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# On the Use of Functional Test Generation in Diagnostic Test Generation for Synchronous Sequential Circuits

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## Abstract

We study the relationship between diagnostic test generation for a gate-level fault model, which is used for generating diagnostic test sets for manufacturing defects, and functional test generation for a high-level fault model. In general, a functional fault may partially represent some of the effects of one gate-level fault but not another. Generating a test sequence for the functional fault is then likely to detect one gate-level fault but not the other, thus distinguishing the two faults. This relationship points to the ability to use a functional test generation procedure (that targets functional fault detection) as a way of generating diagnostic test sequences for gate-level faults. We use this observation in two ways. The more direct way is to define functional faults that correspond to the differences between pairs of gate-level faults. The second way is to use functional test sequences as diagnostic test sequences without explicitly considering gate-level faults. We support the use of the resulting procedures with experimental results.

*Keywords:* diagnostic test generation, functional test generation, state transition faults, synchronous sequential circuits.

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## 1 Introduction

Diagnostic test generation procedures [1]–[7] generate test sets or test sequences that distinguish pairs of faults out of a target fault model, typically stuck-at faults.

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Such test sets are useful for diagnosis of manufacturing defects even if the defects do not behave exactly as the target faults. Diagnostic test generation procedures perform test generation based on fault pairs (or larger subsets of faults) that are not yet distinguished by the test set. Their goal is to generate additional tests or test sequences (or extend an existing test sequence) so as to distinguish additional fault pairs, which are not yet distinguished. The need to consider fault pairs makes the diagnostic test generation process different and more complex than test generation for fault detection. The test generation process can accommodate fault pairs either explicitly, or by modifying the circuit description to inject each one of the faults separately [6]. In the latter case, test generation for fault detection can be carried out on the modified circuits, and a test guarantees that the two faults will be distinguished. However, the circuit needs to be modified for every fault pair separately.

In this work we study the relationship between diagnostic test generation for gate-level faults and functional test generation for high-level faults. This relationship points to the ability to use a functional test generation procedure (that targets functional fault detection) as a way of generating diagnostic test sequences for gate-level faults in synchronous sequential circuits without modifying the circuit. Several functional test generation procedures and fault models exist [8]–[15]. The functional fault model we consider for this study is the state transition fault model [10]. A state transition fault is a fault affecting the next state or output vector of a state transition in the state table of the circuit. Other functional fault models can be used in a similar way. We consider single stuck-at faults as the targets of diagnostic test generation.

The advantage of using state transition faults (or high-level faults in general) for diagnostic test generation can be seen from the following example. Consider a state transition  $s_i \xrightarrow{a_j} s_k$  from state  $s_i$  to state  $s_k$  under primary input vector  $a_j$ , producing primary output vector  $z_l$ . Suppose that a stuck-at fault  $f_{j1}$  changes the next state of this state transition to  $s'_k$ , while a stuck-at fault  $f_{j2}$  does not affect this state transition. Consider a test sequence  $T$  that detects the state transition fault where the next state is  $s'_k$  instead of  $s_k$ . Since  $f_{j1}$  causes the same change to the state table of the circuit as the state transition fault,  $T$  is likely to detect  $f_{j1}$ . Since  $f_{j2}$  does not cause this change to the state table, it is not likely to be detected by  $T$ . If  $T$  detects  $f_{j1}$  but not  $f_{j2}$ , then  $T$  distinguishes the two faults.

In general, a functional fault may partially represent some of the effects of one stuck-at fault but not another. Generating a test sequence for the functional fault is then likely to detect one stuck-at fault but not the other, thus distinguishing the two faults. This observation can be used in one of two ways, both of them explored in this work.

(1) The more direct way to use this observation is to define functional faults that correspond to the *differences* between pairs of stuck-at faults (or subsets of stuck-at faults). By targeting a functional fault that represents the difference between two (or more) stuck-at faults, the test sequence is likely to detect one fault of a pair but not another, thus distinguishing the two faults. The difference between two

stuck-at faults is a subset of state transitions where the two stuck-at faults differ as explained next.

We note that each stuck-at fault  $f$  is equivalent to a single or multiple state transition fault (i.e., a fault that affects one or more state transitions in one or more ways). We denote the state transition fault equivalent to  $f$  by  $ST(f)$ .  $ST(f)$  consists of one or more single state transition faults that are caused by the presence of  $f$ . The differences  $ST(f_{j1}) - ST(f_{j2})$  and  $ST(f_{j2}) - ST(f_{j1})$  between the state transition faults corresponding to two stuck-at faults  $f_{j1}$  and  $f_{j2}$  also constitute single or multiple state transition faults. The faults are considered during diagnostic test generation using a functional test generation procedure.

We first consider the (multiple) faults  $ST(f_{j1}) - ST(f_{j2})$  and  $ST(f_{j2}) - ST(f_{j1})$ . Then, if  $|ST(f_{j1}) - ST(f_{j2})| > 1$ , we also consider each single state transition fault included in  $ST(f_{j1}) - ST(f_{j2})$  separately. Similarly, if  $|ST(f_{j2}) - ST(f_{j1})| > 1$ , we consider each single state transition fault included in  $ST(f_{j2}) - ST(f_{j1})$  separately.

(2) By extension, a functional test sequence that detects all the single state transition faults in a circuit, or all the single state transition faults that are components of stuck-at faults, is likely to be useful as a diagnostic test sequence. This view of the diagnostic test generation problem allows diagnostic test sequences to be generated without considering a gate level implementation, for example, before such an implementation is available. It also supports the use of functional test sequences for defect diagnosis.

We describe the representation of stuck-at faults using single or multiple state transition faults in Section 2. In Section 3 we describe the derivation of state transition faults to be targeted during diagnostic test generation, and we describe a diagnostic test generation procedure based on functional test generation for state transition faults. Experimental results of diagnostic test generation are presented in Section 4. Results using a functional test sequence for single state transition faults are given in Section 5.

## 2 Representation of single stuck-at faults using state transition faults

To demonstrate that stuck-at faults have equivalent state transition faults, we show in Table 1 the state table of finite-state machine benchmark *train4*. The state table is obtained from a gate-level implementation. The circuit has two state variables and four states with state vectors 00, 01, 10 and 11. It has two primary inputs with four input vectors  $a = 00, 01, 10$  and  $11$ , and one primary output with output vectors  $z = 0$  and  $1$ . *PS* stands for the present state and *NS* stands for the next state.

In Table 2 we show the effects of three stuck-at faults,  $f_0$ ,  $f_2$  and  $f_{12}$ , in the gate-level implementation of *train4* on the state table of the circuit. For every stuck-at fault  $f_j$ , we simulate the circuit under every present state  $s \in \{00, 01, 10, 11\}$  and primary input vector  $a \in \{00, 01, 10, 11\}$ . If the faulty next state or output vector is different from the fault free next state or output vector, respectively, we include

Table 1  
State table of *train4*

	$NS, z$			
$PS$	$a = 00$	$a = 01$	$a = 10$	$a = 11$
00	00,0	10,1	10,1	11,1
01	00,0	01,1	01,1	11,1
10	11,1	10,1	10,1	11,1
11	11,1	01,1	01,1	11,1

the faulty entry in the state table following a slash. For example, stuck-at fault  $f_0$  of *train4* causes the next state of state 00 under input vector 10 to be 00 instead of 10, and it causes the output to be 0 instead of 1. We represent this faulty state transition as  $00 \xrightarrow{10/0} 00$ . It consists of the single state transition faults  $00 \xrightarrow{10} 10/00$  and  $00 \xrightarrow{10} 10$ .

Table 2  
Stuck-at faults of *train4*

$f_0$	$NS, z$			
$PS$	$a = 00$	$a = 01$	$a = 10$	$a = 11$
00	00,0	10,1	10/00,1/0	11/10,1
01	00,0	01,1	01/00,1/0	11/01,1
10	11,1	10,1	10/11,1	11/10,1
11	11,1	01,1	01/11,1	11/01,1
$f_2$	$NS, z$			
$PS$	$a = 00$	$a = 01$	$a = 10$	$a = 11$
00	00,0	10/00,1/0	10,1	11/10,1
01	00,0	01/00,1/0	01,1	11/01,1
10	11,1	10/11,1	10,1	11/10,1
11	11,1	01/11,1	01,1	11/01,1
$f_{12}$	$NS, z$			
$PS$	$a = 00$	$a = 01$	$a = 10$	$a = 11$
00	00,0	10,1	10,1	11/10,1
01	00,0	01,1	01,1	11/01,1
10	11,1	10,1	10,1	11/10,1
11	11,1	01,1	01,1	11/01,1

Fault  $f_0$  in Table 2 results in the single state transition faults  $00 \xrightarrow{10} 10/00$ ,  $00 \xrightarrow{11} 11/10$ ,  $01 \xrightarrow{10} 01/00$ ,  $01 \xrightarrow{11} 11/01$ ,  $10 \xrightarrow{10} 10/11$ ,  $10 \xrightarrow{11} 11/10$ ,  $11 \xrightarrow{10} 01/11$ ,  $11 \xrightarrow{11} 11/01$ ,  $00 \xrightarrow{10} 10$  and  $01 \xrightarrow{10} 01$ . Thus,  $f_0$  is equivalent to the multiple state transition fault that consists of the single state transition faults listed above. State transition faults that are equivalent to the other stuck-at faults can be obtained in a similar way.

The state transition fault equivalent to a stuck-at fault  $f$  can be found by com-

binational test generation for  $f$ . Combinational test generation considers only the combinational logic of the circuit. It assigns values to the primary inputs and present state variables, and observes fault effects on the primary outputs and next state variables. A combinational test  $t$  for a fault  $f$  defines a single state transition fault  $s_i \frac{a_j}{z_l} s_k / s'_k$  and/or a single state transition fault  $s_i \frac{a_j}{z_l / z'_l} s_k$ , where  $s_i$  is the state vector included in  $t$ ,  $a_j$  is the primary input vector included in  $t$ ,  $z_l$  is the fault free primary output vector under  $t$ ,  $z'_l$  is the faulty primary output vector under  $t$ ,  $s_k$  is the fault free next state under  $t$ , and  $s'_k$  is the faulty next state under  $t$ . We denote by  $ST(f)$  the set of single state transition faults that define the (single or multiple) state transition fault which is equivalent to  $f$ . For our purposes it is sufficient to use a subset of all the single state transition faults for every fault  $f$ , since detection of a single state transition fault out of the difference between two faults is typically sufficient for distinguishing the faults. Thus, it is possible to use combinational  $n$ -detection test generation in order to compute the sets  $ST(f)$  for target faults, instead of deriving the complete sets  $ST(f)$  ( $n$ -detection test generation attempts to generate  $n$  tests for each target fault, resulting in sets  $ST(f)$  of size  $n$  or more). This observation makes the proposed test generation procedure applicable to large circuits for which state tables are not available or the complete sets  $ST(f)$  cannot be derived efficiently.

For the purpose of diagnostic test generation we will define a set of state transition faults  $ST_{TARGET}$ . An element  $ST_i$  of  $ST_{TARGET}$  will be a single or multiple state transition fault. Diagnostic test generation will consist of generating tests for the faults defined by  $ST_{TARGET}$ . It is possible to use a functional test generation procedure such as the one described in [10] or [11]. Alternatively, test generation for state transition faults can be done at the gate level as follows.

Initially, the test sequence  $T$  is empty and the circuit is in its reset state. For every fault  $ST_i \in ST_{TARGET}$ , a sequential test generation procedure is used for generating a test subsequence  $\hat{T}$  such that when  $\hat{T}$  is added to  $T$  the resulting sequence  $T\hat{T}$  detects  $ST_i$ . If  $\hat{T}$  can be found, it is concatenated to  $T$ . The sequential test generation procedure is similar to one that targets stuck-at faults, with the following differences. (1) Fault activation conditions are extracted from the initial states and primary input vectors of the state transitions in  $ST_i$ . (2) The fault is activated every time a state transition included in  $ST_i$  is traversed. The final state and output values are obtained from  $ST_i$ .

### 3 Diagnostic test generation

Given a set of stuck-at faults  $F$  and an equivalent single or multiple state transition fault  $ST(f)$  for every  $f \in F$ , the sets  $ST(f)$  for  $f \in F$  provide functional faults that are targets for diagnostic test generation as described in this section.

Consider two faults  $f_{j1}, f_{j2} \in F$  with corresponding state transition faults  $ST(f_{j1})$  and  $ST(f_{j2})$ , respectively. The set  $ST(f_{j1}) \cap ST(f_{j2})$  consists of single state transition faults that are common to  $f_{j1}$  and  $f_{j2}$ . Consider the subset  $ST(f_{j1}) - ST(f_{j2})$ . This subset consists of single state transition faults that result

from  $f_{j1}$ , but not from  $f_{j2}$ . Suppose that  $ST(f_{j1}) - ST(f_{j2}) \neq \emptyset$ . A test sequence that detects  $ST(f_{j1}) - ST(f_{j2})$  at time unit  $u$  is likely to detect  $f_{j1}$  at time unit  $u$  (unless some of the remaining single state transition faults in  $ST(f_{j1})$  cancel the fault effects due to  $ST(f_{j1}) - ST(f_{j2})$  and prevent  $f_{j1}$  from being detected at time unit  $u$ ). In addition, a test sequence that detects  $ST(f_{j1}) - ST(f_{j2})$  at time unit  $u$  is not likely to detect  $f_{j2}$  at time unit  $u$ , since none of the single state transition faults that result from  $f_{j2}$  is targeted. We conclude that a test sequence that detects  $ST(f_{j1}) - ST(f_{j2})$  at time unit  $u$  is likely to distinguish  $f_{j1}$  and  $f_{j2}$  at time unit  $u$ .

In a similar way it is possible to argue that if  $ST(f_{j2}) - ST(f_{j1}) \neq \emptyset$ , a test sequence that detects  $ST(f_{j2}) - ST(f_{j1})$  at time unit  $u$  is likely to distinguish  $f_{j1}$  and  $f_{j2}$  at time unit  $u$ .

For illustration, consider  $f_0$  and  $f_2$  of *train4* shown in Table 2.  $ST(f_0) - ST(f_2) = \{00\frac{10}{1}10/00, 01\frac{10}{1}01/00, 10\frac{10}{1}10/11, 11\frac{10}{1}01/11, 00\frac{10}{1/0}10, 01\frac{10}{1/0}01\}$ . The input sequence 10 detects the fault defined by  $ST(f_0) - ST(f_2)$ . The same input sequence detects  $f_0$  but not  $f_2$ . Thus, it distinguishes the two faults.

The faults  $f_0$  and  $f_{12}$  demonstrate a case where  $ST(f_{12}) - ST(f_0) = \emptyset$ . In this case, only  $ST(f_0) - ST(f_{12})$  can be used during diagnostic test generation.

By using  $ST(f_{j1}) - ST(f_{j2})$  and  $ST(f_{j2}) - ST(f_{j1})$ , we perform functional test generation for at most two state transition faults for every pair of stuck-at faults that need to be distinguished. Both  $ST(f_{j1}) - ST(f_{j2})$  and  $ST(f_{j2}) - ST(f_{j1})$  may be multiple faults. It is also possible to consider single state transition faults during functional test generation by considering each  $st \in ST(f_{j1}) - ST(f_{j2})$  and each  $st \in ST(f_{j2}) - ST(f_{j1})$  separately. The number of state transition faults that need to be considered in this case is higher; however, each functional fault consists of a single state transition fault.

In the proposed diagnostic test generation procedure, we first consider the two functional faults  $ST(f_{j1}) - ST(f_{j2})$  and  $ST(f_{j2}) - ST(f_{j1})$  for every pair of stuck-at faults  $f_{j1}, f_{j2}$  that needs to be distinguished. We then consider single state transition faults included in  $ST(f_{j1}) - ST(f_{j2})$  and  $ST(f_{j2}) - ST(f_{j1})$ , but only if  $|ST(f_{j1})| \leq N$  and  $|ST(f_{j2})| \leq N$  for a constant  $N$ . This restriction is imposed in order to limit the number of functional faults considered. It is justified by the expectation that if the difference between  $ST(f_{j1})$  and  $ST(f_{j2})$  is large, the faults are likely to be distinguished by test sequences generated based on other fault pairs. The overall diagnostic test generation process is given as Procedure 1 next.

Procedure 1: Diagnostic test generation based on state transition faults

- (1) Let  $F$  be the set of single stuck-at faults. Let  $ST(f)$  be the state transition fault equivalent to  $f$  for every  $f \in F$ . Let  $P$  be the set of fault pairs defined over  $F$ . Set  $T = \emptyset$ .
- (2) Multiple state transition faults Set  $P_{TARGET} = P$ .
- (3) Select  $f_{j1}, f_{j2} \in P_{TARGET}$ . Remove  $f_{j1}, f_{j2}$  from  $P_{TARGET}$ .
- (4) If  $ST(f_{j1}) - ST(f_{j2}) \neq \emptyset$ :
  - (i) Generate a test subsequence  $\hat{T}$  for  $ST(f_{j1}) - ST(f_{j2})$ . If  $\hat{T}$  is generated:
    - (a) Concatenate  $\hat{T}$  to  $T$ .
    - (b) Perform diagnostic fault simulation of  $T$  and drop distinguished fault pairs

- from  $P$  and from  $P_{TARGET}$ .
- (c) If no fault pair is distinguished, remove  $\hat{T}$  from  $T$ .
- (5) If  $f_{j1}, f_{j2} \in P$  and  $ST(f_{j2}) - ST(f_{j1}) \neq \emptyset$ :
- (i) Generate a test subsequence  $\hat{T}$  for  $ST(f_{j2}) - ST(f_{j1})$ . If  $\hat{T}$  is generated:
- (a) Concatenate  $\hat{T}$  to  $T$ .
- (b) Perform diagnostic fault simulation of  $T$  and drop distinguished fault pairs from  $P$  and from  $P_{TARGET}$ .
- (c) If no fault pair is distinguished, remove  $\hat{T}$  from  $T$ .
- (6) If  $P_{TARGET} \neq \emptyset$ , go to Step 3.
- (7) Single state transition faults Set  $P_{TARGET} = P$ .
- (8) Select  $f_{j1}, f_{j2} \in P_{TARGET}$ . Remove  $f_{j1}, f_{j2}$  from  $P_{TARGET}$ .
- (9) If  $|ST(f_{j1})| \leq N$  and  $|ST(f_{j2})| \leq N$ , for every  $st \in ST(f_{j1}) - ST(f_{j2})$ :
- (i) Generate a test subsequence  $\hat{T}$  for  $st$ . If  $\hat{T}$  is generated:
- (a) Concatenate  $\hat{T}$  to  $T$ .
- (b) Perform diagnostic fault simulation of  $T$  and drop distinguished fault pairs from  $P$  and from  $P_{TARGET}$ .
- (c) If no fault pair is distinguished, remove  $\hat{T}$  from  $T$ .
- (10) If  $|ST(f_{j1})| \leq N$ ,  $|ST(f_{j2})| \leq N$  and  $f_{j1}, f_{j2} \in P$ , for every  $st \in ST(f_{j2}) - ST(f_{j1})$ :
- (i) Generate a test subsequence  $\hat{T}$  for  $st$ . If  $\hat{T}$  is generated:
- (a) Concatenate  $\hat{T}$  to  $T$ .
- (b) Perform diagnostic fault simulation of  $T$  and drop distinguished fault pairs from  $P$  and from  $P_{TARGET}$ .
- (c) If no fault pair is distinguished, remove  $\hat{T}$  from  $T$ .
- (11) If  $P_{TARGET} \neq \emptyset$ , go to Step 8.

## 4 Experimental results

The results of Procedure 1 for finite-state machine benchmarks are shown in Tables 3 and 4. We use  $N = 100$  in Procedure 1. We assume the existence of fault free hardware reset to the all-zero state.

In Table 3, after the circuit name we show the number of primary inputs, the number of primary outputs, and the number of state variables. Under column *flts* we show the number of stuck-at faults  $f$  with  $ST(f) \neq \emptyset$ . These faults constitute the set of target faults  $F$ . We then show the number of fault pairs defined over  $F$ .

In Table 4, under column *mult st flts* we show the results of Procedure 1 after considering faults of the form  $ST(f_{j1}) - ST(f_{j2})$  and faults of the form  $ST(f_{j2}) - ST(f_{j1})$ . Under column *single st flts* we show the results of Procedure 1 after considering single state transition faults out of  $ST(f_{j1}) - ST(f_{j2})$  and  $ST(f_{j2}) - ST(f_{j1})$ . In each case, we show the number of calls to the functional test generation process that produces a test subsequence for a state transition fault, the length of the test sequence  $T$  generated by Procedure 1, the number of stuck-at faults detected by  $T$ , the number of stuck-at fault pairs distinguished by  $T$ , and the percentage of stuck-at fault pairs distinguished by  $T$ .

Table 3  
Circuit parameters

circuit	inp	out	sv	flts	pairs
bbara	4	2	4	138	9453
bbsse	7	7	4	238	28203
bbtas	2	2	3	63	1953
beecount	3	4	3	110	5995
cse	7	7	4	355	62835
dk14	3	5	3	207	21321
dk15	3	5	2	151	11325
dk16	2	3	5	530	140185
dk17	2	3	3	128	8128
dk27	1	2	3	67	2211
dk512	1	3	4	124	7626
ex2	2	2	5	312	48516
ex3	2	2	4	153	11628
ex4	5	9	4	176	15400
ex5	2	2	3	138	9453
ex6	5	8	3	229	26106
ex7	2	2	4	159	12561
keyb	7	2	5	470	110215
lion	2	1	2	40	780
lion9	2	1	3	59	1711
mark1	4	14	4	203	20503
mc	3	5	2	73	2628
opus	5	6	4	181	16290
shiftreg	1	1	3	28	378
tav	4	4	2	64	2016
train11	2	1	4	104	5356
train4	2	1	2	34	561

From Table 4 it can be seen that diagnostic test generation based on multiple state transition faults distinguishes most of the distinguishable fault pairs. Consideration of single state transition faults increases the number of distinguished fault pairs at the cost of increasing the number of calls to the functional test generation procedure.

### 5 Test sequences for single state transition faults

The results of Section 4 indicate that functional test generation for single state transition faults of the form  $s_i \frac{a_j}{z_l} s_k / s'_k$  and  $s_i \frac{a_j}{z_l/z'_l} s_k$  will result in test sequences that are useful for fault diagnosis. This is a result of the fact that any single state transition fault can potentially be included in the difference between the state transition faults equivalent to two stuck-at faults. Targeting it may thus result in a sequence that distinguishes the stuck-at faults.



Table 4  
Results of diagnostic test generation

circuit	mult st flts					single st flts				
	calls	len	det	dist	%dist	calls	len	det	dist	%dist
bbara	107	86	130	9211	97.440	2345	114	130	9249	97.842
bbsse	50	156	235	28167	99.872	1089	180	235	28176	99.904
bbtas	12	52	62	1638	83.871	4471	57	62	1640	83.973
beecount	11	39	109	5969	99.566	258	52	110	5978	99.716
cse	51	217	354	62778	99.909	329	240	354	62783	99.917
dk14	26	56	206	21314	99.967	205	56	206	21314	99.967
dk15	15	37	150	11312	99.885	66	42	150	11316	99.921
dk16	44	166	529	140170	99.989	242	175	529	140174	99.992
dk17	13	45	127	8108	99.754	53	50	127	8110	99.779
dk27	5	21	67	2198	99.412	25	21	67	2198	99.412
dk512	16	57	122	7609	99.777	76	69	122	7612	99.816
ex2	32	164	311	48487	99.940	624	217	311	48500	99.967
ex3	15	57	152	11621	99.940	182	57	152	11621	99.940
ex4	52	95	171	15368	99.792	948	101	171	15369	99.799
ex5	15	55	138	9408	99.524	108	67	138	9419	99.640
ex6	25	59	228	26095	99.958	158	64	228	26096	99.962
ex7	131	70	149	12493	99.459	699	73	149	12494	99.467
keyb	85	366	468	110151	99.942	233	392	468	110165	99.955
lion	30	14	40	693	88.846	470	17	40	701	89.872
lion9	42	28	53	1593	93.103	1105	33	53	1595	93.220
mark1	46	61	197	20466	99.820	934	82	197	20472	99.849
mc	6	20	73	2616	99.543	125	25	73	2617	99.581
opus	38	65	180	16267	99.859	63	73	180	16271	99.883
shiftreg	3	14	28	323	85.450	443	14	28	323	85.450
tav	12	19	64	1967	97.569	1978	19	64	1967	97.569
train11	35	36	100	5285	98.674	1309	58	100	5294	98.842
train4	12	14	33	479	85.383	436	20	33	481	85.740
average	34	77	166	21548	97.268	703	88	166	21553	97.369

We define  $ST = \cup\{ST(f) : f \in F\}$ .  $ST$  is the set of all the single state transition faults that correspond to all the single stuck-at faults (when information about stuck-at faults is not available, it is possible to use all the single state transition faults). We perform functional test generation targeting every single state transition fault  $st \in ST$ . We perform fault simulation and diagnostic fault simulation for stuck-at faults only after the test generation process is complete. The results of this process are shown in Table 5 in a format similar to the one used in Table 4.

From Table 5 it can be seen that targeting single state transition faults typically increases the number of calls to the functional test generation process and the test length. However, it also increases the number of distinguished fault pairs. This points to the usefulness of functional test sequences as diagnostic test sequences for stuck-at faults. More generally, such sequences are expected to be effective for

Table 5  
Results of test generation for all single state transition faults

circuit	all single st flts				
	calls	len	det	dist	%dist
bbara	1179	1274	130	9243	97.778
bbsse	7912	12517	235	28182	99.926
bbtas	93	150	62	1748	89.503
beecount	156	293	110	5979	99.733
cse	3749	17212	355	62781	99.914
dk14	206	270	207	21314	99.967
dk15	50	146	151	11316	99.921
dk16	362	314	529	140175	99.993
dk17	39	159	128	8110	99.779
dk27	20	23	67	2197	99.367
dk512	61	125	122	7614	99.843
ex2	764	623	312	48497	99.961
ex3	230	180	153	11616	99.897
ex4	2176	2861	171	15369	99.799
ex5	39	162	138	9424	99.693
ex6	1012	1114	229	26098	99.969
ex7	372	166	149	12495	99.475
keyb	26648	20206	468	110178	99.966
lion	18	65	40	707	90.641
lion9	52	137	53	1625	94.974
mark1	1944	844	197	20470	99.839
mc	26	86	73	2616	99.543
opus	2850	2016	180	16249	99.748
shiftreg	8	48	28	320	84.656
tav	72	254	64	1964	97.421
train11	178	441	100	5261	98.226
train4	21	78	34	487	86.809
average	1861	2288	166	21557	97.642

defect diagnosis.

## 6 Concluding remarks

We studied the possibility of using functional test generation for state transition faults as part of a diagnostic test generation process for stuck-at faults. A stuck-at fault  $f$  has an equivalent single or multiple state transition fault  $ST(f)$ . It is thus possible to represent the difference between two stuck-at faults  $f_{j1}$  and  $f_{j2}$  by state transition faults that correspond to the difference between  $ST(f_{j1})$  and  $ST(f_{j2})$ . Generating a test sequence for such a functional fault is likely to detect one stuck-at fault but not the other, thus distinguishing the two faults. We used this observation directly to define functional faults that correspond to the differences between pairs of

stuck-at faults. Functional test generation for the differences resulted in a diagnostic test sequence. We also used a functional test sequence for single state transition faults as a diagnostic test sequence without considering stuck-at faults explicitly. We supported the use of these procedures as diagnostic test generation procedures with experimental results.

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