

HW1.

1. $F_0 = 5050 \cdot e^{0.035} = 5229$

Yes, there is an arbitrage opportunity

short sell the gold at 5050 per ounce
and invest at risk free rate.

Go long-forward at 5200 for 1 year
at $T=1$, the investment is 5229 ^{per ounce}, then buy gold at
5200 by forward contract and deliver gold
Profit is \$29 per ounce

ii. Yes, there is arbitrage

borrow \$5050 at 3.5%, buy gold for 5050,
short the forward contract at 5300
at $T=1$, deliver gold and receive 5300 and repay loan

$$\text{Profit} = \$71$$

1. i. $(1 + \frac{0.0325}{2})^2 = 1.032764$

$$\text{Annual} = 3.2764\%$$

ii. $(1 + \frac{q}{4})^4 = 1.032764$

$$1 + \frac{q}{4} = \sqrt[4]{1.032764} = 1.008087$$

$$\frac{q}{4} = .008087$$

$$q = .03235 = 3.235\%$$

iii. $r_c = \ln(1.032764)$
 $= 3.224\%$

$$1.3 \quad B = 10000 \left(1 + \frac{.175}{365}\right)^{30}$$

$$= 10000 \cdot 1.0004699^{30}$$
$$= \$10,142$$

Interest charged: \$142

$$1.4 \quad 1. \quad T = .5 \quad PV = 2.5 e^{-0.03 \cdot 0.5} = 2.463$$

$$T = 1 \quad PV = 2.5 e^{-0.03 \cdot 1} = 2.426$$

$$T = 1.5 \quad PV = 2.5 e^{-0.035 \cdot 1.5} = 2.373$$

$$T = 2 \quad PV = 102.5 e^{-0.035 \cdot 2} = 95,585$$

$$P = 102.85$$

$$2. \quad T = .5, 1 \quad PV = 3e^{-0.03 \cdot 0.5} + 3e^{-0.03 \cdot 1} = 5.89$$

$$T = 1.5, 2 \quad PV = 3e^{-0.035 \cdot 1.5} + 3e^{-0.035 \cdot 2} = 5.55$$

$$T = 2.5, 3, 3.5, 4, 4.5, 5 \quad PV = 3e^{-0.0425 \cdot 2.5} + 3e^{-0.0425 \cdot 3} + 3e^{-0.0425 \cdot 4} + 3e^{-0.0425 \cdot 4.5} + 3e^{-0.0425 \cdot 5} = 15.96$$

$$T = 5.5, \dots, 10 = 84.64$$

$$P = 112.04$$

$$3. \quad 1. \text{ Using calculator } N = 4, PV = -102.85, FV = 100, \\ PMT = 2.5$$

$$I/Y = 1.756 \quad YTM = 3.51\%$$

$$2. \text{ Using calculator } N = 20, PV = -112.04, FV = 100, PMT = 2.5 \\ I/Y = 2.246 \quad YTM = 4.492\%$$

1.5 i. $1,000,000 \cdot 1.175 = \$1,175,000$

with forward: $1,000,000 \cdot 1.150 = \$1,150,000$

Gain of \$25,000 because appreciation was more than forward rate.

ii. $\bar{F}_0 = X_0 e^{(r_{USD} - r_{EUR})T}$

$$1.15 = 1.1 e^{(r_{USD} - r_{EUR}) \cdot 5}$$

$$\ln\left(\frac{1.15}{1.1}\right) = (r_{USD} - r_{EUR}) \cdot 5$$

$$0.044452 = (r_{USD} - r_{EUR}) \cdot 5$$

$$0.088904 = r_{USD} - r_{EUR} = 8.89\%$$