

# Isolation

Assume:

Show

- 1)  $H, TS, ws \rightsquigarrow H', TS', ws'$
- 2)  $isolated(H, TS, ws)$
- 3)  $\vdash H : *$
- 4)  $H \vdash TS$

$$isolated(H', TS', ws')$$

Proof by case distinction on used reduction rule " $\rightsquigarrow$ ":

$$\text{E-FIMSH2: } H, TS, \{(T, l')\} \cup ws' \rightsquigarrow H, \{T\} \cup TS, ws'$$

$$T = (l, k, Fs) \quad T' = (g, k', Gs)$$

$$\forall T' \in TS + ws. \text{ isolated}(H, Fs, Gs) \vee \text{blocks}(ws, g, l) \vee \text{blocks}(ws, l, g) \quad \text{by 2}$$

*(T, l') reduced  $\Rightarrow \neg \text{blocks}(ws, g, l)$*

$$\forall T' \in TS + ws. \text{ isolated}(H, Fs, Gs) \vee \text{blocks}(ws, l, g)$$

$\Rightarrow$  isolated

E-FIMSH1:

$$T = (l, k, F \circ Fs) \quad F = \langle L, \text{let } x = \text{finish } \{t\} \text{ in } s, P \rangle^c$$

$$T_1 = (l', \text{true}, \langle L, t, P \rangle^c)$$

$$T_2 = (l, k, \langle L[x := \text{null}], s, P \rangle \circ Fs)$$

$$TS' = \{T_1\} \cup TS$$

$$ws' = \{(T_2, l')\} \cup ws$$

$$\left\{ \begin{array}{l} \text{isolated}(H, TS', ws) \quad \text{by } T_1\text{-def} \quad \langle L, t, P \rangle^c \approx F \\ \text{isolated}(H, TS, ws) \quad \text{by } T_2\text{-def} \quad \langle L, s, P \rangle^c \approx F \\ \text{isolated}(H, \{T_1\}, \{(T_2, l')\}) \quad \text{by } \text{blocks}(ws', l', l) \\ \text{isolated}(H, TS', ws) \wedge \text{isolated}(H, TS, ws') \wedge \text{isolated}(H, \{T_1\}, \{T_2\}) \Rightarrow \text{isolated}(H, TS', ws') \end{array} \right.$$

*where  $\approx$  means "is isolated as much as"*

should hold in general  
but certainly does here  
(Potential problem: addition of  
a task adds a block chain.  
e.g. T1 awaits T2 awaits T3  
Without T2, no await. But adding  
it should never break isolation (?))

$$TS' = \{T'\} \cup TS$$

$$\{q \mid \text{accRoot}(o, T) \wedge \text{reach}(H, o, q)\}$$

$$= \{q \mid \text{accRoot}(o, T') \wedge \text{reach}(H, o, q)\}$$

= Reachables preserved => Separation preserved

This applies to: E-Null, E-Var, E-Select, E-Assign, E-Return1, E-Return2, E-Open

Same reasoning applies to E-Box, E-Capture, E-Swap

+ they drop some tasks. But:

isolation(H, TS, WS) and (WS' smaller WS) ==> isolation(H, TS, WS')

E-Task-Done similarly

E-Async:

Similar to E-Finish1

If T + TS isolated ==> T1 + TS isolated and T2 + TS isolated (they each are "smaller" than T as they only contain parts of Ts bindings)

T1 + T2 isolated by definition. T1 has no permission for box(x). T2 has only x.

E-Invoke: With the introduced check it should be trivial. Reachset should be identical

E-New: With fixed invoke also fine. New class -> all null. A non-ocap class is only problematic on invokes which we check separately