

Isolation

Assume:

Show

$$1) H, \{T\} \cup TS \sim H, TS'$$

$$isolated(H, TS')$$

$$2) isolated(H, \{T\} \cup TS)$$

$$3) \vdash H : *$$

4) $H \vdash TS$? This was never explicitly used (or defined). What well-formedness do we actually need?
No tasks awaits a itself (or larger await-cycles) etc. is reasonable but what else?
Is this even necessary for isolation?

Proof by case distinction on used reduction rule " \sim ":

E-FINISH2:

$$T = (f, k, \langle \text{FINISH } f' \rangle \circ FS)$$

$$T' = (f, k, FS)$$

$$TS' = \{T'\} \cup TS$$

$$\forall (g, k', GS) \in TS. isolated(H, \langle \text{FINISH } f' \rangle \circ FS, GS) \vee awaits(\{T\} \cup TS, f', g) \vee GS = \langle \text{FINISH } g' \rangle \circ GS' \wedge awaits(\{T\} \cup TS, g', f) \quad by \geq$$

$$isolated(H, \langle \text{FINISH } f' \rangle \circ FS, GS) \Rightarrow isolated(H, FS, GS) \quad by \text{ISO-FS, ACC-FS}$$

$$awaits(\{T\} \cup TS, f', g) \Rightarrow \text{false} \quad by \text{awaits Blocks Reduction}$$

$$awaits(\{T\} \cup TS, g', f) \Rightarrow awaits(\{T'\} \cup TS, g', f) \quad by \text{awaits}(\{(f, k, FS) \cup TS, g, f\}) = awaits(\{(f, k', FS') \cup TS, g, f\})$$

$$\forall (g, k', GS) \in TS. isolated(H, FS, GS) \vee awaits(TS, (g, GS), T_2)$$

E-FINISH1:

$$T = (f, k, F \circ FS) \quad F = \langle L, let\ x = finish\ \{t\}\ in\ s, P \rangle^c \quad U = (f', true, \langle L, t, P \rangle^c)$$

$$T' = (f, k, \langle \text{FINISH } f' \rangle^m \circ \langle L, s, P \rangle^c \circ FS)$$

$$TS' = \{T', U\} \cup TS$$

$$isolated(H, \{T\} \cup TS) \Rightarrow isolated(H, \{U\} \cup TS) \quad by \text{ISO-FS, ACC-FS, FINISH1/NewTask copies Vars}$$

$$isolated(H, \{T\} \cup TS) \Rightarrow isolated(H, \{T'\} \cup TS) \quad by \text{T'-def} \quad \langle L, s, P \rangle^c \approx F$$

$$\langle \text{FINISH } f' \rangle^m \circ FS \leq FS$$

where \leq means "is isolated from more tasks" / more constrained

$$isolated(H, \{T', U\}) \quad by \text{FINISH1-def, ISO-TS} \quad (T' \text{ awaits } U)$$

$$isolated(H, \{T\} \cup TS) \wedge isolated(H, \{U\} \cup TS) \wedge isolated(H, \{T', U\}) \Rightarrow isolated(H, \{T, U\} \cup TS)$$

$$\Rightarrow isolated(H, \{T', U\} \cup TS)$$

should hold in general

but certainly does here

(Potential problem: addition of a task adds an await chain.

e.g. T1 awaits T2 awaits T3

Without T2, no await. But adding it should never break isolation

$$TS' = \{T'\} \cup TS$$

$$\{q \mid \text{accRoot}(o, T) \wedge \text{reach}(H, o, q)\}$$

$$= \{q \mid \text{accRoot}(o, T') \wedge \text{reach}(H, o, q)\}$$

= Reachables preserved => Separation preserved

This applies to: E-Null, E-Var, E-Select, E-Assign, E-Return1, E-Return2, E-Open

Same reasoning applies to E-Box, E-Capture, E-Swap

+ they drop some tasks. But:

isolation(H, TS) and (TS' smaller TS) ==> isolation(H, TS')

E-Task-Done similarly

E-Async:

If T + TS isolated ==> T1 + TS isolated and T2 + TS isolated (they each are "smaller" than T as they only contain parts of Ts bindings)

T1 + T2 isolated by definition. T1 has no permission for box(x). T2 has only x.

E-Invoke, E-New: New value guaranteed separated from everything else through OCAP.

But its not trivial to show this!

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