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Churn prediction on huge telecom data using hybrid firefly based classification



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# a b s t r a c t

Churn prediction in telecom has become a major requirement due to the increase in the number of tele- com providers. However due to the hugeness, sparsity and imbalanced nature of the data, churn predic- tion in telecom has always been a complex task. This paper presents a metaheuristic based churn prediction technique that performs churn prediction on huge telecom data. A hybridized form of Firefly algorithm is used as the classifier. It has been identified that the compute intensive component of the Firefly algorithm is the comparison block, where every firefly is compared with every other firefly to identify the one with the highest light intensity. This component is replaced by Simulated Annealing and the classification process is carried out. Experiments were conducted on the Orange dataset. It was observed that Firefly algorithm works best on churn data and the hybridized Firefly algorithm provides effective and faster results.

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1. Introduction

Increase in the number of telecom providers has led to a huge rise in competition and hence customer churn. Currently organiza- tions have their major focus on reducing the churn by focusing on customers independently. Churn [[1]](#_bookmark10) can be defined as the propen- sity of a customer to cease business transactions with an organiza- tion. The major requirement now is identification of customers who have high probabilities of moving out. The ability of an orga- nization to intervene at the right time could effectively reduce churn.

Churn occurs mainly due to customer dissatisfaction. Identify- ing customer dissatisfaction requires several parameters. A cus- tomer usually does not churn due to a single dissatisfaction scenario [[2]](#_bookmark11). There usually exist several dissatisfaction cases before a customer completely ceases to do transactions with an organiza-

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tion. Several properties associated with the customer and their mode of operations with the organization are recorded by the orga- nizations. This represents the customer’s behavior data. Analyzing this data would present a clear view of the customer’s current status [[3]](#_bookmark13). Hence this can be used as the base data for churn predic- tion. The major difficulty arising from this mode of operation is that the data under discussion tends to be very huge. The hugeness can be attributed to the behavioral nature of the data, depicting all the product lines dealt with by the organization. Further, due to the requirement of structural representation of the data, all the instances are bound to contain all the properties corresponding to a generic customer in the organization [[4,5]](#_bookmark13). This leads to data sparseness, since customers will be associated with only a few properties and not all the properties pertaining to the organization. The hugeness of data and sparsity acts as the major difficulties in the process of churn prediction.

Large companies interact with their customers to provide a variety of services to them [[6]](#_bookmark13). Customer service is one of the key differentiators for companies. The ability to predict if a customer will leave in order to intervene at the right time can be essential for pre-empting problems and providing high level of customer service. The problem becomes more complex as customer behavior data is sequential and can be very diverse.

Churn is an unavoidable process in any industry. However, though difficult, it is possible to identify the causes of churn using several approaches.

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1. Related work

This section discusses the recent approaches for churn predic- tion. A risk prediction technique that identifies probable customers for churn was presented by Coussement et al. in [[7]](#_bookmark13). This technique utilizes Generalized Additive Models (GAM). These models relaxe the linearity constraints, hence allowing complex non-linear fits to the data. This technique is exhibited to improve marketing deci- sions by identifying the risky customers and also providing visual- izations of non-linear relationships.

A neural network based customer profiling technique that can be used for churn prediction was presented by Tiwari et al. in [[8]](#_bookmark13). This technique differs from the other proposed techniques by the fact that most of the techniques are only able to identify the customers who will instantaneously churn. However the neural network based churn prediction model proposes to predict cus- tomer’s future churn behavior, providing the much required buffer for the organizations to perform prevention activities. A similar neural network based model includes [[22,24]](#_bookmark14). The approach in

[[22]](#_bookmark14) is based on the 80-20 rule to identify the key attributes affect- ing churn, while that of [[24]](#_bookmark14) involves identifying the major features of the data to determine churn.

A regression based churn prediction model was presented by Awnag et al. in [[9]](#_bookmark13). This method identifies churn by using multiple regressions analysis. This technique utilizes the customer’s feature data for analysis and proposes to provide good performance.

Class imbalance plays a major role in affecting the reliability of a classifier. The major issue existing due to class imbalance is that the minority class is not well represented and hence the classifier is undertrained on the minority classes. The technique proposed by Zhu et al. in [[10]](#_bookmark13) proposes to eliminate this issue by using transfer learning techniques. The approach presented in [[10]](#_bookmark13) operates by training the classifier using customer related behavioral data obtained from related domains. This approach has its major focus on the banking industry and the results are proposed to exhibit enhanced performance. Another technique that considers the imbalance nature of data to perform churn prediction was pre- sented by Xiao et al. in [[15]](#_bookmark21). A comparison of sampling techniques for effectively operating on churn data was presented by Amin et al. in [[16]](#_bookmark23). Game theory based churn prediction techniques

[[17]](#_bookmark14) are also on the raise.

The complex nature of churn behavior has also enabled several publications on churn prediction using multiple models. A churn prediction model based on cluster analysis and decision tree algo- rithm was presented by Li et al. in [[11]](#_bookmark13). This technique operates on China’s Telecom data. Another technique utilizing multiple predic- tion techniques was proposed by Le et al. in [[12]](#_bookmark15). This technique utilized a combination of k-Nearest Neighbor algorithm and sequence alignment. This technique has its major focus on the temporal categorical features of the data to predict churn.

Utilizing heuristics for predictions are on the raise due to the complex nature of data. A rule generation techniques that employs heuristics for customer churn prediction in telecom services was presented by Huang et al. in [[13]](#_bookmark16). A combination of Self Organizing Maps (SOM) and Genetic Programming (GP) to identify and predict churn was presented by Faris et al. in [[14]](#_bookmark17). SOM is utilized to clus- ter the customers and then outliers are eliminated to obtain clus- ters depicting customer behaviors. An enhanced classification tree is built using GP.

A boosting algorithm that proposes to improve the prediction accuracy of classifier models was proposed by Lu et al. in [[18]](#_bookmark14). This

method boosts the learning process by using a combination of clus- tering and logistic regression. A similar prediction boosting tech-

for the prediction process. Other ensemble based prediction tech- niques include [[20,21,1,23]](#_bookmark14).

1. Churn prediction on huge data using hybrid firefly based classification

Churn prediction on huge data utilizes Hybrid Firefly algorithm to effectively identify churn. This technique modifies the compar- ison component of the actual firefly algorithm with Simulated Annealing to provide faster and effective results.

* 1. Firefly algorithm: WorkingFirefly algorithm [[25]](#_bookmark18) is a nature inspired metaheuristic algorithm that was inspired by the behavior of fireflies attracting other fireflies by flashing lights. The intensity of the light plays a major role in deter- mining the attractiveness of a firefly. It works on the follow- ing assumptions:
     + All fireflies are unisexual, hence any firefly can be attracted to any other firefly.
     + Attractiveness is proportional to the brightness of a firefly.
     + For any two fireflies, the brighter one will attract the other.
     + Brightness decreases as the distance between the fireflies increase.
     + If no firefly is brighter than a given firefly, then it moves randomly.

For an optimization problem, the brightness of a firefly is asso- ciated with the objective function. The objective function contains all the parameters dependent on applications, hence expresses the degree of importance that the current solution holds.

* 1. Firefly algorithm: pros and cons

Firefly algorithm, due to its metaheuristic nature, can effec- tively identify optimal solutions when compared to other statistics based classification algorithms. Movement of the fireflies are direc- ted by the intensity of the fireflies, provided by the firefly intensity parameter. The usage of a single dependent parameter leads to les- ser memory requirements, hence this algorithm is capable of oper- ating on huge data.

The major drawbacks of this algorithm is that for every itera- tion, a firefly is compared with every other firefly in the system [[26]](#_bookmark19), hence increasing the number of computations. Hence as the number of fireflies in the search space increases, the level of com- putations also increases to a large extent.

* 1. Hybrid Firefly: architecture

The hybrid firefly architecture is proposed to eliminate the problem of huge computational requirements due to comparisons. The working of hybrid firefly algorithm is presented in [Fig. 1](#_bookmark1).

Building the search space marks the beginning of the classifica- tion process. The initial population of fireflies is generated and are distributed across the search space. The distribution of fireflies is carried out in random. Position of each firefly is recorded and the initial intensity of the fireflies (Intensity) are identified on the basis of their distance from the test data.

## rXﬃﬃﬃﬃﬃﬃﬃ*a*ﬃﬃ*t*ﬃ*t*ﬃ*r*ﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃﬃ2ﬃﬃ

*Intensityi* = 1/

*j*=1 (*Xtest*,*j* — *Xi*,*j* )

(1)

nique using Genetic Algorithm was proposed by Idris et al. in [[19]](#_bookmark14). This is also an ensemble model utilizing multiple techniques

where Xtest,j refers to the jth attribute of the test data and Xi,j refers to the jth attribute of the firefly i.

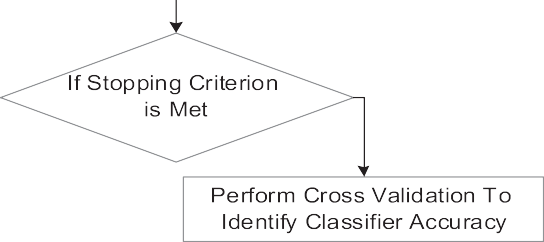
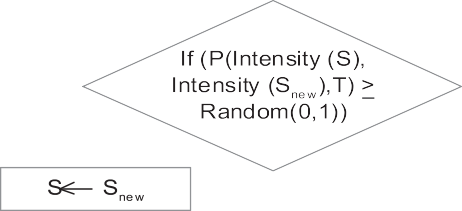


Fig. 1. Hybrid firefly ARCHITECTURE.

Firefly intensities along with the test data are passed to the Sim- ulated Annealing module to identify the optimal solution for the test data. Firefly 0 is placed on the test data and the remaining fire- flies are distributed on the training set.

*Algorithm (Hybrid /irefly with Simulated Annealing):*

1. *Search space boundary identification using base data*
2. *Firefly population generation (ffCount)*
3. *For each firefly i* = *1*.. .*ffCount*
   1. *Firefly initialization*
   2. *Firefly distribution using uniform distribution function*
   3. *FireflyPosition[0]* ← *Test data*
4. *Until the termination criterion is met perform the following*
5. *Index* ← *simulatedAnnealing(fireflyIntensity, ffCount)*
6. *If the intensity of firefly in index is greater than the*

*intensity of the firefly in the test data, move firefly[0] to index*.

1. *Calculate new intensity using eq. (2)*
2. *Perform steps 3 and 4 for all the test data*

*Simulated Annealing(fireflyIntensity, ffCount)*

1. *Let s* = *0*
2. *For k* = *0 through ffCount:*
   1. *T* ← *fireflyIntensity[s]*
   2. *snew* ← *Pick a random firefly*
   3. *If P(fireflyIntensity (s), fireflyIntensity (snew), T)* ≥ *random(0, 1), move to the new state:*

d *s* ← *snew*

1. *Output: the final state s*

*P(e,e*'*,T) was defined as 1 if e*' < *e and exp(-(e*'*-e)/T) otherwise*.

Simulated Annealing [[27,28]](#_bookmark20) is a probabilistic technique used to

identify a global optimum of a given objective function. In this approach, the firefly intensities are considered as the objective function and the requirement for the algorithm is to identify the firefly with maximum intensity for the firefly containing the test data. Identifying the firefly with maximum intensity will directly correspond to the optimal solution and hence the best classifica- tion. Simulated Annealing is assumed to perform best on a discrete search space with large number of solutions. Since the process of identification of fireflies correspond to a similar scenario, using Simulated Annealing is applied here to identify the best firefly cor- responding to the test data.

The intensity values of all the fireflies is passed to the Simulated Annealing module and the intensity of the resultant best firefly is compared with the test data to identify the firefly with maximum intensity (*Intensitymax* ). If the resultant firefly has higher light

intensity when compared to the firefly containing test data, the

firefly containing test data is moved towards the firefly with the best solution. The light intensity of the firefly containing the test data (*Intensitytest*) is updated as

*Intensitytest* = *Intensitytest* + (*b* \* *Exp*(—*c* \* *Intensitymax*)

\* (*Intensitymax* — *Intensitytest* ))+ (*a* + *e*) (2)

where b is of order 1 (ideally), a is the parameter controlling the

step size, c is the absorption coefficient and e is a vector drawn from a Gaussian distribution.

This process is continued until the specified stopping criterion is met. Stopping criterion is usualy set with two conditions. The operations are terminated when a specified maximum generations (*maxgen*) have been reached, or if the system does not move to a better solution for a specified number of iterations. Criteria of the first type is usually set in a production environment, while the sec- ond type is set during development to identify the time complex- ity. This process is carried out for each of the test data. Cross validation is finally performed to identify the accuracy of the classifier.

1. Results and discussion

Firefly algorithm and the Hybrid Firefly algorithm were imple- mented using C#.Net on Visual Studio 2012. Experiments were conducted with the Orange Dataset on both Firefly and the Hybrid Firefly algorithms. Orange is a benchmark dataset that corresponds to a French Telecom company [[29]](#_bookmark22). It was used as a part of KDD 2009 challenge [[30]](#_bookmark24). An analysis of the Orange dataset is presented in [Table 1](#_bookmark2).

The dataset was segregated with 90% data for training and 10% of the data for testing. The search space was populated with 20 fireflies and classification was carried out with a *maxgen* of 1000. The ROC plot obtained by classifying Orange data using the Hybrid Firefly algorithm is presented in [Fig. 2](#_bookmark3). It could be observed from the figure that the plots are concentrated in two areas, top left

Table 1

Dataset analysis.

Property Orange small

Attribute density 230

No of records 50,000

Missing values 60%

No of numerical Attributes 190

No of categorical attributes 40

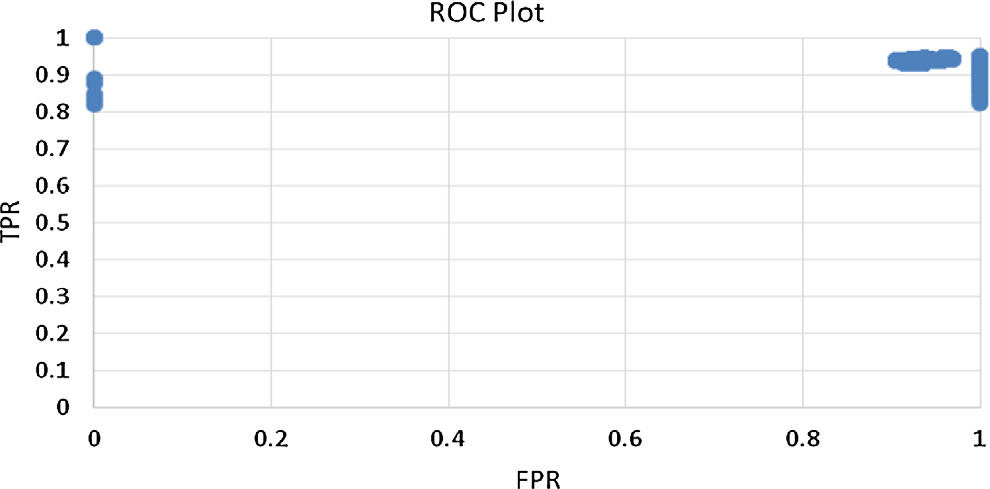


Fig. 2. ROC plot.

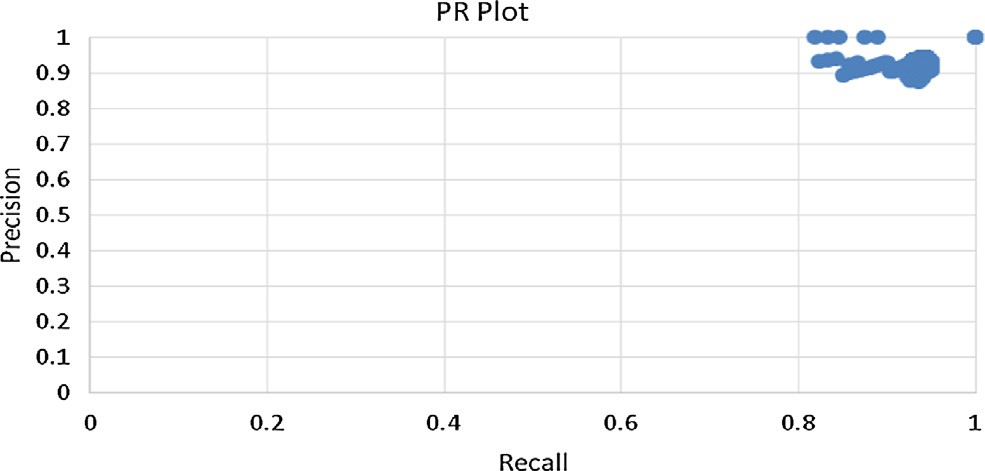


Fig. 3. PR plot.

and the top right. It could be interpreted that the algorithm exhi- bits very high True Positive Rates (TPR), i.e. it performs excellent classification of the positive cases. The False Positive Rates (FPR) are found to be low initially, however, finally the false positives show a huge increase.

Plot depicting Precision and Recall are presened in [Fig. 3](#_bookmark4). Preci- sion refers to the fraction of retrieved instances that are relevant and recall refers to the fraction of relevant instances that are retrieved. High values for precision and recall exhibits high perfor- mance levels of the algorithm. It could be observed from the figure

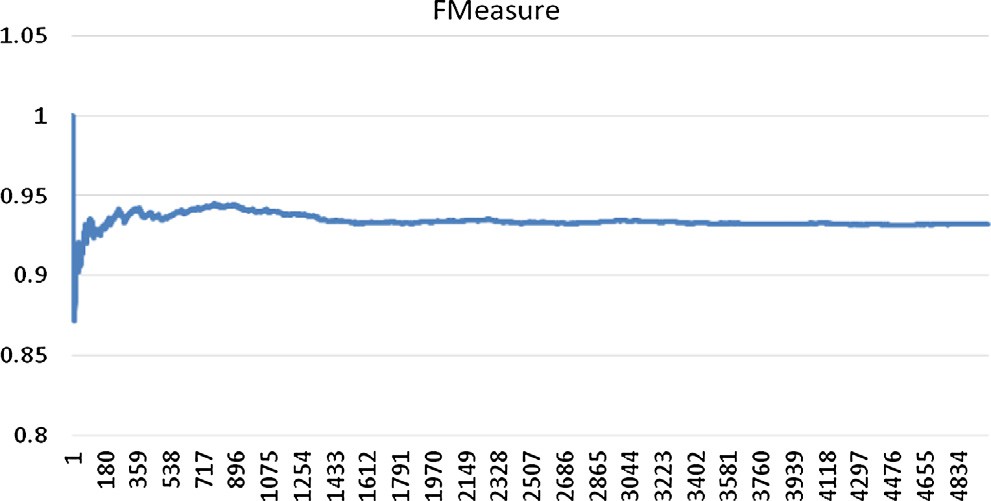


Fig. 4. F-Measure.

that the precision levels range from 0.85 to 1 and the recall levels range from 0.8 to 1 exhibiting very high performance levels.

F-Measure or F1 score is a measure of the accuracy exhibited by the classifier. It considers both precision and recall and can be computed as

*F*1 = 2. *precision*.*recall*

*precision* + *recall*

It could be observed from the figure that the F-Measure ranges

from 0.855 to 1, depicting high accuracy levels (see [Fig. 4](#_bookmark5)).

1. Comparative study

Comparison was carried out by applying the Orange data on Firefly algorithm, with 90% data for training and 10% for testing. The search space was populated with 20 fireflies and classification was carried out with a *maxgen* of 1000. Figures represent the ROC Plot, PR plot and the F-Measure obtained by using the normal Fire- fly algorithm.

It could be observed from the ROC plot ([Fig. 5](#_bookmark8)) that the FPR levels of Firefly algorithm are much higher when compared to the hybrid firefly algorithm. The PR plots ([Fig. 6](#_bookmark9)) exhibit very sim- ilar performance levels compared to hybrid firefly. Though the

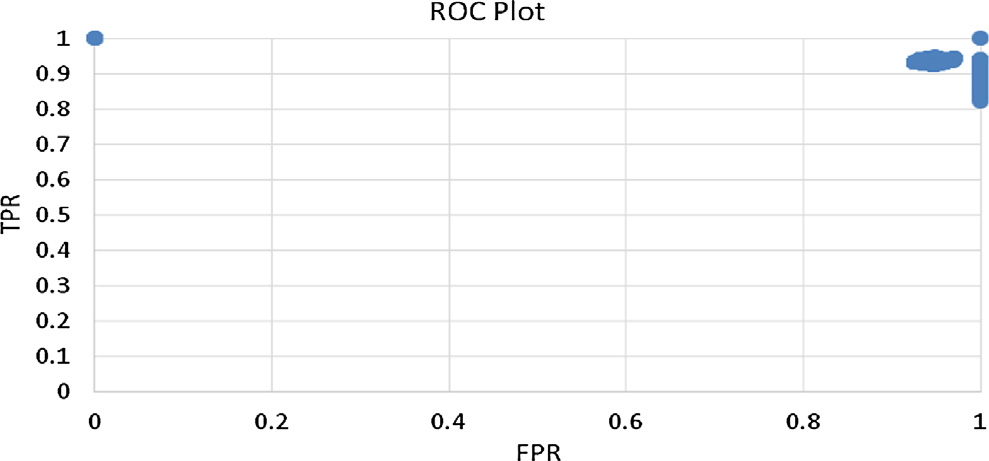


Fig. 5. ROC plot.

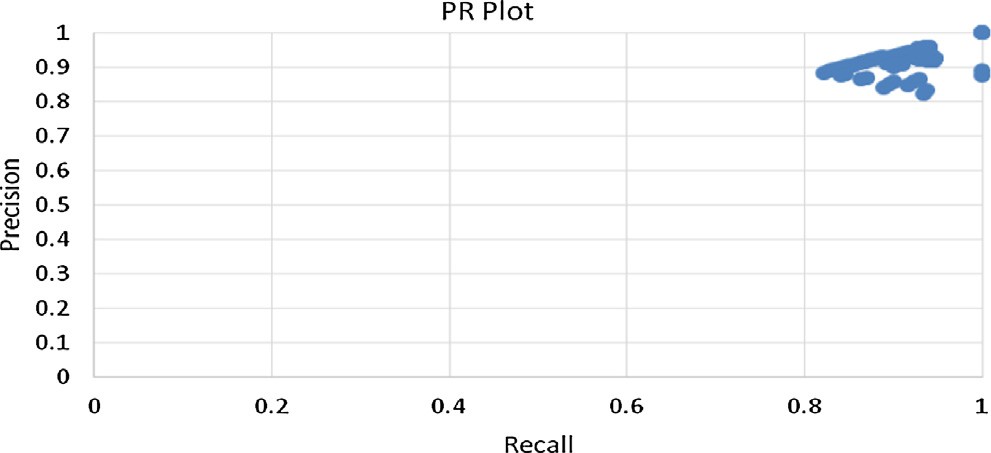


Fig. 6. PR plot.

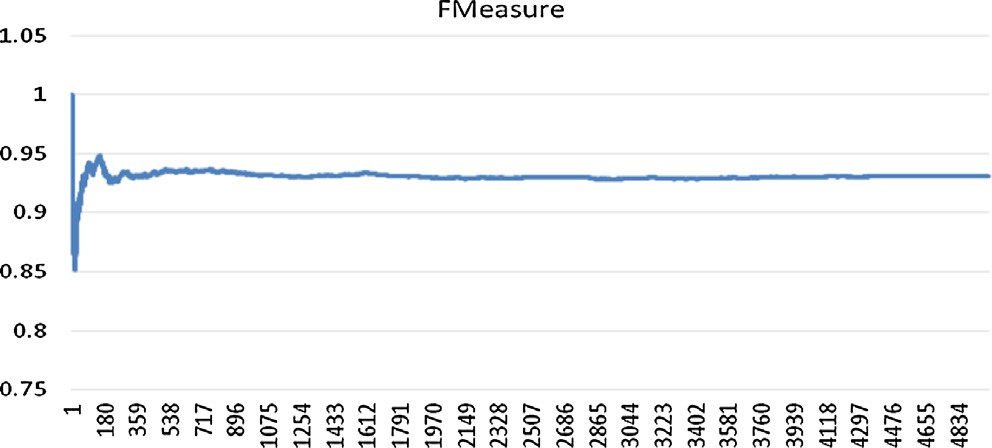


Fig. 7. F-Measure.

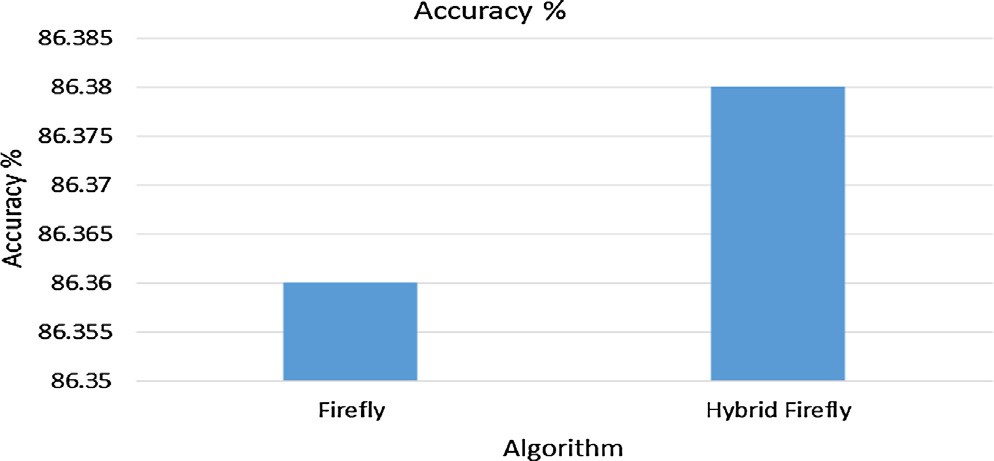


Fig. 8. Accuracy%.

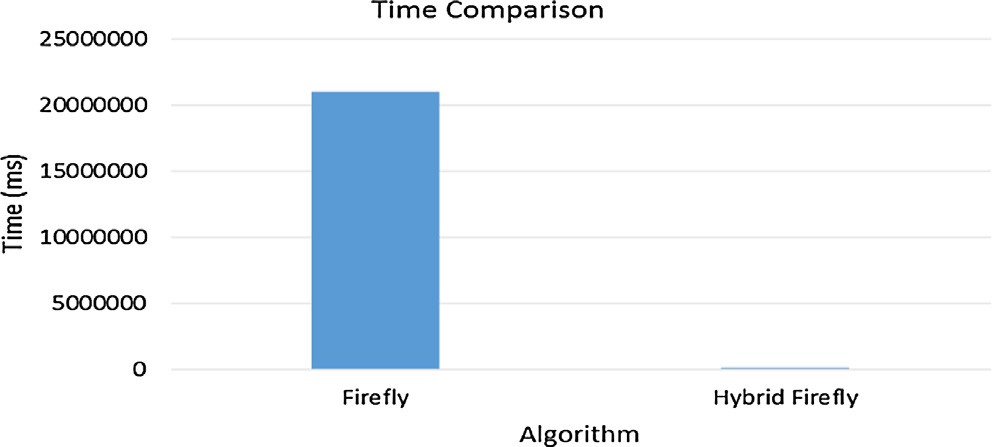


Fig. 9. Time comparison.

algorithm exhibits slightly low F-Measure levels ([Fig. 7](#_bookmark12)), it is still comparable to the hybrid firefly algorithm.

A comparison of the accuracy obtained from firefly and the hybrid firefly algorithm is presented in [Fig. 8](#_bookmark6). It could be observed that the hybrid firefly algorithm exhibits slightly higher accuracy of 86.38% when compared to the firefly algorithm (86.36%).

A time comparison between normal firefly and the hybrid firefly is presented in [Fig. 9](#_bookmark7). It could be observed that the time taken for a normal firefly algorithm is approximately 349.4 min, while that of the hybrid firefly algorithm is 2.5 min. This exhibits the efficiency of the hybridization process.

1. Conclusion

Churn prediction is one of the major requirements of the cur- rent competitive environment. This paper deals with identifying and predicting churn in the telecom data. This paper presents an efficient hybridized firefly algorithm for churn prediction. A com- parison was carried out between the normal firefly algorithm and the proposed algorithm and it was identified that even though the accuracy exhibited by them are similar, hybrid firefly outperforms the normal firefly algorithm by exhibiting very low time latency. Analysis of the algorithms was carried out on the basis of ROC, PR, F-Measure, Accuracy and Time. Future directions will include incorporation of schemes or modifications to reduce the False Pos- itive rates. Further, analysis in terms of imbalance levels and data sparsity will also be carried out. Incorporation of Game theory in the decision making process will also help improve the accuracy levels and in the identification of churn.

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