

Isolation

Assume:

Show:

$$1) H, TS \rightsquigarrow H', TS' \quad \text{isolated}(H', TS')$$

$$2) \text{isolated}(H, TS)$$

$$3) \vdash H : *$$

$$4) H \vdash TS ?$$

Proof by case distinction on used reduction rule " \rightsquigarrow ":

E-FINISH2:

$$(4) H, \overbrace{\{(P, \langle \text{FINISH } P' \rangle \circ FS)\} \cup TS}^{T_1} \rightsquigarrow H, \overbrace{\{(P, FS)\} \cup TS}^{T_2}$$

$\text{isolated}(H, T_1 \cup TS)$ by *assump.*

$$\begin{aligned} & \forall (g, GS) \in TS. \text{isolated}(H, \langle \text{FINISH } P' \rangle \circ FS, GS) \vee \text{awaits}_T(TS, (g, GS), T_1) \vee \text{awaits}_T(TS, T_1, (g, GS)) \\ & \text{isolated}(H, \langle \text{FINISH } P' \rangle \circ FS, GS) \Rightarrow \text{isolated}(H, FS, GS) \text{ by } \text{isolated-def} \\ & \text{awaits}_T(TS, (g, GS), T_1) \Rightarrow \text{awaits}_T(TS, (g, GS), (P, FS)) \text{ by } \text{awaits}_T(TS, T_1, (P, FS)) = \text{awaits}_T(TS, T_1, (P, GS)) \\ & \neg \text{awaits}_T(TS, T_1, (g, GS)) \text{ by } (4), \text{awaits}_T \text{ blocks reduction} \\ & \Rightarrow \forall (g, GS) \in TS. \text{isolated}(H, FS, GS) \vee \text{awaits}_T(TS, (g, GS), T_2) \end{aligned}$$

E-FINISH1:

$$(4) H, \overbrace{\{(P, \langle L, \text{let } x = \text{finish } \{t\} \text{ in } s, P \rangle^L \circ FS)\} \cup TS}^{T_1} \rightsquigarrow H, \overbrace{\{(P, \langle \text{FINISH } P' \rangle^x \circ \langle L, s, P \rangle^L \circ FS)\} \cup TS}^{T_2}$$

$\text{isolated}(H, T_1 \cup TS) \wedge \text{isolated}(H, TS \cup \{T_2\}) \wedge \text{awaits}_T(TS, T_2, T_1)$

$$\begin{aligned} & \forall (g, GS) \in TS. \text{isolated}(H, F_1 \circ FS, GS) \vee \text{awaits}_T(TS \cup \{T_2\}, (g, GS), (P, F_1 \circ FS)) \\ & \text{isolated}(H, TS \cup \{T_3\}) \wedge \text{isolated}(H, TS \cup \{T_2\}) \wedge \text{awaits}_T(TS, T_3, T_2) \end{aligned}$$

other dir impossible as $F_1 \neq \text{FINISH}$

Short analysis of remaining rules:

E-NUL: Trivial

E-VAR: $L \text{ isolated} \rightarrow L(y) \text{ isolated} \rightarrow L[x \rightarrow L(y)] \text{ isolated}$

E-SELECT: $L \text{ isolated} \rightarrow y \text{ isolated} \rightarrow y.f \text{ isolated}$

E-ASSIGN: $L \text{ isolated} \rightarrow x, y, z \text{ isolated}$

E-NEW: $\langle C, f \rightarrow \text{null} \rangle$ is isolated

E-INVOKE: $L \text{ isolated} \rightarrow x, y, z \text{ isolated} \rightarrow$ new Frames also isolated

E-RETURN1, 2: Trivial

E-OPEN, E-BOX: Trivial, only shuffling things around on stack

E-CAPTURE: p' available \rightarrow updated field of o also okay

E-SWAP: The objects remain the same, all objects permissions are available too