

$$1a) 5050 \times 1.035 = 5226.75$$

Yes there is arbitrage short 1 futures contract and put the \$5050 into the risk free asset. Take the \$5226.75 from the account and pay 5200 for the forward profit \$26.75 per contract bought

1b. Yes, buy 10000 futures contract by shorting the risk-free asset. Get 5300 from the contract and use 5226.75 to pay back debt profit 73.75 per contract

$$2a) (1 + 0.0325/2)^2 = 1.0326525 - 1 = 0.03266 \approx 3.266\%$$

$$2b) (1 + 0.0325/2)^2 = (1 + r_u/4)^4 (1.0326525) = (1.0326525)^{1/4} = 0.03231 = 3.231$$

$$2c) (1 + 0.035/2)^2 = e^{r_c} r_c \Rightarrow \ln(1.0326525) = 0.3213 = 3.213$$

$$3) \left(1 + 0.1715 \left(\frac{30}{365}\right)\right)^{\frac{365}{30}} = 1.185663$$

$$10000 \cdot 1.185663 = 11856.63$$

$$4) GM = e^{-0.03/2} = 0.9851 \quad 1Y = e^{-0.03(1)} = 0.9709 \\ 1.5Y = e^{-0.03(1.5)} = 0.9488 \quad 2Y = e^{-0.03(2)} = 0.9324$$

$$a) B_1 = 2.5(0.9851 + 0.9709 + 0.9488) + 102.50(0.9324) B_1 = 2.5(2.9113) + 95.575 = 102.83$$

$$b) \sum_{i=1}^{20} e^{-R(t_i) t_i} = e^{-0.03/2} + e^{-0.03} + e^{-0.035(1)} + e^{-0.035(2)} + e^{-0.0425(2.5)} + \dots + e^{-0.045(10)}$$

$\approx 14.89$

$$B_2 = 3.00(14.89) + 100(0.5370) = 44.67 + 53.70 = 98.37$$

$$c) 102.83 = \sum_{i=1}^9 \frac{2.5}{(1+y/2)^i} + \frac{106}{(1+y/2)^9} \Rightarrow y = 3.42\%$$

$y \approx 6.15\%$

5a)  $1.15 \cdot 1,000,000 = 1,150,000$  owed for futures contract

$1.175 \cdot 1,000,000 = 1,175,000$  realized at maturity

$$1.175 - 1.15 = 0.025$$

$$0.02 \cdot 1,000,000 = \$25,000 \text{ profit}$$

5b)  $1.15 = 1.1e^{\frac{x}{2}}$

$$x = 2 \ln\left(\frac{1.15}{1.1}\right)$$

$$x = 0.0889 \Rightarrow 8.89\%$$