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Minimum number of scans for collagen fibre direction estimation using Magic Angle Directional Imaging (MADI) with a priori information

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A R T I C L E I N F O A B S T R A C T

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Collagen Magic angle

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Soft registration

Tissues such as tendons, ligaments, articular cartilage, and menisci contain significant amounts of organised

intensity response of these tissues is dependent on the angle between the main field, *𝐵*0, and the direction collagen which gives rise to the Magic Angle effect during magnetic resonance imaging (MRI). The MR

of the collagen fibres. Our previous work showed that by acquiring scans at as few as 7–9 different field orientations, depending on signal to noise ratio (SNR), the tissue microstructure can be deduced from the intensity variations across the set of scans. Previously our Magic Angle Directional Imaging (MADI) technique used rigid registration and manual final alignment, and did not assume any knowledge of the target anatomy being scanned. In the present work, fully automatic soft registration is incorporated into the MADI workflow and a priori knowledge of the target anatomy is used to reduce the required number of scans. Simulation studies were performed to assess how many scans are theoretically necessary. These findings were then applied to MRI data from a caprine knee specimen. Simulations suggested that using 3 scans might be sufficient, but in practice 4 scans were necessary to achieve high accuracy. 5 scans only offered marginal gains over 4 scans. A 15 scan dataset was used as a gold standard for quantitative voxel-to-voxel comparison of computed fibre directions, qualitative comparison of collagen tractography plots are also presented. The results are also encouraging at low SNR values, showing robustness of the method and applicability at low field.

# Introduction

Magnetic Resonance Imaging (MRI) is routinely used for diagnos- tic imaging of various parts of the body because it offers unrivalled soft tissue contrast and it is safe, owing to the absence of harmful ionising radiation. However, conventional MRI does not provide suf- ficient information for accurate diagnostics of tissues containing large amounts of collagen, such as ligaments, tendons, articular cartilage, and the meniscus [[1](#_bookmark23)–[4](#_bookmark24)]. Particularly hard to diagnose are injuries such as partial ligament tears, for which surgical techniques such as arthroscopy remain the diagnostic gold standard, although they are normally undertaken only as therapy [[1](#_bookmark23),[5](#_bookmark25),[6](#_bookmark26)].

In these tissues the large collagen molecules are organised in fibre structures, and the MRI signal is produced by the hydrogen nuclei of the water molecules bound to collagen. Here, the major signal decay mechanism is the unaveraged dipolar coupling, resulting in extremely

short relaxation time *𝑇*2 and consequently a very low MRI signal. Such

tissues normally appear very dark or even black, and any bright regions

might be a sign of disease or injury, but they could also be caused by the well-known Magic Angle (MA) effect. Analysis of dipolar interactions leads to a simple formula showing that these interactions are minimised

when the angle between the collagen fibres and the main magnetic field

*𝐵*0 is *𝜃* = 54*.*7◦, the Magic Angle. Therefore, for collagen molecules oriented at this angle, the time *𝑇*2 can be significantly extended (from

1–2 ms to perhaps 20 ms) to result in a strong MRI signal.

The MA effect has long been considered as an unwanted source of imaging artifacts [[7](#_bookmark27)] that can be reduced using certain techniques. However, this effect can also be employed to provide valuable new information about the tissue microstructure. By analysing image inten-

sities in scans obtained at various orientations to the main field, *𝐵*0,

it is possible to estimate the collagen fibre orientation in a voxel and to obtain 3D tractography plots of the fibre structures. For example, Szeverenyi et al. scanned a goat knee meniscus at 15 orientations to

*𝐵*0, and used correlation between the measured intensities and those

predicted using theoretical relationships for a large set of predefined candidate directions [[8](#_bookmark28)]. Seidel et al. performed a similar study on a human iliotibial tract sample [[9](#_bookmark29)]. They performed 35 scans constrained to two planes and computed the fibre directions by analysing the maxima of the intensity vectors versus simulated fibre directions.

In view of the practical difficulties of performing lengthy scanning of humans, our previous work [[10](#_bookmark30),[11](#_bookmark31)] was aimed at minimising the

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number of scan directions required for accurate estimation of fibre directions, for the case when no a priori knowledge about the expected fibre directions is available. We proposed the MAgic Angle Directional Imaging (MADI) method as an extension of the methodology of Szev- ernyi et al. [[8](#_bookmark28)], by choosing the scanning orientations evenly spread over the hemisphere, and by employing an optimisation step to max- imise the accuracy of the computed fibre direction. We found that by doing this it is possible to use only 7 scan directions to robustly estimate fibre directions, even for images with relatively low signal-to-noise ratios (SNR).

The present work addresses the need to minimise the number of scans necessary for the MADI technique, improving on our previous work from [[10](#_bookmark30)] by taking a priori knowledge of target anatomy into account. Clinical application of the MADI technique is limited by data acquisition time and geometry requirements for the scans at various orientations. A single scan can take several minutes, and conventional MRI scanners are static and patients cannot be easily moved relative to them. Geometrical issues are addressed by our research group’s development of a prototype rotatable scanner [[12](#_bookmark32)], yet it is still im- portant to reduce data acquisition time by taking the fewest number of scans possible. This necessitates calculation of the optimal scanning orientations to use. The present work is therefore important to improve and assess the clinical feasibility of the MADI technique.

In this paper we set out to investigate how a priori information about the expected fibre directions may be employed to further reduce the required number of scanning orientations, whilst maintaining the accuracy of the technique. Simulation studies were performed on a vir- tual collagen fibre with known orientation in order to find theoretical optimal scanning orientations within a certain tolerance. MADI was then applied to real MRI data of a caprine knee specimen using 15 scanning orientations. MADI was then also applied to subsets of this 15 scan dataset, using scanning orientations found in the simulation studies, to assess whether only 3, 4, or 5 scans would be necessary.

In clinical practice, scout scans are normally used to capture the overall anatomy and plan the detailed scans. These can also be read- ily used by a medical specialist to define the expected healthy fibre directions in order to define the field orientations for the subsequent detailed scans. For example, in the case of ligaments, the expected fibre orientation would clearly be along the ligament to result in its maximum tensile strength, and local deviations from this could be a sign of injury or disease.

We have also updated the overall image processing pipeline to in- clude soft registration. In our previous work we introduced registration

various directions of *𝐵*0, instead of relying on the measurements of the based on fiducial markers as a method to align 3D images obtained at

rotation angles that was employed by other researchers. However, MR images inevitably involve a certain amount of geometric distortion due to the linearity tolerances of the gradient field as well as the main field, which can make fiducial-based rigid registration insufficiently accurate in high-resolution images and demands manual fine adjustment, though often of no more than one or two voxels. Our aim was therefore to establish that soft registration could be adequately employed to fully automate this task while achieving accurate results.

# Methods

* 1. *Magic Angle Directional Imaging (MADI)*

Fullerton and Rahal [[13](#_bookmark33)] found that at physiological hydration levels, 89% of the water in collagen rich tissues is ‘orientationally restricted’. Dipole–dipole interactions between the proteins that make up collagen and the water molecules orient the water molecules trans- versely to the collagen fibre direction in a regular repeating structure. Due to this there are residual dipolar couplings oriented in the fibre direction, giving collagen rich tissues a very short T2 which yields low MR signal intensity. However, when the fibres are oriented at the

Magic Angle relative to *𝐵*0, the dipole interactions are overcome and

the relaxation time of collagen rich tissues is increased, thus increasing

the measured signal as shown in [Fig.](#_bookmark4) [1](#_bookmark4). Szeverenyi and Bydder [[8](#_bookmark28)] modelled the resulting MR angle sensitivity of collagen fibres as:

*𝐼* = *𝐴* ⋅ exp(−*𝐵* ⋅ (3 cos2 *𝜃* − 1)2) (1)

where *𝐼* is the recorded intensity, *𝐴* and *𝐵* are constants, and *𝜃* is the angle between the collagen fibre direction and *𝐵*0. Knowing this

from multiple scans of the same subject at different *𝐵*0 orientations. relationship, it is possible to deduce the orientation of collagen fibres Each *𝐵*0 orientation, defined in the scanned subject’s reference frame,

is referred to as a scanning orientation.

Following our previous work [[10](#_bookmark30),[11](#_bookmark31)], the overall MADI method may be summarised as follows:

* + 1. Acquire *𝑁* scans of the subject using *𝑁* different *𝐵*0 orientations.
    2. Register the acquired *𝑁* volume images.
    3. Detect voxels with significant intensity variation as the likely collagen-containing voxels; on this basis segment the region of interest (ROI).

calculate theoretical intensities corresponding to *𝑁* scans. 4. For a predefined set of candidate directions, use Eq. ([1](#_bookmark1)) to

1. Estimate fibre direction for each voxel in ROI:
   1. Find the candidate direction in the set, which has the theoretical intensities with the highest correlation to the measured ones, and use it as the initial guess for the optimisation step.
   2. Use an optimisation process to compute the fibre direction that maximises the correlation between the theoretical and measured intensities.

The predefined candidate directions in step [4](#_bookmark2) were a bouquet of 400 directions uniformly distributed on a hemisphere, which had been previously shown to lead to robust initial guess for the subsequent simplex minimisation [[10](#_bookmark30)]. In the cases considered here, where a priori knowledge was available, this was reduced to a subset of 100 candidates, with a higher density near the assumed direction. However, the whole hemisphere was still spanned to avoid overfitting.

The optimisation step [5b](#_bookmark3) was performed using the Nelder–Mead simplex algorithm to minimise:

*𝑁*

*𝐶*(**𝐱**) = (*𝐼𝑀* − *𝐼 𝐶* (**𝐱**))2 (2)

∑

*𝑘 𝑘*

*𝑘*=1

where *𝐶*(**𝐱**) is the cost as a function of the current computed fibre direction **𝐱** with *𝑁* associated intensity values, *𝐼𝑀* is the measured intensity (see [Fig.](#_bookmark7) [2](#_bookmark7)) and *𝐼 𝐶* (**𝐱**) is the computed theoretical intensity of a fibre with orientation **𝐱** .

*𝑘*

*𝑘*

* 1. *Soft registration*

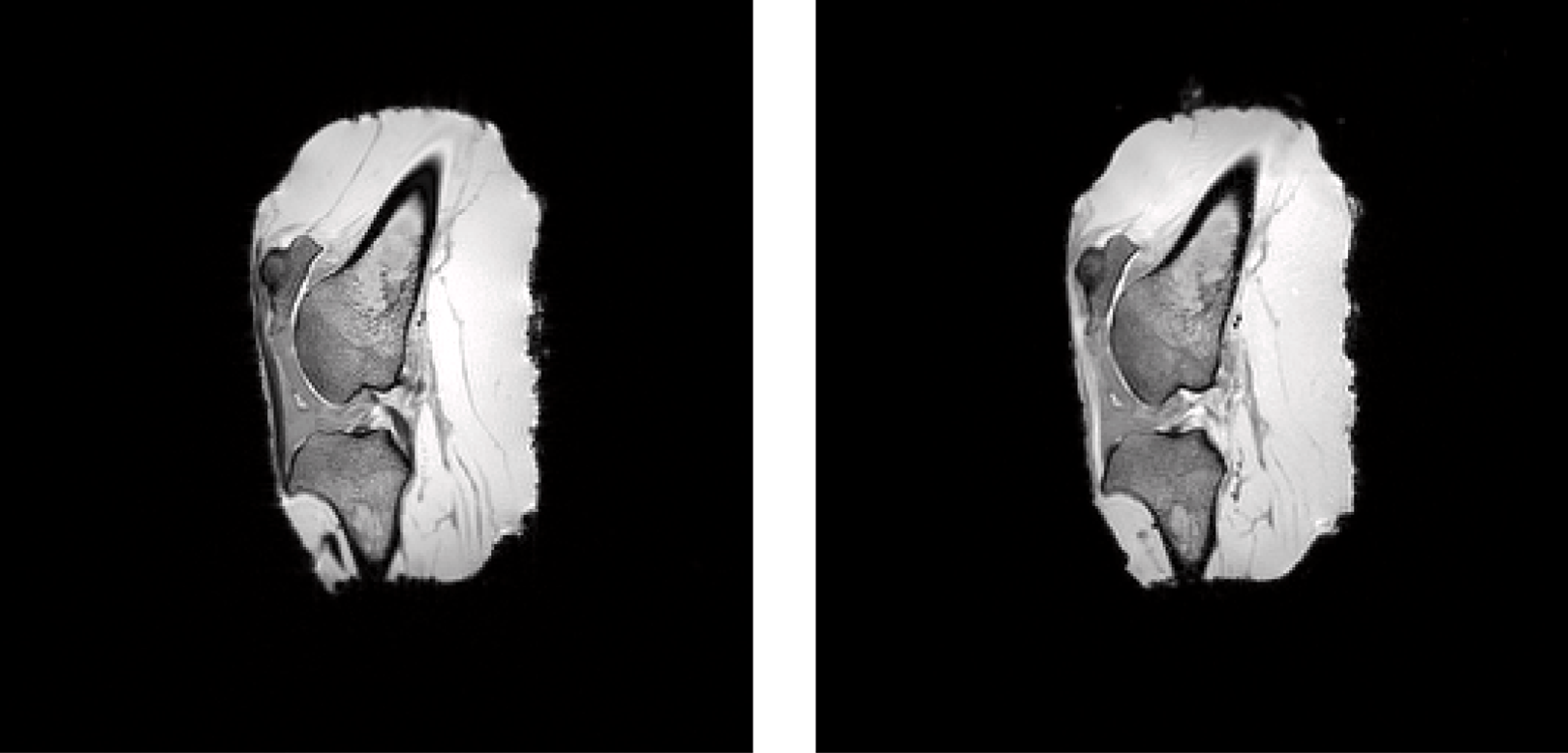
The acquired volume images were first pre-aligned using rigid body registration based on fiducial markers, followed by soft registration which also allowed for any geometric distortions. The pre-alignment stage relies on 3 fiducial markers attached to the specimen, represented by 10 mm diameter water filled spheres (.43 Caliber Clear Paintballs 8000, Rap4 UK). Following the methodology of de Oliveira et al.

[[14](#_bookmark34)] and Brujic et al. [[10](#_bookmark30)], these spheres were located in the MR images using the template matching technique and the Fourier filtering method [[15](#_bookmark35)]. This method was found to give a localisation accuracy of

*<*0*.*3 voxels by Franco et al. [[16](#_bookmark36)]. Since the markers were arranged in an

irregular triangle, each vertex was uniquely defined by which two side

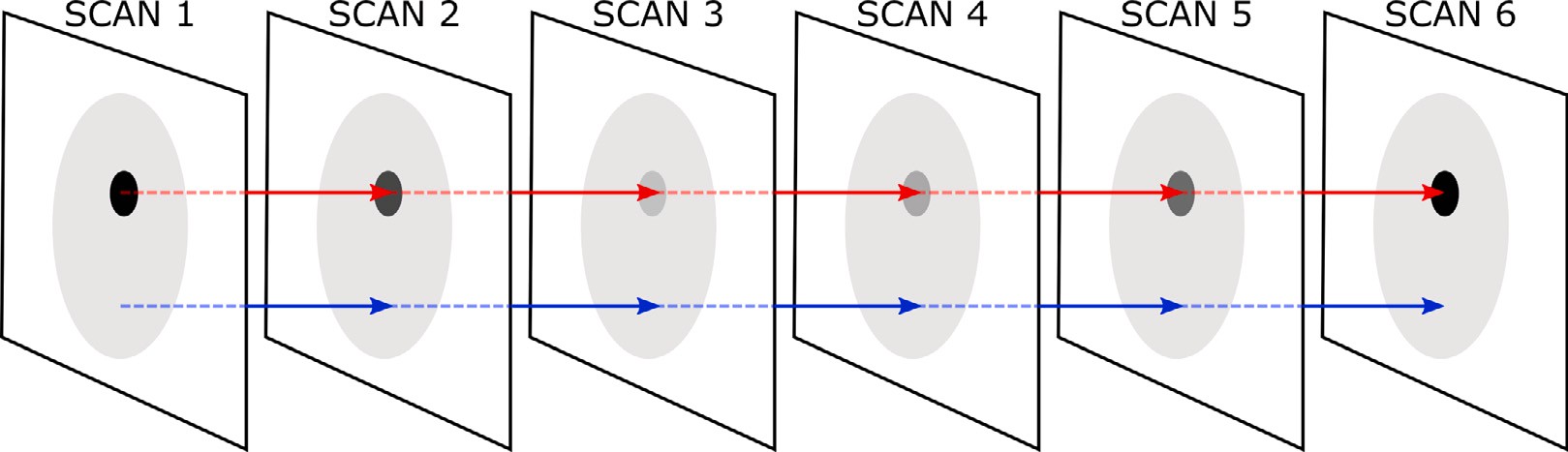
lengths of the triangle associated with it, allowing each marker to be unambiguously identified in a given 3D image. Rigid body registration was therefore performed as the translation and the rotation about the image centre of mass and to align the markers.







**/ig. 1.** Sample images of a caprine knee specimen obtained at different orientations to *𝐵*0. The attachment points of the patella tendon are shown by the white arrows. The Magic Angle effect is illustrated here as the patella tendon is dark in [1(a)](#_bookmark5) yet much brighter in [1(b)](#_bookmark6) as the main field was at approximately 55◦ to the collagen fibres in the tendon.



**/ig. 2.** An example set of six scans with different scanning orientations that have been registered. The dark inner area is representative of collagen and hence shows variable intensity. The red and blue lines show corresponding voxels in collagen rich and non-collagen rich regions respectively. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Soft registration was then performed by optimising a B-spline trans- form from the fixed to the moving image, and then assigning the interpolated values in the moving image to the corresponding vox- els in the fixed image [[17](#_bookmark37)]. The parameterisation of the B-spline

transform [[17](#_bookmark37),[18](#_bookmark38)] was:

The metric employed to quantify registration accuracy was the Mutual Information (MI) [[20](#_bookmark40)–[22](#_bookmark41)], defined by Thévenaz and Unser [[23](#_bookmark42)] as:

∑ ∑ ( *𝑝*(*𝑓 , 𝑚*; *𝜇*) )

*𝑀𝐼* (*𝜇*; *𝐼𝐹* ; *𝐼𝑀* ) =

*𝑚*∈*𝐿*

*𝑓* ∈*𝐿*

*𝑝*(*𝑓 , 𝑚*; *𝜇*) ⋅ log2

*𝑝𝐹*

(*𝑓* ) ⋅ *𝑝𝑀*

(*𝑚*; *𝜇*)

(4)

∑ 3 ( **𝐱** − **𝐱***𝑘* )

*𝑀 𝐹*

*𝑇𝑐* (**𝐱**) = **𝐱** +

*𝑘*

**𝐱***𝑘* ∈*𝑁***𝐱**

*𝑐𝑘𝛽 𝜎*

(3)

where *𝜇* are the transform parameters, *𝐼𝐹*

is the fixed image, *𝐼𝑀*

is the

where **𝐱** is the 3D coordinate being transformed, **𝐱***𝑘* are the control

points, *𝑁***𝐱** is the set of all the control points within the compact

moving image, *𝐿𝐹* and *𝐿𝑀* are regularly spaced intensity bin centres

for the fixed and moving images, *𝑝* is the discrete joint probability, *𝑝𝐹*

support at **𝐱**, *𝑐𝑘*

are the B-spline coefficient vectors, *𝜎* are the B-spline

3

and *𝑝𝑀* are the marginal discrete probabilities of the fixed and moving

images — obtained by summing *𝑝* over *𝑀* and *𝐹* respectively [[17](#_bookmark37)].

control point spacings [[17](#_bookmark37)], and *𝛽* (**𝐱**) is the cubic multidimensional B- spline polynomial [[19](#_bookmark39)]. The coefficient vectors *𝑐𝑘* are the optimisation parameters and not **𝐱***𝑘*. Changes to *𝑐𝑘* affect the position of the control

points and hence are used to optimise the transform rather than move

**𝐱***𝑘* directly.

The images obtained experimentally in this work were 256 × 256

× 208 (1 mm voxel size in each dimension) and the collagen structures of interest existed on length scales of U(100) and U(101) mm. Based on this, the control point spacing *𝜎* was set to 16 voxels (16 mm) in each

direction allowing sufficiently fine control over the B-spline transforms without the need for heavy regularisation. Bending energy was used to penalise excessive curvature of the B-splines based on their second spatial derivatives [[17](#_bookmark37)], however, a low weight of 1 was assigned to this regularisation term, as spurious bending mainly occurs in large homogeneous regions due to lack of information, which was not an issue for our ROI.

Histogram bin widths were chosen based on the dynamic range of the

maximum voxel intensity was *<*400, therefore 32 histogram bins were images. The images in this work had fairly low dynamic range, the

used. MI is suitable for registration of multi modal images [[17](#_bookmark37)] as using MI helps to align features despite potential intensity differences, rather than simply matching intensities. Our data was single mode, but the angle-sensitivity of collagen rich tissues meant that certain structures showed significant intensity changes, necessitating a transform metric that was robust to intensity variations.

parameters *𝜇* = *𝑐𝑘*, based on the metric MI. The adaptive stochas- The B-spline transformation in Eq. ([3](#_bookmark8)) was optimised in terms of

tic gradient descent method [[24](#_bookmark43)] was employed to optimise over a maximum of 1000 iterations. Once the transformation was optimised, the registered image was reconstructed from the moving image by transforming a voxel coordinate from the fixed to the moving image,

in which the intensity at this coordinate was obtained using cubic B- spline interpolation. This intensity was then recorded in a reconstructed image, at the original fixed image voxel coordinate.

When registering multiple scans, one of the 3D images was des- ignated the fixed image and all other images where registered to it. Registration was further improved by applying a binary mask to the fixed image in order to exclude from the scope of the registration the

a 3D Gaussian blur with a kernel size of 61 and *𝜎* = 10 to the fixed noisy air surrounding the sample. The mask was produced by applying

image. A threshold value based on the noise in the air then turned the blurred image into a 3D Boolean mask which included the specimen and a few layers of air around it for registration, whilst excluding the majority of the empty space.

Both the rigid and the soft registration steps were implemented using the elastix toolbox [[17](#_bookmark37)] as the functionality offered was sufficient for our needs.

* 1. *Simulation studies*

Assuming perfect registration, simulation studies involving a single

for different numbers of scans *𝑁* = 3*,* 4*,* 5, at angles *𝜃*1*...𝑁* in the range collagen-rich voxel were performed to assess the overall performance 15◦–85◦ in 1◦ increments. Eq. ([1](#_bookmark1)) was used to simulate MR image

intensity in the voxel with added noise, and the fibre direction was then estimated using the MADI technique described above. The error angle between the computed fibre direction and the ground truth was

recorded and stored in an *𝑁* -dimensional matrix. The ground truth

collagen orientation was along the *𝑍* axis. Intensity values for different angles *𝜃* were with constants *𝐴* = 300 and *𝐵* = 1 in Eq. ([1](#_bookmark1)). The final intensity value was taken from a normal distribution with *𝜇* = *𝐼* from Eq. ([1](#_bookmark1)), and *𝜎* = 20 which was chosen to approximate the standard

deviation seen in the real MR data from Section [2.4](#_bookmark9). Absolute values were taken to avoid negative intensities in low signal regions far from the Magic Angle.

* 1. *MRI data acquisition*

We have previously conducted extensive experiments [[10](#_bookmark30),[11](#_bookmark31)] to ob- tain reference MRI scan data of a caprine knee specimen. The specimen was mounted inside a plastic sphere with marking which allowed the

to *𝐵*0. Scans were obtained at 15 different orientations which were sample to be rotated in order to achieve known orientations relative

chosen to be equally distributed on a hemisphere. A 12-channel head coil was the signal receiver. Volume scans were performed using a 3T hospital scanner (Magnetom Verio, Siemens, Erlangen, Germany), using a 3D T1 FLASH (Fast Low Angle SHot) sequence: TR 13 ms, TE

4.9 ms. The image resolution was 1 mm3 voxels with an image volume

of 256 × 256 × 208 voxels. This data allowed for comparison of the

updated MADI technique to previous work and also served as a gold

standard reference for subset studies in Section [3.2](#_bookmark13).

* 1. *Studies using MRI data*

The reference dataset consisting of all 15 scans was first used with the MADI method described above with no assumed a priori knowledge about the collagen orientation. In this way we generated reference tractography results for the patella tendon, which was subsequently used as the basis for evaluation of results involving reduced number of scans and added image noise. Justification for this approach was our previous work [[10](#_bookmark30)], which has shown that accurate results are obtained

therefore we assumed that using 15 scans with high SNR (SNR *>* 50) is using 7 scans in the case when no a priori knowledge is available,

more than adequate to provide a gold standard of method performance.

In subsequent studies we used subsets of *𝑁* = 3*,* 4*,* 5 from the full set

of 15 reference scans, with orientations that were closest to the desired

ones. Therefore this assumed that the orientation could be controlled

**Table 1**

The average angle the computed fibres in the patella tendon made with *𝐵*0 for each

scan.

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| Scan | 1 | 2 | 3 | 4 5 6 7 8 9 10–15 |
| Mean *𝜃* [◦] | 9.3 | 34.0 | 24.6 | 29.0 35.4 62.0 68.8 61.8 56.5 80–85 |

with an accuracy of about ±7◦, which is considered reasonable for practical situations.

The effect of noise was analysed by adding Rician noise to the images [[25](#_bookmark44)] corresponding to certain SNRs. SNR was calculated as:

*𝑆𝑖𝑔𝑛𝑎𝑙*

= | |

*𝑆𝑁𝑅 𝑆𝑡𝐷𝑒𝑣*(*𝑁 𝑜𝑖𝑠𝑒*) (5)

where *𝑆𝑖𝑔𝑛𝑎𝑙* is the mean signal, calculated by taking the mean

| |

of all intensities in a dataset within a mask of the specimen, and

*𝑆𝑡𝐷𝑒𝑣*(*𝑁 𝑜𝑖𝑠𝑒*) is the standard deviation of the noise in the air around

the specimen. The mask used for the mean signal calculation was a

slimmed version of the registration mask, so not to include the air surrounding the specimen, while an expanded version of the same mask was used to calculate the standard deviation of noise in the air and to exclude any signal from the specimen.

In all studies, the collagen-rich regions of the images were seg- mented via two interactive steps. A cuboid ROI was first selected interactively on the fixed image, and then applied to the subsequent registered images. Standard deviation of the intensity was calculated across all corresponding voxels in the ROI to produce a standard deviation image, where bright, high standard deviation voxels were likely to contain collagen. The standard deviation was normalised by the maximum value and the user then iteratively set a threshold,

[0*...*1], to isolate voxels with significant standard deviation. The user

was presented with a 3D plot of all the voxels in the ROI above the

threshold. This visualisation ensured the collagen structure of interest was suitably captured before fibre direction computation. Discretion was required to avoid inclusion of too many non-collagen containing voxels resulting from artefacts, such as the partial volume effect or registration errors. Once chosen, the user then selected a contiguous collection of voxels that represented the collagen structure of interest to be segmented.

To quantify how accurate a given test configuration was, the angular

voxels between each *𝑁* = 3*,* 4*,* 5 subset and the *𝑁* = 15 scan dataset. The separation (deviation) was recorded for each set of corresponding deviations were binned into histograms with bin sizes of 5◦–25◦ and the

the same segmentation label was used for *𝑁* = 15 and its subsets. proportion of angles in each bin was recorded. This necessitated that

# Results

The MADI technique was applied to the *𝑁* = 15 scan dataset, the scanning orientations used were chosen to allow for any collagen fibre

direction to be estimated and to serve as a gold standard for subsequent comparisons using subsets of this dataset. The patella tendon shown in

[Fig.](#_bookmark4) [1](#_bookmark4) was segmented and represented by 2080 voxels, or 2080 × 15

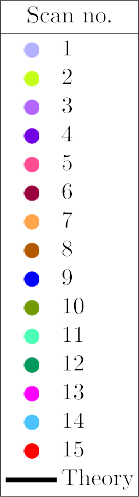
directions. [Fig.](#_bookmark11) [3](#_bookmark11) shows the measured intensity vs the angle to *𝐵*0 corresponding voxels across all scans, yielding 2080 estimated fibre

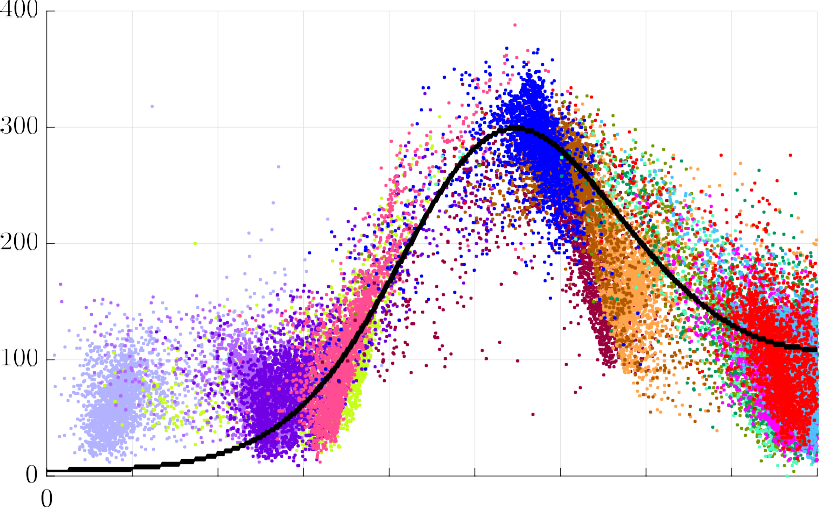
for each computed fibre direction for each scan. Each computed fibre direction relates to 15 data points in [Fig.](#_bookmark11) [3](#_bookmark11), where the straightness of the patella tendon is illustrated by the data points for each scan being grouped together. The theoretical intensity variation from Eq. ([1](#_bookmark1)) is shown to fit well with the measured data, particularly around the Magic Angle.

[Table](#_bookmark10) [1](#_bookmark10) contains the mean of all 2080 fibre directions for each scan relative to B0 for that scan, since the patella tendon is relatively straight, these means were used to quantify the macroscopic tendon

orientation relative to *𝐵*0.

sampled over the full spectrum of angles when using *𝑁* = 15 even [Fig.](#_bookmark11) [3](#_bookmark11) shows that the intensity response of the collagen is well





**/ig. 3.** Intensity vs. *𝜃* for each computed fibre direction in the ROI across all *𝑁* = 15 scans, points in each scan indicated by a distinct colour. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

spaced scanning orientations. We hypothesised that a set of *𝑁* = 3

scanning orientations would be sufficient to estimate fibre directions

if the peak intensity response was sampled at the Magic Angle as well as one data point either side. To identify suitable choices of scanning orientations we performed simulation studies on a single voxel with

known collagen fibre direction along the *𝑍* axis. With *𝑁* = 3 4 5

**Table 2**

Scans chosen for *𝑁* = 3*,* 4*,* 5 subsets and the mean angle of the patella tendon relative to *𝐵*0 for each scan.

N Scans

3 5 (34*.*5◦), 7 (68*.*8◦), 9 (56*.*5◦)

4 4 (29*.*0◦), 5, 7, 9

*, ,* 5 4, 5, 7, 9, 13 (80*.*0◦)

recorded in an *𝑁* dimensional matrix. the deviation of the computed fibre direction from ground truth was

* 1. *Simulation study results*

deviations with *𝜃*1 and *𝜃*2 in the range 15◦–85◦ and the remaining angles [Fig.](#_bookmark14) [4](#_bookmark14) a–f shows the deviation surfaces formed by the recorded

at chosen static values in order to visualise the deviations as a 3D surface. The blue regions highlight areas with deviation of less than

10◦. The results show symmetry along the *𝜃*1 ∶ *𝜃*2 diagonal as expected.

[Fig.](#_bookmark14) [4](#_bookmark14)a shows a low deviation region at [*𝜃*1*, 𝜃*2*, 𝜃*3] = [40◦, 70◦, 55◦] in agreement with our hypothesis. [Fig.](#_bookmark14) [4](#_bookmark14)d shows the results when *𝜃*3 = 50◦ showing that the method is robust even if the intensity peak at the

Magic Angle is not perfectly captured.

[Fig.](#_bookmark14) [4](#_bookmark14)b shows a similar deviation surface with *𝜃*1 and *𝜃*2 in the range 15◦–85◦ and *𝜃*3 = 55◦ and *𝜃*4 = 70◦. The low deviation regions

orientations relative to 3. *𝜃*4 was chosen to visualise the data in [Fig.](#_bookmark14) [4](#_bookmark14)b have expanded suggesting an increased robustness of using 4 scanning

results with *𝜃*3 = 50◦ illustrating robustness across a range of *𝜃*3. from the region of low deviation in [Fig.](#_bookmark14) [4](#_bookmark14)a. Again [Fig.](#_bookmark14) [4](#_bookmark14)e shows the

[Fig.](#_bookmark14) [4](#_bookmark14)c shows a deviation surface with *𝜃*1 and *𝜃*2 in the range 15◦–85◦

and *𝜃*3 = 55◦, *𝜃*4 = 40◦ and *𝜃*5 = 70◦ where the entire surface is a low deviation region. Since the static angles *𝜃*3, *𝜃*4, *𝜃*5 are already good low

angles *𝜃*1 and *𝜃*2 also yield low deviation. The central region of [Fig.](#_bookmark14) [4](#_bookmark14)c deviation choices for scanning orientations, any additional choice of near *𝜃*1 = *𝜃*2 = *𝜃*3 shows the highest deviation as the additional scans are redundant. [Fig.](#_bookmark14) [4](#_bookmark14)f shows the surface with *𝜃*3 = 50◦, also an entirely

low deviation surface.

select the *𝑁* = 3*,* 4*,* 5 subsets to test the MADI technique with fewer The results from the simulation studies and [Table](#_bookmark10) [1](#_bookmark10) were used to

scans. We chose scanning orientations in the low deviation regions found in the simulation studies. The patella tendon was relatively straight hence the means in [Table](#_bookmark10) [1](#_bookmark10) are representative of the tendon’s

angle to *𝐵*0 for a particular scan. The chosen subsets and their mean

orientations to *𝐵*0 are given in [Table](#_bookmark12) [2](#_bookmark12).

* 1. *MRI data subset results*

When imaging a healthy tendon, there is a high degree of fibre alignment which is what the a priori knowledge is based on. Damaged areas can be detected with the MADI technique as shown by Chappell et al. [[11](#_bookmark31)] in our previous work. Damaged/ruptured tendons were identified from tractography and fibre direction data as areas with discontinuous or misaligned fibres. The damage in these regions was subsequently confirmed via dissection. In our previous work, 9 scans were used to achieve these results hence any fibre direction would be very likely to be resolvable. When using only 4 scans and a priori knowledge, we would expect that a damaged area will show mis- aligned/discontinuous fibres or the fibre directions will not converge in this region due to being too far from the a priori assumption; thus damaged areas will still be identifiable. However, the scope of the present work focuses on assessing the accuracy of fibre estimation using minimal numbers of scans, hence we chose to study a healthy caprine patella tendon since it has fairly simple geometry and highly aligned fibres.

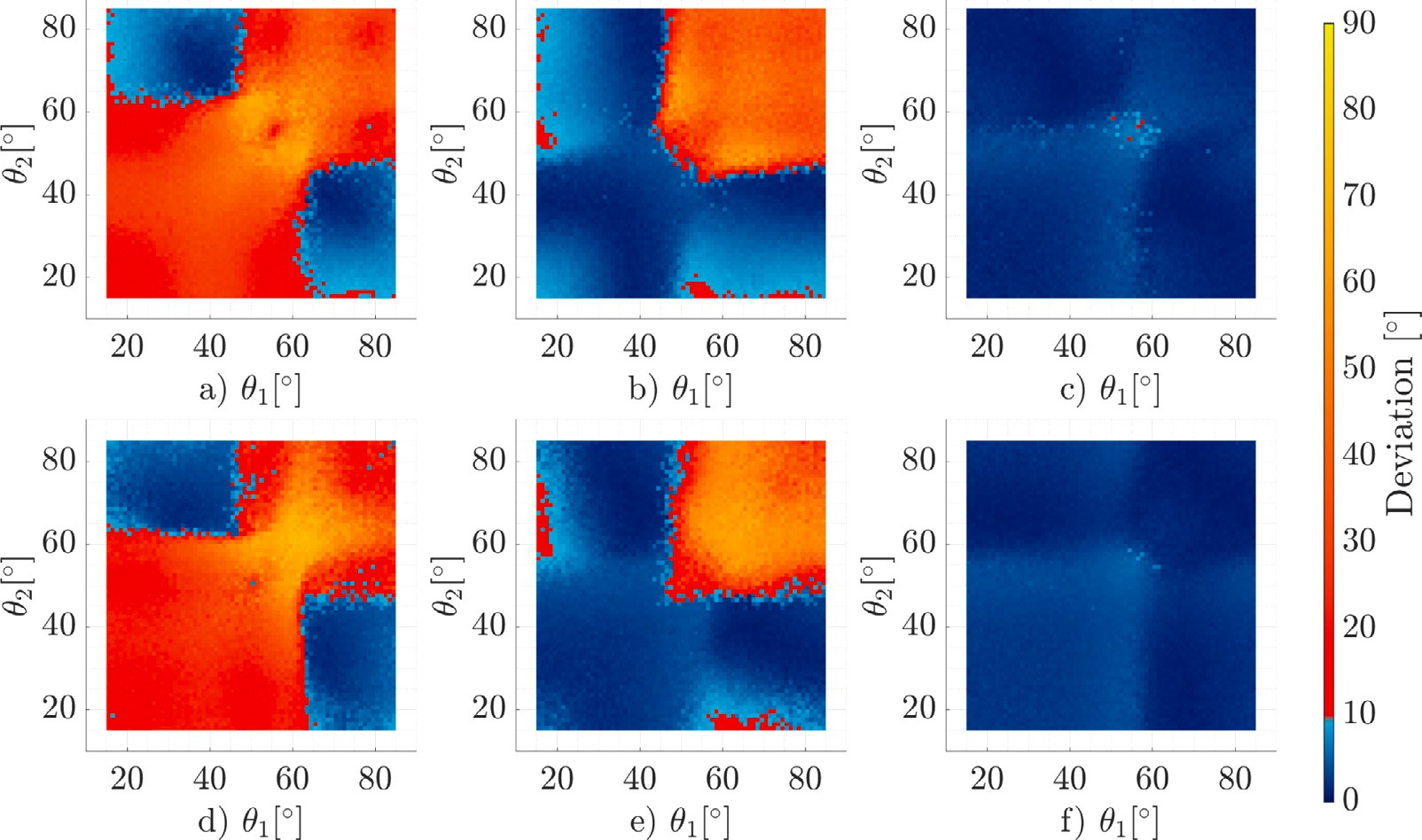
[Fig.](#_bookmark15) [5](#_bookmark15) shows the fibre directions assigned to each voxel for *𝑁* = 3.

This vector field-like representation of the fibres allows for a detailed

view of the local fibre directions within the tendon. Each fibre direction estimation is denoted with a coloured line pointing from a voxel loca-

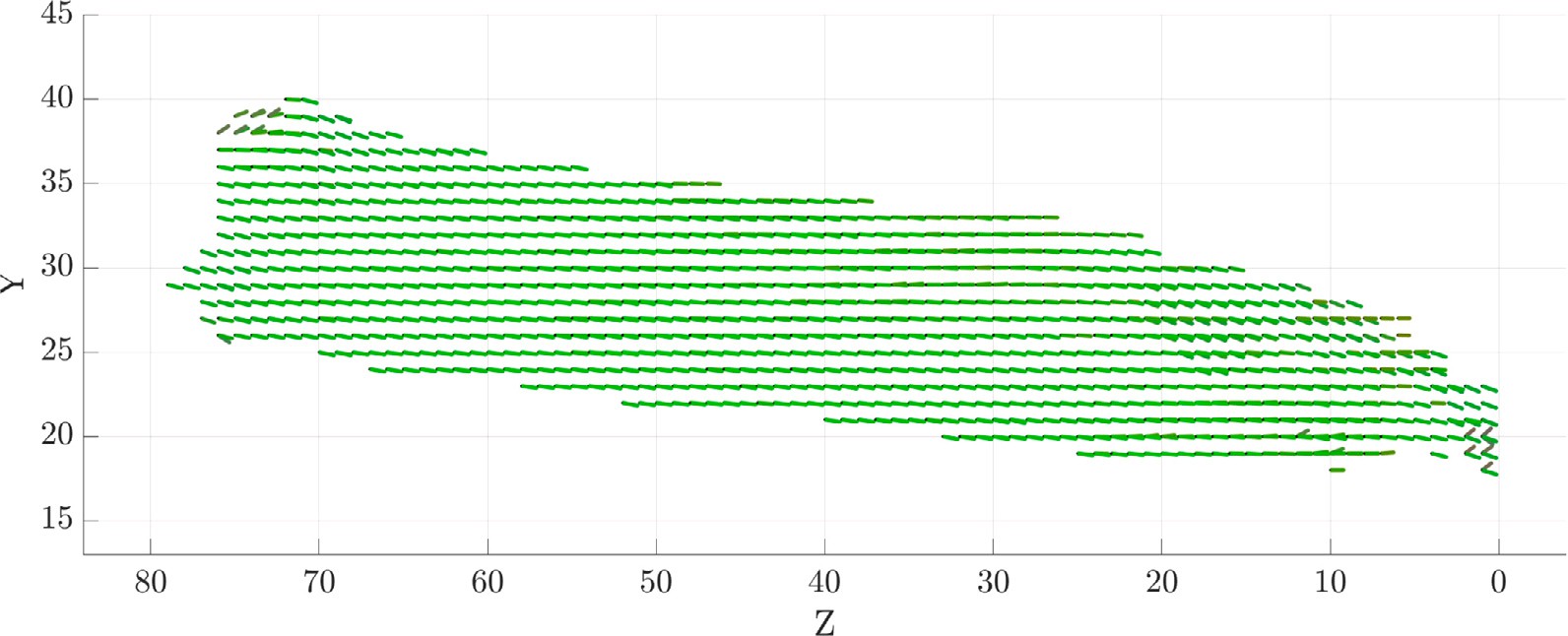
by the axes it aligns with, alignment along the *𝑥* axis would only have tion, marked as a black dot. The RGB colour of the line is determined a red component, and only blue and only green for the *𝑦* and z axes

respectively. For directions not perfectly aligned with an axes the RGB values are interpolated. [Fig.](#_bookmark15) [5](#_bookmark15) shows a high degree of fibre alignment as the fibres can be seen to flow into each other from voxel to voxel and almost all of them are marked green or a shade of green. If damage were present this visualisation technique would be useful for a detailed voxel level view of the region. However, to better understand the tendon structure in 3D and in the context of other anatomy, tractography was generated.



**/ig. 4.** Deviation surfaces from single voxel simulation studies. The top row has *𝜃*3 = 55◦ and the bottom row has *𝜃*3 = 50◦. (a) and (d) show the deviation surface using 3 scanning orientations, (b) and (e) with 4 scanning orientations with *𝜃*4 = 70◦, and (c) and (f) with 5 scanning orientations with *𝜃*4 = 70◦ and with *𝜃*4 = 40◦. (For interpretation

of the references to colour in this figure legend, the reader is referred to the web version of this article.)



**/ig. 5.** Fibre directions assigned to each set of corresponding voxels for *𝑁* = 3. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Tractography results for *𝑁* = 3, *𝑁* = 4 and *𝑁* = 15 scans are shown

in [Fig.](#_bookmark16) [6](#_bookmark16), using the same colouring scheme as in [Fig.](#_bookmark15) [5](#_bookmark15). Tractography

visualisation of the tendons in [Fig.](#_bookmark16) [6](#_bookmark16) was produced using Slicer [[26](#_bookmark45)] with the diffusion tensor imaging extension [[27](#_bookmark46)], by converting our fibre direction estimations into synthetic diffusion tensors. The bones were hand-segmented from the images to provide context to the tendon. Qualitatively, the quality of the tractography improves noticeably from

*𝑁* = 3 to *𝑁* = 4, with *𝑁* = 15 displaying the gold standard. *𝑁* = 4 is

of comparable quality to *𝑁* = 15. *𝑁* = 5 tractography is not shown here but was almost identical to *𝑁* = 4. The tractography results show

We used the same segmentation label for *𝑁* = 15 on all the subsets in highly aligned fibres along the tendon indicating similarly to [Fig.](#_bookmark15) [5](#_bookmark15).

standard and the *𝑁* = 3*,* 4*,* 5 studies. order to allow for direct voxel to voxel comparison between the gold

*𝑁* = 3 yields a large spread of deviations with only 35% and 50% of computed directions being within 5◦ and 10◦ respectively. The improvement when using *𝑁* = 4 is evident as the proportion angles within 5◦ and 10◦ of the gold standard increases to 70% and 95%. The improvement from *𝑁* = 4 to *𝑁* = 5 is less pronounced with less than a 5% increase for angles within 5◦ and less than 2% for angles within 10◦ of the gold standard. [Figs.](#_bookmark17) [7](#_bookmark17)–[9](#_bookmark19) all show a consistent accuracy until

approximately an SNR of 25 at which point there is a steep decline as the data becomes too corrupted to estimate fibre directions.

[Fig.](#_bookmark20) [10](#_bookmark20) shows the alignment index of the patella tendon for *𝑁* = 3,

*𝑁* = 4, and *𝑁* = 15. We previously used alignment index as a measure

of anisotropy of the computed fibre directions which we correlated with

tendon maturity [[11](#_bookmark31)]. The alignment index was calculated by

*𝑛𝑀* − *𝑛𝑟𝑛𝑑*

To quantify how accurate a given test configuration was, the angular separation (deviation) was recorded for each set of corresponding

*𝐴𝐼* =

*𝑛𝑡𝑜𝑡𝑎𝑙*

– *𝑛*

*𝑟𝑛𝑑*

if *𝑛𝑚 > 𝑛𝑟𝑛𝑑* else *𝐴𝐼* = 0 (6)

voxels between each *𝑁* = 3*,* 4*,* 5 subset and the *𝑁* = 15 scan dataset. The deviations were binned into histograms with bin sizes of 5◦–25◦

and the proportion of angles in each bin was recorded.

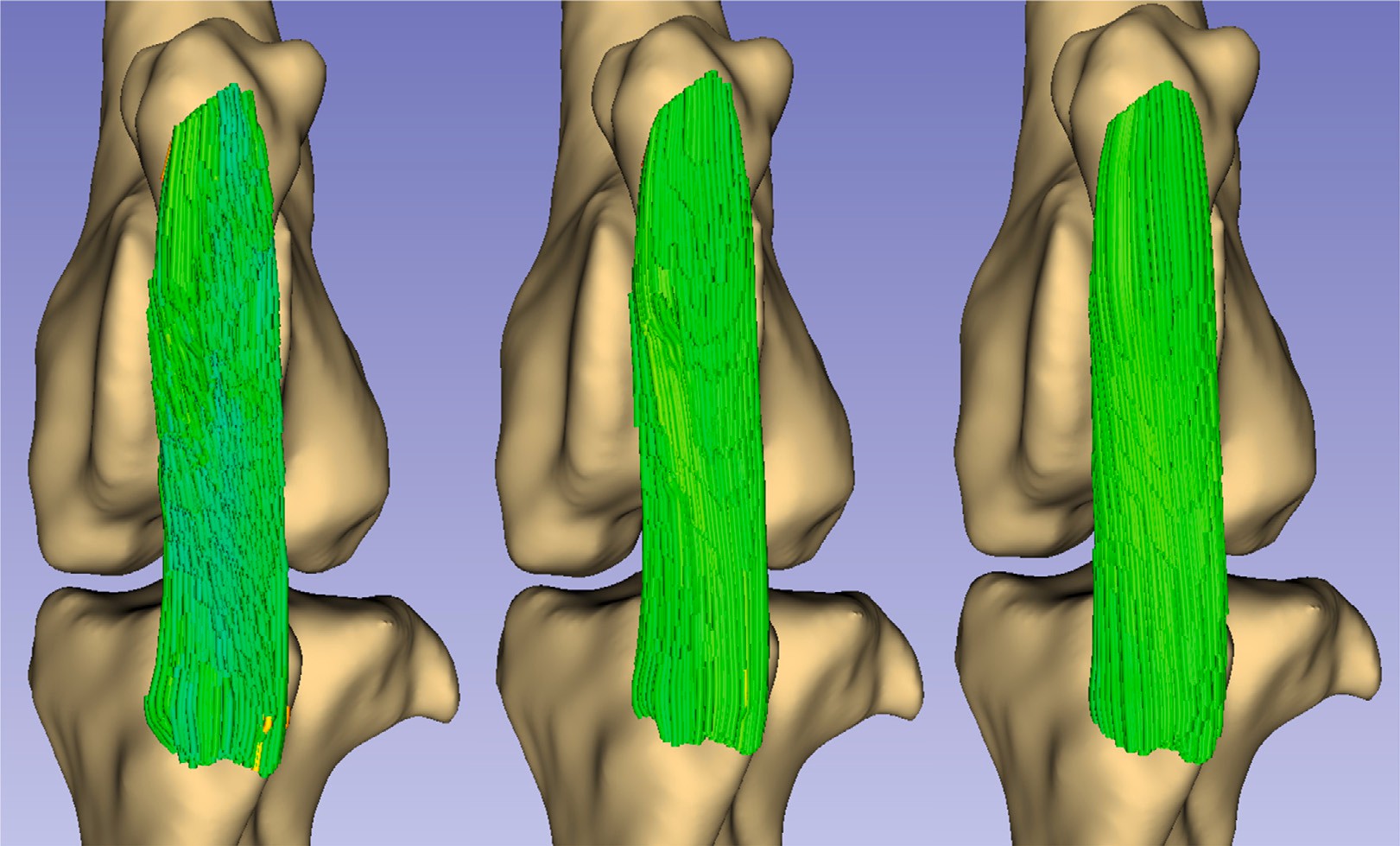
[Figs.](#_bookmark17) [7](#_bookmark17), [8](#_bookmark18), and [9](#_bookmark19) show the accuracy of the *𝑁* = 3*,* 4*,* 5 scan subsets at

different SNRs using voxel to voxel comparison to the gold standard.

where *𝑛𝑡𝑜𝑡𝑎𝑙* was the total number of fibre directions computed, *𝑛𝑀* was

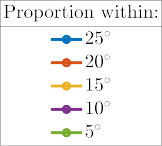
the number of fibre directions within 20◦ of a specified orientation, and *𝑛𝑟𝑛𝑑* is the number of random directions within 20◦ of the specified orientation out of *𝑛𝑡𝑜𝑡𝑎𝑙* random orientations. In our previous work we

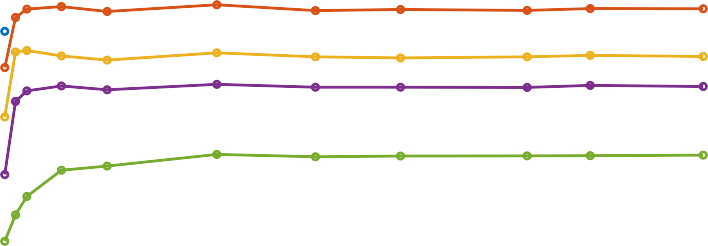
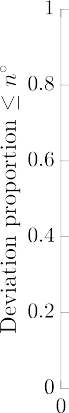
found that more mature tendons had a higher alignment index than



**/ig. 6.** Application of the Magic Angle Directional Imaging technique to render the patella tendon of a caprine knee specimen using tractography. Left to right shows the results

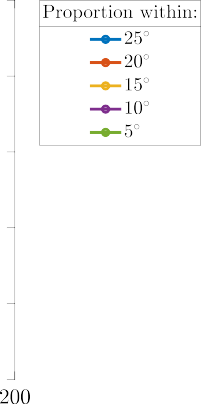
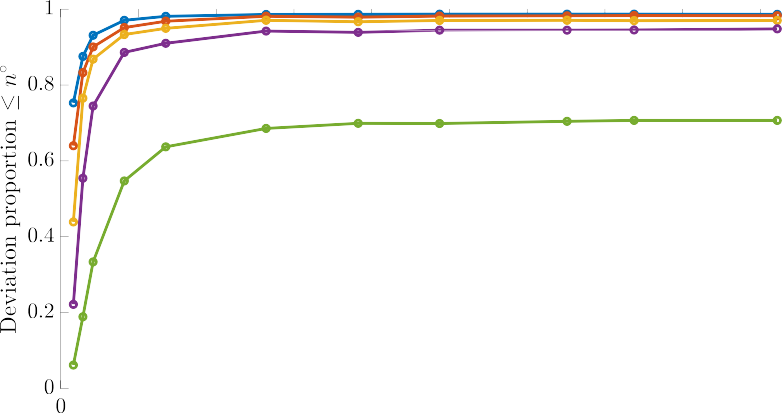
the *𝑦* axis. from 3, 4 and 15 scans respectively, where 15 scans is the gold standard for comparison. The tract colour is a function of its local orientation. Greener regions align more with



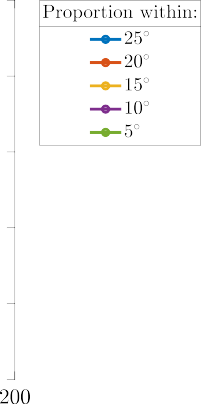
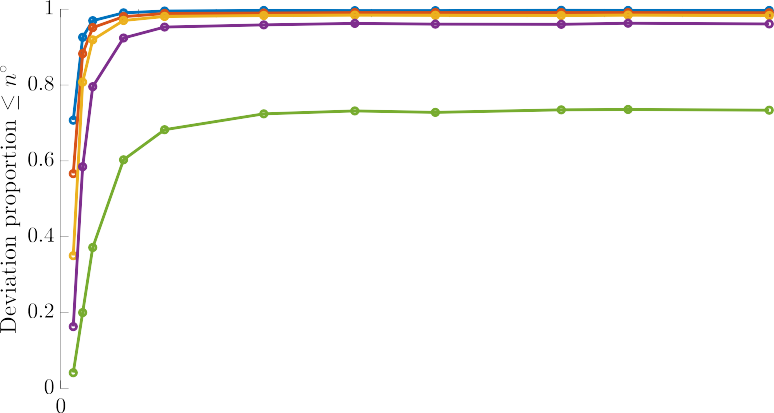


**/ig. 7.** Accuracy and SNR robustness of 3 scan subset when compared to 15 scan gold standard.



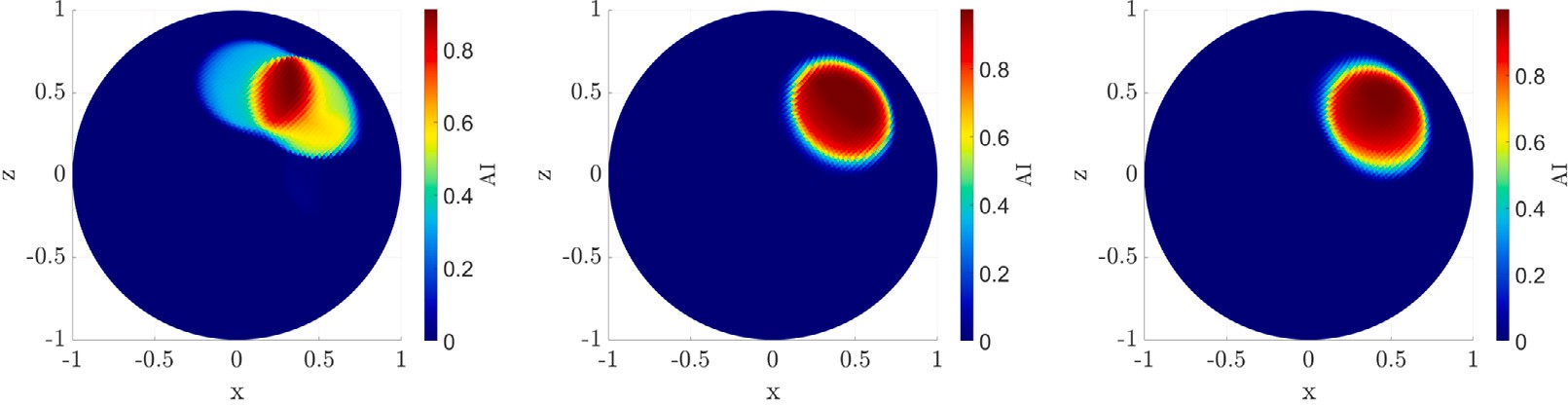


**/ig. 8.** Accuracy and SNR robustness of 4 scan subset when compared to 15 scan gold standard.





**/ig. 9.** Accuracy and SNR robustness of 5 scan subset when compared to 15 scan gold standard.





**/ig. 10.** The alignment indices for [10(a)](#_bookmark21): *𝑁* = 3, [10(b)](#_bookmark22): *𝑁* = 4, [10(c)](#_bookmark22): *𝑁* = 15 plotted on a unit sphere.

shown in the present work in [Fig.](#_bookmark22) [10(c)](#_bookmark22) for the *𝑁* = 15 gold standard. younger tendons provided the tendon was healthy. This result is again [Fig.](#_bookmark21) [10(a)](#_bookmark21) shows the *𝑁* = 3 alignment index which has two obvious

alignment index for *𝑁* = 4 which is very similar to the *𝑁* = 15 result. regions of alignment shown by the dual lobes. [Fig.](#_bookmark22) [10(b)](#_bookmark22) shows the

# Discussion

Previously we have shown that 7−9 scans are sufficient to accurately estimate any collagen fibre direction, with no a priori knowledge

of their orientations, depending on SNR. However, for a given fibre direction, some scans are likely to be redundant due to sampling the same domain of the intensity response as each other. This effect is evident in [Fig.](#_bookmark11) [3](#_bookmark11) where the data from multiple scans overlaps. In the present work we have shown that with some a priori knowledge of the target anatomy this can be avoided and theoretically 3 scans can be used, but in practice 4 scans are necessary to yield sufficiently accurate results. The voxel-to-voxel comparisons and alignment indices shown

in [Figs.](#_bookmark17) [7](#_bookmark17)–[10](#_bookmark20) illustrate that *𝑁* = 4 can yield comparable results to

the gold standard with some a priori knowledge. This is also evident

qualitatively from the tractography in [Fig.](#_bookmark16) [6](#_bookmark16).

Using 3 scans gave somewhat reasonable results, yet with only 3 scans the potential for some directions to be under-constrained was higher. This is particularly evident in the difference between [Figs.](#_bookmark21) [10(a)](#_bookmark21) and [10(b)](#_bookmark22) where the addition of one more scanning orientation was sufficient to correct the alignment of a significant portion of the fibres. Our initial hypothesis was partly correct in that we did have success when sampling the peak intensity response plus one scan either side of it, but we found it necessary to add an additional scan to properly estimate the directions. Since we used data collected assuming no a priori knowledge of the target anatomy, the subsets of scanning orientations used were chosen as they were close enough on average

to what the simulation studies suggested. In future work further gains in accuracy could be made with precise control over the scanning orientations relative to target anatomy, perhaps increasing the viability of using only 3 scans, or further improving the 4 scan results.

With the eventual aim to apply the MADI technique using our prototype low field scanner [[12](#_bookmark32)], fewer scans for accurate results is of practical importance to reduce data acquisition time. A scout scan will likely be necessary to establish a priori knowledge of the target

returns of increasing from *𝑁* = 4 to *𝑁* = 5 suggest that it would not be anatomy, and then the data acquisition will follow. The diminishing

worthwhile to perform an additional scan unless the target anatomy was particularly complex. A curved tendon would in theory require extra scans to compute its fibre directions for the whole tendon as the relative scanning orientation would vary across the structure. In the present work this was not an issue as the patella tendon was relatively straight.

( ) ( )

Since voxels are on the order of U 10−1 to U 100 mm3 in size,

fibres can be considered straight at this scale, hence the method is

as a tendon, which generally have sizes on the order of U 101 mm, always valid for a single given voxel. On a more macroscopic scale such

( )

significant bending or curvature can occur at this scale thus moving the fibres away from the desired relative scanning orientations. However, if the ROI is small, a minimal number of scans would still be sufficient as

with the chosen scanning orientations. Deviations as much as 10◦ were the target anatomy would be locally straight enough for MADI to work

allowed for when choosing scanning orientations, therefore allowing for some local bending/curvature before more scans are necessary.

Because the MADI technique will most likely be applied at low field, the robustness of the method at low SNR is important. [Figs.](#_bookmark17) [7](#_bookmark17)–[9](#_bookmark19) all show that the MADI technique remains accurate until an SNR of roughly 20. Furthermore, since the scanning orientations found in the present work attempt to capture the peak of the Magic Angle effect and

the domain relatively close to it, the signal in the region of interest will boosted.

# Conclusion

The main result presented here is that with a priori knowledge, 4 scanning orientations can be used to accurately estimate the collagen fibre orientations in target anatomy, such as the patella tendon using the MADI technique. The scanning orientations chosen should capture the peak and at least one point either side of it, with an additional scanning orientation to provide extra constraints on the estimated fibre directions. In the case of the patella tendon studied here, the main field

should be oriented at 30◦, 40◦, 55◦, 70◦, relative to the tendon as found

from the simulation studies. The simulation studies suggest there is

≈10◦ of tolerance which enabled the use of (mean) orientations of 29*.*0◦,

34*.*5◦, 56*.*5◦, 68*.*8◦ relative to the patella which yielded accurate results

in comparison to the gold standard reference data.

In practice, application of the technique in vivo would likely consist of a scout scan and then a set of 4 scans based on information from the scout. Even with fairly accurate a priori information, it is unlikely that

*𝐵*0 can be precisely oriented relative to the target anatomy. The lenient

tolerances on the selection of scanning orientations therefore serves to

counter this imprecision. The MADI technique itself has successfully been updated to use fully automatic soft registration which will aid with correction of geometric distortions in the images due to imaging at low field, gradient non-linearities, and soft body deformations. This is a large upgrade over our previous work as registration by manual adjustment is no longer necessary. The technique also shows robustness to low SNR, which will be unavoidable at the low field strength of our prototype scanner. Our scanner can yaw and rotate to capture the necessary images at the angles required for MADI.

In the present work the gold standard dataset was used to generate the segmentation label using standard deviation across the image set as a metric. The same segmentation label was used for all datasets/subsets in order to allow for direct voxel–voxel comparison between them. However, with only 4 scans the standard deviation metric is not as powerful. In lieu of using this metric, manual segmentation of the target anatomy could be performed on the ROI of the fixed image, which could then be applied to the registered images as well. Future work will also focus on other automatic segmentation techniques of the target anatomy such as applying the MADI technique to the whole ROI and then selectively pruning voxels unlikely to contain collagen based on fibre alignment metrics. Even though current segmentation metrics may suffer when using fewer scans, we have shown that fibre estimation accuracy is retained with as few as 4 scans hence allowing for detection of pathologies.

The scope of future work will cover application of MADI on our

ples and in vivo. Having shown that *𝑁* = 4 is sufficient to render fibre prototype scanner and detection and assessment of pathologies in sam-

directions that are close to the assumed direction of the target anatomy, we predict that MADI with minimal scans will detect these regions by either rendering them correctly – if the fibres are within the scanning orientation tolerance – or the fibre directions will not converge in a damaged region. Either scenario would indicate a damaged or diseased region, however, this is something that will be explored as our work develops.

# CRediT authorship contribution statement

**Harry Lanz:** Conceptualization, Methodology, Software, Validation, Formal analysis, Investigation, Data curation, Writing – original draft, Writing – review & editing, Visualization. **Mihailo Ristic:** Conceptual- ization, Methodology, Resources, Writing – review & editing, Supervi- sion, Project administration, Funding acquisition. **Karyn E. Chappell:** Methodology, Validation, Investigation, Resources, Data curation. **John**

**V.M. McGinley:** Methodology.

# Declaration of competing interest

The authors declare that they have no known competing finan- cial interests or personal relationships that could have appeared to influence the work reported in this paper.

# Data availability

Data will be made available on request.

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