

HW7  
FE620

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11) No-arb forward:  $F^* = S_0 e^{rT} = 5050 \cdot e^{0.08 \cdot 1}$   
 $F^* \approx 5230.88$

i)  $5200 < 5230.88 \rightarrow$  underpriced  $\rightarrow$  arb ✓

Arb:

1) short sell 1 oz gold, get +5050

2) Invest 5050 @  $r$  for 1 yr  $\rightarrow$  grows to  $5050 e^{0.08}$

3) Go long 1Y forward @  $F_0 = 5200$

4) @ maturity use forward to buy 1 oz for 5200,

return to cover short

Profit:  $\Pi = 5230.88 - 5200 = 30.88$

ii)  $5300 > 5230.88 \Rightarrow$  forward overpriced

Arb: 1) Borrow 5050 @  $r$

2) Buy 1 unit gold

3) short forward @ 5300

4) Deliver gold @ maturity / repay loan

Cash Flow: Forward = 5300, Loan Repayment =  $5050 e^{0.08} = 5230.88$

Profit:  $\Pi = 5300 - 5230.88 = 69.12$

1-2) Nominal = 3.25%,  $m = 2$

EAR =  $(1 + 0.0325/2)^2 - 1 = 0.03276406$

i)  $3.276\%$

ii)  $(1 + R_y/4)^4 = (1.01625)^2 \Rightarrow (1.01625)^{1/2} = \sqrt{1.01625}$

$R_y = 4((1.01625)^{1/2} - 1) \neq 3.2369\%$

iii)  $R_C = \min(1 + R_m/m)$

$R_C = 2 \ln(1 + 0.0325/2) = 2 \ln(1.01625) \approx 3.224\%$

$$B_0 = 10000$$

$$APR = 17.15\% = 0.1715$$

Daily

(1.3)

$$r_d = 0.1715 / 365 = 0.000469863013699$$

$$B_{30} = 10000 \left( 1 + \frac{0.1715}{365} \right)^{30} \approx 10141.9$$

$$\text{Interest} = 10141.9 - 10000 = 141.92$$

(1.4) ?

1)  $B_1 = 24.5\% \text{ semiannually}$

Cashflows:

$$t=0.5 = 2.5 \text{ (} R = 3\% \text{)}$$

$$t=1.0 = 2.5 \text{ (} R = 3\% \text{)}$$

$$t=1.5 = 2.5 \text{ (} R = 3.5\% \text{)}$$

$$t=2.0 = 102.5 \text{ (} R = 3.5\% \text{)}$$

Discount factors:

$$D(0.5) = e^{-0.03(0.5)}$$

$$D(1) = e^{-0.03}$$

$$D(1.5) = e^{-0.035(1.5)}$$

$$D(2) = e^{-0.035(2)}$$

$$\text{Price: } B_1 = 2.5D(0.5) + 2.5D(1) + 2.5D(1.5) + 102.5D(2)$$

$$B_1 \approx 102.83$$

2) Half yr coupon: 3, Last cashflow @ 10Y is 103

Payment: 0.5, 1, ..., 10 (20 total)

$$B_2 = \sum_{i=1}^{19} 3e^{-R(4i)t_i} + 103e^{-R(10)(10)}$$

$$\approx 111.84$$

$$3) B_1 \text{ yield } y_1: 102.83 = 2.5e^{-y_1(0.5)} + 2.5e^{-y_1(1)} + 2.5e^{-y_1(1.5)} + 102.5e^{-y_1(2)}$$

$$y_1 \approx 0.03491 \Rightarrow 3.491\%$$

$$B_2 \text{ yield } y_2: 111.84 = \sum_{i=1}^{19} 3e^{-y_2 t_i} + 103e^{-y_2(10)}$$

$$y_2 \approx 0.04465 \Rightarrow 4.4465\%$$

1.5)

Pay  $N = 1,000,000$  in 6 months ("2 yr")

Long EUR, mat 6M,  $F = 1.150$  USD/EUR

$x_0 = 1.1$ ,  $x_T = 1.175$ ,  $T = 0.5$

i)  $\text{Payoff} = (x_T - F)_N = (1.175 - 1.15) \cdot 1,000,000$   
 $= 25,000 \text{ USD}$

ii)  $F = x_0 e^{(r_{USD} - r_{EUR})T} \Rightarrow$

$$(r_{USD} - r_{EUR}) = \frac{1}{T} \ln \left( \frac{F}{x_0} \right) = 1/0.5 \ln \left( \frac{1.15}{1.1} \right)$$
$$= 2 \ln (1.04545) \approx 0.088904$$

$$r_{USD} - r_{EUR} \approx 8.89\% \text{ p/yr}$$