



Mining Twitter data for causal links between tweets and real-world outcomes

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ABSTRACT

The authors present an expert and intelligent system that (1) identifies influential term groups having causal relationships with real-world enterprise outcomes from Twitter data and (2) quantifies the appropriate time lags between identified influential term groups and enterprise outcomes. Existing expert and intelligent systems, which are defined as computer systems that imitate the ability of human decision making, could enable computers to identify the spread of Twitter users' enterprise-related feedback automatically. However, existing expert and intelligent systems have limitations on automatically identifying the causal effects on enterprise outcomes. Identifying the causal effects on enterprise outcomes is important, because Twitter users' feedback toward enterprise decisions may have real-world implications. The proposed expert and intelligent system can support decision makers' decisions considering the real-world effects of identified Twitter users' feedback on enterprise outcomes. In particular, (1) a co-occurrence network analysis model is exploited to discover term candidates for generating influential term groups that are combinations of enterprise-related terms, which potentially influence enterprise outcomes. (2) Time series models and (3) a Granger causality analysis model are then employed to identify influential term groups having causal relationships with enterprise outcomes with the appropriate time lags. Case studies involving a real-world internet video streaming and disc rental provider as well as an airline company are used to test the validity of the proposed expert and intelligent system for both predicting enterprise outcomes in a long period and predicting the effects of specific events on enterprise outcomes in a short period.

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1. Introduction

Recently, enterprises have successfully used expert and intelligent systems (i.e., computer systems that imitate the ability of human decision making Jackson, 1998) in order to enable computers to extract social media users' feedback from large-scale and publicly available social media data (e.g., Twitter, Facebook, Instagram) automatically (Holzinger, Krüpl, & Herzog, 2006; Meire, Ballings, & Van den Poel, 2017; Mostafa, 2013). Social media are considered useful not only for enterprises, due to the ease of acquiring users'

feedback, but also for social media users, who can easily post opinions related to a wide range of topics (Tuarob & Tucker, 2015). In particular, due to its popularity and scalability, Twitter has been widely used as a suitable social media platform for expert and intelligent systems to discover users' feedback regarding enterprise decisions (Culnan, McHugh, & Zubillaga, 2010; Daniel, Neves, & Horta, 2017; Ghiassi, Skinner, & Zimbra, 2013; Greer & Ferguson, 2011; Ikeda, Hattori, Ono, Asoh, & Higashino, 2013; Oliveira, Cortez, & Areal, 2017).

While many existing expert and intelligent systems for Twitter user feedback discovery could enable computers to analyze the correlation between Twitter users' feedback (e.g., Twitter users' sentiment) and real-world enterprise outcomes (Asur & Huberman, 2010; Mao, Wei, Wang, & Liu, 2012) automatically, limited contributions have been made to analyze causal effects of Twitter

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ter users' feedback on real-world enterprise outcomes. The term "Twitter users' feedback" means information coming directly from Twitter users about what they feel with a company, a product, or a service. The term "enterprise outcome" is defined as the metric that is typically used to evaluate the success or failure of an enterprise. These include an enterprise's stock price, product sales, number of customers, market valuation, etc. The term "influential term group" is defined as a combination of enterprise-related terms on Twitter (e.g., "passenger", "ceo") that potentially influence enterprise outcomes. Should enterprise decision makers (e.g., CEOs) take Twitter users' feedback seriously when searching for emerging topics that the future market desires? Have enterprises reversed decisions as a result of Twitter users' feedback? Causality is differentiated from mere correlation, since a correlation between two events does not imply that one event (e.g., Twitter user feedback) causes the other (e.g., an enterprise outcome) (Aldrich, 1995).

The main contributions of this research are to propose an expert and intelligent system that enables computers to analyze causal relationships between natural language data (i.e., Twitter data) and real-world events (i.e., real-world enterprise outcomes) automatically. In particular, the proposed expert and intelligent system (1) identifies influential term groups having causal effects on enterprise outcomes from Twitter data and (2) discovers the appropriate time lags between identified influential term groups and enterprise outcomes. While existing expert and intelligent systems could enable computers to identify the spread of Twitter users' enterprise-related feedback automatically, identifying the causal effects on real-world enterprise outcomes is limited. The proposed expert and intelligent system discovers term candidates for influential term groups through (1) a co-occurrence network analysis model. (2) Time series models and (3) a Granger causality analysis model then identify influential term groups that have causal effects on real-world enterprise outcomes. The appropriate time lags between identified influential term groups and enterprise outcomes that have causal relationships are also discovered in order to measure how soon identified influential term groups cause enterprise outcomes. Solving these problems is challenging due to several reasons:

- There are over 500 million tweets (i.e., Twitter messages) generated each day (Bodnar, Dering, Tucker, & Hopkinson, 2016), many of which do not have causal relationships with real-world outcomes. As a result, an expert and intelligent system is needed to determine which Twitter users' feedback causes real-world enterprise outcomes.
- There is no fixed relationship between positive/negative Twitter messages and real-world outcomes. I.e., it is possible for negative Twitter users' sentiment (e.g., the announcement by iHOP that it was changing its name to iHOB) to have a positive impact on real-world outcomes (i.e., the name change inspired 36 billion social media (e.g., Twitter) users' impressions and resulted in a 0.7% increase in sales (Taylor, 2018)). Conversely, negative Twitter users' sentiment (e.g., backlash over United Airlines' passenger ejection decision) can result in negative real-world outcomes (i.e., United Airlines' decreased stock price) (Ohlheiser, 2017). The challenge is determining the impact that Twitter users' feedback will have on real-world outcomes.
- Given the discovery of Twitter users' feedback (i.e., influential term groups) that has been determined to have a causal relationship with real-world outcomes (e.g., stock price), the challenge is determining how long it will take for the discovered Twitter users' feedback to cause the real-world outcome. An expert and intelligent system is needed that provides enterprise decision makers with a timeline as to how long they have after Twitter users' feedback before the real-world impacts of this

feedback occur. This would enable enterprise decision makers to intervene and explore solutions that may mitigate or reverse the potential negative real-world outcomes (e.g., via an apology) before they occur.

On the left-hand side of Fig. 1, a current conceptual decision tree describes how Twitter users' feedback on enterprise decisions could potentially affect (1) enterprise outcomes, such as market sales or stock prices, and (2) enterprise decision makers' future decisions. Enterprise decisions have causal effects on customer reactions displayed on social media networks, including Twitter. For instance, *Microsoft's* digital rights management (DRM) policy announcement – that the *Xbox One* console requires an online check-in at least every 24 hours to validate the ownership of game software – caused strong negative reactions on Twitter (Strickl, 2013). Previous research has explored how enterprise decisions cause certain social media feedback, like Twitter users' feedback (Bruhn, Schoenmueller, & Schäfer, 2012; Kaplan & Haenlein, 2010). However, little work has been done on exploring which Twitter user feedback (i.e., influential term group in this work) causes certain enterprise outcomes. Considering causal effects of Twitter users' feedback is important, because negative Twitter users' feedback can negatively affect other users on Twitter and enterprises' future revenue. For instance, *United Airlines'* stock fell 4% and wiped out \$800 million in just three days after Twitter raged at *United Airlines* due to the CEO's email to his employees that defended those who forcibly dragged a passenger off an overbooked flight in 2017 (Imbert & Thomas, 2017). The proposed expert and intelligent system focuses on identifying overall Twitter users' feedback, instead of only monitoring a few influential users' Twitter messages that potentially cause enterprise outcomes (e.g., Kylie Jenner's one tweet that wiped out \$1.3 billion of Snapchat's market value Vasquez, 2018), because only monitoring a few influential users' tweets is relatively easier than identifying feedback from a large number of tweets written by overall Twitter users (i.e., both influential and ordinary Twitter users) (Bosch et al., 2013).

This research discovers Twitter users' feedback (i.e., influential term groups) that has causal effects on real-world enterprise outcomes. The proposed expert and intelligent system enables enterprise decision makers to change their current decisions before negative Twitter users' feedback about those current decisions decreases future enterprise outcomes. If positive Twitter users' feedback about the current decisions is discovered, enterprise decision makers can make new decisions that intensify positive factors identified from Twitter users' feedback in order to increase future enterprise outcomes. The proposed expert and intelligent system can therefore help enterprise decision makers identify significant Twitter users' feedback in real-time and at a low-cost. In addition, the proposed expert and intelligent system can be used to assist decision makers' decisions that will improve future enterprise outcomes, such as market sales or stock prices. The right-hand side of Fig. 1 illustrates the enterprise decision tree based on the proposed expert and intelligent system.

The remainder of the paper is organized as follows. This section provides an introduction and motivation for this work. Section 2 provides the background of related works. Section 3 proposes the expert and intelligent system to identify Twitter users' feedback (i.e., influential term groups) that causes enterprise outcomes. Section 4 introduces case studies involving a real-world internet video streaming and disc rental provider (i.e., *Netflix*) and an airline company (i.e., *United Airlines*) in order to validate the proposed expert and intelligent system not only for predicting enterprise outcomes in a long period but also for predicting the effects of specific events on enterprise outcomes in a short period. Section 5 presents the experimental results and discussion, and Section 6 concludes the paper.

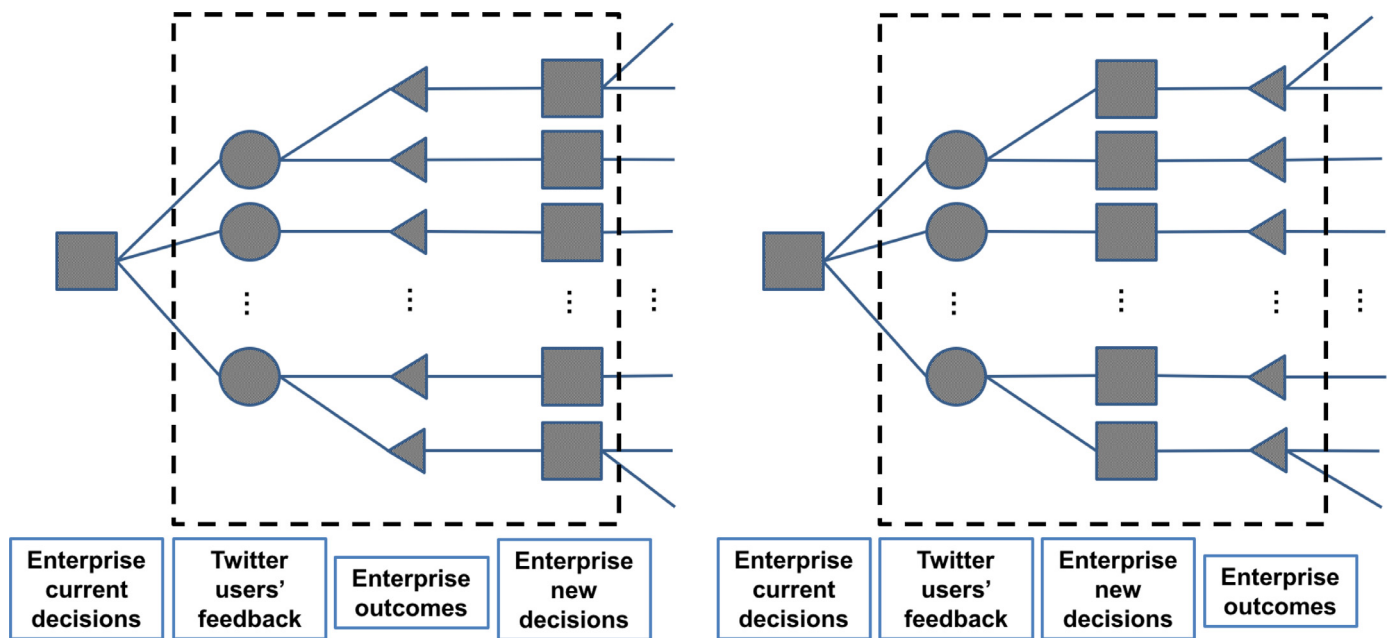


Fig. 1. Enterprise decision trees: without the proposed expert and intelligent system (left-hand side) and with the proposed expert and intelligent system (right-hand side).

2. Literature review

The literature review section contains literature related to social media user feedback extraction (Section 2.1) and using social media data to predict real-world events (Section 2.2).

2.1. Social media user feedback extraction

Identifying customer feedback could enable enterprise decision makers to understand feedback that leads to positive or negative consumer experiences (Chang, Chou, Wu, & Wu, 2017; Lim & Tucker, 2017). Customer feedback extraction methods from textual data are an emerging field. Wang, Youn, Azarm, and Kannan (2011) propose a systematic method that extracts customer data for product design selection based on web-based user-generated content. Yan, Xing, Zhang, and Ma (2015) develop a novel method that ranks candidate terms in online customer reviews in order to automatically elicit enterprise attributes that interest customers. Recently, a sentiment analysis and a case analogical reasoning model have been proposed for extracting enterprise attributes and latent customer needs from online consumer reviews (Zhou, Jiao, & Linsey, 2015).

Over the past years, social media platforms, including Twitter, have been widely used for eliciting customer feedback (Li, Chen, Liou, & Lin, 2014). For instance, Rui, Liu, and Whinston (2013) propose a dynamic panel data model in order to investigate how Twitter word-of-mouth influences movie sales. A novel decision support system is proposed for filtering valuable intelligence frozen in the large number of postings (Abrahams, Jiao, Fan, Wang, & Zhang, 2013) as well as finding, categorizing, and prioritizing automotive defects discussed in social media (Abrahams, Jiao, Wang, & Fan, 2012). Bao and Chang (2014) investigate the relationship between product reports written by journalists, social media feedback written by customers, and product sales (i.e., Amazon book sales) using the New York Times Best Seller List and Amazon user reviews. Using a cluster analysis, Zhang (2015) investigates the factors affecting both a company's overall information disclosure and its financial information disclosure in social media to discover that companies with high adoption levels attract more interested customers using social media than do companies with low levels. Tuarob and

Tucker (2015) propose a mathematical model that discovers latent customer feedback using ground truth data extracted from social media networks. Since ground truth data acquisition from social media data is expensive or unavailable in some cases, Lim and Tucker (2016) propose a Bayesian-based statistical sampling algorithm that extracts customer feedback from social media networks without utilizing ground truth data.

Nevertheless, considering social media user feedback that has causal effects on real-world enterprise outcomes is still limited. This consideration has recently become significant in enterprise decision making. Enterprise outcomes substantially affect business revenue, and real-time social media user feedback is useful for an enterprise's quick response to the market. In this work, the proposed system identifies social media user feedback that causes real-world outcomes for enterprise decision making.

2.2. Using social media data to predict real-world events

Predicting future events is significant for real-world businesses, because the ability to predict future events affects enterprise decision making and relates to market success (Fourt & Woodlock, 1960). Recently, several researchers have proposed methods that use social media data, including Twitter data, to predict real-world events (Liu, Wu, Li, & Li, 2015). For example, in order to predict population health indices, Nguyen et al. (2017) propose a mathematical model based on the distributions of textual features over Twitter data. Gerber (2014) presents a crime prediction model, based on linguistic analysis and statistical topic modeling, that uses spatiotemporally tagged tweets across Chicago, Illinois. Researchers show that their prediction methods that use social media data outperform existing predictors that forecast real-world events, such as Oscar award winners (Bothos, Apostolou, & Mentzas, 2010), energy utilization patterns (Bodnar, Dering, Tucker, & Hopkinson, 2016), and box-office revenues (Asur & Huberman, 2010; Ding, Cheng, Duan, & Jin, 2017).

In particular, sentiment expressed on social media networks has been widely utilized to predict enterprise outcomes (Khadjeh Nasirtoussi, Aghabozorgi, Ying Wah, & Ngo, 2014). Tuarob and Tucker (2013) propose a mathematical algorithm that quantifies the correlation between sentiment on social media networks

Table 1
Summary of previous studies and this research on predicting real-world enterprise outcomes.

Reference	Correlation between social media users' sentiment and enterprise outcomes	Correlation between social media user feedback and enterprise outcomes	Causation between social media users' sentiment and enterprise outcomes	Causation between social media user feedback and enterprise outcomes	Sentiment metric	The unit of analysis	Domain	Enterprise Outcome
Tuarob and Tucker (2015)	✓				3 classes (negative, neutral, and positive)	Products	Product markets	Product sales
Bogle and Potter (2015)	✓				3 classes (negative, neutral, and positive)	Jamaica Stock Exchange	Stock markets	Stock prices
Ding et al. (2017)	✓				2 classes (neutral and positive)	Movies	Box offices	Box office sales
Ho et al. (2017)	✓				A range of −2 to 2	Companies	Stock markets	Stock returns
Asur and Huberman (2010)		✓			—	Movies	Box offices	Box office revenues
Bollen et al. (2011)			✓		6 classes (calm, alert, sure, vital, kind, and happy)	Dow Jones Industrial Average (DJIA)	Stock markets	Stock prices
Bae and Lee (2012)			✓		3 classes (negative, neutral, and positive)	Audiences of popular users	Social media and real-world	The sentiment of audiences and real-world phenomena
Smailović, Grčar, Lavrač, and Žnidaršič (2013)			✓		The ratio of positive messages	Companies	Stock markets	Stock market movements
Ranco, Aleksovski, Caldarelli, Grčar, and Mozetič (2015)			✓		3 classes (negative, neutral, and positive)	Companies	Stock markets	Stock price returns
Checkley, Higón, and Alles (2017)			✓		A range of 0 to 4 for bullish and bearish sentiment	Companies	Stock markets	Financial indicator (return, trading volume, volatility)
Ours			✓	✓	A range of −5 to 5	Companies	Stock markets	Stock prices

and product market adoption in order to predict product sales. Nguyen, Shirai and Velcin (2015) analyze sentiment of the topics, which are extracted from social media networks using latent Dirichlet allocation (LDA), for stock market prediction. Ho, Damien, Gu, and Konana (2017) investigate a potential dynamic relationship between sentiment expressed on social media networks and future stock returns.

Table 1 shows a summary of existing studies and the proposed research on predicting real-world enterprise outcomes. While previous expert and intelligent systems have been widely applied to predict real-world enterprise outcomes, identifying social media user feedback that causes future enterprise outcomes, which can support enterprise decision makers' future decisions, remains ambiguous. Identifying social media user feedback helps enterprise decision makers understand how social media user feedback causes future enterprise outcomes. This work's novelty is that the expert and intelligent system presented identifies not only Twitter users' sentiment but also Twitter user feedback that has causal effects on real-world enterprise outcomes, while Bollen, Mao, and Zeng (2011) only consider Twitter users' overall sentiment that affects enterprise outcomes through Granger causality analysis. This work also provides the appropriate time lags between identified Twitter user feedback and real-world enterprise outcomes.

3. Method

Fig. 2 outlines the proposed expert and intelligent system with the steps involved in identifying Twitter users' feedback that

causes future enterprise outcomes, along with the appropriate time lags. First, textual and temporal data are extracted from Twitter data, and data preprocessing is employed. Term candidates for influential term groups, which are considered able to potentially affect enterprise outcomes, are identified through the co-occurrence network analysis model. Time series analysis models then analyze the patterns of Twitter users' feedback (i.e., Twitter users' sentiment and influential term groups) on enterprise decisions as well as the trend of real-world enterprise outcomes. Finally, the Granger causality analysis model identifies influential term groups, along with Twitter users' sentiment, that affect enterprise outcomes. The appropriate time lags between identified influential term groups and Twitter users' sentiment and real-world enterprise outcomes are also discovered through the Granger causality analysis model.

3.1. Twitter data acquisition and preprocessing

Tweets containing the name of the company (e.g., "netflix"), along with temporal information, are extracted, because only enterprise-related tweets are necessary for this research. If the name of the enterprise is not unigram (e.g., *United Airlines*), similar expressions, including the abbreviation of the enterprise, (e.g., "united airlines", "united airline", "unitedairlines", "unitedairline", "ua") are considered. Twitter application program interface (API) is used for Twitter data acquisition.

Tweets are filled with noise that can induce unexpected results (Russell, 2013). Therefore, data preprocessing is necessary for removing noise and enhancing the quality of the experimen-

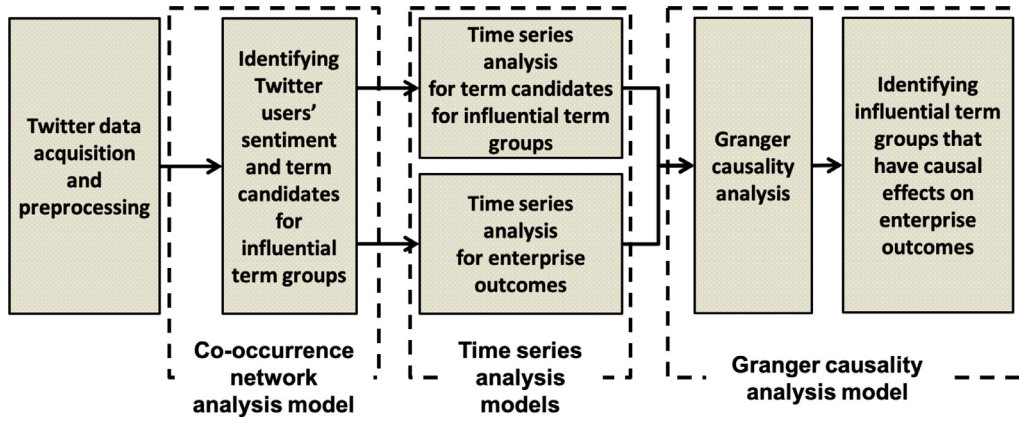


Fig. 2. Overview of the proposed expert and intelligent system.

tal results (Symeonidis, Effrosynidis, & Arampatzis, 2018). Out-of-vocabulary (OOV) words, such as typos (e.g., “dilivery” instead of “delivery”), single-word abbreviations (e.g., “luv” instead of “love”), and phonetic substitutions (e.g., “2day” instead of “today”) are transformed to in-vocabulary (IV) words using existing OOV word databases (e.g., Apache Lucene (Apache Lucene, 2010) and Spell Checker Oriented Word Lists (SCOWL) and Friends (Atkinson, 2017)), because tweets contain a high rate of OOV words (Nikfarjam, Sarker, O'Connor, Ginn, & Gonzalez, 2015). In this work, SCOWL and Friends, which is an English word database that contains 657,798 words useful for generating high quality word lists suitable for use in spell checkers of most English dialects, is used. A web application checks if a word is in SCOWL and assigns a score that indicates if a word should or should not be included based on its frequency in Google Book's corpus. Stemming is implemented using the Porter stemming algorithm (Porter, 2006) in order to improve result accuracy. For example, an original tweet “C U 2morrow” is converted to “see you tomorrow” after preprocessing.

3.2. Analyzing twitter users' sentiment and discovering term candidates for influential term groups

Analyzing Twitter users' sentiment and discovering term candidates for influential term groups are used to identify Twitter users' feedback that can affect future enterprise outcomes. In this work, time, which has a continuous nature, is approximated as a discrete time window. t is defined based on a unit of time (e.g., one day) for the discrete time window. It is assumed that the data belonging to the same time frame (i.e., the same sub-interval) are stationary (Kaźmierski & Morawiec, 2011), and this assumption is used in Granger causality analysis in further steps.

3.2.1. Sentiment analysis using Twitter data

SentiStrength, which is a trained sentiment classifier developed by Thelwall, Buckley, Paltoglou, Cai, & Kappas (2010), is used for sentiment analysis in this research. Each tweet is used as an input, and the output has a sentiment score that ranges from -5 to 5 . Positive and negative numbers indicate positive sentiment and negative sentiment, respectively, and 0 is neutral. Let $K(t)$ be the average of sentiment scores for all tweets written during the time period t ($t \in \{1, \dots, T\}$).

3.2.2. Discovering term candidates for influential term groups

In this research, term candidates for influential term groups are composed of enterprise-related terms by time period. Significant enterprise-related terms can be determined differently by different applications, because important factors for an insurance company's outcomes and important factors for an online retailer's out-

comes can differ. For instance, “shipping” may be one of the most significant enterprise-related terms for online retailers (e.g., *Amazon.com*), but it may not be an important factor for insurance companies (e.g., *GEICO*). It is therefore necessary to propose a generalized model for discovering Twitter users' feedback in order to apply the model to different applications.

In this section, enterprise-related term candidates are identified for creating influential term groups. Bigram and trigram keywords, as well as unigram keywords, are considered when identifying enterprise-related term candidates from tweets, because some enterprise-related expressions are bigrams or trigrams (e.g., “tv series” for *Netflix*) instead of unigrams. S is defined as a set of all tweets containing the name of the enterprise (e.g., “netflix”) for the whole time period.

Let S_1 , S_2 , and S_3 be sets of the frequent unigrams, bigrams, and trigrams, respectively, which are identified in S . Only unigrams, bigrams, and trigrams that appear more than 0.5% of S are contained in S_1 , S_2 , and S_3 , respectively, because it is considered that terms that appear with low frequency (i.e., less than 0.5% of S) do not have significant effects on enterprise-related term candidate discovery (Davidov, Tsur, & Rappoport, 2010; Stringam & Gerdes, 2010). Stop words (e.g., “it”, “to”) are excluded from S_1 , because language-specific functional terms and frequently occurring words in the English dictionary (i.e., stop words) are superfluous for enterprise-related term discovery. In addition, only bigrams and trigrams listed in *Urban Dictionary* (Peckham, 2009) are considered candidates for S_2 and S_3 (e.g., “tv series”). This is because *Urban Dictionary* is widely used in social media analytics as a website that provides user-generated content and voting mechanisms for defining colloquial terms (Marwick & boyd, 2011; Paul, Agrawal, Liao, & Choudhary, 2016; Peleja, Santos, & Magalhães, 2014; Thompson, Rivara, & Whitehill, 2015; Wu, Morstatter, & Liu, 2016). Only bigrams and trigrams listed in *Urban Dictionary* are considered term candidates for influential term groups in this research, because most of bigrams and trigrams (e.g., “worth it”, “it free”, “worth it free” in the sentence “Worth it! Free wifi, straight getting paid to Netflix and chill”) are not idiomatic expressions (Bodnar, Dering, Tucker, & Hopkinson, 2016). Conjunctions are not disregarded if they are part of the bigrams or trigrams. A frequent bigram in S_2 or a frequent trigram in S_3 , which is composed of a frequent unigram(s), is considered a different frequent terms with frequent unigrams for the same reason. For instance, “chill” and “netflix and chill”, which have different meanings, are considered different terms. Four-grams or larger are not considered in this research, because (1) it is assumed that S_1 , S_2 , or S_3 contain the sub-sequences of the appropriate four-gram or larger terms (Fürrnkranz, 1998; Bodnar, Dering, Tucker, & Hopkin-

son, 2016), and (2) tweets commonly consist of short messages and have a limit of 140 characters (Lim, Tucker, & Kumara, 2017).

The co-occurrence network analysis model is proposed to cluster the co-occurring unigrams, bigrams, and trigrams for creating influential term groups. A co-occurrence is a term interconnection based on their paired existence within a specified unit of text (Lim, Tucker, Jablokow, & Pursel, 2018). For instance, the terms “free” and “netflix and chill” co-occur if they both appear in a particular tweet (e.g., “Worth it! Free wifi, straight getting paid to Netflix and chill”). Let w_{ij} be a co-occurrence weight of the term k_i for another keyword k_j ($k_i, k_j \in \{S_1 \cup S_2 \cup S_3\}, i \neq j$). In this research, w_{ij} is defined in a method similar to the term expansion ranking function, which is introduced by Ruthven and Lalmas (2003) as Eq. (1). w_i is defined as Eq. (2).

$$w_{ij} = \log \frac{n_{ij}/(n_i - n_{ij})}{(n_j - n_{ij})/(n - n_i - n_j + n_{ij})} \cdot \left| \frac{n_{ij}}{n_i} - \frac{n_j - n_{ij}}{n - n_i} \right| \quad (1)$$

$$w_i = w_{i1} + w_{i2} + \dots + w_{i(i-1)} + w_{i(i+1)} + \dots + w_{iI}, \quad \forall i, j = 1, \dots, I \quad (2)$$

where:

n : the total number of tweets in S (i.e., a set of all tweets containing the enterprise name for the whole time period)

n_i : the number of tweets containing the enterprise name and a term k_i

n_{ij} : the number of tweets containing the enterprise name as well as terms k_i and k_j ($i \neq j$)

$$I = |S_1 \cup S_2 \cup S_3|$$

A weighted adjacency matrix A , which is a co-occurrence matrix among the terms from S_1 , S_2 , and S_3 , is then generated based on the co-occurrence weights as Eq. (3). A matrix A is not a triangular symmetric matrix, since $\frac{w_{ij}}{w_i} \neq \frac{w_{ji}}{w_j}$.

$$A = \begin{matrix} & \begin{matrix} k_1 & k_2 & k_3 & \dots & k_l \end{matrix} \\ \begin{matrix} k_1 \\ k_2 \\ k_3 \\ \vdots \\ k_l \end{matrix} & \begin{bmatrix} - & \frac{w_{12}}{w_1} & \frac{w_{13}}{w_1} & \dots & \frac{w_{1l}}{w_1} \\ \frac{w_{21}}{w_2} & - & \frac{w_{23}}{w_2} & \dots & \frac{w_{2l}}{w_2} \\ \frac{w_{31}}{w_3} & \frac{w_{32}}{w_3} & - & \dots & \frac{w_{3l}}{w_3} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ \frac{w_{l1}}{w_l} & \frac{w_{l2}}{w_l} & \frac{w_{l3}}{w_l} & \dots & - \end{bmatrix} \end{matrix} \quad (3)$$

An edge-weighted graph G of co-occurrence can be generated based on a matrix A . A graph G is expressed as a directed graph, since a matrix A is not a triangular symmetric matrix and the direction is important in this case. Only components of the matrix A that are above or equal to the average weights for each row (i.e., $\frac{w_{ij}}{w_i}$ that is greater than or equal to $\frac{1}{I-1}$) are used to construct the co-occurrence graph G , because the components having below the average weights are not considered to have a significant co-occurrence compared to other terms in the document (i.e., all tweets). In addition, each term group is defined as strongly connected components in the graph G , in a method similar to Cataldi, Di Caro, and Schifanella (2010). Fig. 3 shows an example of a (partial) co-occurrence graph for Netflix, where $S_1 = \{\text{“movie”}, \text{“show”}, \text{“episode”}, \text{“season”}, \text{“time”}\}$, $S_2 = \{\text{“bing watch”}, \text{“tv series”}\}$, and $S_3 = \{\text{“netflix and chill”}\}$. In this example, two term groups that contain multiple terms are identified: one contains the keywords “movie”, “show”, and “tv series”, and the other contains the keywords “episode”, “season”, and “time”. Some single components are not disregarded, because some frequent terms can be the term groups themselves, even if they do not have strongly connected neighbors (e.g., the term “netflix and chill” does not have strongly connected neighbors in Fig. 3.). In this work, a single term k_i is

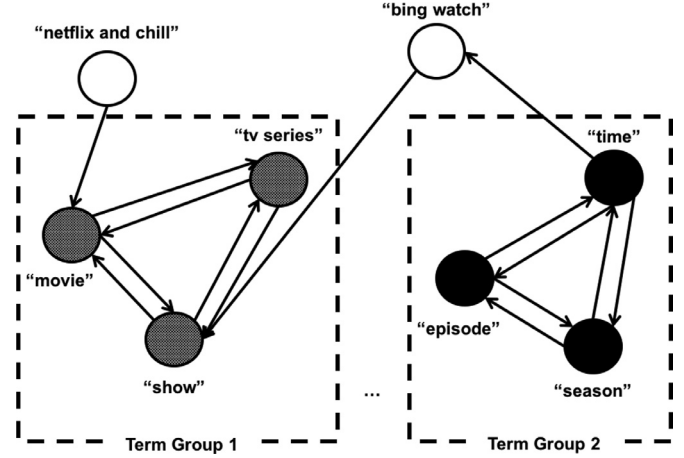


Fig. 3. An example of a partial co-occurrence graph G for Netflix.

considered an independent term group if the number of tweets containing both the enterprise name (e.g., the term “netflix”) and the term k_i is greater than or equal to the minimum value of the number of tweets containing the enterprise name and at least one term belonging to the same term group identified from the graph G (e.g., “episode”, “season”, or “time”). In this work, $X_p(t)$ is defined as Eq. (4) for period t based on its definition.

$$X_p(t) = \frac{n(p, t)}{n(t)}, \quad \forall p = 1, \dots, P, \quad \forall t = 1, \dots, T \quad (4)$$

where:

$n(t)$: the total number of tweets containing the enterprise name for period t .

$n(p, t)$: the number of tweets containing the name of the enterprise and at least one term belonging to the p^{th} term group for period t , where the number of identified term groups is P .

3.3. Time series analysis models

Time series models analyze a sequence of data points over time in order to extract the given data's statistical characteristics and predict future values based on previously observed data (Hamilton, 1994). Time series models are often used to predict the change of enterprise outcomes (Lee, Cho, Kwon, & Sohn, 2019; Luo, Zeng, & Duan, 2016; Rosas-Romero, Díaz-Torres, & Etcheverry, 2016; Weng, Lu, Wang, Megahed, & Martinez, 2018). In this research, two kinds of time series analysis models are proposed for identifying Twitter user's feedback that has causal effects on enterprise outcomes: (1) a time series analysis model that analyzes Twitter users' sentiment and influential term groups and (2) a times series analysis model that analyzes real-world enterprise outcomes.

Time series analysis model used for analyzing Twitter users' feedback quantifies the trend of Twitter users' sentiment and influential term groups. $K(t)$ is a time series analysis model for Twitter users' sentiment (see Section 3.2.1), and $X_p(t)$ ($p = 1, \dots, P$) is a time series analysis model for the p^{th} term groups for period t (see Section 3.2.2). Time series analysis models used for analyzing enterprise outcomes investigate the trend of real-world enterprise outcomes over time. Let $Y_j(t)$ ($j = 1, \dots, J$) be a time series analysis model used for analyzing the j^{th} enterprise outcome (e.g., market sales, stock prices) for period t , where the number of the enterprise outcomes is J .

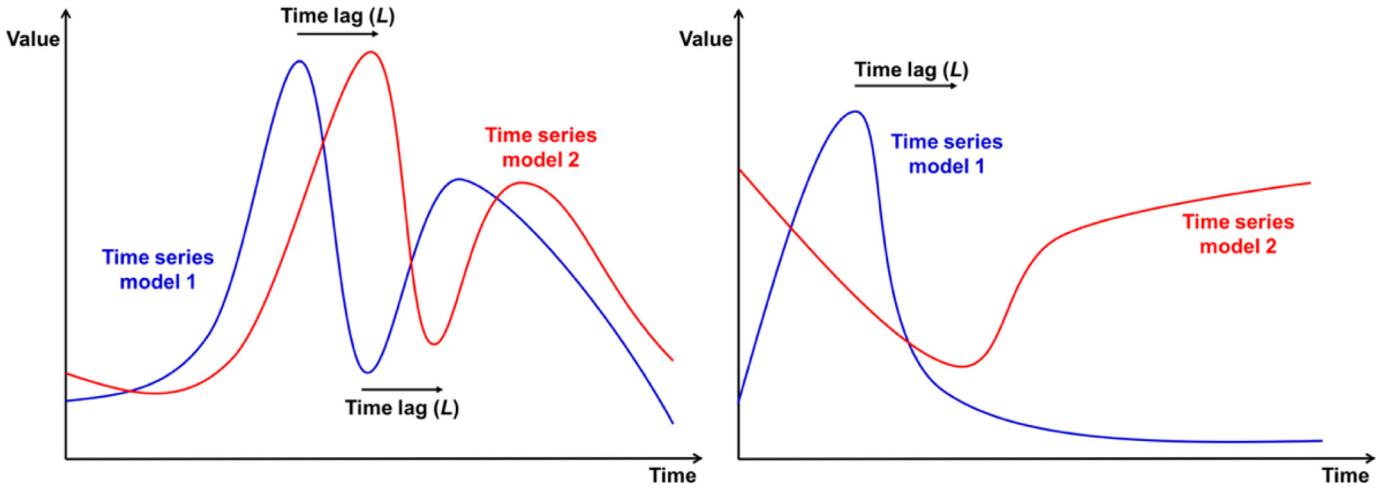


Fig. 4. Illustrations of two different time series models having positive causal relationships (left-hand side) and negative causal relationships (right-hand side).

3.4. Granger causality analysis model for twitter users' feedback and real-world enterprise outcomes

X is said to cause Y if it can be shown that X provides statistically significant information about the future values of Y . Causality is differentiated from mere correlation, because a correlation between two events does not imply that one event (e.g., Twitter users' feedback) causes the other (e.g., an enterprise outcome) (Aldrich, 1995). While traditional regressions consider correlations, causality analysis can test a predictive causal relationship between two time series models (Diebold, 2001). First introduced by C. W. Granger, Granger causality analysis identifies whether one stationary time series model can be used to predict the future values of the other stationary time series model. A Granger causal relationship is defined based on two principles (Granger, 1969). The first principle is *temporal precedence of causes*, which means that the effect does not happen prior to its cause. This first principle is commonly accepted by existing probabilistic causation theories (Good, 1961a,b; Suppes, 1970).

The second principle is predictability and can be validated through the following mathematical approach (Eichler, 2012; Liu & Bahadori, 2012). On the left-hand side of Fig. 4 illustrates how one time series model (i.e., the blue line) has positive causal effects on the other time series model (i.e., the red line) with a time lag L . On the right-hand side of Fig. 4 shows how one time series model (i.e., the blue line) has negative causal relationships with the other time series model (i.e., the red line) with a time lag L . Granger causality analysis is applicable to this work, since time series analysis models (i.e., $K(t)$, $X_p(t)$ ($p = 1, \dots, P$), and $Y_j(t)$ ($j = 1, \dots, J$)) are divided into sub-intervals based on a unit of time t and it is assumed that the time series are stationary in each sub-interval in this work (see Section 3.2) (Liu & Bahadori, 2012). A time lag L is not set to zero, because (1) it is known that a time delay in enterprise outcome responses (e.g., stock price responses) to news or events exists (Hou & Moskowitz, 2005) and (2) this research is used for predicting future outcomes that lead to future market success rather than discovering the correlation of current enterprise outcomes with Twitter users' feedback. In a further step, the appropriate values of a time lag L are also discovered.

In this research, the null hypothesis (i.e., $H_0(p, j)$) and the alternative hypothesis (i.e., $H_a(p, j)$) are defined as Eqs. (5) and (6), respectively. $Y_j(t)$ can be expressed as Eq. (7), which is a time series analysis model for the j^{th} enterprise outcomes that reflect causal effects of (1) Twitter users' sentiment ($K(t)$, set $p=0$) or (2) the p^{th} influential term group ($X_p(t)$ ($p = 1, \dots, P$)) (i.e., the full model).

Eq. (8) is the same time series analysis model with Eq. (7) except one additional regressor (i.e., $X_p(t-l)$). Eq. (9) is a time series analysis model for the j^{th} enterprise outcomes that does not reflect causal effects of any Twitter users' sentiment or influential term group (i.e., the reduced model):

$$H_0(p, j). \text{ Neither } K(t) \text{ or } X_p(t) \text{ causes } Y_j(t), B(l) = 0 \text{ or } C_p(l) = 0, \forall l = \dots, M \quad (5)$$

$$H_a(p, j). \text{ Either } K(t) \text{ or } X_p(t) \text{ causes } Y_j(t), B(l) \neq 0 \text{ or } C_p(l) \neq 0, \exists l = \dots, M \quad (6)$$

$$Y_j(t) = \sum_{m=1}^M A_j(m) \cdot Y_j(t-m) + \sum_{i=l+1}^M B(i) \cdot K(t-i) + \sum_{i=l+1}^M C_p(i) \cdot X_p(t-i) + \varepsilon_{j,l+1}, \quad \forall j = 1, \dots, J, \forall t = M, \dots, T \quad (7)$$

$$Y_j(t) = \sum_{m=1}^M A_j(m) \cdot Y_j(t-m) + \sum_{i=l+1}^M B(i) \cdot K(t-i) + \sum_{i=l+1}^M C_p(i) \cdot X_p(t-i) + \varepsilon_{j,l+1}, \quad \forall j = 1, \dots, J, \forall t = M, \dots, T \quad (8)$$

$$Y_j(t) = \sum_{m=1}^M A_j(m) \cdot Y_j(t-m) + \varepsilon_j, \quad \forall j = 1, \dots, J, \forall t = M, \dots, T \quad (9)$$

where:

$X_1(t)$: the value of the average sentiment scores at time t

$K(t)$: the average of sentiment scores for all tweets written during the time period t

$X_p(t)$: the proportion of tweets which mention a term from the p^{th} influential term group, out of all tweets containing the enterprise name at time t , $\forall p = 1, \dots, P$

$Y_j(t)$: the value of the j^{th} enterprise outcome at time t , $\forall j = 1, \dots, J$

$A_j(m)$: Coefficients for indicating the influence of the previous value of $Y_j(t)$, $\forall j = 1, \dots, J$

$B(i)$: Coefficients for indicating the influence of the previous value of $K(t)$

$C_p(i)$: Coefficients for indicating the influence of the previous value of $X_p(t)$, $\forall p = 1, \dots, P + 1$

P : the number of term groups extracted from Twitter users' feedback

J : the number of enterprise outcomes used for Granger causality analysis

M : the number of previous values used for predicting $Y_j(t)$ (i.e., the maximum possible value of time lags)

$\varepsilon_{j,l}$, ε_j : the prediction error, $\forall j = 1, \dots, J, \forall l = 0, \dots, M - 1$

M (i.e., the number of previous values used for predicting $Y_j(t)$) is set to 8 as the default value in this research. Commonly used lag parameter values of Granger causality for future market analysis is not greater than 8, and 8 is commonly used as the number of previous values for predicting $Y_j(t)$ (Bollen et al., 2011; Liew, 2004; Thornton & Batten, 1985). $H_0(p, j)$ is not rejected if and only if $C_p(1) = C_p(2) = \dots = C_p(M) = 0$ in Eq. (7) (or Eq. (8)). Partial F -tests are used to test the hypothesis. If the p -value is less than α (i.e., the significance level, implying that it is permissible to have an α probability of incorrectly rejecting the null hypothesis), the null hypothesis (i.e., $H_0(p, j)$) is rejected. It is then concluded that causal effects of (1) Twitter users' sentiment (set $p = 0$) or (2) the p^{th} term group on the j^{th} enterprise outcome exist. The proposed Granger causality analysis model identifies Twitter users' feedback that affects enterprise outcomes over the whole time period ($t \in \{1, \dots, T\}$). Decision makers can set the period for training the systems (i.e., T : the number of previous time units used for discovering Twitter users' feedback), while it is known that $T \geq 14$ is appropriate for the default value (Bollen et al., 2011; Makrehchi, Shah & Liao, 2013; Si et al., 2013).

The next step is identifying the appropriate time lag for each Twitter users' sentiment or term group. If $\hat{\sigma}_{j,l}^2$ (i.e., the estimated variance of $\varepsilon_{j,l}$ in Eq. (8)) is statistically significantly smaller than $\hat{\sigma}_{j,l+1}^2$ (i.e., the estimated variance of $\varepsilon_{j,l+1}$ in Eq. (7)), it is concluded that $X_p(t-l)$ has a significant causal effect on predicting $Y_j(t)$. The measure of causality at time lag l is defined as Eq. (10). The measure of causality can be tested using the likelihood ratio (LR) test statistic (Eq. (11)) (Gourieroux & Monfort, 1997; Gelper, Lemmens, & Croux, 2007):

$$C_j = \ln \frac{\hat{\sigma}_{j,l+1}^2}{\hat{\sigma}_{j,l}^2} \quad (10)$$

$$LR = 2(\log L(\theta_j) - \log L(\theta_{j+1})) \quad (11)$$

where:

$\log L(\theta_{j+1})$: the likelihood at the time series model that does not contain the additional regressor $X_k(t-l)$ (i.e., Eq. (7)), with θ_j the parameter vector collecting the estimate of all $A_j(m)$, $B(i)$, all $C_j(i)$, and the variance of the error term

$\log L(\theta_j)$: the likelihood at the time series model that contains the additional regressor $X_k(t-l)$ (i.e., Eq. (8)), with θ_j the parameter vector collecting the estimate of all $A_j(m)$, $B(i)$, all $C_j(i)$, and the variance of the error terms

Gourieroux and Jasiak (2001) show that $LR = N \times C_j \sim \chi_{1,1-\alpha}^2$, where N is the total number of observations. $\chi_{1,1-\alpha}^2$ is the α -upper quantile of the chi-squared distribution, where the degree of freedom is 2. Algorithm 1 summarizes the steps to identify the appropriate value of a time lag L . These steps are similar to the procedure proposed by Gourieroux & Monfort, 1997:

The proposed expert and intelligent system supports enterprise decision makers' future decisions based on identified Twitter users' feedback (see the right-hand side of Fig. 1). In particular, identified

Algorithm 1 Identification of the appropriate value of a time lag L .

STEP 1 Set $l = M - 1$.

STEP 2 If C_j is less than or equal to the critical value $\frac{\chi_{1,1-\alpha}^2}{N}$, go to STEP 3. Otherwise, go to STEP 4.

STEP 3 Set $l = l - 1$ and go to STEP 2.

STEP 4 Stop. Set $L = l + 1$ and return L (i.e., the appropriate value of a time lag).

Twitter users' feedback (i.e., influential term groups) helps enterprise decision makers change their decisions (or make new decisions) in real-time in order to predict and improve future enterprise outcomes. For instance, suppose that the term group "price" and "discount", is identified as an influential term group that has causal effects on future enterprise outcomes, and the appropriate time lag is four days. It is expected that real-time Twitter users' feedback regarding a price discount affects future enterprise outcomes after four days. The proposed expert and intelligent system then helps decision makers analyze Twitter users' feedback regarding a price discount in order to improve future enterprise outcomes.

4. Applications

This section introduces case studies involving an internet video streaming and disc rental provider (i.e., *Netflix*) and an airline company (i.e., *United Airlines*). These case studies are used to verify the proposed expert and intelligent system for a relatively long period (i.e., one year) and for a specific event (i.e., the *United Express Flight 3411* incident Victor & Stevens, 2017), respectively. Experiments are conducted on a 2.5 GHz Intel Core i7 with 16GB RAM using *Python* 2.7.14 and *R* 3.4.3. Two Twitter datasets, which were random subsamples using Twitter API, along with temporal information, are exploited for the case studies of *Netflix* and *United Airlines*, respectively. Tweets not written in English are disregarded in this case study. Apache Lucene API as well as Spell Checker Oriented Word Lists are used to transform OOV words to IV words. The Fox stop list (Fox, 1989) is used to remove stop words. Default values are used to set α (i.e., 0.05) and M (i.e., 8).

The results of the proposed expert and intelligent system, which considers keyword frequencies and co-occurrences for discovering Twitter users' feedback (see Section 3.2.2), are compared with the results of a random-keyword-sampling method in order to validate the need to consider keyword frequencies and co-occurrences. A random-keyword-sampling method is defined as a method that, instead of considering keyword frequencies and co-occurrences, randomly samples terms from all tweets as term candidates for influential term groups.

4.1. Case study for Netflix

On the one hand, a case study for *Netflix* validates whether or not the proposed expert and intelligent system is applicable for identifying Twitter users' feedback that has causal effects on enterprise outcomes for a relatively long period (i.e., one year). Twitter data over a time period from January 4, 2016 to December 30, 2016 in the United States is used in the case study for *Netflix*. Among the whole dataset, 17,170,347 tweets containing the term "netflix" are extracted for this case study.

Netflix's *Nasdaq* index is selected as the *Netflix*-related outcome for this case study, because it is the only *Netflix*-related daily outcome. Most other *Netflix*-related outcomes (e.g., market sales, the number of subscribers) are quarterly outcomes, which are too sparse for detailed analysis. J is 1, because only one enterprise outcome (i.e., the *Netflix's* *Nasdaq* index) is used in this case study. Let t be the t^{th} day on weekdays from January 4, 2016 to December

Table 2

Netflix-related attributes identified from the co-occurrence graph G and by the random-keyword-sampling method, their p -values, and the appropriate time lags (L).

		The number of n-grams in the group			p -value for enterprise outcome (stock price)	L
		Unigrams	Bigrams	Trigrams		
$S_1 = \{\text{"watch", "show", "series", "movie", "season", "chill", "need", "day", "tv", "time", "love", "youtube", "episode", "night", "start", "bing", "hulu", ..., "trailer", ...}\}$ (the total number of unigrams: 33)						
$S_2 = \{\text{"bing watch", "tv series", "tv show"}\}$ (the total number of bigrams: 3)						
$S_3 = \{\text{"netflix and chill"}\}$ (the total number of trigrams: 1)						
Twitter users' sentiment Netflix-related term group identified from the graph G (by the proposed model)	"watch", "bing", "hulu", "bing watch"	3	1	0	0.31 0.49	— —
	"show", "series", "movie", "tv", "tv show", "tv series"	4	2	0	0.04	4
	"season", "time", "episode"	3	0	0	0.03	3
	"need", "day", "love"	3	0	0	0.17	—
	"chill", "night", "netflix and chill"	2	0	1	0.21	—
	"youtube", "start", "trailer"	3	0	0	0.03	3
	Netflix-related term group consisting of randomly sampled keywords (by the random-keyword-sampling method)	3	1	0	0.77	—
	"essay", "pandora", "documentary", "thank", "luke cage", "fuller house"	4	2	0	0.55	—
	"walk", "life", "day"	3	0	0	0.86	—
	"eat", "good", "cute"	3	0	0	0.79	—
	"random", "website", "haters back off"	2	0	1	0.96	—
	"best", "daredevil", "suggestion"	3	0	0	0.55	—

30, 2016 (i.e., 252 weekdays), and T is set to 252. $Y_1(t)$ is defined as the Netflix's Nasdaq index.

4.2. A case study for United Airlines

On the other hand, a case study for *United Airlines* validates whether or not the proposed expert and intelligent system is applicable to identify Twitter users' feedback having causal effects on enterprise outcomes for the specific event (i.e., the *United Express Flight 3411* incident) and a relatively short period (i.e., 15 weekdays). Twitter data in a time period from April 3, 2017 to April 24, 2017 (i.e., from five weekdays before the incident on April 9 to ten weekdays after the incident) in the United States is used in the case study for *United Airlines*. Among the whole dataset, 140,286 tweets containing the term "united airlines", "united airline", "unitedairlines", "unitedairline", or "ua" (i.e., the abbreviation for "united airlines") are extracted for this case study.

Like the case of Netflix, the *United Airlines' Nasdaq* index is used as the *United Airlines*-related outcome for this case study as well, because it is the only *United Airlines*-related daily outcome. Other *United Airlines*-related outcomes, such as market sales, are quarterly outcomes, which are too sparse for detailed analysis. J is 1, because only one enterprise outcome (i.e., the *United Airlines' Nasdaq* index) is selected in this study. Let t be the t^{th} day on weekdays from April 3, 2017 to April 24, 2017 (i.e., 15 weekdays) and T is set to 15. $Y_1(t)$ is defined as the *United Airlines' Nasdaq* index on the t^{th} day. In addition, sensitivity analysis is implemented to discover the effects of changing time windows and window sizes.

5. Results and discussion

5.1. Results for Netflix case study

Table 2 shows the partial results of S_1 , S_2 , and S_3 , which are Netflix-related unigrams, bigrams, and trigrams that appear more than 0.5% of S (see Section 3.2.2), respectively (i.e., components of the co-occurrence graph G). The full results can be found in the

Appendix A (Table A1). Table 2 illustrates six Netflix-related term groups that consist of unigrams, bigrams, and trigrams, along with their numbers, identified from the co-occurrence graph G . It also provides another six Netflix-related term groups, which consist of the same numbers of unigrams, bigrams, and trigrams identified by the random-keyword-sampling method. Table 2 shows the p -values of $H_0(p, 1)$ and the appropriate time lags (i.e., L) identified through Algorithm 1. Only Netflix-related term groups that have p -values less than 0.05 provide the appropriate time lags (see Section 3.4). Fig. 5 illustrates the time series of Netflix's Nasdaq index as well as identified influential term groups, which has p -values less than 0.05 in Table 2. Figs. 6 and 7 show the partial graphs of Fig. 5 in order to highlight the causal relationships between identified influential term groups and (1) an increase in Netflix's Nasdaq index and (2) a decrease in Netflix's Nasdaq index, respectively.

5.2. Results for United Airlines case study

Table 3 illustrates the partial results of S_1 , S_2 , and S_3 , which are United Airlines-related unigrams, bigrams, and trigrams that appear more than 0.5% of S (see Section 3.2.2), respectively (i.e., components of the co-occurrence graph G). The full results can be found in the Appendix A (Table A2). It shows five United Airlines-related term groups that consist of unigrams, bigrams, and trigrams, along with their numbers, identified from the co-occurrence graph G . Table 3 also shows another five United Airlines-related term groups, which consist of the same numbers of unigrams, bigrams, and trigrams, identified by the random-keyword-sampling method. It indicates the p -values of $H_0(p, 1)$ and the appropriate time lags (i.e., L) are identified through Algorithm 1 as well. Only United Airlines-related term groups, which have p -values less than 0.05, provide the appropriate time lags (see Section 3.4). Fig. 8 illustrates the time series of United Airlines' Nasdaq index as well as identified influential term groups, which has p -values less than 0.05 in Table 3.

5.2.1. Sensitivity analysis for United Airlines case study

While Netflix case study uses a relatively long period (i.e., one year), United Airlines case study uses a short period (i.e., 15 week-

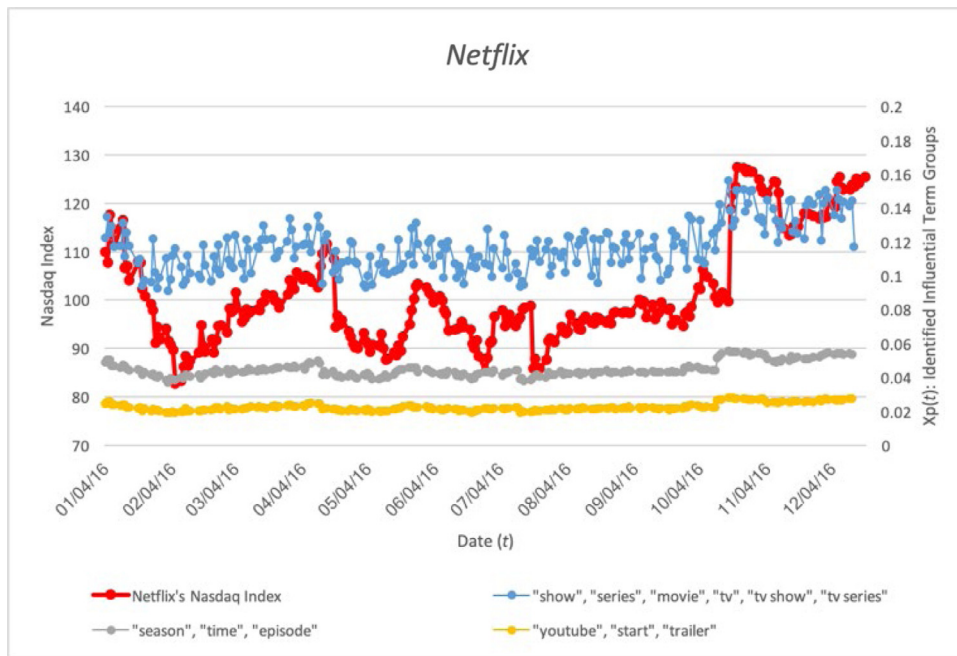


Fig. 5. Time series of Netflix' Nasdaq index as well as identified influential term groups.

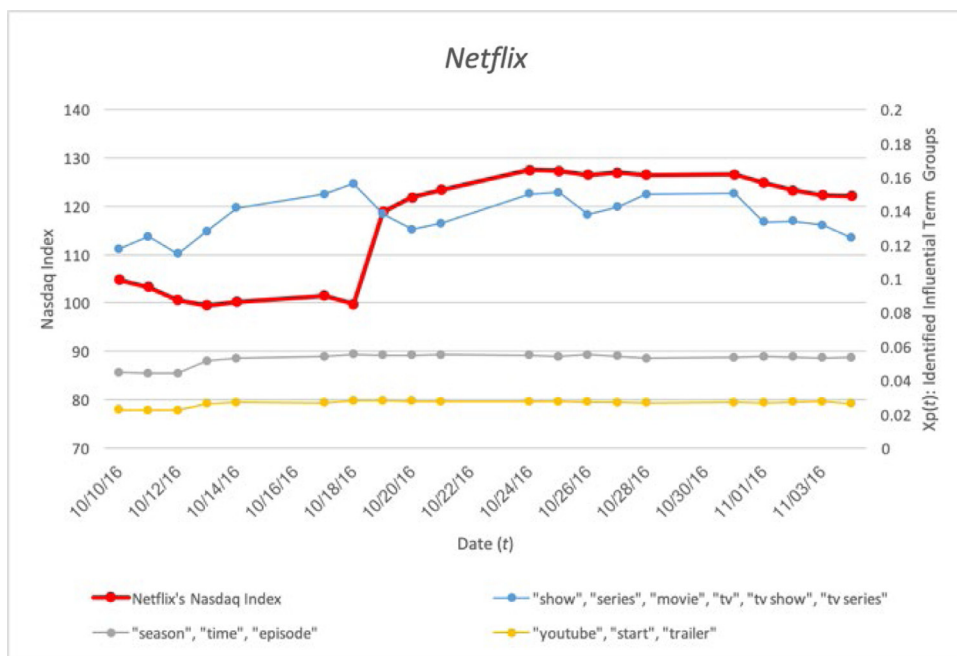


Fig. 6. A partial graph of Fig. 5 (October 10, 2016–November 5, 2016).

days), so selecting time windows and window sizes can be sensitive to the results of *United Airlines'* case study. Sensitivity analysis is therefore implemented in order to discover whether or not different time windows (i.e., different first day) and different window sizes (i.e., different T) affect the causal relationships between Twitter users' feedback and *United Airlines'* Nasdaq index. Table 4 shows the results of sensitivity analysis using three different first days (i.e., April 3, 2017, March 30, 2017, and April 5, 2017) and three different T (i.e., 15, 10, and 20) for the same identified influential term groups. It illustrates the influential term groups, the p -values of $H_0(p, 1)$, and the appropriate time lags (i.e., L) for each time window and window size.

5.3. Overall discussion

According to Sections 5.1 and 5.2, the proposed expert and intelligent system can be used for identifying Twitter users' feedback not only to predict future enterprise outcomes over a long term (Section 5.1) but also to identify the effects of specific events on future enterprise outcomes in a short period (Section 5.2). Identified Twitter users' feedback can be used by enterprise decision makers to change their current decisions before Twitter users' feedback about current decisions or events affecting future enterprise outcomes (i.e., time lags), as shown on the right-hand side of Fig. 1. The results of Tables 2 and 3 (and Tables A1 and A2) show that

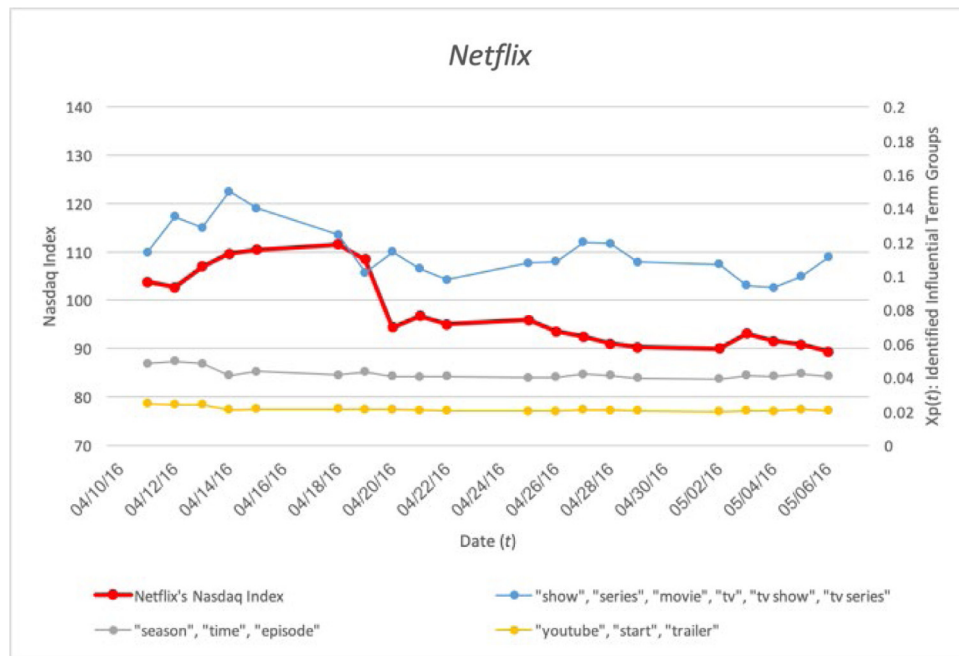


Fig. 7. A partial graph of Fig. 5 (April 11, 2016–May 7, 2016).

Table 3

United Airlines-related attributes identified from the co-occurrence graph G and by the random-keyword-sampling method, their p -values, and the appropriate time lags (L).

$S_1 = \{\text{"flight", "passenger", "drag", "overbook", "remove", "man", "video", "plane", "ceo", "customer", "forcible", "seat", "incident", ..., "news", "apology", ..., "time", ..., "munoz", "oscar", ..., "youtube", ..., "social", ..., "media", "twitter", ...}\}$ (the total number of unigrams: 114)

$S_2 = \{\text{"oscar munoz", "social media"}\}$ (the total number of bigrams: 2)

$S_3 = \emptyset$ (the total number of trigrams: 0)

		The number of n-grams in the group			p-value for enterprise outcome (stock price)	L
		Unigrams	Bigrams	Trigrams		
Twitter users' sentiment		—	—	—	0.24	—
United Airlines-related term group identified from the graph G (by the proposed model)	"passenger", "drag", "remove", "plane", "seat"	5	0	0	0.03	2
	"flight", "overbook"	2	0	0	0.15	—
	"man", "video", "customer", "youtube"	4	0	0	0.29	—
	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	7	2	0	0.04	2
	"incident", "forcible", "news", "time"	4	0	0	0.22	—
United Airlines-related term group consisting of randomly sampled keywords (by the random-keyword-sampling method)	"fatigue", "number", "europe", "exit", "demo"	5	0	0	0.64	—
	"lesson", "die"	2	0	0	0.79	—
	"trash", "gate", "collect", "vote"	4	0	0	0.41	—
	"damn", "mention", "agent", "cover", "leader", "risk", "san francisco", "jet lag"	7	2	0	0.64	—
	"photo", "bathroom", "refund", "woman"	4	0	0	0.59	—

frequent enterprise-related terms are different for different applications. They also indicate that most frequent *Netflix*-related terms and frequent *United Airlines*-related terms are unigrams (i.e., 33 out of 37 and 114 out of 116, respectively). It is postulated that tweets commonly consist of short messages (Lim & Tucker, 2016). The number of selected frequent *United Airlines*-related terms (i.e., 116) is more than three times greater than the number of selected frequent *Netflix*-related terms (i.e., 37). It is postulated that specific events (e.g., the *United Express Flight 3411* incident in this

case study) lead to the use of certain terms (e.g., "drag", "remove", "forcible" in Tables 2 and A1), but further analysis is necessary in the future. Tables 2 and 3 illustrate that frequent bigrams and trigrams and their subsequences are contained in the same group (e.g., "watch", "bing", and "bing watch" in Table 2 and "munoz", "oscar", "social", "media", "oscar munoz", and "social media" in Table 3). These results demonstrate the reason why only bigrams and trigrams listed in *Urban Dictionary* are considered and four-grams or larger sizes are disregarded in this research.

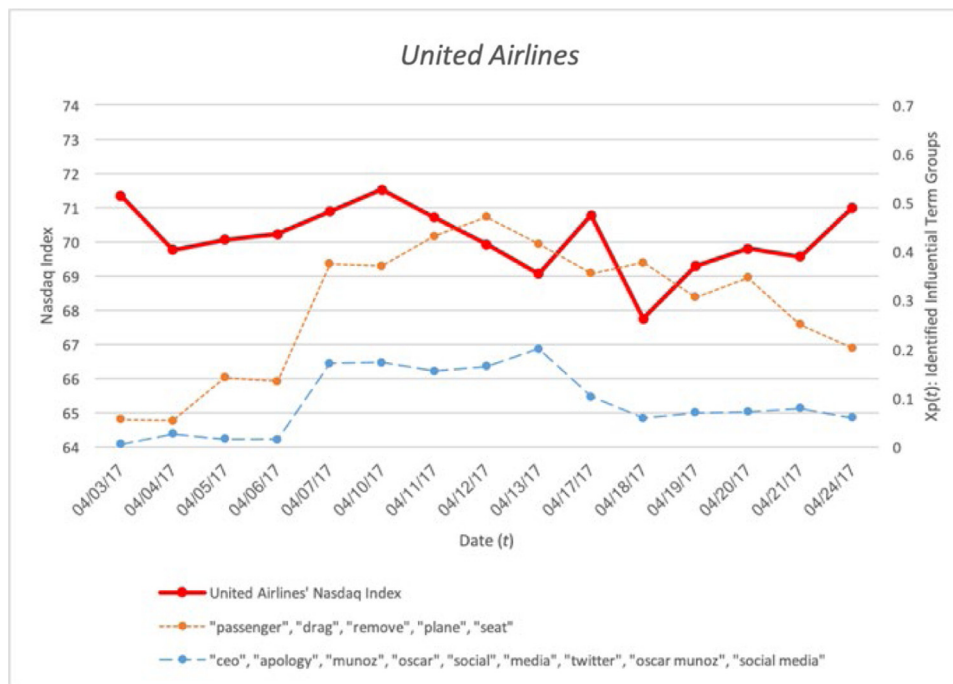


Fig. 8. Time series of *United Airlines' Nasdaq* index as well as identified influential term groups.

Table 4
The results of sentiment analysis for *United Airlines* case study.

Case	First day	T	Influential term group	p-value for enterprise outcome (stock price)	L
1	April 3, 2017	15	"passenger", "drag", "remove", "plane", "seat"	0.03	2
2	April 3, 2017	10	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.04	2
3	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.02	2
4	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
5	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
6	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.04	2
7	April 3, 2017	15	"passenger", "drag", "remove", "plane", "seat"	0.04	2
8	April 3, 2017	10	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.04	2
9	April 3, 2017	10	"passenger", "drag", "remove", "plane", "seat"	0.03	2
10	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.04	2
11	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
12	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
13	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
14	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
15	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
16	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
17	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
18	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
19	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
20	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
21	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
22	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
23	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
24	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
25	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
26	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
27	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
28	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
29	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
30	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
31	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
32	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
33	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
34	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
35	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
36	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
37	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
38	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
39	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
40	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
41	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
42	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
43	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
44	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
45	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
46	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
47	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
48	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
49	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
50	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
51	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
52	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
53	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
54	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
55	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
56	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
57	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
58	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
59	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
60	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
61	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
62	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
63	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
64	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
65	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
66	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
67	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
68	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
69	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
70	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
71	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
72	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
73	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
74	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
75	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
76	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
77	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
78	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
79	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
80	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
81	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
82	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
83	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
84	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
85	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
86	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
87	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
88	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
89	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
90	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
91	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
92	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
93	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
94	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
95	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
96	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
97	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
98	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2
99	April 3, 2017	20	"passenger", "drag", "remove", "plane", "seat"	0.03	2
100	April 3, 2017	20	"ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media"	0.03	2

According to Tables 2 and 3, the proposed expert and intelligent system, which considers term frequencies and co-occurrences, identifies three influential term groups that affect *Netflix's Nasdaq* index over a long term and two influential term groups that affect *United Airlines' Nasdaq* index in a short period. (The proposed expert and intelligent system identifies three influential term groups that affect *United Airlines' Nasdaq* index when $T=10$.) By contrast, term combinations selected by the random-keyword-sampling method (i.e., randomly sampled terms) are not causally associated with stock prices of both *Netflix* and *United Airlines*. It is concluded that considering term frequencies and co-occurrences is necessary to identify Twitter users' feedback that has causal effects on enterprise outcomes. Tables 2 and 3 also show that only using overall Twitter users' sentiment is not appropriate for predicting future enterprise outcomes in this case study, because their p -values are greater than 0.05 (i.e., 0.31 in Table 2 and 0.24 in Table 3, respectively). However, further research should investigate

these phenomena in detail. It is postulated that keywords related to launching new series or episodes (e.g., "show", "series", "movie", "season", "episode", "start", "trailer" in Table 2) can be used to predict *Netflix's* future outcomes (i.e., stock prices in this case study). It is also postulated that terms related to the *United Express Flight 3411* incident (e.g., "passenger", "drag", "remove", "plane", "seat" in Table 3) and terms related to the *United Airlines* CEO's follow-up action (e.g., "ceo", "apology", "oscar munoz", "social media" in Table 3) had casual effects on *United Airlines'* stock prices. On the other hand, randomly sampled terms (e.g., "kid", "girl", "origin", "stranger things" in Table 2 and "fatigue", "number", "europe", "exit", "demo" in Table 3) are not appropriate for identifying Twitter users' feedback that causes both *Netflix's* and *United Airlines'* outcomes (i.e., stock prices). For example, Table 5 illustrates a random subsample of (1) tweets containing terms relating launching new series/episodes (i.e., "episode", "trailer", and "series") and (2) tweets not containing those terms in order to identify whether or

Table 5

A random subsample of (1) tweets containing terms relating launching new series/episodes and (2) tweets not containing those terms.

Tweet	Terms relating launching new series/episodes	Whether or not the tweet is actually related to launching new series/episodes
New episode of orphan black out on Netflix and I couldn't be happier	"episode"	Yes
Netflix announces 'The Little Prince' release with beautifully moving trailer	"trailer"	Yes
Drew Barrymore to Star In Upcoming Netflix Comedy Series , Santa Clarita Diet, and I'm Glad	"series"	Yes
Netflix and Chill Type of Night	–	No
@dyxxxxxx Need to get Netflix	–	No

not terms in the influential term groups are indeed used in tweets relating to launching new series/episodes on *Netflix*.

On the one hand, Fig. 5 shows that all three identified influential term groups (i.e., Twitter users' feedback) for *Netflix* positively affect *Netflix*'s *Nasdaq* index (see Table 2). On the other hand, Fig. 6 indicates that all two identified influential term groups for *United Airlines* negatively affect *United Airlines*' *Nasdaq* index (see Table 3). Tables 2 and Fig. 5 illustrate that time lags between the time series of the identified influential term groups and the time series of *Netflix*'s outcomes have a value of 3 or 4 in this case study, which are also known as common values of the appropriate time lags of existing Granger causality models for future market analysis (Bollen et al., 2011; Thornton & Batten, 1985). On the other hand, Table 3 and Fig. 6 show that time lags between the time series of all two identified influential term groups and the time series of *United Airlines*' outcomes have a value of 2. It is postulated that time lags for a specific event(s) (e.g., the *United Express Flight 3411* incident in this case study) are relatively shorter than common values of the appropriate time lags (i.e., 3 or 4), but further investigation is necessary.

Table 4 illustrates that the first two influential term groups (i.e., "passenger", "drag", "remove", "plane", "seat" and "ceo", "apology", "munoz", "oscar", "social", "media", "twitter", "oscar munoz", "social media") have causal relationships with *United Airlines*' *Nasdaq* index and their appropriate time lags are 2 for all nine cases. These results indicate that different time windows and different window sizes do not significantly affect the causal relationship between the identified influential term groups and enterprise outcomes (i.e., *United Airlines*' *Nasdaq* index).

6. Conclusions and future work

The novel contribution of this research is to propose the expert and intelligent system that enables computers to identify Twitter users' feedback having causal effects on real-world enterprise outcomes automatically. While existing expert and intelligent systems can be used to identify the spread of Twitter users' enterprise-related feedback (Asur & Huberman, 2010; Mao et al., 2012), identifying the causal relationships between Twitter users' feedback and enterprise outcomes is limited. Twitter users' feedback having causal effects, which is identified using the proposed expert and intelligent system, supports decision makers to improve future enterprise outcomes (e.g., future stock price values, market sales).

This paper is comprised of four main steps. First, textual and temporal information are extracted from Twitter data, and data preprocessing is exploited. Term groups that potentially affects enterprise outcomes are identified through the co-occurrence network analysis model. Time series analysis models are implemented for analyzing (1) the trend of identified Twitter users' feedback (i.e., Twitter users' sentiment and term groups) and (2) the trend of real-world enterprise outcomes. Finally, the Granger causal analysis model identifies Twitter users' feedback that has causal effects on enterprise outcomes. The Granger causality analysis model identifies the appropriate time lags between identified Twitter

users' feedback (i.e., Twitter users' sentiment or influential term groups) and enterprise outcomes as well.

Case studies involving Twitter data related to (1) a real-world internet video streaming and disc rental provider (i.e., *Netflix*) and (2) an airline company (i.e., *United Airlines*) are used to test the validity of this research. Experimental results present several insightful implications. While the proposed expert and intelligent system considers not only frequent unigrams but also frequent bigrams and trigrams for identifying influential term groups, experimental results of two case studies illustrate that most frequent terms of influential term groups are unigrams, because Twitter messages typically consist of short messages. Experimental results of *United Airlines* case study illustrate that specific events (e.g., the *United Express Flight 3411* incident) induce Twitter users to use certain terms (e.g., "drag", "remove", "forcible"). Experimental results also indicate that identified influential term groups can be used to predict enterprise future outcomes, since it is discovered that identified influential term groups (i.e., (1) terms related to launching new series or episodes of *Netflix* case study and (2) terms related to the *United Express Flight 3411* incident and the *United Airlines* CEO's follow-up action of *United Airlines* case study) had causal effects on enterprises' stock prices.

It is therefore concluded that the expert and intelligent system presented in this work, which considers term frequencies and co-occurrences, can be useful for identifying Twitter users' feedback that causes future market success and for helping enterprise decision makers improve future enterprise outcomes. It is postulated that the proposed expert and intelligent system can be applied to predict long-term future enterprise outcomes and to identify the effects of a specific event(s) on short-term future enterprise outcomes.

Although this research proposes the expert and intelligent system that enables computers to identify Twitter users' feedback having causal relationships with enterprise outcomes automatically, there are still several ways to improve its performance as below:

- This research considers only overall Twitter users' sentiment regarding the company, but future work will also consider Twitter users' sentiment for each influential term group separately, because Twitter users' sentiment can be different for the different events regarding the same company (e.g., the *United Express Flight 3411* incident and the *United Airlines* CEO's follow-up action).
- Future research will consider not only Twitter users' sentiment and enterprise-related terms but also Twitter user information (e.g., gender, age, and posting frequency) in order to improve the performance of the proposed expert and intelligent system.
- Synonyms, which are not considered in this research, will be considered in future research, because there exist different terms with a similar meaning (e.g., "see" and "watch"), which can be included in the same influential term group.
- Topic models (e.g., latent Dirichlet allocation) can be applied for generating a co-occurrence graph *G* in order to improve the performance of the co-occurrence network analysis model.

- Tables A1 and A2

[illegible]

Table A2

Frequent <i>United Airlines</i> -related terms (k_i)	“flight”	“passenger”	“drag”	“overbook”	“remove”	“man”	“video”	“plane”	“ceo”	“customer”	“forcible”
Total number of tweets containing k_i (n_i)	18,124	17,591	12,980	10,830	8508	7818	7783	7543	6797	6135	5177
$\frac{n_i}{n}$ (%)	12.92	12.54	9.25	7.72	6.06	5.57	5.55	5.38	4.85	4.37	3.69
Frequent <i>United Airlines</i> -related terms (k_i)	“seat”	“incident”	“people”	“doctor”	“go”	“news”	“apology”	“say”	“beat”	“time”	“pepsi”
Total number of tweets containing k_i (n_i)	4438	4016	3869	3718	2994	2991	2898	2890	2887	2850	2832
$\frac{n_i}{n}$ (%)	3.16	2.86	2.76	2.65	2.13	4.85	4.37	3.69	3.16	2.86	2.76
Frequent <i>United Airlines</i> -related terms (k_i)	“need”	“munoz”	“oscar”	“shame”	“pay”	“boycott”	“trump”	“show”	“think”	“way”	“youtube”
Total number of tweets containing k_i (n_i)	2705	2662	2493	2431	2417	2408	2260	2178	2177	2096	2033
$\frac{n_i}{n}$ (%)	2.65	2.13	1.78	1.73	1.72	1.72	1.61	1.55	1.55	1.49	1.45
Frequent <i>United Airlines</i> -related terms (k_i)	“disgust”	“happen”	“treat”	“hope”	“stock”	“use”	“give”	“see”	“police”	“bad”	“travel”
Total number of tweets containing k_i (n_i)	2021	2001	1992	1982	1975	1894	1882	1880	1866	1856	1769
$\frac{n_i}{n}$ (%)	1.44	1.43	1.42	1.41	1.41	1.35	1.34	1.34	1.33	1.32	1.26
Frequent <i>United Airlines</i> -related terms (k_i)	“book”	“look”	“today”	“know”	“thing”	“watch”	“want”	“sky”	“day”	“social”	“assault”
Total number of tweets containing k_i (n_i)	1684	1677	1677	1653	1619	1606	1534	1520	1494	1479	1477
$\frac{n_i}{n}$ (%)	1.20	1.20	1.20	1.18	1.15	1.14	1.09	1.08	1.06	1.05	1.05
Frequent <i>United Airlines</i> -related terms (k_i)	“media”	“twitter”	“friend”	“guy”	“ticket”	“dao”	“come”	“call”	“resign”	“crisis”	“kick”
Total number of tweets containing k_i (n_i)	1439	1421	1439	1403	1377	1373	1367	1319	1278	1262	1257
$\frac{n_i}{n}$ (%)	1.03	1.01	1.03	1.00	0.98	0.98	0.97	0.94	0.91	0.90	0.90
Frequent <i>United Airlines</i> -related terms (k_i)	“market”	“shit”	“week”	“offer”	“year”	“fire”	“staff”	“chicago”	“board”	“boss”	“sue”
Total number of tweets containing k_i (n_i)	1215	1179	1158	1142	1138	1131	1120	1108	1088	1086	1074
$\frac{n_i}{n}$ (%)	0.87	0.84	0.83	0.81	0.81	0.81	0.80	0.79	0.78	0.77	0.77
Frequent <i>United Airlines</i> -related terms (k_i)	“david”	“asian”	“fuck”	“ask”	“face”	“class”	“thank”	“work”	“fight”	“drop”	“troll”
Total number of tweets containing k_i (n_i)	1073	1054	1050	1045	1034	1032	1007	990	982	963	944
$\frac{n_i}{n}$ (%)	0.76	0.75	0.75	0.74	0.74	0.74	0.72	0.71	0.70	0.69	0.67
Frequent <i>United Airlines</i> -related terms (k_i)	“train”	“problem”	“help”	“club”	“world”	“slogan”	“stop”	“poor”	“sure”	“reason”	“fliht3411”
Total number of tweets containing k_i (n_i)	934	907	895	893	884	868	867	852	852	847	841
$\frac{n_i}{n}$ (%)	0.67	0.65	0.64	0.64	0.63	0.62	0.62	0.61	0.61	0.60	0.60
Frequent <i>United Airlines</i> -related terms (k_i)	“public”	“avoid”	“air”	“leg”	“hear”	“rule”	“love”	“may”	“hospital”	“delta”	“post”
Total number of tweets containing k_i (n_i)	813	791	785	782	777	765	764	752	744	742	738
$\frac{n_i}{n}$ (%)	0.58	0.56	0.56	0.56	0.55	0.55	0.54	0.54	0.53	0.53	0.53
Frequent <i>United Airlines</i> -related terms (k_i)	“free”	“tweet”	“internet”	“china”							
Total number of tweets containing k_i (n_i)	731	726	715	705							
$\frac{n_i}{n}$ (%)	0.52	0.52	0.51	0.50							
Frequent <i>United Airlines</i> -related terms (k_i)	“oscar munoz”	“social media”									
Total number of tweets containing k_i (n_i)	2303	1008									
$\frac{n_i}{n}$ (%)	1.64	0.72									

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