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## Study of the accuracy of ultrasonic flowmeters for liquid

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### Abstract

How to estimate the differential time of flight accurately is a challenging problem in the area of ultrasonic flow measurement. High time resolution is necessary, especially in a small inner diameter, short sound path measurement environment, since sound velocity in the liquid is quite fast and the order of magnitude is nanosecond. A newer method to obtain the differential time of flight is a Spline-Based algorithm. Although the calculation accuracy of a Spline-Based algorithm is higher than the common method, cross-correlation algorithm, the calculated quantity of this algorithm is huge. For this reason, an improved Spline-based algorithm is proposed to reduce the computational cost while keeping the accuracy. In addition, installation location of transducers is one of the most important factors affecting the measurement accuracy of ultrasonic flowmeter. This paper also analyzes the affection of the differential separation distance between transducers. Experiments have shown that the improved algorithm is effective and the separation distance affects the result seriously.

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### 1. Introduction

Ultrasonic flowmeters (USFM) have been rapidly developed in recent years. Due to the non-destructive testing and facilitation of installation and removal, USFMs became more and more important in fluid flow

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measurement<sup>[1]</sup>. These meters can be used as a spool-piece meter or as a clamp-on meter. But the transit-time clamp-on USFMs are not very robust. Many papers aim to improve the accuracy of the flowmeter. The fluid velocity distribution in the pipe can be obtained using the computational fluid dynamic (CFD) modeling approach<sup>[2]</sup>. The relationships between correction factor K and Reynolds number for different ultrasound paths can be obtained through numerical calculation<sup>[3]</sup>. The accuracy of measuring flow rates changes with the incidence angles<sup>[4]</sup> and upstream installations<sup>[5]</sup>. Especially, absolute propagation time (the upstream and downstream transit times) always contains the delays caused by emitting and receiving circuits and the transit time when the signal spreads in the wall and acoustic wedge. Thus this paper attempts to address this problem.

One of the most important parameters is the differential of transit time. We can get it by several ways. The first one is the cross-correlation algorithm. The peak-searching algorithm identifies the peak of the discrete function of the cross-correlation using Cosine interpolation algorithm<sup>[6]</sup>, Gaussian interpolation algorithm<sup>[7]</sup> or Parabolic interpolation algorithm. The second one is the sample tracking algorithm. In this algorithm, the time shift of each sample in a delayed echo signal is measured with respect to a continuous, interpolated representation of the reference echo signal<sup>[8]</sup>. The third one is Spline-Based algorithm. The algorithm uses cubic splines to produce a continuous time representation of a reference signal, and then computes an analytical matching function between this reference and a delayed signal. This method is about 500 times better than normalized cross-correlation and entails a substantial computational cost<sup>[9]</sup>.

The proposed method improves the Spline-Based algorithm by combining with the cross-correlation algorithm. The improved algorithm reduces the computational cost without reducing the accuracy. This proposed method is evaluated in experiments. In addition, an important part of the installation process is the transducer separation distance previously described. If the signal received by a transducer when set up at the wrong position, the calculation result would be definitely wrong. This paper analyzes the affection of the differential separation distance between transducers to show the importance to determine the correct position. Experiments have shown that the separation distance affects the result seriously.

## 2. Proposed Method

The flow velocity is calculated by Eq.(1)

$$v = \frac{2D}{\sin 2\gamma} \cdot \frac{\Delta t}{(t_{up} - t_{delay}) \cdot (t_{dn} - t_{delay})} \quad (1)$$

$t_{dn}$  and  $t_{up}$  in (1) represent the downstream and upstream transit times.  $\Delta t$  denotes the differential time of

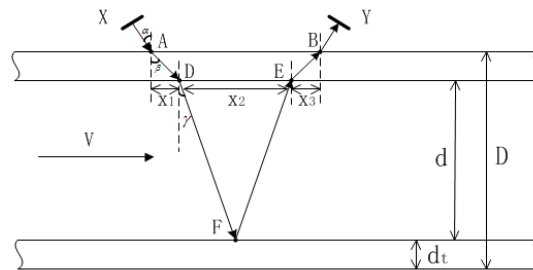


Fig.1. Ultrasonic transducers are mounted in accordance with V-shape.

flight.  $t_{\text{delay}}$  is the transit time that signal takes when it is not in the liquid.  $D$  is the diameter of the steel pipes.  $\gamma$  is the refraction angle when the signal passes through the steel-water interface.

Ultrasonic transducers are mounted in accordance with the V-shape shown in Fig.1. Transducer X emits ultrasonic waves, and transducer Y receive them. On the contrary, Transducer Y emits ultrasonic waves, and transducer X receive them.

### 2.1. Improved Spline-Based Algorithm

The differential time of flight,  $\Delta t$ , is a key parameter, and its order of magnitude is nanoseconds. Since sound velocity in the water is quite fast, so high time resolution is necessary, especially in a small inner diameter, short sound path measurement environment. Typically, the cross-correlation algorithm is the most widely used algorithm. And this method is good at restraining white noise. But simulation results show that the calculation accuracy of the Spline-Based algorithm is higher than the cross-correlation algorithm.

Assume  $S_1$  and  $S_2$  are discrete signals of reference signal and delayed signal (continuous time signal), and each group signal has 2048 points. Extract the kernel signal from  $S_1$  and  $S_2$  starts from the same point. The kernel signal is the effective part of the ultrasonic. Assume  $S_1[n]$  and  $S_2[n]$  represent the kernel signal. The length of  $S_1[n]$  is  $N$  and The length of  $S_2[n]$  is  $M$ , where  $M < N$ . As is shown in Fig.2, extracting kernel signal is depending on experience. If  $M$  and  $N$  are too big, the kernel signal will include useless points. In contrast, if  $M$  and  $N$  are too small, the useful points will be missed.

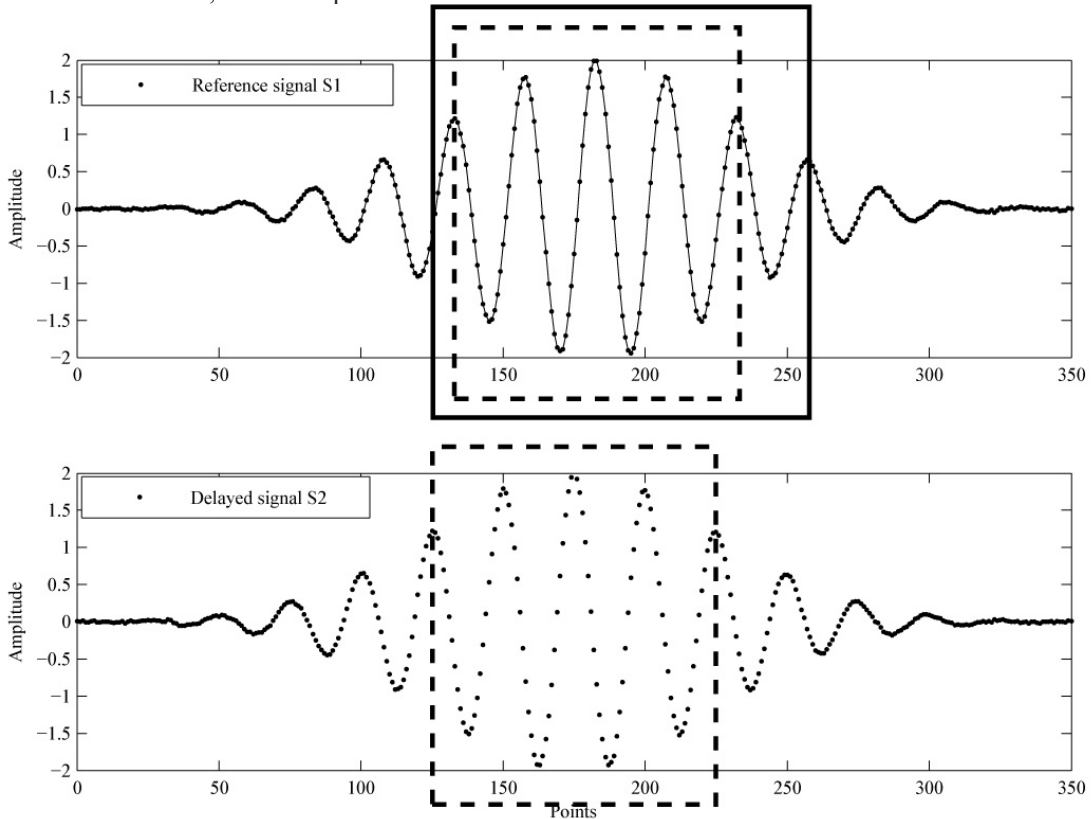


Fig.2. Kernel signal extraction

Signal  $S_1[n]$  is processed by cubic splines. The spline interpolant is piecewise continuous over an interval  $[0 \ 1] \cdot \sigma$ ,  $\sigma$  is sampling period, as Eq.(2). Signal  $S_2[n]$  is still discrete signal.

$$S_1(t) = \begin{cases} f_1(t) = a_1 \cdot (t/\sigma - T_1)^3 + b_1 \cdot (t/\sigma - T_1)^2 + c_1 \cdot (t/\sigma - T_1) + d_1, & 0 < t < 1 \cdot \sigma \\ \dots & \dots \\ f_i(t) = a_i \cdot (t/\sigma - T_i)^3 + b_i \cdot (t/\sigma - T_i)^2 + c_i \cdot (t/\sigma - T_i) + d_i, & (i-1)\sigma < t < i \cdot \sigma \\ \dots & \dots \\ f_{N-1}(t) = a_{N-1} \cdot (t/\sigma - T_{N-1})^3 + b_{N-1} \cdot (t/\sigma - T_{N-1})^2 + c_{N-1} \cdot (t/\sigma - T_{N-1}) + d_{N-1}, & (N-2)\sigma < t < (N-1) \cdot \sigma \end{cases} \quad (2)$$

$f_i(t)$  is the  $i$ -th piecewise function. There are  $N-1$  segments in total.. If  $T_i=i-1$  and  $t'=t/\sigma-T_i$ , the Eq.(2) simplifies to Eq.(3)

$$\begin{cases} f_1(t') = a_1 \cdot (t')^3 + b_1 \cdot (t')^2 + c_1 \cdot (t') + d_1, & 0 < t' < 1 \\ \dots & \dots \\ f_i(t') = a_i \cdot (t')^3 + b_i \cdot (t')^2 + c_i \cdot (t') + d_i, & 0 < t' < 1 \\ \dots & \dots \\ f_{N-1}(t') = a_{N-1} \cdot (t')^3 + b_{N-1} \cdot (t')^2 + c_{N-1} \cdot (t') + d_{N-1}, & 0 < t' < 1 \end{cases} \quad (3)$$

Eq.(3) shows abscissa of each segment starts from 0. The value of  $t$  obtained by Eq.(4) that minimizes the  $\varepsilon(t')$  is called local delay estimate here.

$$\varepsilon(t') = \sum_{i=1}^M (f_i(t') - S_2[i])^2 \quad (4)$$

The subscript of  $f_i(t')$  is different from Eq.(3). Signal  $S_2[n]$  has only  $M$  points, so  $f_i(t')$  is the  $i$ 'th segment of  $M$  segments which involved in computation. First time,  $k=0$ , points of signal  $S_2[n]$  compute with the first to the  $M$ 'th segment of  $S_1[t]$ . Second time,  $k=1$ , points of signal  $S_2[n]$  compute with the second to the  $M+1$ 'th segment of  $S_1[t]$ , and so on. Finally, there are  $(N-M)$   $t$ -values. And there must be a  $t$  lying between 0 and 1, which called global delay estimate. Differential time of flight  $\Delta t$  is calculated by Eq.(5).

$$\Delta t = (t' + k) \cdot \partial \quad (5)$$

The calculated quantity of the Spline-Based algorithm is huge. The proposed method can reduce the running time of Spline-Based algorithm while keeping the accuracy.

Before calculating Eq.(4), we can find the maximum point  $m_i$  of the cross-correlation function of discrete signals  $S_1$  and  $S_2$  by Fast Fourier Transform. If  $m_{i-1} < m_{i+1}$ , then  $k=i$ ; Else if  $m_{i-1} > m_{i+1}$ ,  $k=i-1$ .  $k$  is the parameter we need in Eq.(5). Since  $k$  is a known parameter, we can get  $t$  by computing only once. Points of signal  $S_2[n]$  compute with the  $k+1$  to the  $k+M$ 'th segment of  $S_1[t]$  by Eq.(4). It is clear that  $N-M-1$  times calculate quantities are removed. And the speed of algorithm will be increased.

## 2.2. Initial position of transducers

Installation location of transducers is one of the most important factors affecting the measurement accuracy

of ultrasonic flowmeter. When the wall thickness, the wall material, and the fluid medium are all known quantities and the acoustic path is determined in accordance with the V-shape, the separate distance between each transducer should be definite. Assume transducer acoustic wedge is organic glass, and the material of the wall is steel. The fluid medium is water and incidence angle of ultrasonic wave is 37 degree.

The Snell law is given in Eq.(6) and is used to calculate the refraction angle in different medium.

$$\sin \alpha / C_1 = \sin \beta / C_2 = \sin \gamma / C_3 \quad (6)$$

$\alpha$  is the incident angle when signal passes through the organic glass-steel interface.  $\beta$  is the refraction angle when signal passes through the organic glass-steel interface or the incident angle when signal passes through the steel-water interface.  $\gamma$  is the refraction angle when signal passes through the steel-water interface.  $C_1$ ,  $C_2$  and  $C_3$  are sound velocities in organic glass, steel wall and water respectively.

$\alpha=37^\circ$ , and longitudinal wave velocity in organic glass is 2730m/s. If shear wave velocity in steel wall is 3230m/s, we can get  $\beta=45^\circ$ . Longitudinal wave velocity in water is 1480m/s at 20°C, then  $\gamma=19^\circ$ . The differential distance between transducer X and transducer Y is calculated based these angles.

$$L_{AB} = 2 \cdot d_t \cdot \tan \beta + 2 \cdot d \cdot \tan \gamma \quad (7)$$

In Eq.(7),  $d_t$  is wall thickness,  $d$  is inner diameter. At the same time, the value of  $L_{AB}$  in turn affect the value of  $\gamma$  in Eq(1). Assume the position of transducer Y shifts to the right axially 2mm from the correct position. This will cause to refraction angle,  $\gamma$ , 3 degrees bigger than the true value. As a result, the calculation error of water velocity will be up to 11% based on Eq.(1). Moreover, this impact is more pronounced to small diameter measurement environment. So it is necessary to fine tune the transducer location.

### 3. Experiment results

The experiments are carried out using the clamp-on meter mounted on a stainless-steel pipe which outer diameter is 23 mm and wall thickness is 3 mm. The fluid medium is water. Control chip is FPGA of Altera's EP2C8Q208.

#### 3.1. Calculating the differential time of flight by proposed method.

Assume each group signal has 2048 points. The kernel signal,  $S_1[n]$ , is the 1000'th to the 1800'th points of reference signal,  $N=801$ ; The kernel signal,  $S_2[n]$ , is the 1200'th to the 1700'th points of reference signal,  $M=501$ . Compared with improved algorithm, the Spline-Based algorithm will compute  $M-N=300$  times more.

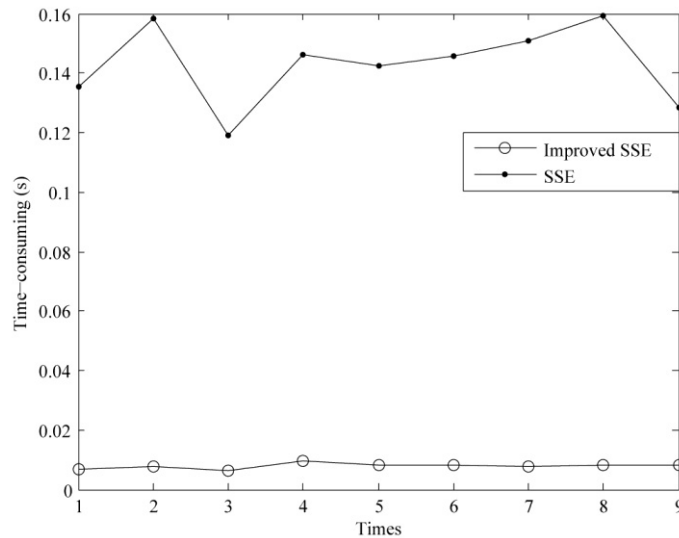


Fig.3. Time consuming of Spline-Based algorithm and improved algorithm.

In Fig.3, SSE represents the Spline-Based algorithm. Time consuming of Spline-Based algorithm is about 130ms. Time consuming of improved algorithm is approximately 8ms. Obviously, the improved method can reduce the running time while keeping the accuracy.

### 3.2. Effect of axial movement of transducers

Experiment results are shown in Fig.4. The water velocity is calculated by Eq.(1). Moving the transducer B axially to the right from the correct position will lead to increasing of  $\gamma$ , then water velocity will decrease. The velocity is in an inverse ratio of  $\gamma$ . Despite other unknown factors, we only consider the error of separate distance axially. Assume zero point is the correct position.

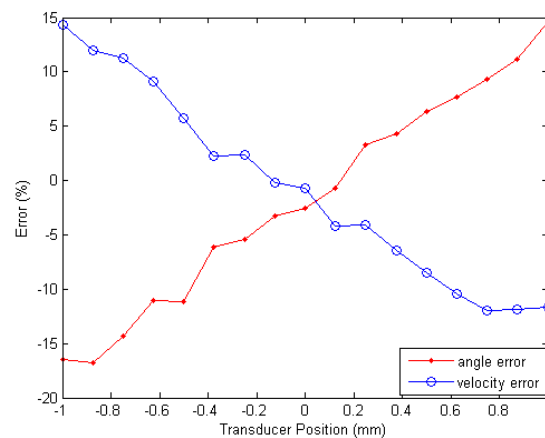


Fig.4. The relationship between water velocity and refraction angle when the transducer position is changed.

#### 4. Conclusion

The improved Spline-Based method can reduce the running time effectually, and its stability is slightly better than the cross-correlation algorithm as is shown in the environment results. Furthermore, mounting position of transducers should be paid more attention since it could affect the accuracy of result seriously.

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