



# Cryptanalysis on “a secure three-factor user authentication and key agreement protocol for TMIS with user anonymity ”

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## ABSTRACT

The health-care delivery services were made possible by telecare medicine information systems (TMIS). These systems are paving the way for a world where computerised telecare facilities and automated patient medical records are the norm. Authentication schemes are common mechanisms for preventing unauthorised access to medical records via insecure networks. Amin and Biswas recently proposed an authentication scheme for TMIS, asserting that their scheme can withstand various attacks. Despite this, their scheme still has significant security weaknesses. In this paper, we present a cryptanalysis of Amin and Biswas' scheme and show that it is subject to a variety of attacks.

## 1. Introduction

The increased proliferation of distributed networks has resulted in more resource and service exchange among user devices. As a result, during this cyber-connected period, there has been an increase in transaction volume.

Due to the open nature of network that is dispersed, for application systems, system security and robust privacy protection techniques have become an inevitable requirement. As a result, authentication of the user may be a critical security element that must be included in such systems in order to distinguish legitimate users from potential threats.

One of the applications of distributed networks is the Telecare medical information system (TMIS). TMIS creates an effective and practical connection through an insecure internet between the patient and the doctor. Therefore, in order to access critical medical data over unsecure communication, data security, privacy, and user authentication are of utmost importance. There have been numerous user authentication mechanisms for TMIS proposed recently [1–22], but it has been shown that the majority of these protocols fall short of meeting all security requirements.

Recently, Mishra et al. [23] suggested a user authentication technique with anonymity for the users. Unfortunately, according to Amin and Biswas [24], user anonymity is not guaranteed by the technique and mutual authentication in Mishra et al.'s strategy. Furthermore, Amin and Biswas concluded that Mishra et al.'s is susceptible to a variety of attacks. Then, to address the shortcomings in Mishra et al.'s scheme, Amin and Biswas provided an updated authentication scheme. First, we show that Amin and Biswas's strategy [24] is not able to satisfy the user anonymity property and doesn't give complete forward secrecy and mutual authentication.

It's also susceptible to forging and password guessing attacks when used offline.

The remainder of the paper is divided into the following sections. The scheme devised by Amin and Biswas is examined in Section 2. Section 3 discusses the problems in Amin and Biswas' strategy. In Section 4, you'll find the conclusions.

## 2. Review of the scheme [24]

Registration, login, authentication, and password update are the four sections of the authentication process. The explanations are as follows:

### 2.1. Notations

The notations used in this paper are defined in the table.

Notation	Description
$U_j$	User
$r$	Random variable
$A$	Adversary
$ID_j$	Identity of the user
$PWD_j$	Password of the user
$T_j$	fingerprint
$H()$	Bio-hash function
$h(\cdot)$	One-way hash function
SC	Smart card
$SK$	Session key
$  $	Concatenation operation
$\cdot$	ECC based scalar point multiplication
$\oplus$	Bit-wise exclusive OR operation

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## 2.2. User registration phase

The medical server accepts registrations from anyone during this phase to gain access to medical services.

1. User selects  $ID_j$ , password  $PWD_j$ , and biometric template such as fingerprint  $T_j$ . Then,  $U_j$  submits  $ID_j$ ,  $A_j$ , and  $F_j$  through secure link or in person to the medical server after computing  $A_j = h(ID_j || PWD_j)$  and  $F_j = H(T_j)$ .
2. Then, Medical server  $S$  computes  $A_j = h(ID_j || PWD_j)$ ,  $K = h(ID_s || z || ID_j)$ ,  $B_j = h(ID_j || A_j)$ ,  $CID_j = E_z(ID_j || r)$  and issues a SC for the  $U_j$  after storing  $F_j$ ,  $A_j$ ,  $B_j$ ,  $CID_j$ ,  $h(\cdot)$ ,  $H(\cdot)$  into the memory of the SC using protected channel. We assume that a user selects low entropy  $ID_j$ ,  $PWD_j$  that are individually guessable in time that is polynomial.

## 2.3. Login phase

The  $U_j$  can use a medical server with a card reader or terminal device to access the medical server at any time and from any location after successfully completing the registration procedure. The following is a list of all the steps in this phase:

1. The  $U_j$  first embeds his or her SC into the card reader device, then embeds the biometric template  $T_j$  into the sensor device.  $F_j^* = H(T_j)$  is computed by the card reader and compared to the stored  $F_j$ . Biometric verification is successful if it matches, and the  $U_j$  is asked to input  $ID_j$ ,  $PWD_j$ ; otherwise, the connection is terminated.
2.  $A_j^* = h(ID_j || PWD_j)$  is computed by the card reader and compared to the stored  $A_j$ . The matching result determines whether or not the  $U_j$  provided valid  $ID_j$ ,  $PWD_j$ . Proceed to the next stage if it matches; Else, the connection will be canceled.
3. The terminal generates a nonce at random  $r_j$  and calculates  $D_1 = r_j \cdot N$ ,  $K = B_j \oplus h(ID_j || A_j^*)$ ,  $D_2 = r_j \oplus K$ ,  $D_4 = h(ID_j || r_j || K)$  and sends  $D_2$ ,  $D_4$  and  $CID_j$  over the public/open channel as a login message to the medical server.

## 2.4. Authentication and key agreement phase

The  $U_j$  and the medical server must establish mutual authentication and a shared session key agreement at this phase. All of the steps in this phase are listed below:

1. The medical server decrypts  $CID_j$  using the server's secret key  $z$  and gets  $(ID_j^* || r) = DE_z(CID_j)$ ,  $K = h(ID_s || z || ID_j^*)$ ,  $r_j^* = D_2 \oplus K$ ,  $D_1^* = r_j^* \cdot N$ ,  $D_4^* = h(ID_j || r_j^* || K)$  and matches  $D_4^*$  with the received  $D_4$ . The medical server trusts it if it matches the  $U_j$ 's legitimacy.
2. The medical server generates a nonce at random  $r_k$  and calculates  $D_1 = r_k \cdot N$ ,  $SK = r_k \cdot D_1^* = r_k \cdot r_j^* \cdot N$ ,  $J_1 = H_1 + D_1^*$ ,  $L_j = h(ID_j^* || h(H_1) || K)$ ,  $CID_j' = E_z(ID_j^* || r')$  and transmits a reply message  $L_j$ ,  $J_1$  and  $CID_j'$  to the  $U_j$  through the public channel, where  $r'$  is the medical server generates a random number.
3. The  $U_j$  computes  $H_1^* = J_1 - D_1^*$ ,  $L_j^* = h(ID_j || h(H_1^*) || K)$ ,  $SK = r_j \cdot H_1^* = r_j \cdot r_k \cdot N$ , and matches  $L_j^*$  with the received  $L_j$  depending on the reply message received. If they match, the  $U_j$  trusts the medical server's legitimacy, then the protocol performs mutual authentication by sharing  $SK$ . After mutual authentication, the  $U_j$  replaces the previous  $CID_j$  in the SC's memory with the new  $CID_j'$ . Finally, the  $U_j$  computes  $Z_j = h(ID_r || SK)$  and sends it via the public channel to the medical server.
4. Following receipt, the server calculates  $Z_j^* = h(ID_j^* || SK)$  and compares it to the received  $Z_j$ . If they're compatible, both sides begin secure communication.

## 2.5. Password change phase

It's a useful attribute for adding a password change phase to any password-based user authentication mechanism, allowing users to change their passwords without the need for a medical server.

1. The  $U_j$  first puts the SC into the card reader and performs steps 1 and 2 of the login phase to verify the  $U_j$ 's authenticity. After that, the card reader performs the procedures below to successfully change the password.
2. After user authentication, the card reader prompts the user to enter a new password,  $PWD_j^{new}$ , into the  $U_j$ , and after doing so, the card reader computes the values  $A_j^{new} = h(ID_j || PWD_j^{new})$  and  $B_j^{new} = h(ID_j || A_j^{new}) \oplus K$ , where  $K$  is the old parameter, and then the card reader replaces  $A_j$ ,  $B_j$  with the new values  $A_j^{new}$ ,  $B_j^{new}$  and the password change phase is successfully completed.

## 3. Cryptanalysis of Amin and Biswa's scheme

This section describes the security limitations of the scheme in Amin and Biswas [24].

### 3.1. Adversary model

Adversary modeling is a crucial component of creating an authenticated protocol. A strategy for strengthening security by categorizing vulnerabilities and goals, and hence establishing protective measures against threats to the system, is known as adversary modeling. In this context, a threat could be a harmful attack carried out by an enemy, such as an adversary who could harm the resources. The adversary model is based on the assumptions below. These assumptions regarding an adversary's prowess are legitimate, and they've been made in contemporary works as well:

1. The message that was communicated across the insecure communication channels has little influence on the adversary. Intercepting, altering, and deleting any conveyed message are all examples of this [25–27].
2. Using a power analysis technique, the adversary can retrieve the security parameters encoded in the smart card [28–31].
3. The password dictionary can be enumerated offline by adversary [32,33].

### 3.2. Fails to offer user anonymity

Assume Adversary acquires the value  $A_j$ ,  $B_j$  under assumption 2 from the stolen smart card, and the adversary intercepts the  $U_j$ 's login request message  $(D_2, CID_j, D_4, T_j, T_u)$ . Now, Adversary has values  $(A_j, B_j, D_2, CID_j, D_4, T_j, T_u)$ . Adversary can find the user  $U_j$ 's  $ID_j$  by doing the following:

1. Adversary assumes the identify of the user as  $ID_a$ .
2. Compute  $K_a = B_j \oplus h(ID_a || A_j) = h(ID_j || A_j) \oplus h(ID_s || z || ID_j) \oplus h(ID_a || A_j)$ .
3. Compute  $r_j^* = D_2 \oplus K_a = r_j \oplus K \oplus K_a$ .
4. Compute  $D_4^* = h(ID_a || r_j^* || K_a)$ .
5. Compare  $D_4^* \stackrel{?}{=} D_4$ . If this is the case, the adversary's guessed identity is right.
6. If false, the adversary must repeat steps (1–4) until the current identity is obtained.

Hence, the attacker can learn the user's identify. The foregoing steps have a time complexity of  $O(|D_{ID}| \times (4T_{xor} + 6T_h))$ , where  $|D_{ID}|$  denotes the identity space size,  $T_{xor}$  denotes the XOR operation execution time, and  $T_h$  denotes the hash operation execution time. As a result, Amin and Biswas's scheme fails to offer user anonymity.

### 3.3. Prone to offline password guessing attack

Assume Adversary obtain the values  $\{A_j, B_j, J_i, h(\cdot)\}$  under assumption 2, the login request message is intercepted by Adversary from the stolen/lost  $SC$  of  $(ID_j, D_2, CID_j, D_4, T_j, T_u)$  under assumption 1. As previously stated, Adversary can uncover a user's original identification  $ID_j$ . Adversary can perform an offline password guessing attack using these values as follows:

1. Adversary assumes password of the user  $U_j$  as  $PWD_a$ .
2. Compute  $z_j^* = J_i \oplus h(A_j \oplus PWD_j) = z_j \oplus h(A_j \oplus PWD_j) \oplus h(A_j \oplus PWD_j) = z_j$ .
3. Compute  $A_j^* = h(ID_j || PWD_a)$ .
4. Compare  $A_j = A_j^*$ . If this is the case, adversary's guessed  $PWD_a$  is correct.
5. If false, the adversary must repeat steps (1–4) till you get your hands on the current password.

Hence, the attacker can learn the user's password.

The foregoing steps take  $O(|D_{PWD}| \times (6T_{xor} + 4T_h))$ , where  $|D_{PWD}|$  denotes the identity space size,  $T_{xor}$  presents the XOR operation execution time, and  $T_h$  presents the hash operation execution time. In reality, the password space is usually somewhat limited, such as  $|D_{PWD}| \leq 10^6$ . As a result, Amin and Biswas's strategy is susceptible to an offline password guessing attack.

### 3.4. Fails to offer perfect forward secrecy

Assume that under assumption 2, Adversary intercepted and documented the messages that had previously been conveyed  $(ID_j, D_2, CID_j, D_4, T_j, T_u)$  and  $(T_s, M_j)$  and obtained the value  $(A_j, B_j, J_i, h(\cdot))$  from the  $SC$ . If the attacker has the user password  $PWD_j$  as previously discussed, the previously traded session key can be calculated as follows:

1. Adversary computes  $A_j = h(ID_j || PWD_j)$  and  $z_j = J_i \oplus h(A_j || PWD_j)$ .
2. Then Adversary computes the  $SK = h(ID_j \oplus A_j \oplus z_j \oplus T_u \oplus T_s)$ .

As a result, since revealing the user's password affects the secrecy of previous session keys, Amin and Biswa's scheme doesn't provide perfect forward secrecy.

### 3.5. Prone to forgery attack

Under assumption 2, Adversary acquires the values  $\{A_j, B_j, J_i, h(\cdot)\}$  from the smart card. As previously stated, Adversary can obtain  $U_j$ 's identification  $ID_j$  and password  $PWD_j$ . Using this information, the adversary can complete the login phase steps and submit the login request message  $\{ID_j, D_2, CID_j, D_4, T_j, T_a\}$  to the server, where  $T_a$  represents the Adversary's current time stamp. Server can check the newness of the timestamp  $T_a$  when it receives the message  $\{ID_j, D_2, CID_j, D_4, T_j, T_a\}$  from attacker. Because Adversary utilises the correct timestamp, the verification is valid. The server then performs the processes of the authentication phase to verify that the adversary is a valid user. It's obvious that the server won't notice anything or any deformity because the login request  $\{ID_j, D_2, CID_j, D_4, T_j, T_a\}$  is genuinely made by adversary using the valid  $U_j$ 's identity  $ID_j$  and password  $PWD_j$ . The message  $(T_s, M_j)$  is then sent to user  $U_j$  by Server  $S$ . As a result,  $S$  will accept Adversary's login request from  $U_j$ . Adversary intercepts the  $(T_s, M_j)$  communication and finds  $SK = h(ID_j \oplus A_j \oplus z_j \oplus T_u \oplus T_s)$ . Finally, both the Server and the Adversary will have the same  $SK$ . As a result, since the adversary can impersonate a valid user by successfully signing in using the credentials of server  $S$ , Amin and Biswa's scheme is vulnerable to forgery attack.

### 3.6. Fails to offer mutual authentication

Mutual authentication is accomplished using an effective password authentication approach, which means that the server not only verifies

the authenticity of the user, but the user can also verify the server's legitimacy. Furthermore, no unauthorised users or cloud servers have the ability to impersonate a legitimate user or server. An attacker can mimic a valid user, as previously stated. As a result, the mutual authentication setup is broken. As a result, mutual authentication is not achievable.

## 4. Conclusion

We investigated Amin and Biswas's authentication technique and found that it is not able to deliver user anonymity, mutual authentication and perfect forward secrecy. Offline password guessing and forging attacks are also possible. As a result, Amin and Biswas's technique for wireless network communication is unsafe. Future efforts will be focused on bolstering Amin and Biswas's scheme, which will be capable of meeting all security criteria and objectives.

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## Data availability statement

Data sharing is not applicable to this article as no new data were created or analyzed in this study.

## Declaration of Competing Interest

Authors declare that they have no conflict of interest.

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