## Uncommon Schools Change History.

### **AP Calculus AB**

Q3 Interim Assessment April 2016

# Section II – Part B (60 Minutes) No Calculators Allowed

Student Name:			
School:			
Teacher:			

#### NO CALCULATOR ALLOWED

t (seconds)	0	3	5	8	12
k(t) (feet per second)	0	5	10	20	24

- 3. Kathleen skates on a straight track. She starts from rest at the starting line at time t = 0. For  $0 < t \le 12$  seconds, Kathleen's velocity k, measured in feet per second, is differentiable and increasing. Values of k(t) at various times t are given in the table above.
  - (a) Use the data in the table to estimate Kathleen's acceleration at time t=4 seconds. Show the computations that lead to your answer. Indicate units of measure.

(b) Use a right Riemann sum with the four subintervals indicated by the data in the table to approximate  $\int_0^{12} k(t) dt$ . Indicate units of measure. Is this approximation an overestimate or an underestimate for the value of  $\int_0^{12} k(t) dt$ ? Explain your reasoning.

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(c) Nathan skates on the same track, starting 5 feet ahead of Kathleen at time t = 0. Nathan's velocity, in feet per second, is given by  $n(t) = \frac{150}{t+3} - 50e^{-t}$ . Write, but do not evaluate, an expression involving an integral that gives Nathan's distance from the starting line at time t = 12 seconds.

(d) Write an expression for Nathan's acceleration in terms of t.

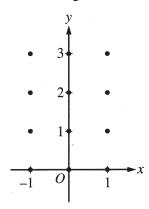
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#### NO CALCULATOR ALLOWED

- 4. Consider the differential equation  $\frac{dy}{dx} = \frac{x(y-1)}{4}$ .
  - (a) On the axes provided, sketch a slope field for the given differential equation at the twelve points indicated.



(b) Let y = f(x) be the particular solution to the differential equation with the initial condition f(1) = 3. Write an equation for the line tangent to the graph of f at the point (1, 3) and use it to approximate f(1.4).

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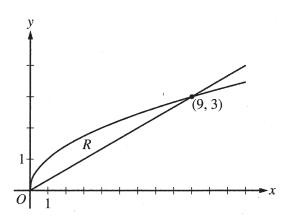
(c) Find the particular solution y = f(x) to the given differential equation with the initial condition f(1) = 3.

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- 5. Let R be the region in the first quadrant enclosed by the graphs of  $g(x) = \sqrt{x}$  and  $h(x) = \frac{x}{3}$ , as shown in the figure above.
  - (a) Find the area of region R.

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(b) Write, but do not evaluate, an expression involving one or more integrals that gives the volume of the solid generated when R is revolved about the horizontal line y = 4.

(c) Find the maximum vertical distance between the graph of g and the graph of h between x = 0 and x = 16. Justify your answer.

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6. Let  $g(x) = 4(x+1)^{-2/3}$  and let f be the function defined by  $f(x) = \int_0^x g(t) dt$  for  $x \ge 0$ .

(a) Find f(26).

(b) Determine the concavity of the graph of y = f(x) for x > 0. Justify your answer.

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(c) Let h be the function defined by h(x) = x - f(x). Find the minimum value of h on the interval  $0 \le x \le 26$ .

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