

# Noob's Guide to L<sup>A</sup>T<sub>E</sub>X

Willem Adriaan Smit  
14052131

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Marno Grobler

Eduan Oosthuizen

Department of Chemical Engineering  
University of Pretoria

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## Synopsis

Welcome to the Noob's guide. This section has only been included for reference on how to use it when comparing the source code to the resulting document. Please continue to the Introduction, Section ??.

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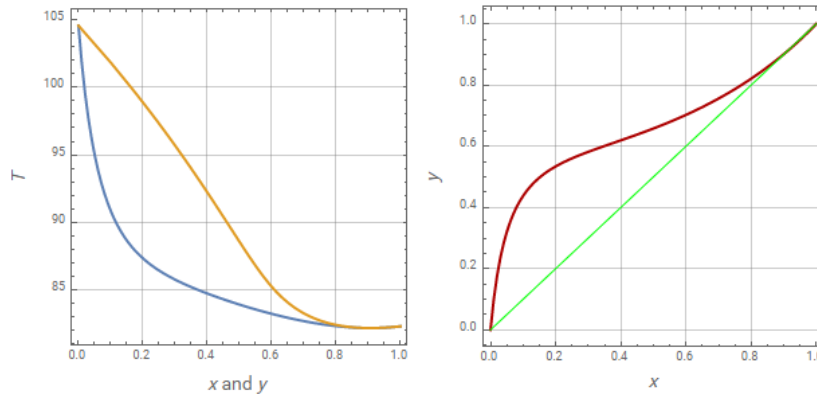
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# 1 Introduction

Renewable energy is becoming a major role player in the world today. As people are starting to shift away from fossil fuel based technology and energy generation, the focus is shifting to alternative methods of energy (and fuel) production.

One such a method involves the use of ethanol as an alternative fuel. Ethanol particularly is an excellent contender for a major alternative fuel, as it can be produced from crops or by means of biological fermentation. [A lot of] research is currently done on methods to generate ethanol in order for it to power the future.

Producing ethanol, however, is not the only problem to overcome. After the production process (usually from fermentation), the ethanol has to be separated from the product mixture in order to purify it. This poses to be a challenge (and a very energy intensive operation) due to the thermodynamic properties of the homogeneous mixture between water and ethanol. As noted in Figure 1, the system contains an azeotrope. This leads to very expensive separation operations, as pressure swing distillation has to be implemented for high purity separation.



**Figure 1:** Vapour Liquid Equilibrium (VLE) data for the water ethanol system at 1 bar.

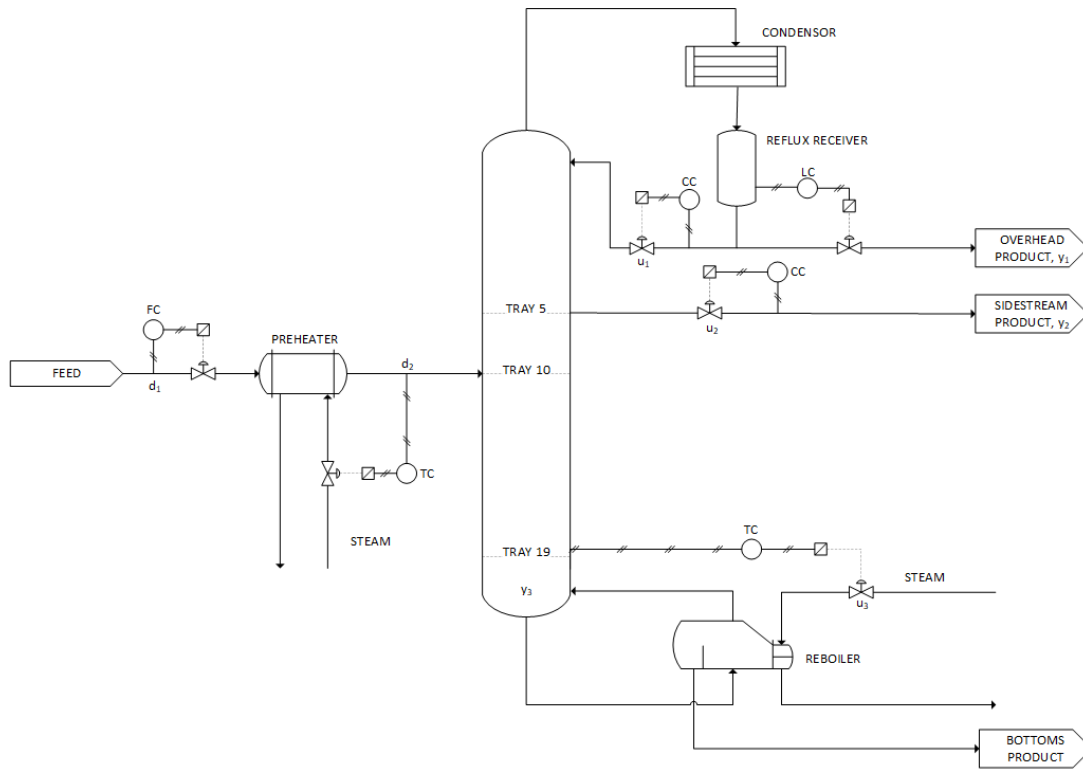
In this report, an investigation regarding the controllability of the ethanol water separation process is investigated. The plant investigated is a pilot plant that is testing the feasibility for scale up of the process. Control has to be implemented to ensure that the system reaches a steady state, as well as to improve the overall profitability by reducing the standard deviation in the product quality.

A plant wide control system will not be investigated. Only the distillation column is analysed. The current proposed control system is discussed in Section [REF!!!]. This report will investigate the validity of such a proposed control scheme, as well as the where the physical constraints in the system lie.

## 2 Process Model Description

### 2.1 System Diagram

The Process Flow Diagram of the system, with all the relevant inputs, outputs and disturbances are displayed in Figure 2.



**Figure 2:** Process flow diagram of the system

### 2.2 System Description

The system involves the separation of water and ethanol (in a solution), with the aim of producing an ethanol product that can be used as an alternative fuel source.

The system can be summarized as follows:

- The distillation column of the pilot scale plant is a 19 tray, 12 inch diameter column.
- The column has variable feed and side stream draw off locations.
- The side stream flow is varied to control the composition of the stream.



- The distillate vapour draw off stream is fully condensed, and then separated into the reflux and product streams.
- The product stream is set to control the level in the condenser, while the reflux stream controls the composition of the distillate product.
- A kettle re-boiler is used to add energy to the column. Steam is the main utility.
- The amount re-boiled bottoms product is controlled by varying the steam supplied to the re-boiler.
- The feed temperature and flow rate can be controlled to simulate disturbances on the system. These variables are strictly defined as disturbances, as they are part of another section's (the bio-reactor or chemostat) control scheme.
- Currently all variables are controlled with single input single output (SISO) control loops.

## 2.3 Measurement of Variables

The compositions are measured/determined through various on-line sensors (densitrometry and refractometry). Temperatures are monitored using thermocouples. Flow rates are measured with thermal mass flow meters. Levels are measured by inference from static head, measured with a pressure sensor. The product model and serial numbers are not available.

## 2.4 System Variables

All variables in the ethanol water distillation column system is summarised in Table 1. The current steady state values hold reference to the tested conditions on site.

**Table 1:** Summary of all the model variables.

Input Variables			
Variable	Description	Steady State Value	Units
$u_1$	Reflux flow rate	0.18	gpm
$u_2$	Side stream product flow rate	0.046	gpm
$u_3$	Reboiler steam pressure	20	psi
Output Variables			
Variable	Description	Steady State Value	Units
$y_1$	Overhead ethanol mole fraction	0.7	-
$y_2$	Side stream ethanol mole fraction	0.52	-
$y_3$	Tray #19 temperature	92	°C
Disturbance Variables			
Variable	Description	Steady State Value	Units
$d_1$	Feed flow rate	0.8	gpm
$d_2$	Feed temperature	78	°C

## 2.5 System Model

The model was determined by conducting pulse testing on the system. In most cases a first order plus dead time model gave a sufficiently accurate fit to experimental data. The sum of squares of an adequate fit during model development was a values of greater than 0.98. In some relationships more complex dynamics had to be derived and a second order system with a first order lag and dead time, was used to accurately describe the impulse response (based on the same adequate fit method described above). The equations used for fitting were

$$\frac{y_i(s)}{u_i(s)} = \frac{K_i e^{-\theta_i s}}{\tau_i s + 1} \quad (1)$$

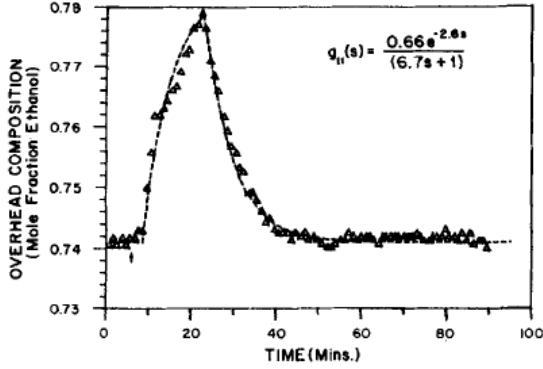
for the first order plus dead time system, and

$$\frac{y_i(s)}{u_i(s)} = \frac{K_i(\tau_{1i}s + 1)e^{-\theta_i s + 1}}{(\tau_{2i}s + 1)(\tau_{3i}s + 1)} \quad (2)$$

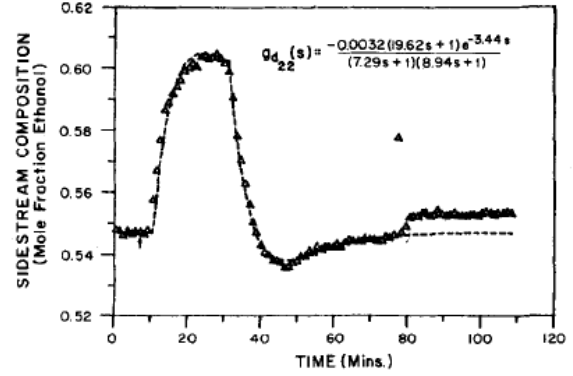
for the relationships with more complex dynamics.

The fitting curves of two pulse tests are displayed in Figure 3 and Figure 4. An important

thing to note is that the unit of time is minutes, and therefore all responses and analysis will be conducted with this unit for time.



**Figure 3:** Overhead composition response to a pulse of 15 minutes duration in the reflux rate.



**Figure 4:** Side stream composition response to a pulse of 15 minutes duration in feed temperature.

The model was then written in the standard form of a linear MIMO system [REF!!!],

$$\mathbf{y}(s) = \mathbf{G}(s)\mathbf{u}(s) + \mathbf{G}_d(s)\mathbf{d}(s) \quad (3)$$

where

$$\hat{\mathbf{G}}(s) = \begin{bmatrix} G_{11} & G_{12} & G_{13} \\ G_{21} & G_{22} & G_{23} \\ G_{31} & G_{32} & G_{33} \end{bmatrix} = \begin{bmatrix} \frac{0.66e^{-2.6s}}{6.7s+1} & \frac{-0.61e^{-3.5s}}{8.64s+1} & \frac{-0.0049e^{-s}}{9.06s+1} \\ \frac{1.11e^{-6.5s}}{3.25s+1} & \frac{-2.36e^{-3s}}{5.0s+1} & \frac{-0.012e^{-1.2s}}{7.09s+1} \\ \frac{-34.68e^{-9.2s}}{8.15s+1} & \frac{46.2e^{-9.4s}}{10.9s+1} & \frac{0.87(11.61s+1)e^{-s}}{(3.89s+1)(18.8s+1)} \end{bmatrix} \quad (4)$$

and

$$\hat{\mathbf{G}}_d(s) = \begin{bmatrix} G_{d11} & G_{d12} \\ G_{d21} & G_{d22} \\ G_{d31} & G_{d32} \end{bmatrix} = \begin{bmatrix} \frac{0.14e^{-12s}}{6.2s+1} & \frac{-0.0011(26.32s+1)e^{-2.66s}}{(7.85s+1)(4.63s+1)} \\ \frac{0.53e^{-10.5s}}{6.9s+1} & \frac{-0.0032(19.62s+1)e^{-3.44s}}{(7.29s+1)(8.94s+1)} \\ \frac{-11.54e^{-0.6s}}{7.01s+1} & \frac{0.32e^{-2.6s}}{7.76s+1} \end{bmatrix} \quad (5)$$

## 2.6 Scaling the System

In order to perform a controllability analysis on the system, the system had to be scaled according to the method described in [Reff!!!].

In order to perform the scaling operation, the upper and lower limits of all the variables have to be defined. The initial boundary values of all system variables are summarized in Table 2, Table 3, and Table 4.

**Table 2:** The boundaries of the manipulated variables in the system.

Manipulated Variable	Lower Constraint	Upper Constraint	Steady State Value
$u_1$ , Reflux Flow Rate	0.068	0.245	0.18
$u_2$ , Side Stream Flow Rate	0.00694	0.1	0.046
$u_3$ , Reboiler Steam Pressure	15.6	34	20

**Table 3:** The boundaries of the controlled variables in the system.

Controlled Variable	Maximum Set Point Change	Steady State Value
$y_1$ , Overhead Mole Fraction Ethanol	0.05	0.7
$y_2$ , Side Stream Mole Fraction Ethanol	0.1	0.52
$y_3$ , Temperature on Tray #19	8	92

**Table 4:** The boundaries of the controlled variables in the system.

Disturbance Variable	Lower Constraint	Upper Constraint	Steady State Value
d1, Feed Flow Rate	0.6	1.1	0.8
d2, Feed Temperature	50	102	78

Using the information above the following matrices can be deduced, that will be used to scale the system

$$D_e = \begin{bmatrix} 0.01 & 0 & 0 \\ 0 & 0.01 & 0 \\ 0 & 0 & 4 \end{bmatrix} \quad (6)$$

$$D_u = \begin{bmatrix} 0.065 & 0 & 0 \\ 0 & 0.03906 & 0 \\ 0 & 0 & 4.4 \end{bmatrix} \quad (7)$$

$$D_d = \begin{bmatrix} 0.3 & 0 \\ 0 & 28 \end{bmatrix} \quad (8)$$

$$r = \begin{bmatrix} 0.05 & 0 & 0 \\ 0 & 0.1 & 0 \\ 0 & 0 & 8 \end{bmatrix} \quad (9)$$

Using the above matrices, the scaled system can be calculated using the following equations from [REF!!!],

$$G = D_e^{-1} \hat{G} D_u \quad (10)$$

$$G_d = D_e^{-1} \hat{G}_d D_d \quad (11)$$

From Equation 10 and Equation 11, the scaled system can be written as

$$G(s) = \begin{bmatrix} G_{11} & G_{12} & G_{13} \\ G_{21} & G_{22} & G_{23} \\ G_{31} & G_{32} & G_{33} \end{bmatrix} = \begin{bmatrix} \frac{4.29e^{-2.6s}}{6.7s+1} & \frac{-2.38266e^{-3.5s}}{8.64s+1} & \frac{-2.156e^{-s}}{9.06s+1} \\ \frac{7.215e^{-6.5s}}{3.25s+1} & \frac{-9.21816e^{-3s}}{5.0s+1} & \frac{-2.156e^{-1.2s}}{7.09s+1} \\ \frac{-0.56355e^{-9.2s}}{8.15s+1} & \frac{0.451143e^{-9.4s}}{10.9s+1} & \frac{1.1(10.1007s+0.87)e^{-s}}{(3.89s+1)(18.8s+1)} \end{bmatrix} \quad (12)$$

and

$$G_d(s) = \begin{bmatrix} G_{d11} & G_{d12} \\ G_{d21} & G_{d22} \\ G_{d31} & G_{d32} \end{bmatrix} = \begin{bmatrix} \frac{4.2e^{-12s}}{6.2s+1} & \frac{-2800(0.028952s+0.0011)e^{-2.66s}}{(7.85s+1)(4.63s+1)} \\ \frac{15.9e^{-10.5s}}{6.9s+1} & \frac{-2800(-0.062784s+0.0032)e^{-3.44s}}{(7.29s+1)(8.94s+1)} \\ \frac{-0.8655e^{-0.6s}}{7.01s+1} & \frac{2.24e^{-2.6s}}{7.76s+1} \end{bmatrix} \quad (13)$$

with

$$R = \begin{bmatrix} 5 & 0 & 0 \\ 0 & 10 & 0 \\ 0 & 0 & 2 \end{bmatrix} \quad (14)$$

## References

Çengel, Y A and Ghajar, A J (2015) *Heat and Mass Transfer*, 5th ed. McGraw-Hill, New York.

Forster, K and Zuber, N (1955) “Dynamics of vapour bubbles and boiling heat-transfer”  
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