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Time, Abstraction, Causality and Modularity in Interactive Systems

# Extended Abstract

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Abstract

We study discrete models of interactive distributed systems structured into components and op- erating concurrently in a time frame. For such models of the data or signal flow in interactive system we assume that there is a source and a cause for each communication event and its asso- ciated information. To understand the logical dependencies for the events of systems causality is a key issue for reasoning about the event flow. Being interested in a structured modular approach we want to be able to abstract away all internal aspects of systems that are used as components within a system’s architecture. We speak of interface abstraction. The interface abstraction is to keep only the aspects relevant for the usage of the component and the construction of the in- terface abstraction of the architecture. We speak of modularity if the interface abstraction of an architecture is the result of the composition of the interface abstractions of all its components. In particular, we discuss and study the relationship and dependencies between causality, input and output, compositionality, and the granularity of time.

*Keywords:* Interactive systems, time, composition, modularity, causality, input/output, abstraction

# Fundamentals

We study the information flow in a system of components. Information flow evolves in physical or technical systems in a time frame. There are many ways to represent events and information (and on the contrary there are many

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ways to interpret certain phenomena as carrying information) that evolve in physical or technical systems.

In fact one way to look at this issue is to see causality as a principle that holds for any form of information processing systems independent of their technical or physical representation.

Of course, we can also model causality for event structures that model systems by concurrent traces. There causality is a logical relationship between the events and actions of a system.

We study a specific form of causality for system structured into families of components. Here we concentrate on the causality between input and output events. We claim that:

* there is a canonical notion of causality between input and output.

Causality is closely related to a model of time. A fundamental question concerns the model of time. Basically there are two essentially different models of time, discrete (digital) time and continuous (analog) time. A first critical question for system models has to do with time:

* Is it necessary to work with continuous time or is discrete time good enough?

Whenever two subsystems interact and thus mutually influence each other within a larger system we may interpret this as a form of information exchange. Often the information flows in both directions. This leads to a set of further questions:

* Can we model information exchange always as a directed process with a sender and a receiver (modeling mutual exchange as two steps of directed information exchange)?
* Do we need a model of information exchange that takes into account the states of two or more subsystems and calculates from that state the new state of the system?

We are interested basically in two issues:

* What are the universal laws of causality?
* How does causality and time relate?

The basic principle of causality in information flow of components with input and output is as simple as that (here we assume that a system cannot predict its future input and thus there is no anticipating gate no gate that can predict its future input)

* Information (input) can only be processed and forwarded as soon as/after it had been received.

We discuss the notion of strong and that of weak causality. In strong causality the time model strictly separates all events that may be causal for other events from those that are causal for them.

We consider a system in several time granularities. We assume the follow- ing principles:

* If we choose the time granularity fine enough then
  + If the time scale of the input is fine enough then there is no non-deter- minism/underspecification left in the system due to missing information about the input timing.
  + If the time scale is finer than the minimal delay, then the behavior function is *strongly causal*.
  + Every system behavior is weakly causal. Strong causality may be ab- stracted away by too coarse time models.
* Every system behavior is implicitly strongly causal. This means there exists a strongly causal behavior such that the system behavior is a time coarsen- ing.

If we choose the time granularity not fine enough then we get a system behavior that is only weakly causal but implicitly strongly causal.

# Causality in Interface Abstractions

For input/output information processing devices there is a crucial notion of causality. Certain output depends causally on certain input. Causality indi- cates dependencies between the actions of information exchange of a system. So far interface behaviors are nothing but relations represented by set valued functions. In the following we introduce and discuss the notion of causality for interface behaviors.

Interface behaviors generate their output and consume their input in a time frame. This time frame is useful to characterize causality between input and output. Output that depends causally on certain input cannot be generated before this input has been received.

Nevertheless, proper timing permits instantaneous reaction [[8](#_bookmark1)]: the output at time t may depend on the input at time t. This may lead into problems with causality if we consider in addition delay free feedback loops. To avoid these problems we strengthen the concept of proper time flow to the notion of causality.

If F is time guarded then the output in the t-th time interval does not depend on input that is received after the (t-1)-th time interval. Then F is properly timed and in addition reacts to input received in the (t-1)-th time

interval not before the t-th time interval. This way causality between input and output is guaranteed and explicitly visible according to the fine time granularity.

# Causality in Composition

When composing components systems causality proves crucial. Each compo- nent acts and reacts. Which if each steps are proactive and happen indepen- dent of the existence of steps of other components and which happen only in response (“reaction”) to steps of other components can only be determined by the logic of causality of a component.

If we do not have the full notion of causality in the interface abstraction of a component we cannot determine which events will definitely happen, which events will happen in reaction to those and which will not take place due to causality properties. Then it may become impossible to exclude behaviors the represent so-called causal loops and therefore are operationally impossible. In particular, the dead lock properties cannot be deduced correctly from the interface abstraction of system components.

# Coarsening the Time Scale

To make for a component the time scale coarser by the factor n is a form of abstraction. This coarsening may introduce some kind of nondeterminism and underspecification due to the coarser time scale. In particular we are interested in the problem of loosing causality information by such a time coarsening.

A special case is to get rid of all time information. If the output of a component is depending on the timing of the input a behavior generated by full time abstraction shows a lot of nondeterminism. However, if the output produced does not depend on the timing of the input messages but only on their values and the order in which they arrive behavior generated by full time abstraction will rather be more deterministic. However causality information may be lost that way.

If a component is weakly causal its time abstraction by a finite factor n is weakly casual, too. However, strong causality is not maintained.

# A Formal Approach to Causality

As formulated above, we assume that for each real system behavior there is a time scale that is fine enough to capture all time differences especially for the

delay between input and output. In such a time scale the behavior is strongly causal.

For a feedback loop being the result of a component composition a behav- ioral fixpoint is causal, if all output is causal by some input.

Strong causality has a number of advantages since it makes the reasoning about systems more concrete and simpler. In particular, it is easy to treat feedback loops by fixpoints for strongly causal behaviors since time guarded- ness guarantees for instance unique fixpoints for deterministic functions. In other words, for strong causality all fixpoints are causal.

The disadvantage of time guardedness is its limited abstractness illustrated by the fact that in sequential composition the delays accumulate. As a result composition is not as abstract as needed. A composed system has always delays larger than two. This difficulty is avoided by weak causality. But then the reasoning about fixpoints gets more involved. There exist fixpoints that are not causal.

This shows that the assumption of causality leads to proof principles for systems.

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