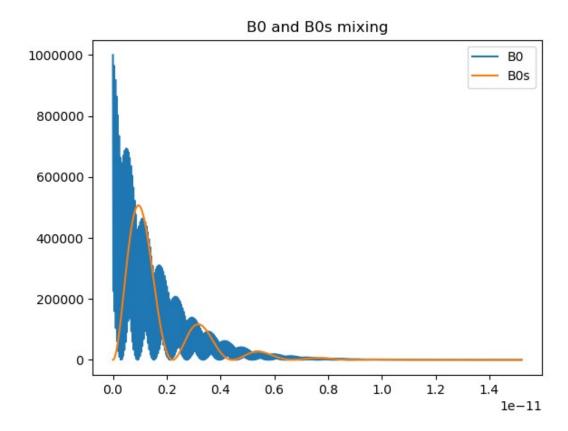


2d

The same expressions used for K^0 mixing can be applied to the B^0 and to the B_s . Use the PDG to find the values of Γ_1 , Γ_2 and Δm for the B^0 and the B_s . Using these numbers repeat 2c for these two neutral mesons.

```
In [26]: %matplotlib notebook
```

```
In [28]: \# convention: 1 = B0, 2 = B0s
         m B0 = 5279.61 \# MeV
         m \ BOs = 5366.79 \# MeV
         tau B0 = 1.520*10**(-12) #s
         tau B0s = 1.510*10**(-12) #s
         gammaB0 = 1/tau B0
         gammaB0s = 1/tau B0s
         deltam B = (m B0 - m B0s)/2
         deltam B0s = 1.1688*10**(-8) #MeV
         deltam B0 = 0.32 \ \#MeV
         hMeV = h*(10**(-6)) \#MeV*s
         deltam B0s /= hMeV #s
         deltam B0 /= hMeV \#s
         new times = np.linspace(0, 10/gammaB0, 1000)
         B0 = KtoK(new times, gammaB0, gammaB0s, deltam B0)*num K0
         B0s = KtoK(new times, gammaB0, gammaB0s, deltam B0s, bar = True)*num K0
         plt.figure()
         plt.title("B0 and B0s mixing")
         plt.plot(new times, B0, label = 'B0')
         plt.plot(new times, B0s, label = 'B0s')
         plt.legend()
         plt.show()
```



In []: