

R Markdown and RMD files

The most common way to use R in this class will be in R Markdown (.Rmd) files. These can combine LaTeX type setting, R code chunks, and visual outputs. For example, you can write the following true statement:

$$\forall w, b, n \in \mathbb{W} \text{ such that } w \geq n \text{ and } b \geq n, \sum_{k=0}^n \frac{\binom{w}{k} \binom{b}{n-k}}{\binom{w+b}{n}} = 1$$

(Why is this true?)

1. Write a true statement with an integral.

TODO: Write a true statement.

R with flow control

While loops

If you doubted the first statement, you can verify it by adding an R chunk with code. To add a chunk, click on the green +C button up top and select R (or just type out the dashes).

```
w <- 10 # Sets w to 10
b = 20 # Sets b to 20, same as <-
n <- 15
total <- 0
k <- 0

while (k <= n) { # Run the statements inside the loop until k > n
  # Set the 'total' variable to itself plus the next term in the sum.
  total <- total + (choose(w, k) * choose(b, n-k)) / choose(w + b, n)

  # Increment k
  k <- k + 1
}

print(total)

## [1] 1
```

To run the chunk, either hit **Command-Shift-Enter** or hit the green arrow in the top right of the chunk.

2. Write a loop that prints the integers from -5 to 5 inclusive.

```
# TODO: Write a loop
```

Manually

In the earlier chunk, `choose` is an R function that calculates a binomial coefficient. You can run `?choose` to see more information about this function.

You can also type `?choose` in the “Console” at the bottom of the screen to get the same effect without adding a chunk. In the console, you can also verify that variables outside of functions are stored in memory until erased. For example, type `total` or `print(total)` into the console to see that it still contains the value 1.

For loops, vectorization, and apply

We can also evaluate this sum four other ways. First we'll use a for loop:

```
total <- 0

for (k in 0:n) { # For k = 0, then k = 1, ... finally k = n
  total <- total + (choose(w, k) * choose(b, n-k)) / choose(w + b, n)
}

print(total)

## [1] 1
```

A for loop automatically increments k without an extra line to explicitly do so.

Second, we'll use a while loop with an if statement:

```
total <- 0
k <- 0

while (TRUE) { # Run forever until broken
  total <- total + (choose(w, k) * choose(b, n-k)) / choose(w + b, n)

  k <- k + 1

  if (k > n) { # Break the while loop when k > n
    break
  }
}

print(total)

## [1] 1
```

Third, we'll use vectorization. This is the best way to use R.

```
k <- 0:n # Assign k to be a vector containing the elements 0 through n
print(k)

## [1] 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15

print(k[1:10]) # Print a subvector of the first 10 elements (R uses 1-based indexing)

## [1] 0 1 2 3 4 5 6 7 8 9

# Use vectorization and sum over all the elements
total <- sum((choose(w, k) * choose(b, n-k)) / choose(w + b, n))

print(total)

## [1] 1
```

Fourth, we'll create a function and apply it over a vector.

```
# Create a function called single_hyper with k, w, b, and n as parameters
single_hyper <- function(k, w, b, n) {
  value_to_return <- (choose(w, k) * choose(b, n-k)) / choose(w + b, n)
  return (value_to_return) # Return the calculated value
}

# Apply the function single_hyper to each element in k and sum the result
total <- sum(sapply(k, single_hyper, w, b, n))
```

```
print(total)
```

```
## [1] 1
```

3. Use a for loop, vectorization, and `sapply` to calculate $\sum_{i=1}^{1000} \frac{1}{i}$.

```
# TODO: Calculate the sum
```

R Functions and more vectorization

There are many other functions built in for R. For example, the function we just wrote already has a built-in version:

```
k <- 0:15
total <- sum(dhyper(k, w, b, n))

print(total)
```

```
## [1] 1
```

This function calculates the probability mass function of a hypergeometric with parameters w, b , and n evaluated at k . Basic operations are also vectorized in R:

```
v1 <- c(2, 4, 6) # Create vector with 3 elements by hand
v2 <- seq(5, 6, 0.5) # All real numbers from 5 to 6 spaced by 0.5
print(v1 * v2)
```

```
## [1] 10 22 36
```

A convenient (or annoying) feature of R is that vectorized operations will duplicate the smaller vector elements to match the length of the larger vector.

```
# For example,
print(3 * 1:3)
```

```
## [1] 3 6 9
```

```
# And also
v3 <- seq(5, 9, 0.5)
print(v1)
```

```
## [1] 2 4 6
```

```
print(v3)
```

```
## [1] 5.0 5.5 6.0 6.5 7.0 7.5 8.0 8.5 9.0
```

```
print(v1 * v3)
```

```
## [1] 10 22 36 13 28 45 16 34 54
```

```
# But this throws a warning
```

```
v4 <- seq(5, 8, 0.5)
print(v1 * v4)
```

```
## Warning in v1 * v4: longer object length is not a multiple of shorter object
## length
```

```
## [1] 10 22 36 13 28 45 16
```

There is some thought that vectorization in R is always faster...

```

now <- Sys.time() # Start timer
to_time <- 10^6
n <- 10
output <- vector(length = to_time)
for (i in 1:to_time) { # Multiply elements in a for loop
  output[i] <- i^2
}
print(difftime(Sys.time(), now))

```

```
## Time difference of 0.02754092 secs
```

```

now <- Sys.time()
output <- (1:to_time)^2 # Do vectorized multiplication of elements (in a good way)
print(difftime(Sys.time(), now))

```

```
## Time difference of 0.002336025 secs
```

```

now <- Sys.time()
# Do vectorized multiplication of elements (in a bad way)
output <- sapply(1:to_time, `^`, 2)
print(difftime(Sys.time(), now))

```

```
## Time difference of 0.396754 secs
```

But using the `apply` functions doesn't give you much speed up. Unless there's a built-in vectorized method (which there usually is), it might be clearer to just use a `for` loop.

4. Print the average of $1, 1/2, 1/3, \dots, 1/10^8$ in the fastest way you can. What is the limit of the mean of $1, 1/2, 1/3, \dots, 1/n$ as $n \rightarrow \infty$?

```
# TODO: Print the average
```

TODO: Find the limit.

Knitting

Now is a good point to knit your code. Press **Command-Shift-K** or the blue knit button at the top.

Setting headers in your chunk can have helpful effects. For example, `cache=T` stores the chunk outputs when knitting so they don't have to run again unless you change the code. The option `warning=F` prevents ugly warning messages from appearing in your output. The option `echo=F` includes the code output but not the code. The option `eval=F` includes the code but not the output. The option `include=F` skips the chunk when knitting (no code or output).

```
## [1] "Chunk was here"
```

Importing data, working with data, and plotting

Importing data

You can import data from a CSV (comma separated values) file to a `data.frame` as follows. If the data cannot be found, make sure you're in the right directory by right clicking `Nickols_R_Bootcamp.Rmd` at the top left and selecting "Set Working Directory."

```
countries <- read.csv("data/countries.csv")
```

This section will deal with a data set of country-level statistics from [this source](#) with an explanation of the data encoding found [here](#).

A few columns will be useful for the following questions.

- `mad_gdppc`: GDP per capita
- `spi_ospi`: Overall social progress index on 0-100 scale
- `wdi_expedu`: Government expenditure on education as percent of GDP

Selecting rows and columns

You can select columns by name or by index:

```
print(countries$mad_gdppc[1:10]) # Print the first 10 GDP per capitas
```

```
## [1] 1934.555 11104.166 14228.025      NA  7771.442      NA 16628.055
## [8] 18556.383 49830.801 42988.070
```

```
print(countries[,849][1:10]) # Same thing
```

```
## [1] 1934.555 11104.166 14228.025      NA  7771.442      NA 16628.055
## [8] 18556.383 49830.801 42988.070
```

The comma in the second line above is important. You can select rows by putting the number before the comma.

```
print(countries[1,][1:10]) # First 10 columns of row 1
```

```
## ccode      cname ccode_qog  cname_qog ccodealp ccodecow      version
## 1         4 Afghanistan      4 Afghanistan      AFG      700 QoGStdCSjan22
## aii_acc aii_aio aii_cilser
## 1         NA      NA      NA
```

```
print(countries[1:5,1:10]) # First 10 columns of rows 1-5
```

```
## ccode      cname ccode_qog  cname_qog ccodealp ccodecow      version
## 1         4 Afghanistan      4 Afghanistan      AFG      700 QoGStdCSjan22
## 2         8  Albania      8  Albania      ALB      339 QoGStdCSjan22
## 3        12  Algeria     12  Algeria      DZA      615 QoGStdCSjan22
## 4        20  Andorra     20  Andorra      AND      232 QoGStdCSjan22
## 5        24  Angola      24  Angola      AGO      540 QoGStdCSjan22
## aii_acc aii_aio aii_cilser
## 1         NA      NA      NA
## 2         NA      NA      NA
## 3        6.25    12.5      0
## 4         NA      NA      NA
## 5       18.75    17.5      0
```

You can also select rows by a condition.

```
print(dim(countries)) # Original dimensions

## [1] 194 1714

# Subset the data frame to only countries with GDPs per capita of over $10000
print(dim(countries[countries$mad_gdppc > 10000,]))

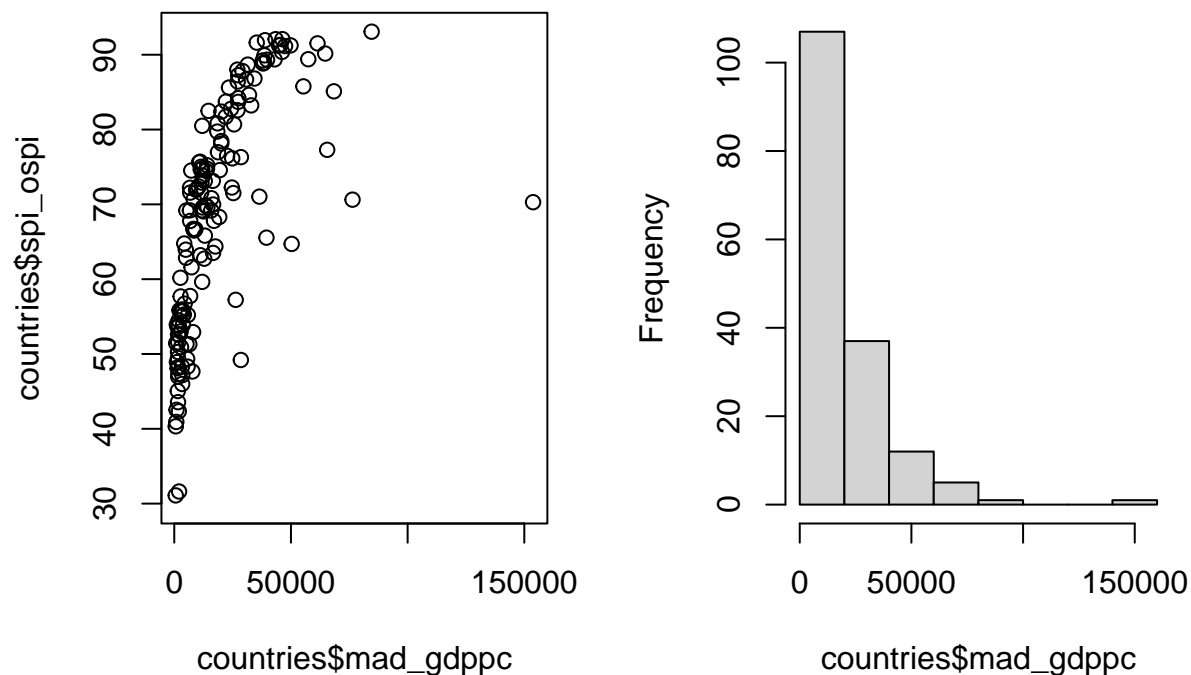
## [1] 126 1714
```

Base R plots

The following code plots the relationship between GDP and OSPI:

```
par(mfrow = c(1,2)) # Place two plots side by side (1 row, 2 columns)
plot(countries$mad_gdppc, countries$spi_ospi)
hist(countries$mad_gdppc)
```

Histogram of countries\$mad_gdp



These are quite ugly, but we can make them prettier in `ggplot`.

GGplot

The following chunk installs and loads the package `ggplot`. You'll need to install packages only once but load them in each file.

```
if("ggplot2" %in% rownames(installed.packages()) == FALSE) {
  install.packages("ggplot2")
}
library(ggplot2)

if("gridExtra" %in% rownames(installed.packages()) == FALSE) {
  install.packages("gridExtra")
}
```

```
}
library(gridExtra)
```

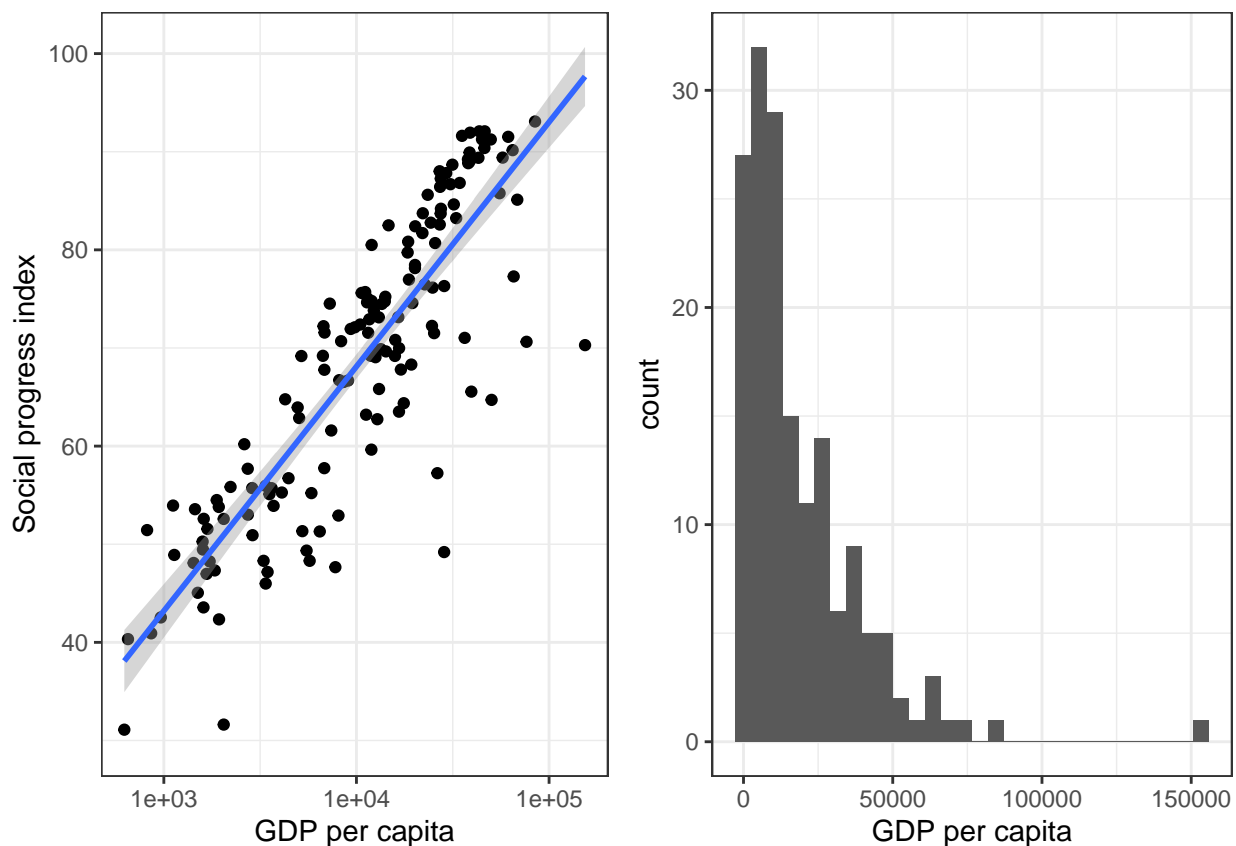
The following code creates the earlier plots, but prettier.

```
# GDP per capita is x, OSPI is y
p1 <- ggplot(countries, aes(x = mad_gdppc, y = spi_ospi)) +
  geom_point() + # Plot points
  geom_smooth(method = 'lm', formula = "y~x") + # Plot line
  # Log transform x axis and set break points
  scale_x_continuous(trans = 'log', breaks = c(1000, 10000, 100000)) +
  ylab("Social progress index") + # Rename y axis
  xlab("GDP per capita") + # Rename x axis
  theme_bw() # Change background

p2 <- ggplot(countries, aes(x = mad_gdppc)) +
  geom_histogram(bins = 30) +
  xlab("GDP per capita") +
  theme_bw()

# You can display individual plots by not assigning them to p1 or p2

grid.arrange(p1, p2, ncol=2) # Put plots side by side
```



- Plot the relationship between OSPI and education expenditures in countries with GDP per capitass of at least \$20,000.

```
# TODO: Subset and plot
```

Random number usage

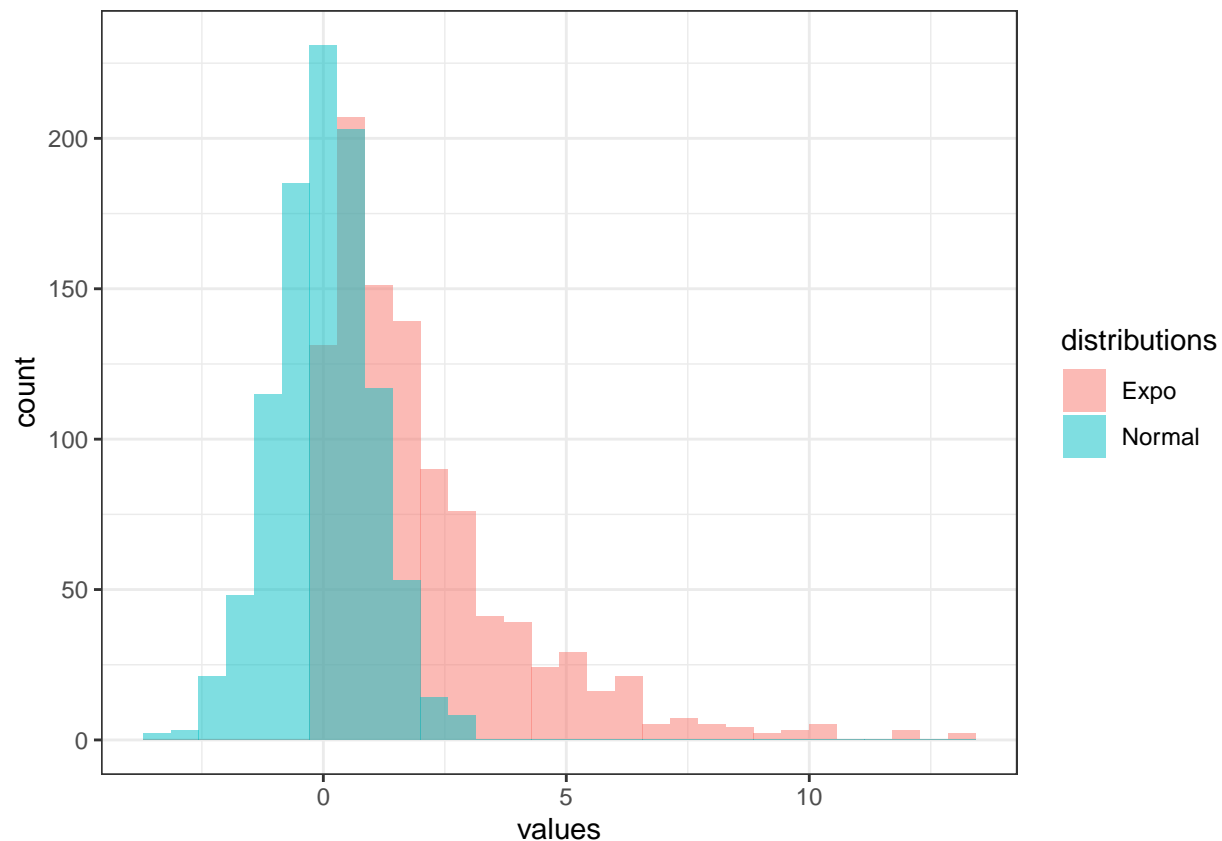
One of the main benefits of R is its ability to generate and manipulate random numbers easily. Most common distributions are already ready to go. Make sure to set a seed so your code is reproducible. For example:

```
set.seed(111)

n <- 1000
normals <- rnorm(n, 0, 1) # Generate 1000 standard normals
expos <- rexp(n, 1/2) # 1000 exponentials with rate 1/2 (mean 2)

# Create a data.frame with the normal and exponentials in one column
# and the names in another column
df <- data.frame("values" = c(normals, expos),
                  "distributions" = rep(c("Normal", "Expo"), each = n))

ggplot(df, aes(x = values, fill = distributions)) +
  geom_histogram(alpha = 0.5, position="identity", bins = 30) +
  theme_bw()
```



You can also calculate summary statistics for the distributions:

```
print(c(mean(normals), median(normals)))
```

```
## [1] 0.01080923 0.01967487
```



```
print(summary(normals))
```

```
##      Min.   1st Qu.   Median     Mean   3rd Qu.     Max.
## -3.32334 -0.65366  0.01968  0.01081  0.67559  2.92603
```

There are also quantile functions (they start with “q”), density functions (they start with “d”), and cumulative density functions (they start with “p”).

```
print(pnorm(-3:3))
```

```
## [1] 0.001349898 0.022750132 0.158655254 0.500000000 0.841344746 0.977249868
## [7] 0.998650102
```

```
print(qnorm(c(1 - (1-0.997)/2, 1 - (1-0.95)/2, 1 - (1-0.68)/2)))
```

```
## [1] 2.9677379 1.9599640 0.9944579
```

(Which rule does the line above show?)

The functions `rep` is useful for repeating values, and the function `replicate` is useful for replicating computations.

```
print(rep(10, 5))
```

```
## [1] 10 10 10 10 10
```

```
print(replicate(10, mean(rnorm(100, mean = 1, sd = 2))))
```

```
## [1] 0.8934618 1.0457099 0.9842224 1.2385490 1.1066039 0.5112138 1.0136824
## [8] 1.2919768 1.2427886 0.9372874
```

6. Show visually the law of large numbers applying to draws from $\mathcal{N}(0, 1)$.

```
# Show the LLN
```

Simulations

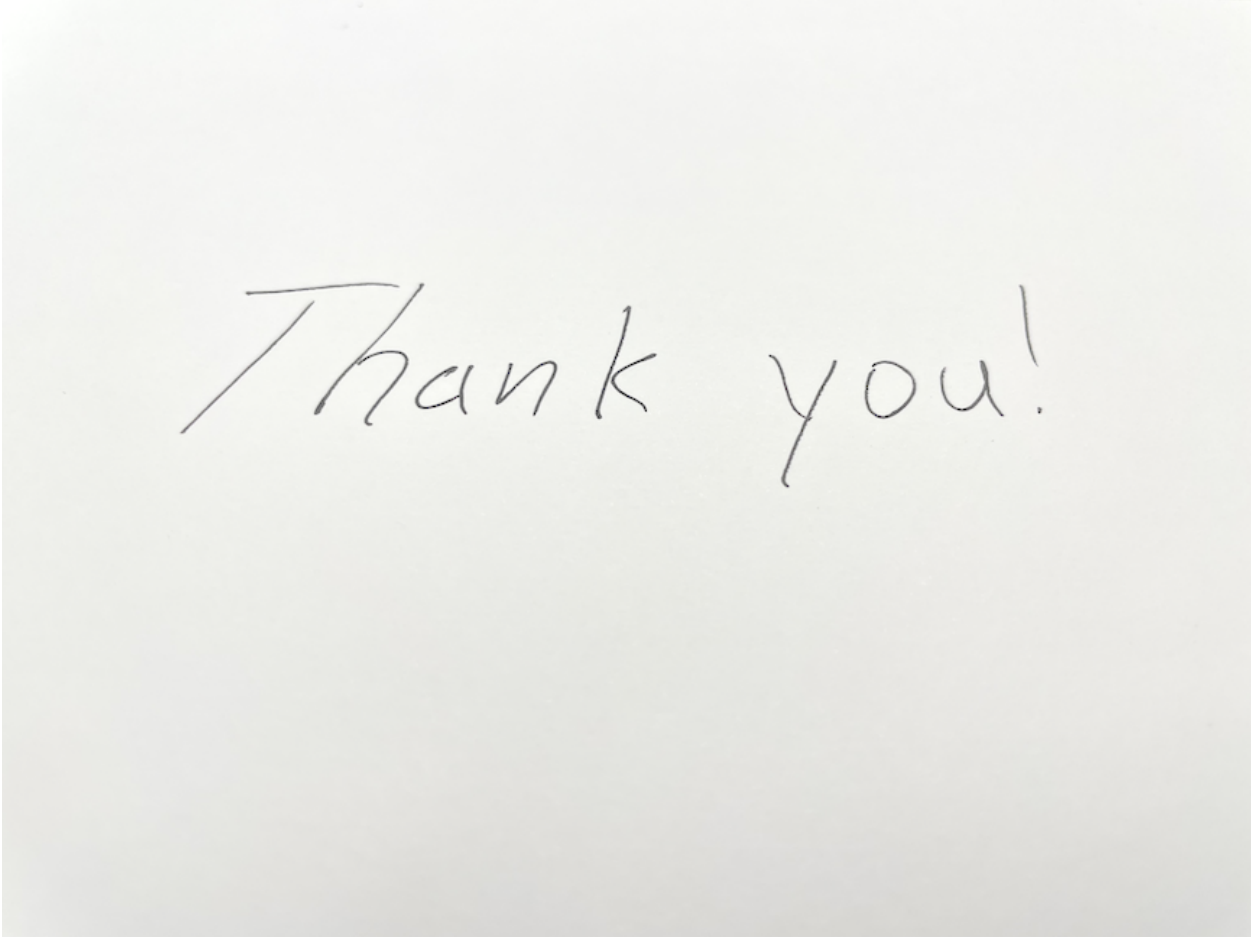
7. One common application of R is in simulations. Consider the following scenario that would be difficult to solve analytically. Suppose there are three board members choosing the new CEO of a large company. To narrow down their options, they will each write the names of their top few choices on slips of paper, each put their slips in their own hat, each draw a certain number of the slips, and see which drawn names intersect. Suppose there are s names that all three board members write down (they each write those s names and put them in their own hats). Also, for $i \in \{1, 2, 3\}$, board member i writes n_i names that don't intersect all three ways. (Therefore, person i 's hat contains $n_i + s$ slips.) Each board member then chooses m names from his or her hat. What is the distribution of the number of names that overlap among all their samples (i.e. all three board members draw the name)? Let $s = 10, n_1 = 15, n_2 = 20, n_3 = 25$, and $m = 20$ for concreteness. Write R code to show a histogram of the distribution, and compare your results to random draws from the function `rchyper` in the package `chyper`. How do these compare to the exact PMF as calculated from the function `dchyper` in `chyper`? In addition to previous functions, the functions `sample`, `length`, `intersect`, and `table` may be useful.

```
if("chyper" %in% rownames(installed.packages()) == FALSE) {
  install.packages("chyper")
}
library(chyper)

s <- 10
n_1 <- 15
n_2 <- 20
n_3 <- 25
m <- 20

# TODO: Take samples, find the intersection, compare to chyper
```

This concludes the instructional material. One last thing is that you can include a picture like the following:

A photograph of a piece of white paper with the words "Thank you!" written in a cursive, handwritten style in dark ink. The paper is slightly wrinkled and has a soft shadow on the surface it's resting on.

Thank you!