901

APPENDIX B | TABLE OF DERIVATIVES

General Formulas

$$1. \ \frac{d}{dx}(c) = 0$$

2.
$$\frac{d}{dx}(f(x) + g(x)) = f'(x) + g'(x)$$

3.
$$\frac{d}{dx}(f(x)g(x)) = f'(x)g(x) + f(x)g'(x)$$

4.
$$\frac{d}{dx}(x^n) = nx^{n-1}$$
, for real numbers n

5.
$$\frac{d}{dx}(cf(x)) = cf'(x)$$

6.
$$\frac{d}{dx}(f(x) - g(x)) = f'(x) - g'(x)$$

7.
$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = \frac{g(x)f'(x) - f(x)g'(x)}{(g(x))^2}$$

8.
$$\frac{d}{dx}[f(g(x))] = f'(g(x)) \cdot g'(x)$$

Trigonometric Functions

9.
$$\frac{d}{dx}(\sin x) = \cos x$$

10.
$$\frac{d}{dx}(\tan x) = \sec^2 x$$

11.
$$\frac{d}{dx}(\sec x) = \sec x \tan x$$

12.
$$\frac{d}{dx}(\cos x) = -\sin x$$

13.
$$\frac{d}{dx}(\cot x) = -\csc^2 x$$

14.
$$\frac{d}{dx}(\csc x) = -\csc x \cot x$$

Inverse Trigonometric Functions

15.
$$\frac{d}{dx}(\sin^{-1}x) = \frac{1}{\sqrt{1-x^2}}$$

16.
$$\frac{d}{dx}(\tan^{-1}x) = \frac{1}{1+x^2}$$

17.
$$\frac{d}{dx}(\sec^{-1}x) = \frac{1}{|x|\sqrt{x^2 - 1}}$$

902 Appendix B

18.
$$\frac{d}{dx}(\cos^{-1}x) = -\frac{1}{\sqrt{1-x^2}}$$

19.
$$\frac{d}{dx}(\cot^{-1}x) = -\frac{1}{1+x^2}$$

20.
$$\frac{d}{dx}(\csc^{-1}x) = -\frac{1}{|x|\sqrt{x^2 - 1}}$$

Exponential and Logarithmic Functions

21.
$$\frac{d}{dx}(e^x) = e^x$$

$$22. \ \frac{d}{dx}(\ln|x|) = \frac{1}{x}$$

23.
$$\frac{d}{dx}(b^x) = b^x \ln b$$

$$24. \ \frac{d}{dx}(\log_b x) = \frac{1}{x \ln b}$$

Hyperbolic Functions

25.
$$\frac{d}{dx}(\sinh x) = \cosh x$$

26.
$$\frac{d}{dx}(\tanh x) = \operatorname{sech}^2 x$$

27.
$$\frac{d}{dx}(\operatorname{sech} x) = -\operatorname{sech} x \tanh x$$

28.
$$\frac{d}{dx}(\cosh x) = \sinh x$$

29.
$$\frac{d}{dx}(\coth x) = -\operatorname{csch}^2 x$$

30.
$$\frac{d}{dx}(\operatorname{csch} x) = -\operatorname{csch} x \operatorname{coth} x$$

Inverse Hyperbolic Functions

31.
$$\frac{d}{dx}(\sinh^{-1}x) = \frac{1}{\sqrt{x^2 + 1}}$$

32.
$$\frac{d}{dx} \left(\tanh^{-1} x \right) = \frac{1}{1 - x^2} (|x| < 1)$$

33.
$$\frac{d}{dx} (\operatorname{sech}^{-1} x) = -\frac{1}{x\sqrt{1-x^2}} \quad (0 < x < 1)$$

34.
$$\frac{d}{dx}(\cosh^{-1}x) = \frac{1}{\sqrt{x^2 - 1}}$$
 (x > 1)

35.
$$\frac{d}{dx} \left(\coth^{-1} x \right) = \frac{1}{1 - x^2} \quad (|x| > 1)$$

36.
$$\frac{d}{dx}(\operatorname{csch}^{-1} x) = -\frac{1}{|x|\sqrt{1+x^2}}(x \neq 0)$$