Functional Hash Maps in a Data Parallel Language

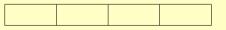
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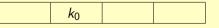
August 22nd, 2025

Contact: widu@di.ku.dk

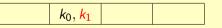
- Keys $k_0, k_1 \in K$.
- Hash function $h: K \rightarrow \{0, 1, 2, 3\}$.
- $h(k_0) = h(k_1) = 1.$



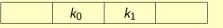
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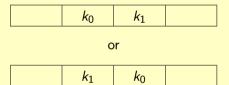


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Core Ideas

- Concurrency.
- Collision resolution.



Hash Maps in Functional Data Parallel Languages

- Avoid collisions.
- Bulk operations.

$$\begin{split} \texttt{map}: (\alpha \to \beta) \to [\textit{n}] \alpha \to [\textit{n}] \beta \\ \texttt{from_array}: [\textit{n}] (\alpha, \beta) \to \texttt{hashmap} \ \alpha \ \beta \end{split}$$

Hash Maps in Functional Data Parallel Languages

- Avoid collisions.
- Bulk operations.
- Fredman-Komlós-Szemerédi (FKS) construction.

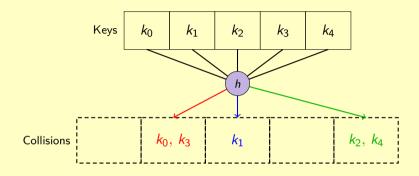
$$\texttt{map}: (\alpha \to \beta) \to [n]\alpha \to [n]\beta$$

$$\texttt{from_array}: [n](\alpha, \beta) \to \texttt{hashmap} \ \alpha \ \beta$$

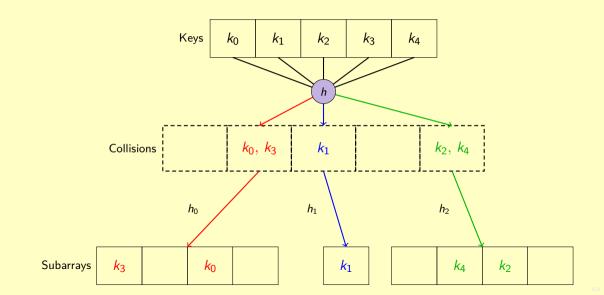
Perfect Hashing with FKS

| Keys | k ₀ | k_1 | k ₂ | k ₃ | k ₄ |
|------|----------------|-------|----------------|----------------|----------------|
|------|----------------|-------|----------------|----------------|----------------|

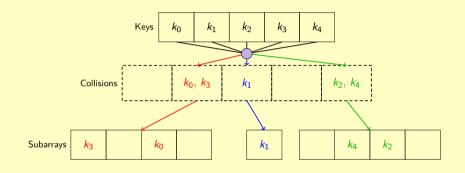
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Perfect Hashing with FKS

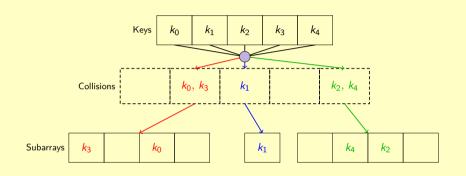


Flattening The Finding of Collision-free Hash Functions



map $\lambda subarrays o$ while h_i leads to collisions do Pick a random hash function h_i

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 \mapsto

while any collisions in subarrays do ${\tt map}\; \lambda \textit{keys} \to {\tt pick}\; {\tt new}\; {\tt hash}\; {\tt functions}$

Benchmarks

| | 64-bit integer Construction | keys $(n = 10^7)$ Lookup |
|-------------------------|-----------------------------|-----------------------------|
| Futhark (hash maps) | 18.3 | 3.3 |
| Futhark (binary search) | 40.9 | 6.2 |
| Futhark (Eytzinger) | 42.3 | 4.3 |
| cuCollections | 2.7 | 1.1 |

All times in milliseconds measured on an A100 GPU.

The End

Towards Efficient Hash Maps in Functional Array Languages

https://arxiv.org/abs/2508.11443

Code

https://github.com/diku-dk/containers

https://github.com/diku-dk/futhark-hashmap-experiments