



## Full Length Article

# Optimal scheduling of solar-surface water source heat pump system based on an improved arithmetic optimization algorithm

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## ABSTRACT

Integrating solar energy into the combined energy supply of surface water source heat pump systems is expected to reduce the electricity consumption and carbon emissions. In this paper, a solar-surface water source heat pump system model is established to maximize system performance and save economic cost. In order to find the optimal operation scheme, an improved arithmetic optimization algorithm (iAOA) is proposed. This algorithm integrates elite opposition-based and nonlinear acceleration functions to solve the model. The effectiveness of the proposed model and algorithm is verified by applying it to a SWSHP district energy system in the central area of Xiangtan city. Experimental results demonstrate that incorporating solar energy into the SWSHP district energy system can improve system performance and reduce operational costs. In comparison with several other optimization algorithms, this algorithm has a faster convergence speed and a higher convergence accuracy. Therefore, it is considered an effective method for solving solar-surface water source heat pump district energy systems.

## 1. Introduction

The increasingly severe energy challenges have made carbon peak and carbon neutrality an increasingly important goal for Chinese energy development. Of all energy consumption, building energy consumption represents 45.5% of total Chinese energy consumption and contributes to 50.9% of Chinese carbon emissions [1]. As a percentage of total building operation energy consumption, air conditioning accounts for 40% to 50%. Energy-efficient ground source heat pump (GSHP) is environmentally friendly air conditioning technology that provide both heating and cooling. GSHP saves more than 40% of the energy that traditional air conditioners require. It has widely recognized and used due to their energy-saving, environmentally friendly, and stable operating benefits. However, because GSHP systems are subject to a range of factors such as temperature variations and unit efficiency [2–5], it is essential to optimize their scheduling and determine the best operating strategy to enhance system performance and reduce operating costs.

Water source heat pump (WSHP) technology, a type of GSHP, surface water or groundwater is used as the source of heat and cold for energy transfer from low grade to high grade. However, due to the differences between ground source heat pump systems, not all existing research on GSHP systems is applicable to WSHP systems. Therefore,

WSHP systems have been studied by many researchers. For example, Schibuola et al. [6] tracked the annual performance of a WSHP system at the Venice Center and compared its energy consumption to an air source heat pump system and a hybrid energy system, demonstrating that water source and ground source are subject to smaller temperature fluctuations, and surface water source heat pumps have higher stability. Cardemil et al. [7] proposed a new WSHP system for heating in Mediterranean climates, demonstrating the feasibility of outdoor swimming pools as heat sources in warm climates. Chen et al. [8] developed an intelligent control strategy integrates WSHP and ice storage district cooling systems aiming at the lowest operating cost per unit cooling capacity, saving 8.7%–9.3% of operating cost compared with the traditional control strategy. Ma et al. [9] investigated an office building in Suzhou and found that WSHP systems have more stable longterm performance than soil source heat pump systems. The research of the above scholars has verified the superiority of water source heat pump, but it does not take into account the long-term operation of the water source system. If the cooling and heating loads of the system differ significantly and Water is used as a long-term heat source, the chemical environment of the water source may become imbalanced, changing the temperature, concentration, pH value, and hardness of the water source, ultimately decreasing the coefficient of performance (COP) of the system. In these studies, the COP of the heat pump unit is a fixed

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value, and the variable operating condition of the heat pump system is not taken into account.

Solar energy is a consistent clean energy, but a single solar heating system is not a reliable source for heating due to its vulnerability to weather conditions. However, by combining solar energy and WSPHs, energy efficiency of WSPHs can be enhanced while solar energy's instability in heating can be mitigated. Several academic studies have demonstrated the significance of solar energy in balancing environmental imbalances. For example, Bordignon et al. [10] showed that incorporating photovoltaic power can help balance the thermal load on the ground, improve electrical efficiency, and system performance. Similarly, Wang et al. [11] proposed a GSHP-PVT(photovoltaic and thermal) system and demonstrated that the system can prevent ground source temperature drop and improve operation efficiency. Huang et al. [12] developed a TRNSYS model of a solar-assisted ground source heat pump (SAGSHP) system that reduced energy consumption and operating costs while ensuring ground heat balance. In addition, Yang et al. [13] created a household GSHP system that utilized waste heat from photovoltaic power to improve net power generation and maintain soil heat balance. Scholars have also focused on the performance of solar-GSHP systems. For instance, Mi et al. [14] developed a new hot water supply system by integrating PVT and WSHP that improved system energy efficiency and economic benefits compared to other multi-source hot water systems. Liu et al. [15] built a mathematical model of a direct-expansion PVT heat pump system, which demonstrated that the coupled system can enhance the operation performance of heat pump systems. Zhang et al. [16] investigated an actual hybrid solar ground source heat pump (HSGSHP) system. It was found to improve performance by nearly 25.8% when the solar space heating was added. Wang et al. [17] proposed matching principles for key parameters of hybrid heating systems using particle swarm optimization and the coordinate search algorithm to optimize system performance parameters and reduce costs. Cao et al. [18] designed a thermodynamic model of direct-expansion solar-assisted heat pump water heaters and determined optimal parameters for enhancing system performance. The above studies have proved the superiority of the combination of solar energy and ground source heat pump system, but they are based on the empirical operating conditions to optimize the system parameters and structure, among which the solar-surface water source heat pump (SSWSHP) system unit optimization scheme is less.

In this study, the economic dispatching model of SSWSHP regional energy system is established. In addition, according to the characteristics of high dimension, nonlinear and multi-constraint of SSWSHP system, an improved arithmetic optimization algorithm is proposed to obtain a better operation scheme. It integrates an elite inverse strategy and a nonlinear acceleration function. Experimental results indicate that the SSWSHP system has a higher coefficient of performance. What's more, comparing with other intelligent optimization algorithms the proposed algorithm performs well in solving the optimal scheduling of the SSWSHP system.

The paper is organized as follows: Section 2 introduces the model of the SSWSHP system, followed by iAOA algorithm in Section 3. A comprehensive experimental demonstration is provided in Section 4. Lastly, presents the conclusions of this work are presented in Section 5.

## 2. System and model

Fig. 1 illustrates the various components of the SSWSHP district energy system under investigation. The system is primarily comprised of WSHP units, PVT collectors, heat exchangers, absorption chillers, and other associated components. The primary energy source is the WSHP units, while solar energy acts as the auxiliary energy source. On one hand, photovoltaic power generation provides electricity to the HP units, while the PVT collectors supply heat and electric energy to the system, reducing the heat load pressure of the heat pump system. Under

refrigeration conditions, absorption chillers can decrease the cooling demand of the heat pump system, thereby improving energy efficiency.

### 2.1. The PVT collector

PVT technology is a combination of photovoltaic and solar thermal energy. It involves combining PV panels and collectors to extract heat from the PV panels. As a result, the utilization efficiency of solar energy is improved, and the temperature of the panels is reduced. The electricity generated by the PVT is dependent on various factors such as light intensity, external temperature, and other factors [19], as shown in Eq. (1).

$$P_{pv} = P_{stc} \frac{I_{ac}}{I_{stc}} (1 + k(T_c - T_{stc})) \quad (1)$$

Where  $P_{stc}$  is the maximum output power of the PV panel under standard test conditions ambient temperature;  $I_{ac}$  is the light intensity;  $k$  is the temperature coefficient;  $I_{stc}$  and  $T_{stc}$  are the light intensity and ambient temperature under standard test conditions;  $T_c$  is the actual temperature of the solar panel, which can be expressed by the ambient temperature, light intensity, as shown in Eq. (2) [20].

$$T_c = T_a + 30 \frac{I}{I_{stc}} \quad (2)$$

In addition to providing electrical energy, the PVT collector also provides a certain amount of thermal energy as shown in Eq. (3) [21].

$$Q_s = A_s I \eta_s \quad (3)$$

Where  $A_s$  is the area of the collector;  $I$  is the light intensity;  $\eta_s$  is the collector efficiency, which can be expressed by the light intensity and ambient temperature, as shown in Eq. (4) [22].

$$\eta_s = 0.7408 - 0.0432(T_{mean} - T_a)/I - 0.000503((T_{mean} - T_a)/I)^2 \quad (4)$$

Where  $T_{mean}$  is the mean temperature of the collector;  $T_a$  is the ambient temperature.

### 2.2. The WSHP unit

The mathematical model of WSHP unit cooling/heating is shown in Eq. (5).

$$Q_i = COP \times P_i \quad (5)$$

Where,  $Q_i$  is the cooling/heating capacity of the  $i$ th heat pump unit.  $P_i$  is the electrical power required by the  $i$ th heat pump unit;  $COP$  is influenced by the load factor, and the relationship with the load rate is depicted in Fig. 2 [23].

As a result of the heat pump unit cooling or heating, the discharge water temperature has changed, and its calculation formula is shown in Eq. (6).

$$T_{out} = T_{in} + \frac{Q_{hp}}{\rho V c} \quad (6)$$

Where  $T_{in}$  and  $T_{out}$  are inlet and outlet water temperature, respectively;  $\rho$  and  $c$  are the density and specific heat capacity of water respectively;  $V$  is circulating water flow.

### 2.3. The absorption chiller

Absorption chillers are cooling device that uses thermal energy as power. The heat produced by solar energy is used to heat the chillers. The cooling capacity of the absorption chiller is shown in Eq. (7) [21].

$$Q_{ac} = \eta_{ac} Q_s \quad (7)$$

Where  $\eta_{ac}$  is the cooling coefficients of absorption chiller.

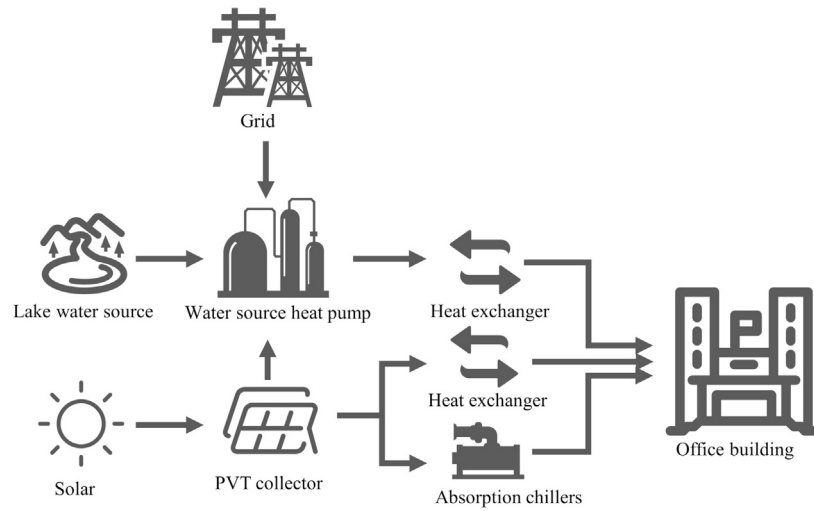


Fig. 1. Structure diagram of the SSWSHP system.

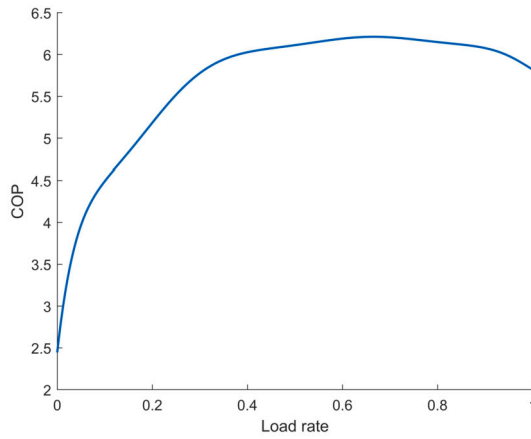


Fig. 2. The curve of heat pump unit.

$$\sum_{i=1}^N P_i^t - P_{pv}^t - P_e^t = 0 \quad (12)$$

Where  $Q_{load}^t$  is the load of the system at moment  $t$ ;  $Q_i^t$  is the cooling/heating capacity of unit  $i$  at moment  $t$ ;  $Q_{sun}^t$  is the cooling/heating capacity of solar energy at moment  $t$ ;  $P_i^t$  is the electrical power required by unit  $i$  at moment  $t$ ;  $P_{pv}^t$  is the solar power generated in moment  $t$ ;  $P_e^t$  is the electricity purchased by the system from the grid in moment  $t$ .

The outlet water temperature restriction is shown in Eq. (13).

$$T_{min} < T_{out} < T_{max} \quad (13)$$

As seen in Eq. (14), the upper and lower boundaries of the unit are restricted.

$$Q_{min} < Q_i^t < Q_{max} \quad (14)$$

Where  $T_{min}$  and  $T_{max}$  are the minimum and maximum temperatures of outlet water, respectively;  $Q_{min}$  and  $Q_{max}$  are minimum cooling/heating and maximum cooling/heating respectively.

### 3. Improved arithmetic optimization algorithm

#### 3.1. Arithmetic optimization algorithm

The arithmetic optimization algorithm (AOA) [25] is a relatively novel meta-heuristic algorithm that was proposed in 2021. AOA leverages the distributional properties of arithmetic operators to identify the optimal elements from a pool of candidate solutions, and it comprises two key stages: exploration and exploitation. First, an initial population of  $N$  solutions with a  $d$ -dimensional search variable denoted as  $X_i = \{x_{i1}, x_{i2}, \dots, x_{id}\} (i = 1, 2, \dots, N)$  is generated. The phase of the method is then determined using the Math Optimizer Accelerated (MOA) function. The MOA is calculated using the Eq. (15). Allow  $r_1$  to be a number between 0 and 1. When  $r_1 > MOA$ , AOA performs exploration; when  $r_1 < MOA$ , AOA performs exploitation.

$$MOA(iter) = Min + iter \left( \frac{Max - Min}{iter_{max}} \right) \quad (15)$$

Where  $iter$  represents the current number of iterations;  $MOA(iter)$  is the calculated value of MOA at the  $iter$ th iteration;  $iter_{max}$  is the maximum number of iterations;  $Max$  and  $Min$  are the maximum and minimum values of the MOA function, expressed as 1 and 0.2, respectively.

Division (D) and multiplication (M) calculations can produce highly distributed values or strategies, facilitating exploration. In the exploration phase, the update formula is shown in Eq. (16).

#### 2.4. Objective function

Since the HP units consume the majority of the system power [24], the optimization objective of the system is based on the heat pump operation cost including power purchase cost and operation maintenance cost. The optimization objective function is represented by Eq. (8).

$$\min C = \min(C_{ex} + C_{om}) \quad (8)$$

$$C_{ex} = \sum_{t=1}^T c_e^t P_e^t \quad (9)$$

$$C_{om} = \sum_{i=1}^{N_w} (om_{hp} P_i^t + om_s P_{pv}^t) \quad (10)$$

Where  $C_{ex}$  is the power purchase cost;  $C_{om}$  is operation maintenance cost;  $c_e^t$  is the unit price of electricity in moment  $t$ ;  $om_{hp}$  is the unit maintenance cost of HP unit;  $om_s$  is the unit maintenance cost of PVT collector;  $P_e^t$  is the electric energy purchased from grid in moment  $t$ ;  $N_w$  is the number of HP unit;  $T$  is the scheduling period of the system.

#### 2.5. Constraints restrictions

The power balance constraint is shown in Eq. (11) - (12).

$$Q_{load}^t = \sum_{i=1}^N Q_i^t + Q_{sun}^t \quad (11)$$

$$X_{i,j}(iter) = \begin{cases} X_{best,j}(iter) \div (MOP + \varepsilon) \times \\ ((UB_j - LB_j) \times \mu + LB_j) & r_2 < 0.5 \\ X_{best,j}(iter) \times MOP \times \\ ((UB_j - LLB_j) \times \mu + LB_j) & otherwise \end{cases} \quad (16)$$

Where  $X_{i,j}$  is the position of the  $i$ th individual  $j$ th dimension of the optimal solution at the  $iter$ th iteration;  $X_{best,j}$  is the position of the  $j$ th dimension of the optimal individual at the  $iter$ th iteration;  $r_2$  is a random number between 0 and 1;  $\varepsilon$  represents a little positive number that prevents the divisor from becoming zero;  $\mu$  is to adjust the search control parameter, which is generally set to 0.5, to generate a value randomly at each iteration;  $UB_j$  and  $LB_j$  are the upper and lower boundaries of the individuals of  $j$ th dimension; MOP stands for Math Optimizer Probability, and it is determined by Eq. (17).

$$MOP(iter) = 1 - \frac{iter^{1/\alpha}}{iter_{max}^{1/\alpha}} \quad (17)$$

Where  $\alpha$  is a sensitive parameter that determines the precision of exploitation during the iterative phase and is commonly set at 5.

Due to the low dispersion of these operations and easier approach to the target, addition (A) and subtraction (S) operations are used in the exploitation phase, with the iterative formula shown in Eq. (18), where  $r_3$  is a number chosen between 0 and 1 randomly.

$$X_{i,j}(iter) = \begin{cases} X_{best,j}(iter) - MOP \times \\ ((UB_j - LB_j) \times \mu + LB_j), & r_3 < 0.5 \\ X_{best,j}(iter) + MOP \times \\ ((UB_j - LB_j) \times \mu + LB_j), & otherwise \end{cases} \quad (18)$$

### 3.2. The elite opposition-based strategy

In meta-heuristic algorithms, the quality of the initialized population plays an importance role in the algorithm performance in finding the best solution. The initial population generated at random by AOA often lacks the population diversity necessary to facilitate the search for optimal solutions. An elite opposition-based strategy [26] is employed in this research to initialize population and enhance population diversity. The elite opposition-based learning strategy selects elite solutions from the population, creates an opposite-based population in opposition to the elite solutions, compares the elite opposition-based population to the elite population, and chooses the best solutions as the initialized population. An elite solution is denoted as  $X_i = \{x_{i,1}, x_{i,2}, \dots, x_{i,d}\}$ , and the opposition-based solution  $\bar{X}_i = \{\bar{x}_{i,1}, \bar{x}_{i,2}, \dots, \bar{x}_{i,d}\}$  is shown in Eq. (19).

$$\bar{x}_{i,j} = r_4 \times (UB_j + LB_j) - x_{i,j} \quad (19)$$

Where  $r_4$  is a number chosen between 0 and 1 randomly.

When the solution crosses the boundary, it is reset by Eq. (20).

$$\bar{x}_{i,j} = \text{rand}(LB_j, UB_j), \text{ if } \bar{x}_{i,j} < LB_j \text{ or } \bar{x}_{i,j} > UB_j \quad (20)$$

### 3.3. Nonlinear Math Optimizer Accelerated function

In the AOA algorithm, maintaining harmonious relationship between the exploitation and exploration phases is crucial for achieving optimal results. The exploration phase seeks to explore a wide range of the search space, while the exploitation phase focuses on exploiting the most promising areas of the search space. The MOA is an essential component of the AOA algorithm, which controls the balance between these two phases. However, MOA is a linear control approach that increases linearly with the number of iterations and may not fully capture the

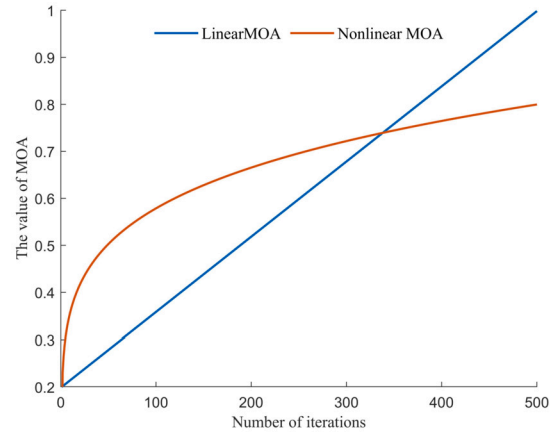


Fig. 3. Comparison curve before and after MOA modification.

complex and nonlinear search process of the algorithm. To address this issue, an new nonlinear acceleration function, iMOA, based on the exponential function is proposed. The update formula for iMOA is shown in the Eq. (21).

$$iMOA(iter) = (Max - Min) \times \left( \frac{iter}{iter_{max}} \right)^{\beta} \quad (21)$$

Where  $Max$  and  $Min$  are consistent with the AOA algorithm;  $\beta$  is the nonlinear adjustment index.

Fig. 3 depicts the nonlinear MOA curve. In comparison to the linear increasing MOA, the nonlinear MOA grows rapidly at the start of the algorithm iteration, which is conducive to fast algorithm convergence, and flat at the end, which is conducive to exploitation. The iMOA function helps prevent the algorithm from getting stuck in local optima and improves its ability to explore the search space.

### 3.4. Pseudo-code of iAOA algorithm

The Pseudo-code of the improved arithmetic optimization algorithm (iAOA) proposed by combining the aforementioned improvement strategies was described in Algorithm 1. The flowchart of iAOA algorithm is depicted in Fig. 4.

#### Algorithm 1 Pseudo-code of iAOA algorithm.

- 1: Initialize correlation parameters
- 2: Initialize a population  $X$  with random solutions and calculate their fitness values;
- 3: Sort all individuals based on their fitness values, and then select the top  $N/2$  individuals as elite population;
- 4: generate elite opposition-based population  $EO$ ;
- 5: Merge the populations  $X$  and  $EO$ , then select  $N$  solutions with higher fitness values to form the initial population, and note the current optimal solution  $X_{best}$ .
- 6: **while**  $iter < iter_{max}$  **do**
- 7:   calculate the iMOA value according to Eq. (21).
- 8:   calculate the MOP value according to Eq. (17).
- 9:   **for**  $i = 1$  to  $N$  **do**
- 10:     **for**  $j = 1$  to  $d$  **do**
- 11:       Randomly generate  $r_1, r_2$  and  $r_3$  values between  $[0,1]$ .
- 12:       **if**  $r_1 < MOA$  **then**
- 13:         Update the  $i$ th individuals position according to Eq. (16).
- 14:       **else**
- 15:         Update the  $i$ th individuals position according to Eq. (18).
- 16:       **end if**
- 17:     **end for**
- 18:   **end for**
- 19:    $t = t + 1$
- 20: **end while**
- 21: **return** the best individual  $X_{best}$

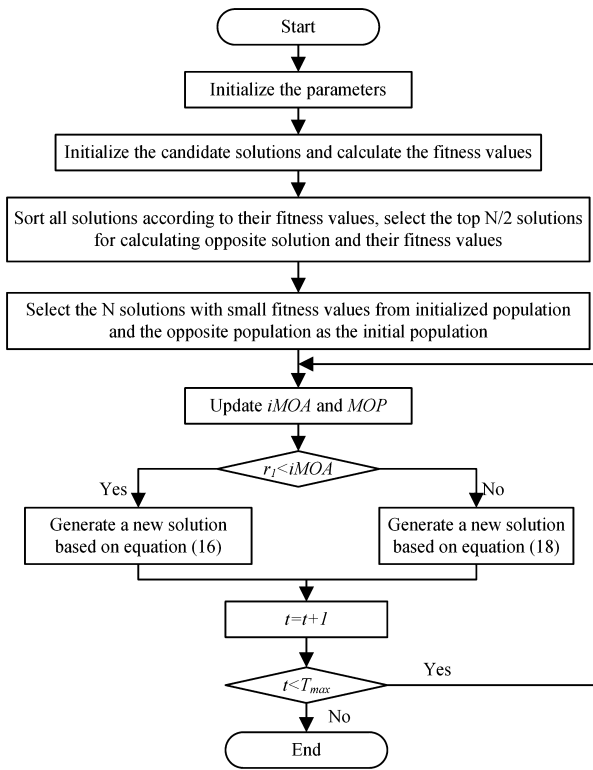


Fig. 4. Flowchart of iAOA algorithm.

#### 4. Constraint handling

The updated solution is difficult to be within the feasible domain, which will be more difficult especially when multiple constraints are considered. Therefore, to ensure the feasibility of the solution, the constraints must be handled. To overcome this challenge, the infeasible solution is adjusted through a combination of boundary absorption mechanism, dynamic heuristic constraint handling, and variable reduction strategy to ensure compliance with the relevant constraints. The specific implementation steps are as follows:

**Step 1:** According to Eq. (6), the constraints of water temperature in Eq. (14) can be transformed. Therefore, the heat pump unit output has two upper and lower boundary values, which can be expressed as Eq. (22)-(23)

$$Q'_{\min} = \max\{Q_{\min}, (T_{\min} - T_{in})\rho Vc\} \quad (22)$$

$$Q'_{\max} = \min\{Q_{\max}, (T_{\max} - T_{in})\rho Vc\} \quad (23)$$

The updated solutions, if they do not satisfy the inequality constraint, are subject to boundary absorption. This means that them must equal to the boundary value.

**Step 2:** A modified heuristic constraint treatment is used for the hot and cold load balance constraints.

Step 2.1: Calculate  $\delta$  according to Eq. (24), and determine whether the equation constraint is satisfied.

$$\delta = \sum_{i=1}^N Q'_i + Q_s - Q_{load} \quad (24)$$

Step 2.2: Each value is corrected according to Eq. (25) and again to determine whether the constraint is satisfied. If it is satisfied, the next step is executed; otherwise, Step 2.2 is continued, if the number of executions of Step 2 reaches the threshold  $L$  and the condition is still not satisfied, the set of solutions is discarded.

$$Q'_i = Q'_i + \frac{\delta}{N} \quad (25)$$

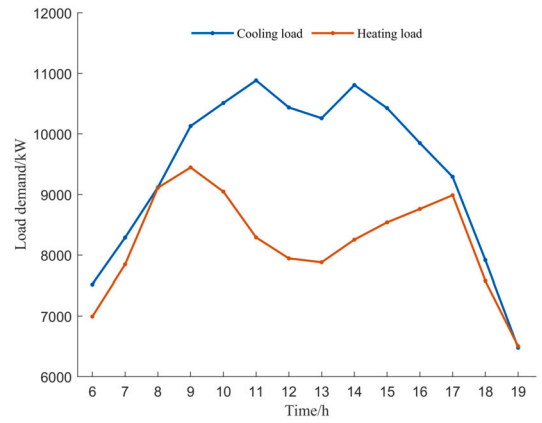


Fig. 5. Hourly cooling heating load demand.

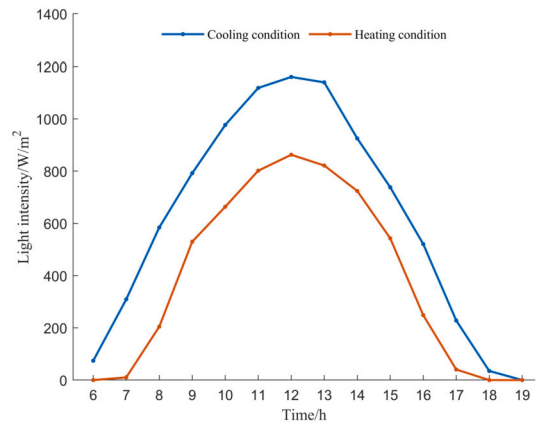


Fig. 6. Light intensity.

**Table 1**  
Purchasing electricity price.

Time period	Price (¥/kWh)
6:00-7:00	0.36
12:00-16:00	0.78
8:00-11:00, 17:00-19:00	1.30

**Table 2**  
Nameplate data of heat pump unit.

Working Condition	Cooling	Heating
Cooling/Heating capacity (kW)	1140	1288
Water source flow (m³/h)	174	174
Circulating water flow (m³/h)	146.7	146.7
Outlet water temperature (°C)	7-12	45-50

**Step 3:** The variable reduction strategy is used for the electric load balance constrain [27]. This strategy refers to reducing the dimensionality of the decision variables by using some of them to represent another part of the variables during the iterative process according to the relevant equation constraints. According to it, Eq. (12) is necessary equality optimality condition, and the variable  $P_e$  is reduced variable, which can be expressed by core variable  $P_t$ ,  $P_s$ . Thus, the purpose of the eliminated equation is achieved, and the processed objective function is as Eq. (26).



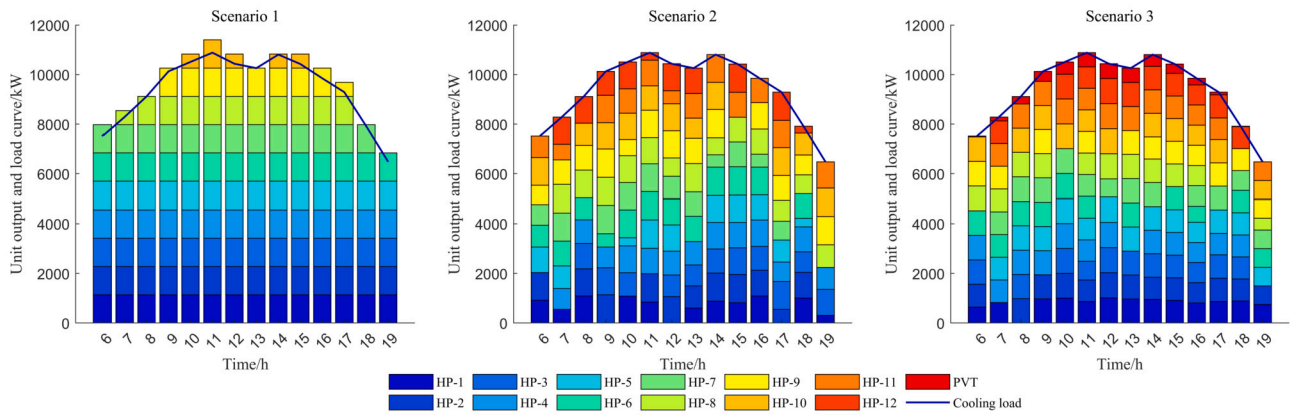


Fig. 7. Cooling load supply under cooling conditions.

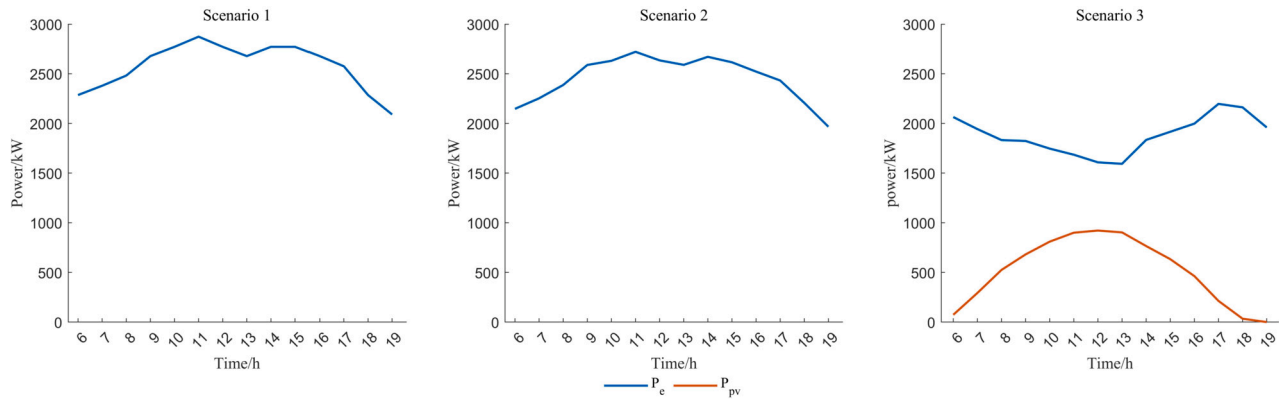


Fig. 8. Electricity load supply under cooling conditions.

$$\begin{aligned}
 \min C &= \min \sum_{i=1}^T (c_e^i (\sum_{j=1}^{N_w} P_j^i - P_{pv}^i) + \sum_{j=1}^{N_w} om_s P_j^i + om_{pv} P_{pv}^i) \\
 &= \min \sum_{i=1}^T \sum_{j=1}^{N_w} (c_e^i + om_{hp}) P_j^i - (c_e^i + om_s) P_{pv}^i
 \end{aligned} \quad (26)$$

## 5. Experiments and results

### 5.1. Simulation details

The surface water source heat pump district energy system located in Xiangtan City is the focus of this study. The system operates from 6:00 to 19:00, with a duration of 14 hours, as it provides centralized heating and cooling for government office buildings, and there is no demand during the nighttime. The system cooling loads in summer and heating loads in winter are illustrated in Fig. 5, and the light intensity data is shown in Fig. 6 [24]. A time-of-day tariff is adopted by the system, as presented in Table 1 [28], while Table 2 displays the relevant information about the heat pump units. Due to the low heating load, only 9 units operate under heating conditions, while the remaining 12 units are set to cooling mode to minimize unit losses and prolong their service life. In the iAOA algorithm, the following parameters are set: the size of population  $N = 100$ , the maximum iteration number  $T_{max} = 500$ , the Nonlinear adjustment parameter  $\beta = 0.2$ .

This optimization model was tested against three scenarios in order to validate its effectiveness. Scenario 1 is the current operation scheme, and the units only have two states of full load or half load. In Scenario 2, the system includes only water source heat pump units, providing cool and heat energy while purchasing electricity from the grid to meet cooling or heating demands. In Scenario 3, the system incorporates heat pump units, photovoltaic solar thermal collectors, and

absorption chillers. The solar and heat pump units work together to provide cooling and heating, while the electrical load of the system is met by a combination of photovoltaic power generation and grid power. An improved arithmetic optimization algorithm was utilized to optimize the scheduling process with the goal of minimizing operating costs in the last two scenarios.

### 5.2. Result analysis

#### 5.2.1. Analysis of cooling conditions

The results of the cooling conditions scheduling are presented in Fig. 7. In Scenario 1 and Scenario 2, the entire cooling load is provided by the 12 heat pump units. However, in Scenario 3, the PVT with absorption chillers is introduced to assist the heat pump system for cooling, and its contribution is primarily during high solar radiation hours, from 9:00 am to 4:00 pm. In Scenario 3 the utilization of solar energy leads to a reduction in electricity costs. The electricity purchased in each time period is shown in Fig. 8, with Scenario 1 and Scenario 2 ranging between 2000 kW and 2800 kW, while Scenario 3 ranges between 1500 kW and 2300 kW. In Scenario 1 and Scenario 2, the peak electricity consumption coincides with the peak of the electricity price, whereas the incorporation of photovoltaic power generation lowers the electricity purchase cost from the grid during the peak price period in Scenario 3.

The COP of each heat pump unit is determined by its load rate, which in turn affects the system overall efficiency. Fig. 9 displays the average COP of the three scenarios during cooling conditions, which reflects the system conversion efficiency during each time period. The average COP during each time period ranges from 3.5 to 4.0 in Scenario 1 and Scenario 2, with daily averages of 3.65 and 3.84, respectively. In Scenario 3, the COP varies with the level of insolation, reaching a peak

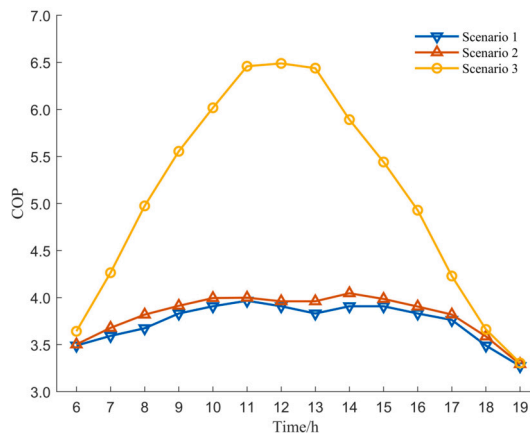


Fig. 9. COP curve under cooling conditions.

**Table 3**  
Economic cost and COP under cooling condition.

Scenarios	Economic cost (¥)	COP
Scenario 1	36579.6	3.65
Scenario 2	34863.0	3.84
Scenario 3	26730.4	5.00

**Table 4**  
Economic cost and COP under heating condition.

Scenarios	Economic cost (¥)	COP
Scenario 1	33759.5	3.48
Scenario 2	32266.0	3.64
Scenario 3	26031.5	4.51

at 12:00 am and gradually decreasing in the afternoon due to a decrease in insolation. At 18:00 p.m. and 19:00 p.m., when insolation is insufficient, the COP is similar to that of Scenario 2. According to Table 3, the average daily COP of the system increases 36.9% in Scenario 3, and the economic cost is reduced to ¥26730.4/day, resulting in a cost saving of approximately 27.1% compared to the current operating scenario.

### 5.2.2. Analysis of heating conditions

In heating condition, adjust the heat pump unit and collector mode to be in heating condition. The optimized scheduling results for both scenarios are analyzed similarly to the cooling condition, as shown in Fig. 10. Unlike the cooling condition, the heating condition necessitates more heat load in the morning and evening, while as the temperature rises in the afternoon, the system necessitates less heat load. Fig. 11 depicts the electrical power output of system under heat production conditions. As shown in Fig. 11, as the thermal load required for temperature increase decreases, light intensity increases, the electrical and heating energy provided by solar energy increases in the meantime, so the electricity supplied from the grid is reduced accordingly in all scenarios, with the reduction being especially noticeable in scenario 3, which effectively reduces peak electricity consumption and saves about 22.9% of the operating cost.

The COP for each time period in different scenarios varies with the amount of electricity purchased, as illustrated in Fig. 12. The COP ranges from 3.3 to 3.8 at various times in Scenario 1 and Scenario 2, with average COPs of 3.65 and 3.86 for the day, respectively. Scenario 3 maintains the same system COP as Scenario 2 during the hours of 6 to 7 and 17 to 19 when there is no light. When sufficient light is available, the system COP can reach up to 6.16. According to Table 4, Scenario 1 incurs the highest operating costs. However, with the addition of PVT

collectors and the use of the iAOA algorithm, the COP correspondingly increase 29.5%.

Furthermore, the empirical operation strategy often results in a waste of energy since the system cooling or heating capacity is frequently greater than the load demand. A comparison of the three scenarios under cooling and heating conditions shows that the WSHP district energy system with PVT can effectively reduce economic operating costs and enhance system conversion efficiency, providing it with an edge over the single WSHP district energy system.

### 5.3. Comparison of various algorithms

The superior performance of the proposed iAOA algorithm is demonstrated by comparing it with other optimization algorithms, such as Arithmetic Optimization Algorithm (AOA), Arithmetic Optimization Algorithm with Aquila Optimizer (AOAAO) [29], crisscross AOA Algorithm (CSOAOA) [30], PSO [31], Neighborhood Adaptive Particle Swarm Optimization Algorithm (NAPSO) [23], and Sine Cosine Algorithm (SCA) [32] in Scenario 3. It can be seen from Fig. 13 and 14 that under the same environmental parameters and number of iterations, iAOA not only has shorter running time, but also achieves a cost reduction of approximately 27.1% in cooling and 23.3% in heating. In order to further test the superiority of the algorithm, Friedman test was conducted after each algorithm was run 30 times, and the test results were shown in Table 5 and 6. According to the Friedman test, iAOA algorithm has the smallest mean rank, average value and standard deviation in both cooling and heating conditions, indicating that iAOA algorithm has obvious advantages compared with other algorithms. In summary, the iAOA algorithm exhibits faster convergence speed and improved convergence accuracy, making it an effective solution for solving the optimization operation problem of a solar-ground source heat pump system.

## 6. Conclusions

In this paper, an economic dispatch model is proposed for a solar-surface water source heat pump district energy system that integrates photovoltaic solar thermal with a SWSHP. An improved arithmetic optimization algorithm is developed to efficiently solve the optimization model, combining an elite opposition-based strategy with a nonlinear Math Optimizer Accelerated function. The experimental results demonstrate that the combination of photovoltaic thermal and surface water source heat pump system with solar power generation leads to a significant improvement in the system efficiency coefficient COP and reduces the economic operation cost by 27.1% and 23.3% under cooling and heating conditions, respectively. According to the Friedman test, compared with other algorithms, iAOA algorithm has stronger searching ability in convergence speed and accuracy, which indicates that iAOA algorithm is effective in solving the district energy system of solar-surface water source heat pump.

However, the operation of solar-surface water source heat pump system is complicated, and there may be uncertain factors such as system load fluctuation in actual operation. iAOA algorithm has obtained a better solution in solving certainty optimization, but its effect in solving load variation and working condition uncertainty has not been verified. Therefore, further consideration of load and working condition uncertainty to optimize the ground source heat pump system is our future research direction.

### Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

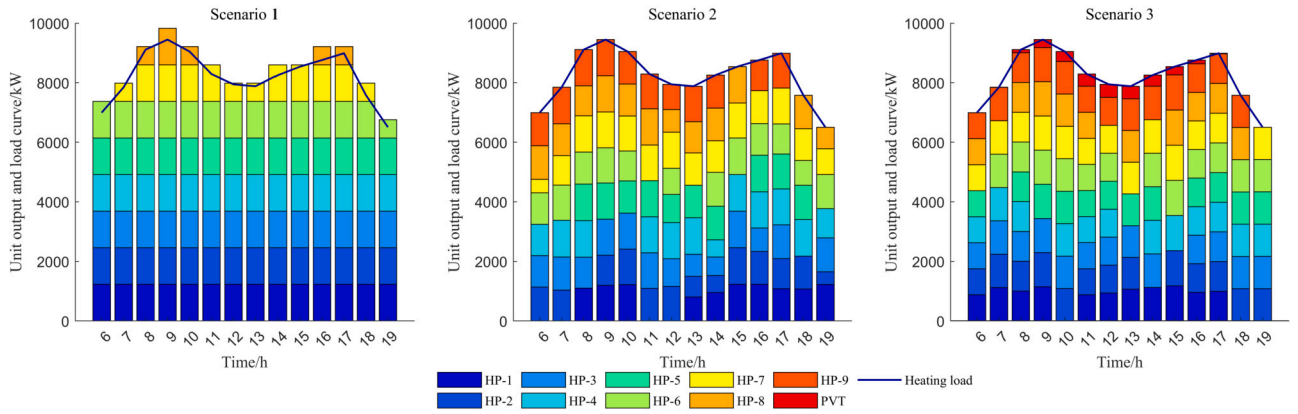


Fig. 10. Heating load supply under heating conditions.

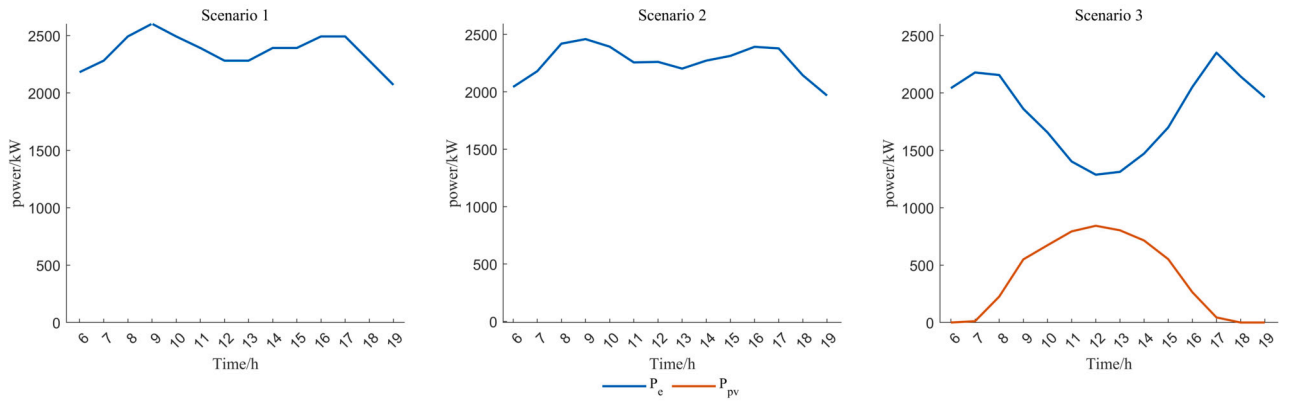


Fig. 11. Electricity load supply under heating conditions.

Table 5

Friedman test results under cooling condition.

Algorithms	Average ranks	Mean	Std	Min	Max	Time spent
iAOA	1.3	26730.4	48.0	26637.4	26814.7	11.76
AOA	2.73	26846.0	61.5	26632.6	26969.8	12.81
AOAAO	2.4	26834.9	113.08	2666.3	27061.5	24.69
CSOAOA	3.57	26920.9	61.5	26753.9	27037.3	80.62
PSO	6.4	30433.0	353.0	29605.1	20943.8	21.45
NAPSO	5.2	29805.9	416.9	29129.6	30746.8	137.00
SCA	6.4	30517.6	482.3	29513.2	31327.8	146.64

Table 6

Friedman test results under heating condition.

Algorithms	Average ranks	Mean	Std	Min	Max	Time spent
iAOA	1.4	26031.5	44.8	25957.8	26115.0	14.15
AOA	3.30	26153.2	51.9	26080.3	26266.5	16.83
AOAAO	2.43	26088.2	98.1	25921.5	26218.7	24.7
CSOAOA	2.87	26136.0	36.0	26070.9	26136.0	70.53
PSO	6.30	28974.7	322.8	27996.3	29413.5	16.98
NAPSO	5.33	28505.4	386.6	27556.0	29399.7	167.03
SCA	6.37	29055.2	381.0	28077.9	29511.4	183.64



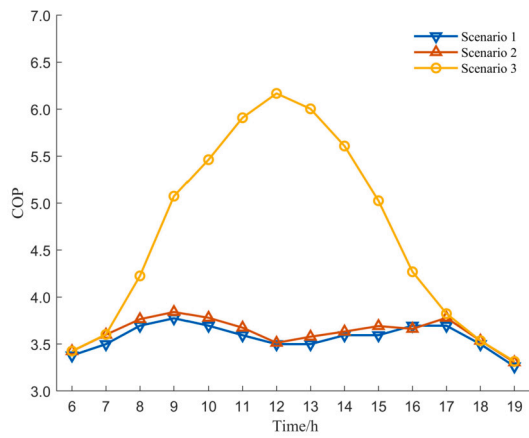


Fig. 12. COP curve under heating conditions.

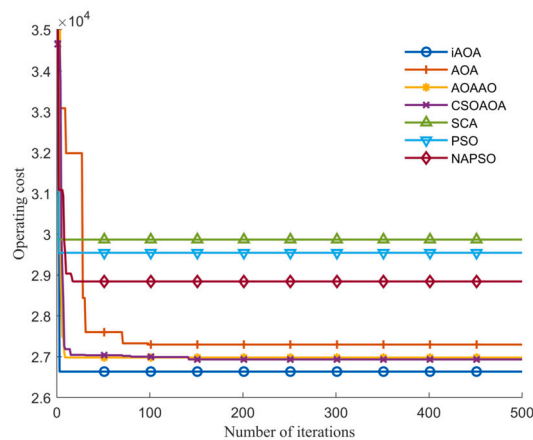


Fig. 13. Convergence curves under heating conditions.

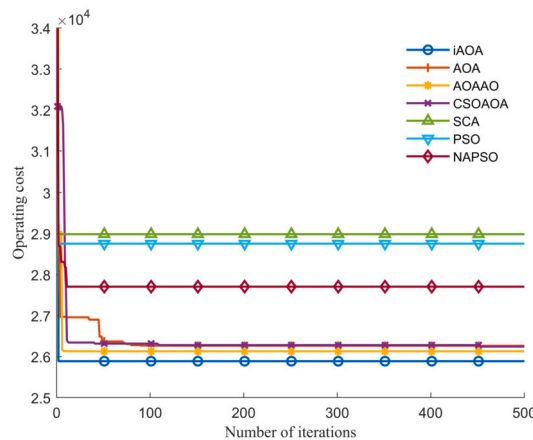


Fig. 14. Convergence curves under heating conditions.

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