finc584_ps5

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Problem 1a

name	coefs	se	t
(Intercept)	0.010	$0.001 \\ 0.052$	12.393 -2.382

Both variables are significant at the 95% level.

Problem 1b

$$cov(OV_{t-1}, OV_t) = cov(V_{t-1} + \eta_{t-1}, V_t + \eta_t) =$$

$$cov(V_{t-1}, V_t) + cov(V_{t-1}, \eta_t) + cov(V_t, \eta_{t-1}) + cov(\eta_{t-1}, \eta_t) = cov(V_{t-1}, V_t) > 0$$

$$cov(OV_{t-1}, \epsilon_t) = cov(V_{t-1} + \eta_{t-1}, \epsilon_t) = cov(V_{t-1}, \epsilon_t) + cov(\eta_{t-1}, \epsilon_t) = 0$$

name	coefs	se_robust
$\overline{(Intercept)}$	0.012	0.001
OV	-0.195	0.058

The coefficients are different but still fairly close to the original estimate. The new estimates are greater in magnitude which is typical for errors-in-variables problems.

Problem 1c

```
vrp_gmm <- vrp %>%
  mutate(ov_lag1 = lag(OV), ov_lag5 = lag(OV, 5)) \%\% drop_na()
12_metric <- function(x){</pre>
  return(sum(colMeans(x)^2))
gmm_moments <- function(betas, data = vrp_gmm){</pre>
  e <- (data["VRP"] - betas[1] - betas[2]*data["OV"]) %>% as.matrix()
  z <- data[c("ov_lag1", "ov_lag5")] %>% as.matrix()
  #moment_conditions
  moment1 <- e
  moment2 \leftarrow e * z[,1]
  moment3 \leftarrow e * z[,2]
  return(cbind(moment1, moment2, moment3))
}
naive \leftarrow optim(par = c(0,0), fn = function(betas)
  12_metric(gmm_moments(betas, data = vrp_gmm)))
w_optimal <- solve(t(gmm_moments(naive$par)) %*% gmm_moments(naive$par))</pre>
optimal_beta <- optim(par = c(0,0), fn = function(betas)</pre>
 t(colMeans(gmm_moments(betas))) %*% w_optimal %*% colMeans(gmm_moments(betas)))
```

var	naive	optimal
(intercept)	0.0136	0.0117
OV	-0.2747	-0.1528

The optimal GMM estimates are similar to what we found in the 2SLS estimates from part B.