

UNIVERSITY OF COPENHAGEN
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Parallel Parsing using Futhark
Subtitle

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1 Introduction

2 Theory

2.1 *LL(k)* Parser Generator

For the construction of a *LLP(q, k)* parser generator the construction of first and follow-set [2, p. 5] and a *LL(k)* parser generator is needed. A short explanation of the construction of a *LL(k)* parser generator will be given since in the research of this project $k = 1$ was quite often explained but never $k > 1$ in a manner the author found understable.

The first and follow-set algorithms described comes from modifying Torben Mogensen description in his introductory compiler design book [1, p. 55-65]. The modification are using the truncated product instead of unions as described in the *LL(k)* parser Wikipedia article¹ [3].

Definition 2.1 (Truncated product). Let $G = (N, T, P, S)$ be a context-free grammar and $A, B \subseteq P((N \cup T)^*)$ be sets of symbol strings. The truncated product is defined in the following way.

¹At the time of writing the Wikipedia article does have a description of constructing first and follow-sets for $k > 1$. The problem is the algorithm described does not fullfill the definition of first and follow-sets that is being used in the LLP paper [2, p. 5].

Definition 2.2 (Nonempty substring pairs). Let $G = (N, T, P, S)$ be a context-free grammar and $\omega \in (N \cup T)^*$ be a symbol string. The set of every nonempty way to split ω into two substrings is defined to be.

$$\varphi(\omega) \stackrel{\text{def}}{=} \{(\alpha, \beta) : \alpha \in (T \cup N)^+, \beta \in (T \cup N)^+, \alpha\beta = \omega\}$$

Algorithm 2.1 (Solving $FIRST_k$ set). Let $G = (N, T, P, S)$ be a context-free grammar, the first-sets can be solved as followed.

$$\begin{aligned} FIRST_k(\epsilon) &= \{\epsilon\} \\ FIRST_k(t) &= \{t\} \\ FIRST_k(A) &= \bigcup_{\delta : A \Rightarrow \delta \in P} FIRST_k(\delta) \\ FIRST_k(\omega) &= \bigcup_{(\alpha, \beta) \in \varphi(\omega)} FIRST_k(\alpha) \odot_k FIRST_k(\beta) \end{aligned}$$

This may result in an infinite loop if implemented as is so fixed point iteration is used. Let $\mathcal{M} : N \rightarrow P(T^*)$ be a surjective function which is used as a dictionary which maps nonterminals to sets of terminal strings. $FIRST'_k$ is then the following modified version of $FIRST_k$.

$$\begin{aligned} FIRST'_k(\epsilon, \mathcal{M}) &= \{\epsilon\} \\ FIRST'_k(t, \mathcal{M}) &= \{t\} \\ FIRST'_k(A, \mathcal{M}) &= \mathcal{M}(A) \\ FIRST'_k(\omega, \mathcal{M}) &= \bigcup_{(\alpha, \beta) \in \varphi(\omega)} FIRST'_k(\alpha, \mathcal{M}) \odot_k FIRST'_k(\beta, \mathcal{M}) \end{aligned}$$

This function is then used to solve for a $FIRST_k$ function for a fixed k with fixed point iteration the following way.

1. Initialize a dictionary \mathcal{M}_0 such that $\mathcal{M}_0(A) = \emptyset$ for all $A \in N$.
2. A new dictionary $\mathcal{M}_{i+1} : N \rightarrow P(T^*)$ is constructed by $\mathcal{M}_{i+1}(A) = \bigcup_{\delta : A \Rightarrow \delta \in P} FIRST'_k(\delta, \mathcal{M}_i)$ for all $A \in N$ where \mathcal{M}_i is the last dictionary that was constructed.
3. If $\mathcal{M}_{i+1} = \mathcal{M}_i$ then terminate the algorithm terminates else recompute step 2.

Let \mathcal{M}_f be the final dictionary after the algorithm terminates then it holds that $FIRST_k(\omega) = FIRST'_k(\omega, \mathcal{M}_f)$ if k stays fixed.

Algorithm 2.2 (Solving $FOLLOW_k$ set). Let $G = (N, T, P, S)$ be a context-free grammar, the follow-sets can be solved as followed.

$$FOLLOW_k(A) = \bigcup_{B: B \rightarrow \alpha A \beta \in P} FIRST_k(\beta) \odot_k FOLLOW_k(B)$$

Once again this may not terminate so fixed point iteration can be used with following altered $FOLLOW_k$ and letting $\mathcal{M} : N \rightarrow P(T^*)$ be a surjective function.

$$FOLLOW_k(A, \mathcal{M}) = \bigcup_{B: B \rightarrow \alpha A \beta \in P} FIRST_k(\beta) \odot_k \mathcal{M}(B)$$

This $FOLLOW_k$ function for a fixed k can then be computed using the following algorithm.

1. Extend the grammar $G = (N, T, P, S)$ using $G' = (N', T', P', S') = (N \cup \{S'\}, T \cup \{\square\}, P \cup \{P \rightarrow S\square^k\}, S')$.
2. Initialize a dictionary \mathcal{M}_0 such that $\mathcal{M}_0(A) = \emptyset$ for all $A \in N \setminus \{S\}$ and $\mathcal{M}_0(S) = \{\square^k\}$.
3. A new dictionary $\mathcal{M}_{i+1} : N \rightarrow P(T^*)$ is constructed by $\mathcal{M}_{i+1}(A) = \bigcup_{B: B \rightarrow \alpha A \beta \in P} FIRST_k(\beta) \odot_k \mathcal{M}_i(B)$ for all $A \in N$ where \mathcal{M}_i is the last dictionary that was constructed.
4. If $\mathcal{M}_{i+1} \neq \mathcal{M}_i$ then recompute step 3.
5. Let \mathcal{M}_f be the final dictionary after step 4. is completed. Let \mathcal{M}_u be another dictionary where $\mathcal{M}_u(A) = \{\alpha : \alpha\square^* \in \mathcal{M}_f(A)\}$ for all $A \in N \setminus \{S'\}$

It then holds that $FOLLOW_k(A) = \mathcal{M}_u(A)$ if k stays fixed for grammar G .

2.2 $LLP(q, k)$ Parser Generator

3 Implementation

4 Testing

5 Conclusion

References

- [1] Torben Ægidius Mogensen. *Introduction to Compiler Design*. 2nd ed. London: Springer Cham. DOI: <https://doi.org/10.1007/978-3-319-66966-3>.
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- [3] Wikipedia. *LL parser* — *Wikipedia, The Free Encyclopedia*. <http://en.wikipedia.org/w/index.php?title=LL%20parser&oldid=1145098081>. [Online; accessed 03-May-2023]. 2023.