



AP Calculus BC

Q3 Interim Assessment

Test Booklet 1

Multiple Choice - Non-Calc

April 2017

Student Name: _____

Period: _____

Teacher: _____

School: _____

A A

CALCULUS BC

SECTION I, Part A

Time—60 minutes

Number of questions—30

NO CALCULATOR IS ALLOWED FOR THIS PART OF THE EXAM.

Directions: Solve each of the following problems, using the available space for scratch work. After examining the form of the choices, decide which is the best of the choices given and place the letter of your choice in the corresponding box on the answer sheet. No credit will be given for anything written in this exam booklet. Do not spend too much time on any one problem.

In this exam:

- (1) Unless otherwise specified, the domain of a function f is assumed to be the set of all real numbers x for which $f(x)$ is a real number.
- (2) The inverse of a trigonometric function f may be indicated using the inverse function notation f^{-1} or with the prefix “arc” (e.g., $\sin^{-1} x = \arcsin x$).

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A A

1. If $f(x) = (x^2 - 3)^4$, then $f'(1) =$

- (A) -64 (B) -32 (C) -16 (D) 32

2. $\int_{-2}^1 (8x^3 - 3x^2) \, dx =$

- (A) -561 (B) -90 (C) -39 (D) 81

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3. An object moves in the xy -plane so that its position at any time t is given by the parametric equations $x(t) = t^3 - 3t^2 + 2$ and $y(t) = \sqrt{t^2 + 16}$. What is the rate of change of y with respect to x when $t = 3$?
- (A) $\frac{1}{90}$ (B) $\frac{1}{15}$ (C) $\frac{3}{5}$ (D) $\frac{5}{2}$

4. Snow is falling at a rate of $r(t) = 2e^{-0.1t}$ inches per hour, where t is the time in hours since the beginning of the snowfall. Which of the following expressions gives the amount of snow, in inches, that falls from time $t = 0$ to time $t = 5$ hours?
- (A) $2e^{-0.5} - 2$
- (B) $0.2 - 0.2e^{-0.5}$
- (C) $4 - 4e^{-0.5}$
- (D) $20 - 20e^{-0.5}$

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7. At time $t \geq 0$, a particle moving in the xy -plane has a velocity vector given by $v(t) = \langle \cos(2t), e^{3t} \rangle$. What is the acceleration vector of the particle?

(A) $\langle -2 \sin(2t), 3e^{3t} \rangle$

(B) $\langle -2 \sin(2t), e^{3t} \rangle$

(C) $\left\langle \frac{1}{2} \sin(2t), \frac{1}{3} e^{3t} \right\rangle$

(D) $\langle 2 \sin(2t), 3e^{3t} \rangle$

8. Consider the geometric series $\sum_{n=1}^{\infty} a_n$, where $a_n > 0$ for all n . The first term of the series is $a_1 = 48$, and the third term is $a_3 = 12$. Which of the following statements about $\sum_{n=1}^{\infty} a_n$ is true?

$$(A) \quad \sum_{n=1}^{\infty} a_n = 64$$

$$(B) \sum_{n=1}^{\infty} a_n = 96$$

(C) $\sum_{n=1}^{\infty} a_n$ converges, but the sum cannot be determined from the information given.

(D) $\sum_{n=1}^{\infty} a_n$ diverges.

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10. Which of the following series can be used with the limit comparison test to determine whether the series

$$\sum_{n=1}^{\infty} \frac{n^2}{n^3 + 1} \text{ converges or diverges?}$$

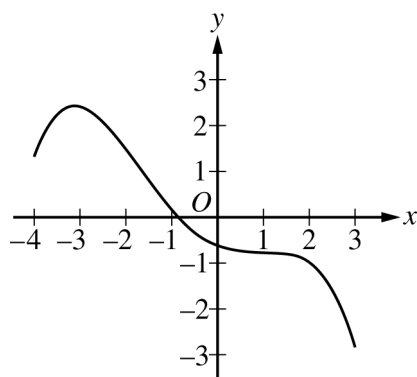
- (A) $\sum_{n=1}^{\infty} \frac{1}{n}$ (B) $\sum_{n=1}^{\infty} \frac{1}{n^3}$ (C) $\sum_{n=1}^{\infty} \frac{n}{n+1}$ (D) $\sum_{n=1}^{\infty} \frac{1}{n^2+1}$

(A) $\frac{6e^5 - 1}{25}$ (B) $\frac{4e^5 + 1}{25}$ (C) $\frac{1 - e^3}{3}$ (D) e^4

12. An object moves along a straight line so that at any time t its acceleration is given by $a(t) = 6t$. At time $t = 0$, the object's velocity is 10 and the object's position is 7. What is the object's position at time $t = 2$?

- (A) 22 (B) 27 (C) 28 (D) 35

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Graph of f

13. The graph of a differentiable function f is shown above on the closed interval $[-4, 3]$. How many values of x in the open interval $(-4, 3)$ satisfy the conclusion of the Mean Value Theorem for f on $[-4, 3]$?
- (A) Zero (B) One (C) Two (D) Three

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14. $\int_0^x \sin(t^6) \, dt =$

$$(A) \quad \frac{x^2}{2} - \frac{x^4}{4} + \frac{x^6}{6} - \dots + \frac{(-1)^{n+1}x^{2n}}{2n} + \dots$$

$$(B) \quad \frac{x^2}{2} - \frac{x^4}{4 \cdot 3!} + \frac{x^6}{6 \cdot 5!} - \cdots + \frac{(-1)^{n+1} x^{2n}}{2n \cdot (2n-1)!} + \cdots$$

$$(C) \quad \frac{x^7}{7} - \frac{x^{19}}{19} + \frac{x^{31}}{31} - \dots + \frac{(-1)^{n+1} x^{6(2n-1)+1}}{6(2n-1)+1} + \dots$$

$$(D) \quad \frac{x^7}{7} - \frac{x^{19}}{19 \cdot 3!} + \frac{x^{31}}{31 \cdot 5!} - \cdots + \frac{(-1)^{n+1} x^{6(2n-1)+1}}{(6(2n-1)+1) \cdot (2n-1)!} + \cdots$$

15. The speed of a runner, in miles per hour, on a straight trail is modeled by

$f(m) = \frac{1}{10}(-2m^3 + 9m^2 - 12m) + 7$, where m is the runner's distance, in miles, from the start of the trail.

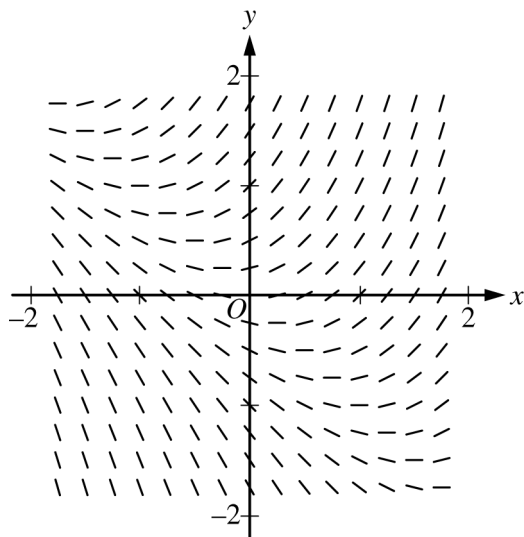
What is the maximum speed of the runner for $0 \leq m \leq 3$?

- (A) 6.5 (B) 6.6 (C) 7.0 (D) 7.5

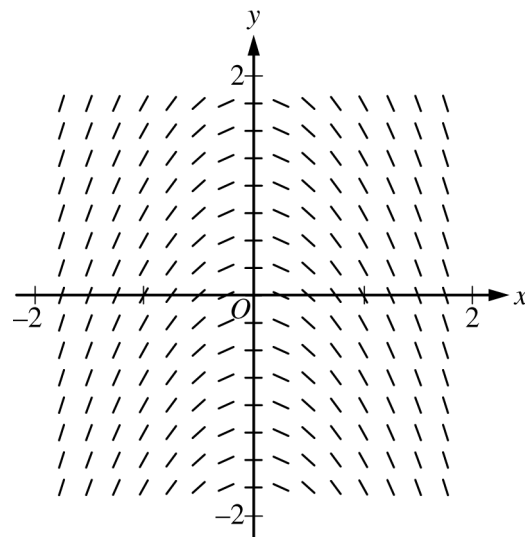
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16. Which of the following could be a slope field for the differential equation $\frac{dy}{dx} = x^2 + y$?

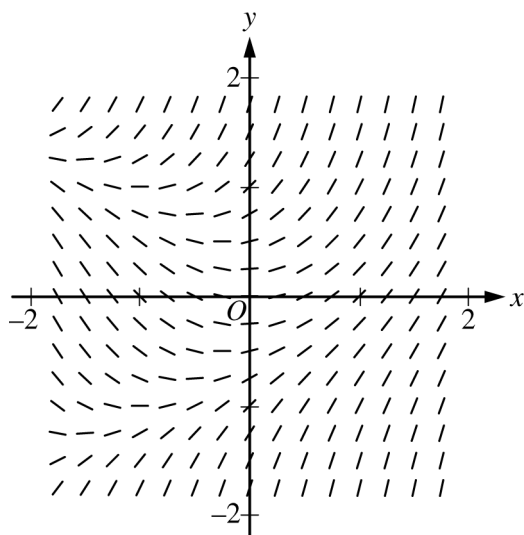
(A)



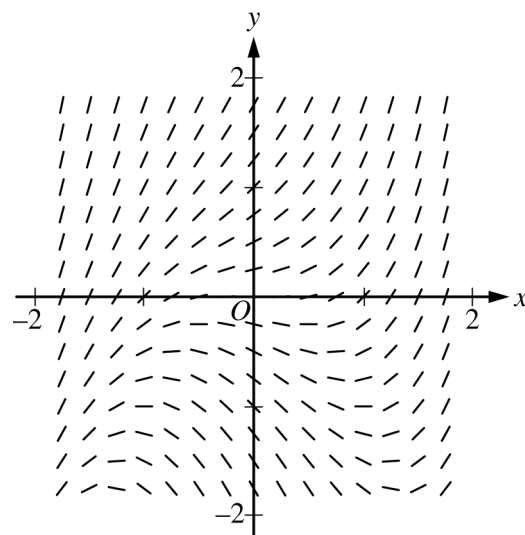
(B)



(C)



(D)



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17. $\int \frac{8x - 10}{(2x - 1)(x + 1)} dx =$

- (A) $-4 \ln |2x - 1| + 6 \ln |x + 1| + C$
 (B) $-2 \ln |2x - 1| + 6 \ln |x + 1| + C$
 (C) $3 \ln |2x - 1| - 4 \ln |x + 1| + C$
 (D) $6 \ln |2x - 1| - 4 \ln |x + 1| + C$

18. What is the slope of the line tangent to the polar curve $r = 2 \cos \theta - 1$ at the point where $\theta = \pi$?

- (A) -3 (B) 0 (C) 3 (D) The slope is undefined.

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20. What is the radius of convergence for the series $\sum_{n=0}^{\infty} \frac{(x-5)^n}{2^n(2n+3)^2}$?
- (A) $\frac{1}{2}$ (B) 1 (C) 2 (D) 5

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(D) The integral diverges because $\lim_{x \rightarrow \frac{\pi}{2}^-} \tan x$ does not exist.

(D) II and III only

A A

23. $\int_0^{\ln 2} \frac{e^x}{1 + (e^x - 1)^2} dx =$

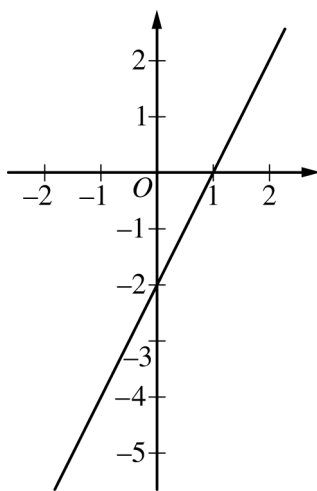
- (A) $\arctan(\ln 2)$ (B) $\ln 2$ (C) $\frac{\pi}{4}$ (D) $\frac{\pi}{2}$

24. $\lim_{x \rightarrow 3} \frac{\tan(x-3)}{3e^{x-3} - x}$ is

- (A) 0 (B) $\frac{1}{3}$ (C) $\frac{1}{2}$ (D) nonexistent

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Graph of f

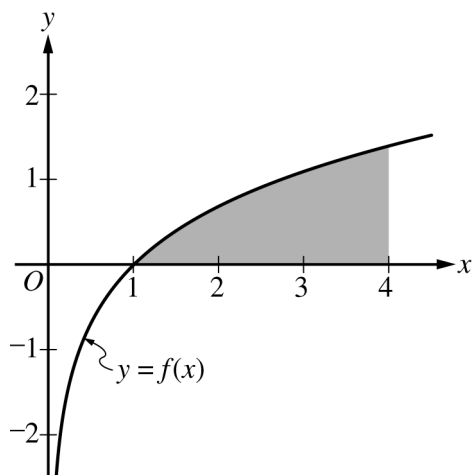
27. The graph of the function f is shown above for $-2 < x < 2$. Let g be the function defined by $g(x) = \int_0^x f(t) \, dt$.

On what open interval is g negative and decreasing?

- (A) $-2 < x < 0$ only
- (B) $-2 < x < 1$
- (C) $0 < x < 1$ only
- (D) $0 < x < 2$

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29. The function f is given by $f(x) = \ln x$. The graph of f is shown above. Which of the following limits is equal to the area of the shaded region?

- (A) $\lim_{n \rightarrow \infty} \sum_{k=1}^n \left(1 + \ln \left(\frac{3k}{n} \right) \right) \frac{3}{n}$
- (B) $\lim_{n \rightarrow \infty} \sum_{k=1}^n \ln \left(1 + \frac{3k}{n} \right) \frac{3}{n}$
- (C) $\lim_{n \rightarrow \infty} \sum_{k=1}^n \ln \left(\frac{4}{n} \right) \left(1 + \frac{4k}{n} \right)$
- (D) $\lim_{n \rightarrow \infty} \sum_{k=1}^n \ln \left(1 + \frac{4k}{n} \right) \frac{4}{n}$

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- (A) $\frac{1}{2^4 \cdot 5!}$
 (B) $\frac{1}{2^5 \cdot 6!}$
 (C) $\frac{1}{2^6 \cdot 7!}$
 (D) $\frac{1}{2^{10} \cdot 11!}$

DO NOT GO ON TO PART B UNTIL YOU ARE TOLD TO DO SO.