



# Parallel Parsing

## The Implementation of a Parallel LL Parser Generator

William Henrich Due  
30rd June 2023

KØBENHAVNS UNIVERSITET



# Introduction

- Parallel LL parser generator.
- $LLP(q, k) \subseteq LL(k)$ .
- Pareas uses  $LLP(1, 1)$ .
- Two mistakes in the paper that describes LLP.
- Tested the parser generator thoroughly.

## LL parsing

Here is a LL(1) grammar.

$$1) T \rightarrow R \quad 2) T \rightarrow aTc \quad 3) R \rightarrow \varepsilon \quad 4) R \rightarrow bR$$

## LL parsing

Here is a LL(1) grammar.

$$1) T \rightarrow R \quad 2) T \rightarrow aTc \quad 3) R \rightarrow \varepsilon \quad 4) R \rightarrow bR$$

$$(abc, T, ( ))$$

## LL parsing

Here is a LL(1) grammar.

$$1) T \rightarrow R \quad 2) T \rightarrow aTc \quad 3) R \rightarrow \varepsilon \quad 4) R \rightarrow bR$$

$$(abc, T, ()) \vdash (abc, aTc, 2)$$

## LL parsing

Here is a LL(1) grammar.

$$1) T \rightarrow R \quad 2) T \rightarrow aTc \quad 3) R \rightarrow \varepsilon \quad 4) R \rightarrow bR$$

$$(abc, T, ()) \vdash (abc, aTc, 2) \vdash (bc, Tc, 2)$$

## LL parsing

Here is a LL(1) grammar.

$$1) T \rightarrow R \quad 2) T \rightarrow aTc \quad 3) R \rightarrow \varepsilon \quad 4) R \rightarrow bR$$

$$(abc, T, ()) \vdash (abc, aTc, 2) \vdash (bc, Tc, 2) \vdash (bc, Rc, (2, 1))$$

## LL parsing

Here is a LL(1) grammar.

$$1) T \rightarrow R \quad 2) T \rightarrow aTc \quad 3) R \rightarrow \varepsilon \quad 4) R \rightarrow bR$$

$$(abc, T, ()) \vdash (abc, aTc, 2) \vdash (bc, Tc, 2) \vdash (bc, Rc, (2, 1)) \\ \vdash (bc, bRc, (2, 1, 4))$$



## LL parsing

Here is a LL(1) grammar.

$$1) T \rightarrow R \quad 2) T \rightarrow aTc \quad 3) R \rightarrow \varepsilon \quad 4) R \rightarrow bR$$

$$\begin{aligned} (abc, T, ()) \vdash (abc, aTc, 2) \vdash (bc, Tc, 2) \vdash (bc, Rc, (2, 1)) \\ \vdash (bc, bRc, (2, 1, 4)) \vdash (c, Rc, (2, 1, 4)) \end{aligned}$$

## LL parsing

Here is a LL(1) grammar.

$$1) T \rightarrow R \quad 2) T \rightarrow aTc \quad 3) R \rightarrow \varepsilon \quad 4) R \rightarrow bR$$

$$\begin{aligned} (abc, T, ()) &\vdash (abc, aTc, 2) \vdash (bc, Tc, 2) \vdash (bc, Rc, (2, 1)) \\ &\vdash (bc, bRc, (2, 1, 4)) \vdash (c, Rc, (2, 1, 4)) \\ &\vdash (c, c, (2, 1, 4, 3)) \end{aligned}$$

## LL parsing

Here is a LL(1) grammar.

$$1) T \rightarrow R \quad 2) T \rightarrow aTc \quad 3) R \rightarrow \varepsilon \quad 4) R \rightarrow bR$$

$$\begin{aligned} (abc, T, ()) &\vdash (abc, aTc, 2) \vdash (bc, Tc, 2) \vdash (bc, Rc, (2, 1)) \\ &\vdash (bc, bRc, (2, 1, 4)) \vdash (c, Rc, (2, 1, 4)) \\ &\vdash (c, c, (2, 1, 4, 3)) \vdash (\varepsilon, \varepsilon, (2, 1, 4, 3)) \end{aligned}$$

Accepted! the string “*abc*” can be parsed.

# LLP Parsing

Augment the grammar, this grammar is LL(1) and LLP(1, 1).

$$0) T' \rightarrow \vdash T \dashv$$

Now we parse the string " $\vdash abc \dashv$ " instead and a LLP table is needed.

1. Initial pushdown store.
2. Final pushdown store.
3. Left parse.

	$\vdash$	$a$	$b$	$c$	$\dashv$
$\varepsilon$	$(T', T \dashv, 0)$				
$\vdash$		$(T, Tc, 2)$	$(T, R, (1, 4))$		$(T \dashv, \varepsilon, (1, 3))$
$a$		$(T, Tc, 2)$	$(T, R, (1, 4))$	$(Tc, \varepsilon, (1, 3))$	
$b$			$(R, R, 4)$	$(Rc, \varepsilon, 3)$	$(R \dashv, \varepsilon, 3)$
$c$				$(c, \varepsilon, ())$	$(\dashv, \varepsilon, ())$

## LLP Parsing

Augment the grammar, this grammar is LL(1) and LLP(1, 1).

$$0) \quad T' \rightarrow \vdash T \dashv$$

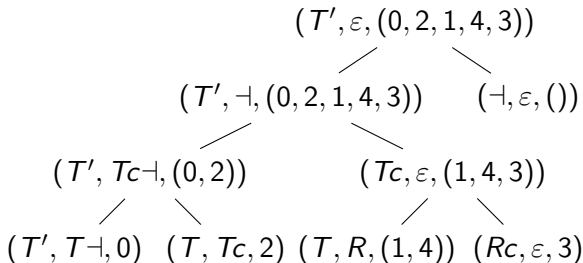
Now we parse the string " $\vdash abc \dashv$ " instead and a LLP table is needed.

1. Initial pushdown store.
2. Final pushdown store.
3. Left parse.

$(\varepsilon, \vdash)$	$(\vdash, a)$	$(a, b)$	$(b, c)$	$(c, \dashv)$
$(T', T \dashv, 0)$	$(T, Tc, 2)$	$(T, R, (1, 4))$	$(Rc, \varepsilon, 3)$	$(\dashv, \varepsilon, ( ))$

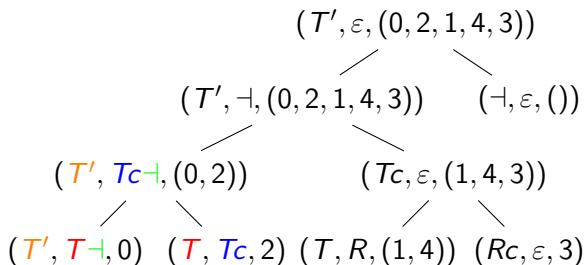
## LLP Parsing using Parallel Reduce

Use the associative **glue** operation.



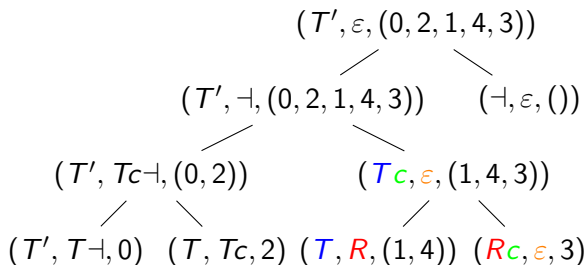
# LLP Parsing using Parallel Reduce

Use the associative **glue** operation.



# LLP Parsing using Parallel Reduce

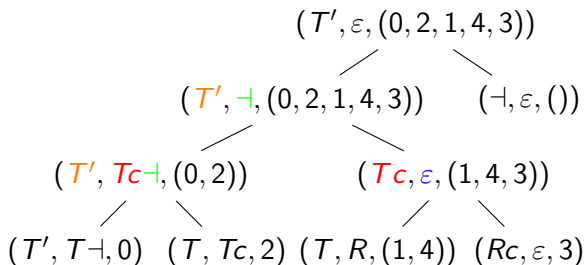
Use the associative **glue** operation.





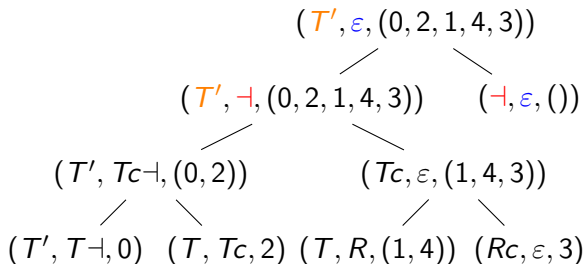
# LLP Parsing using Parallel Reduce

Use the associative **glue** operation.



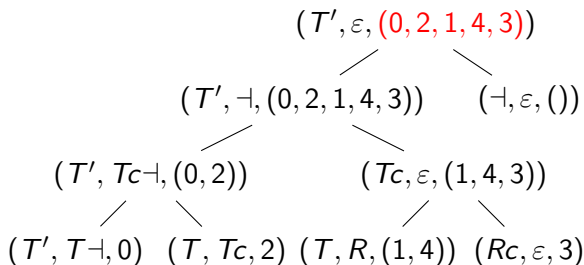
# LLP Parsing using Parallel Reduce

Use the associative **glue** operation.



# LLP Parsing using Parallel Reduce

Use the associative **glue** operation.



## LLP Parsing using Bracket Matching

$(\varepsilon, \vdash)$	$(\vdash, a)$	$(a, b)$	$(b, c)$	$(c, \dashv)$
$(T', T \dashv, 0)$	$(T, Tc, 2)$	$(T, R, (1, 4))$	$(Rc, \varepsilon, 3)$	$(\dashv, \varepsilon, ( ))$

## LLP Parsing using Bracket Matching

$(\varepsilon, \vdash)$	$(\vdash, a)$	$(a, b)$	$(b, c)$	$(c, \dashv)$
$(T', T \dashv, 0)$	$(T, Tc, 2)$	$(T, R, (1, 4))$	$(Rc, \varepsilon, 3)$	$(\dashv, \varepsilon, ( ))$
$(T', T \dashv)$	$(T, Tc)$	$(T, R)$	$(Rc, \varepsilon)$	$(\dashv, \varepsilon)$

# LLP Parsing using Bracket Matching

$(\varepsilon, \vdash)$	$(\vdash, a)$	$(a, b)$	$(b, c)$	$(c, \dashv)$
$(T', T \dashv, 0)$	$(T, Tc, 2)$	$(T, R, (1, 4))$	$(Rc, \varepsilon, 3)$	$(\dashv, \varepsilon, ( ))$
$(T', T \dashv)$	$(T, Tc)$	$(T, R)$	$(Rc, \varepsilon)$	$(\dashv, \varepsilon)$
$(T', \dashv T)$	$(T, cT)$	$(T, R)$	$(Rc, \varepsilon)$	$(\dashv, \varepsilon)$

# LLP Parsing using Bracket Matching

$(\varepsilon, \vdash)$	$(\vdash, a)$	$(a, b)$	$(b, c)$	$(c, \dashv)$
$(T', T \dashv, 0)$	$(T, Tc, 2)$	$(T, R, (1, 4))$	$(Rc, \varepsilon, 3)$	$(\dashv, \varepsilon, ( ))$
$(T', T \dashv)$	$(T, Tc)$	$(T, R)$	$(Rc, \varepsilon)$	$(\dashv, \varepsilon)$
$(T', \dashv T)$	$(T, cT)$	$(T, R)$	$(Rc, \varepsilon)$	$(\dashv, \varepsilon)$
$(\varepsilon, [\dashv]^T)$	$(\lceil^T, [^c]^T)$	$(\lceil^T, [^R]$	$(\lceil^R]^c, \varepsilon)$	$(\lceil^{\dashv}, \varepsilon)$

# LLP Parsing using Bracket Matching

$(\varepsilon, \vdash)$	$(\vdash, a)$	$(a, b)$	$(b, c)$	$(c, \dashv)$
$(T', T \dashv, 0)$	$(T, Tc, 2)$	$(T, R, (1, 4))$	$(Rc, \varepsilon, 3)$	$(\dashv, \varepsilon, ( ))$
$(T', T \dashv)$	$(T, Tc)$	$(T, R)$	$(Rc, \varepsilon)$	$(\dashv, \varepsilon)$
$(T', \dashv T)$	$(T, cT)$	$(T, R)$	$(Rc, \varepsilon)$	$(\dashv, \varepsilon)$
$(\varepsilon, [\dashv [^T)$	$(\lceil ^T, [^c [^T)$	$(\lceil ^T, [^R)$	$(\lceil ^R ]^c, \varepsilon)$	$(\lceil ^\dashv, \varepsilon)$

Now perform bracket matching and assert their types match up.

$$[\dashv [^{\textcolor{blue}{T}} ]^{\textcolor{blue}{T}} [^{\textcolor{green}{c}} [^{\textcolor{orange}{T}} ]^{\textcolor{orange}{T}} [^{\textcolor{red}{R}} ]^{\textcolor{red}{R}} ]^{\textcolor{green}{c}} ]^{\dashv}$$



# LLP Parsing using Bracket Matching

$(\varepsilon, \vdash)$	$(\vdash, a)$	$(a, b)$	$(b, c)$	$(c, \dashv)$
$(T', T \dashv, 0)$	$(T, Tc, 2)$	$(T, R, (1, 4))$	$(Rc, \varepsilon, 3)$	$(\dashv, \varepsilon, ( ))$
$(T', T \dashv)$	$(T, Tc)$	$(T, R)$	$(Rc, \varepsilon)$	$(\dashv, \varepsilon)$
$(T', \dashv T)$	$(T, cT)$	$(T, R)$	$(Rc, \varepsilon)$	$(\dashv, \varepsilon)$
$(\varepsilon, [\dashv [^T)$	$(\lceil ^T, [^c [^T)$	$(\lceil ^T, [^R)$	$(\lceil ^R ]^c, \varepsilon)$	$(\lceil ^\dashv, \varepsilon)$

Now perform bracket matching and assert their types match up.

$$[\dashv [^T ]^T [^c [^T ]^T [^R ]^R ]^c ]^{\dashv}$$

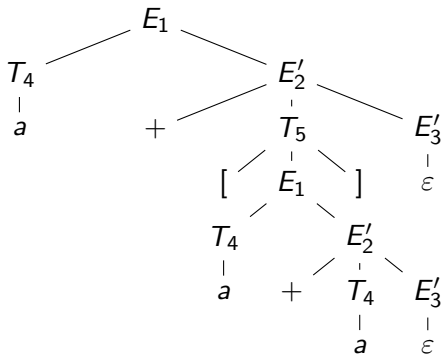
Construct the production sequence.

$$0, 2, 1, 4, 3$$

# Syntax Tree

$$1) E \rightarrow TE' \quad 2) E' \rightarrow +TE' \quad 3) E' \rightarrow \varepsilon \quad 4) T \rightarrow a$$

$$(a + [a + a], E, ()) \vdash^* (\varepsilon, \varepsilon, (1, 4, 2, 5, 1, 4, 2, 4, 3, 3))$$



## LLP Table

To perform LLP parsing a LLP table is needed.

1. Find the initial pushdown.
2. Parse the first symbol of the lookahead string to get the final pushdown store.
3. Construct LLP configuration.

## The Problem

Consider the following augmented LL(2) grammar.

$$0) S' \rightarrow \vdash S \dashv \quad 1) A \rightarrow \varepsilon \quad 2) S \rightarrow aAa \quad 3) A \rightarrow a$$

## The Problem

Consider the following augmented LL(2) grammar.

$$0) S' \rightarrow \vdash S \dashv \quad 1) A \rightarrow \varepsilon \quad 2) S \rightarrow aAa \quad 3) A \rightarrow a$$

The PSLS (Prefix of a Suffix of a Leftmost Sentential) table. The grammar is LLP(2,2) since all the sets are singletons.

	$\dashv$	$a \dashv$	$aa$
$\vdash$			$\{S\}$
$\vdash a$		$\{A\}$	$\{A\}$
$aa$	$\{\dashv\}$	$\{a\}$	

# The Problem

Consider the following augmented LL(2) grammar.

$$0) S' \rightarrow \vdash S \dashv \quad 1) A \rightarrow \varepsilon \quad 2) S \rightarrow aAa \quad 3) A \rightarrow a$$

The PSLS (Prefix of a Suffix of a Leftmost Sentential) table. The grammar is LLP(2,2) since all the sets are singletons.

	$\vdash$	$a \dashv$	$aa$
$\vdash$			$\{S\}$
$\vdash a$		$\{A\}$	$\{A\}$
$aa$	$\{\vdash\}$	$\{a\}$	

A small example of a PSLS value.

$$S \Rightarrow_{lm}^* \vdash S \dashv \Rightarrow \vdash aAa \dashv \Rightarrow^* \vdash aa \dashv$$

This corresponds to the entry  $\text{PSLS}(\vdash a, a \dashv) = \{A\}$ .

## The Problem

Construct the LL(2) table.

	$\vdash a$	$aa$	$a \vdash$
$S'$	$S' \rightarrow \vdash S \vdash$		
$S$		$S \rightarrow aAa$	
$A$		$A \rightarrow a$	$A \rightarrow \varepsilon$

## The Problem

Construct the LL(2) table.

	$\vdash a$	$aa$	$a \dashv$
$S'$	$S' \rightarrow \vdash S \dashv$		
$S$		$S \rightarrow aAa$	
$A$		$A \rightarrow a$	$A \rightarrow \varepsilon$

Try LL parsing the initial pushdown store  $PSLS(\vdash a, a \dashv) = \{A\}$ .

$$(a \dashv, A, ()) \vdash (a \dashv, \varepsilon, 1)$$

Due to this the final pushdown store cannot be determined since the first symbol can not be parsed.



## The Problem

The problem is due to the PSLS definition.

$$\begin{aligned} \text{PSLS}(x, y) = & \{ \alpha : \exists S \Rightarrow_{lm}^* wuA\beta \Rightarrow wxB\gamma \Rightarrow^* wxy\delta, \\ & w, u \in T^*, A, B \in N, \alpha, \beta, \gamma, \delta \in (N \cup T)^*, u \neq x, \\ & \alpha \text{ is the shortest prefix of } B\gamma \text{ such that } \text{FIRST}_1(y) \subseteq \text{FIRST}_1(\alpha) \} \\ \cup & \{ a : \exists S \Rightarrow^* wuA\beta \Rightarrow wxa\gamma \Rightarrow^* wxy\delta, \\ & a = \text{FIRST}_1(y), w, u \in T^*, \beta, \gamma, \delta \in (N \cup T)^*, u \neq x \} \end{aligned}$$

# The Problem

The problem is due to the PSLS definition.

$$\begin{aligned} \text{PSLS}(x, y) = & \{ \alpha : \exists S \Rightarrow_{lm}^* wuA\beta \Rightarrow wxB\gamma \Rightarrow^* wxy\delta, \\ & w, u \in T^*, A, B \in N, \alpha, \beta, \gamma, \delta \in (N \cup T)^*, u \neq x, \\ & \alpha \text{ is the shortest prefix of } B\gamma \text{ such that } \text{FIRST}_1(y) \subseteq \text{FIRST}_1(\alpha) \} \\ \cup & \{ a : \exists S \Rightarrow^* wuA\beta \Rightarrow wxa\gamma \Rightarrow^* wxy\delta, \\ & a = \text{FIRST}_1(y), w, u \in T^*, \beta, \gamma, \delta \in (N \cup T)^*, u \neq x \} \end{aligned}$$

$$\text{FIRST}_1(y) \subseteq \text{FIRST}_1(\alpha)$$

$$\not\Rightarrow$$

$$(y, \text{PSLS}(x, y), ()) \vdash^* (b, \omega, \pi) \text{ where } ab = y, a \in T \text{ and } b \in T^*$$

# The Problem

$$\begin{aligned} \text{PSLS}_k(x, y) = & \{ \alpha : \exists S \Rightarrow_{lm}^* wuA\beta \Rightarrow wxB\gamma \Rightarrow^* wxy\delta, \\ & w, u \in T^*, A, B \in N, \alpha, \beta, \gamma, \delta \in (N \cup T)^*, u \neq x, \\ & \alpha \text{ is the shortest prefix of } B\gamma \text{ such that } y \in \text{FIRST}_k(\alpha) \} \\ \cup & \{ y : \exists S \Rightarrow^* wuA\beta \Rightarrow wxa\gamma \Rightarrow^* wxy\delta, \\ & a = \text{FIRST}_1(y), w, u \in T^*, \beta, \gamma, \delta \in (N \cup T)^*, u \neq x \} \end{aligned}$$

## The Problem

$$\begin{aligned} \text{PSLS}_k(x, y) = & \{ \alpha : \exists S \Rightarrow_{lm}^* wuA\beta \Rightarrow wxB\gamma \Rightarrow^* wxy\delta, \\ & w, u \in T^*, A, B \in N, \alpha, \beta, \gamma, \delta \in (N \cup T)^*, u \neq x, \\ & \alpha \text{ is the shortest prefix of } B\gamma \text{ such that } y \in \text{FIRST}_k(\alpha) \} \\ & \cup \{ y : \exists S \Rightarrow^* wuA\beta \Rightarrow wxa\gamma \Rightarrow^* wxy\delta, \\ & a = \text{FIRST}_1(y), w, u \in T^*, \beta, \gamma, \delta \in (N \cup T)^*, u \neq x \} \end{aligned}$$

- The time complexity is not impacted.
- The problem of deriving too many symbols.

“Since the length of both  $\alpha_i$  and  $\omega_i$  is limited by some constant  $z$  for the grammar, the time complexity is  $O(z) = O(1)$ .” (Vagner, 2007)

## The Problem

Construct the new  $\text{PSLS}_2$  table.

	$\vdash$	$a \vdash$	$aa$
$\vdash$			$\{S\}$
$\vdash a$		$\{Aa \vdash\}$	$\{Aa\}$
$aa$	$\{\vdash\}$	$\{a \vdash\}$	

## The Problem

Construct the new  $\text{PSLS}_2$  table.

	$\neg$	$a \neg$	$aa$
$\vdash$			$\{S\}$
$\vdash a$		$\{Aa \neg\}$	$\{Aa\}$
$aa$	$\{\neg\}$	$\{a \neg\}$	

Try LL parsing the initial pushdown store  $\text{PSLS}_2(\vdash a, a \neg) = \{A\}$ .

$$(a \neg, Aa \neg, ()) \vdash (a \neg, a \neg, 1) \vdash (\neg, \neg, 1)$$

Now the final pushdown store can be found. Resulting in the LLP configuration  $(Aa \neg, \neg, 1)$ .

## The Problem

The problem is due to the PSLS definition.

$$\begin{aligned} \text{PSLS}(x, y) = & \{ \alpha : \exists S \Rightarrow_{lm}^* wuA\beta \Rightarrow wxB\gamma \Rightarrow^* wxy\delta, \\ & w, u, y' \in T^*, a \in T, A, B \in N, \alpha, \beta, \gamma, \delta \in (N \cup T)^*, u \neq x, \\ & y = ay', \alpha \text{ is the shortest prefix of } B\gamma \\ & \text{such that } (y, \alpha, ()) \vdash^* (y', \omega, \pi) \} \\ \cup & \{ a : \exists S \Rightarrow^* wuA\beta \Rightarrow wxa\gamma \Rightarrow^* wxy\delta, \\ & a = \text{FIRST}_1(y), w, u \in T^*, \beta, \gamma, \delta \in (N \cup T)^*, u \neq x \} \end{aligned}$$

# The Problem

The problem is due to the PSLS definition.

$$\begin{aligned} \text{PSLS}(x, y) = & \{ \alpha : \exists S \Rightarrow_{lm}^* wuA\beta \Rightarrow wxB\gamma \Rightarrow^* wxy\delta, \\ & w, u, y' \in T^*, a \in T, A, B \in N, \alpha, \beta, \gamma, \delta \in (N \cup T)^*, u \neq x, \\ & y = ay', \alpha \text{ is the shortest prefix of } B\gamma \\ & \text{such that } (y, \alpha, ()) \vdash^* (y', \omega, \pi) \} \\ \cup & \{ a : \exists S \Rightarrow^* wuA\beta \Rightarrow wxa\gamma \Rightarrow^* wxy\delta, \\ & a = \text{FIRST}_1(y), w, u \in T^*, \beta, \gamma, \delta \in (N \cup T)^*, u \neq x \} \end{aligned}$$

1. Not tested.
2. It was created by Vladislav Vagner.



## The Problem

Using Vladislav Vagners newer PSLS definition.

	$\neg$	$a \neg$	$aa$
$\vdash$			$\{S\}$
$\vdash a$		$\{Aa\}$	$\{A\}$
$aa$	$\{\neg\}$	$\{a\}$	

Do LL parsing.

$$(a \neg, Aa, ()) \vdash (a \neg, a, 1) \vdash (\neg, \varepsilon, 1)$$

## My Mistakes

- The dictionaries are not surjective functions.

## My Mistakes

- The dictionaries are not surjective functions.
- The property tested for is  $\forall s \in T^* : \Pi(s) = \varphi(s)$ .

## My Mistakes

- The dictionaries are not surjective functions.
- The property tested for is  $\forall s \in T^* : \Pi(s) = \varphi(s)$ .
- “This changed definition would still work for LLP parsing.” is conjecture.

## My Mistakes

- The dictionaries are not surjective functions.
- The property tested for is  $\forall s \in T^* : \Pi(s) = \varphi(s)$ .
- “This changed definition would still work for LLP parsing.” is conjecture.
- The stack and input string does not need to equal each other in the definition of  $\vdash$ .

## My Mistakes

- The dictionaries are not surjective functions.
- The property tested for is  $\forall s \in T^* : \Pi(s) = \varphi(s)$ .
- “This changed definition would still work for LLP parsing.” is conjecture.
- The stack and input string does not need to equal each other in the definition of  $\vdash$ .
- “ $\mathcal{M}_0(A) = \emptyset$  for all  $A \in N' \setminus \{S\}$  and  $\mathcal{M}_0(S) = \{\square^k\}$ ” is the correct initial dictionary when constructing  $\text{FOLLOW}_k$ .

## My Mistakes

- The dictionaries are not surjective functions.
- The property tested for is  $\forall s \in T^* : \Pi(s) = \varphi(s)$ .
- “This changed definition would still work for LLP parsing.” is conjecture.
- The stack and input string does not need to equal each other in the definition of  $\vdash$ .
- “ $\mathcal{M}_0(A) = \emptyset$  for all  $A \in N' \setminus \{S\}$  and  $\mathcal{M}_0(S) = \{\square^k\}$ ” is the correct initial dictionary when constructing  $\text{FOLLOW}_k$ .
- $N'$  should be used in step 3. of the  $\text{FOLLOW}_k$  algorithm.

## My Mistakes

- The dictionaries are not surjective functions.
- The property tested for is  $\forall s \in T^* : \Pi(s) = \varphi(s)$ .
- “This changed definition would still work for LLP parsing.” is conjecture.
- The stack and input string does not need to equal each other in the definition of  $\vdash$ .
- “ $\mathcal{M}_0(A) = \emptyset$  for all  $A \in N' \setminus \{S\}$  and  $\mathcal{M}_0(S) = \{\square^k\}$ ” is the correct initial dictionary when constructing  $\text{FOLLOW}_k$ .
- $N'$  should be used in step 3. of the  $\text{FOLLOW}_k$  algorithm.
- Algorithm 2.3 should use  $v_j \in \text{FIRST}_k(\gamma)$  not  $y \in \text{FIRST}_k(\gamma)$ .



## My Mistakes

- The dictionaries are not surjective functions.
- The property tested for is  $\forall s \in T^* : \Pi(s) = \varphi(s)$ .
- “This changed definition would still work for LLP parsing.” is conjecture.
- The stack and input string does not need to equal each other in the definition of  $\vdash$ .
- “ $\mathcal{M}_0(A) = \emptyset$  for all  $A \in N' \setminus \{S\}$  and  $\mathcal{M}_0(S) = \{\square^k\}$ ” is the correct initial dictionary when constructing  $\text{FOLLOW}_k$ .
- $N'$  should be used in step 3. of the  $\text{FOLLOW}_k$  algorithm.
- Algorithm 2.3 should use  $v_j \in \text{FIRST}_k(\gamma)$  not  $y \in \text{FIRST}_k(\gamma)$ .
- When showing the infinite loop,  $\text{FIRST}_k$  should be  $\text{FIRST}_1$ .

## Usefulness

- Parsing large quantities of a formal language.
  - JSON.

# Usefulness

- Parsing large quantities of a formal language.
  - JSON.
  - Large code bases in reproducible environments.

## Usefulness

- Parsing large quantities of a formal language.
  - JSON.
  - Large code bases in reproducible environments.
- The LLP grammar class is limited: problems with JSON, Lua, Regular Language.

## Usefulness

- Parsing large quantities of a formal language.
  - JSON.
  - Large code bases in reproducible environments.
- The LLP grammar class is limited: problems with JSON, Lua, Regular Language.
- I had trouble finding useful grammars that are  $LL(k)$  grammars where  $k > 1$ . But extending the lookback is somewhat different to the lookahead.

## Usefulness

- Parsing large quantities of a formal language.
  - JSON.
  - Large code bases in reproducible environments.
- The LLP grammar class is limited: problems with JSON, Lua, Regular Language.
- I had trouble finding useful grammars that are  $LL(k)$  grammars where  $k > 1$ . But extending the lookback is somewhat different to the lookahead.
- Parsing more complex grammars, an example is allowing “—” to mean both the binary and unary operation for numbers, while ignore parenthesis. When testing this such a grammar was found to be  $LLP(2, 1)$ .

## Usefulness

- Parsing large quantities of a formal language.
  - JSON.
  - Large code bases in reproducible environments.
- The LLP grammar class is limited: problems with JSON, Lua, Regular Language.
- I had trouble finding useful grammars that are  $LL(k)$  grammars where  $k > 1$ . But extending the lookback is somewhat different to the lookahead.
- Parsing more complex grammars, an example is allowing “—” to mean both the binary and unary operation for numbers, while ignore parenthesis. When testing this such a grammar was found to be  $LLP(2, 1)$ .
- There exists a larger grammar class  $LLP^*$  which can parse all regular languages and more of LL.

# A Little Example

**A LISP parser**