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Learning to rank method combining multi-head self-attention with conditional generative adversarial nets

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The existing methods of learning to rank often ignore the relationship between ranking features. If the relationship between them can be fully utilized, the performance of learning to rank methods can be improved. Aiming at this problem, an approach of learning to rank that combines a multi-head self-attention mechanism with Conditional Generative Adversarial Nets (CGAN) is proposed in this paper, named \*GAN-LTR. The proposed approach improves some design ideas of Information Retrieval Generative Adversarial Networks (IRGAN) framework applied to web search, and a new network model is constructed by integrating convolution layer, multi-head self-attention layer, residual layer, fully connected layer, batch normalization, and dropout technologies into the generator and discriminator of Conditional Generative Adversarial Nets (CGAN). The convolutional neural network is used to extract the ranking feature representation of the hidden layer and capture the internal correlation and interactive information between features. The multi-head self-attention mechanism is used to fuse feature information in multiple vector subspaces and capture the attention weight of features, so as to assign appropriate weights to different features. The experimental results on the MQ2008-semi learning to rank dataset show that compared with IRGAN, our proposed learning to rank method \*GAN-LTR has certain performance advantages in various performance indicators on the whole.

# Introduction

Search and recommendation are the most dominant ways to access information in the Internet era, and learning to rank is one of the key techniques. Learning to rank [[1](#_bookmark13)], which uses machine learning methods to train ranking models to solve ranking problems, is a research hot spot of information retrieval and machine learning, which plays an important position in practical applications such as search engines and recommendation systems. More and more learning to rank methods are widely used in these scenarios.

In recent years, with the explosive development of deep learning techniques, it has become a mainstream approach in academia and in- dustry to design learning to rank methods to solve the ranking problem in information retrieval using deep learning algorithms or models such as generative adversarial networks [[2](#_bookmark14)], recurrent neural networks [[3](#_bookmark15)], convolution neural networks [[4](#_bookmark16)], deep neural networks [[5](#_bookmark17)], and deep Q-networks [[6](#_bookmark18)]. Literature [[7](#_bookmark19)] deeply investigated the problems asso- ciated with applying shallow or deep neural networks to train ranking models in information retrieval. Google’s TF-Ranking [[8](#_bookmark20)] is an open- source library for training large-scale learning to rank models using

deep learning algorithms in the TensorFlow framework, which contains a variety of deep neural network-based learning to rank methods.

Current learning to rank approaches only consider the correlation between individual features and the ranking results, and it do not consider the correlation between the local combinations among the features and the ranking results. To address this problem, this paper proposes a method of learning to rank combining a multi-head self- attention mechanism and conditional generative adversarial nets to further improve the ranking performance, which considers the relation- ship between ranking features, mines the potential features and assigns corresponding weights for training the models of learning to rank.

The main contributions of this paper are as follows.

1. Combining multi-head self-attention with Conditional Genera- tive Adversarial Nets (CGAN), we propose a method of learning to rank, named \*GAN-LTR, which is a novel and improved method based on Information Retrieval Generative Adversarial Networks (IRGAN). To the best of our knowledge, \*GAN-LTR is the state-of-the-art one.
2. Our \*GAN-LTR approach constructs a new network model of the generator and discriminator, which integrates the convolutional layer,

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multi-head self-attention layer, residual layer, fully connected layer, batch normalization, dropout technology and other improvements into the generator and discriminator of the CGAN framework.

1. A set of experiments are performed and analyzed. Compared with the frontier method of current learning to rank method IRGAN, the experimental results indicate that our \*GAN-LTR obtains some better results in multiple performance indicators, especially, our method has a faster convergence speed.

# Related work

This paper investigates learning to rank methods that combine multi-head self-attention mechanisms and conditional generative ad- versarial nets. The main works closely related to this paper contains: learning to rank methods based on generative adversarial networks, learning to rank methods based on attention mechanisms, and genera- tive adversarial networks based on attention mechanisms.

* 1. *Learning to rank methods based on generative adversarial networks*

The first pioneering work on solving information retrieval prob- lems using Generative Adversarial Networks (GAN) is the Information Retrieval Generative Adversarial Network (IRGAN) proposed by Wang et al. [[2](#_bookmark14)], which implements a unified description of two schools of thinking of generative retrieval models and discriminative retrieval models in information retrieval modeling. IRGAN uses the idea of con- frontation between generator and discriminator in GAN, and adopts a minimax algorithm in game theory to integrate the generative retrieval model and discriminative retrieval model into a unified framework in a way of confrontation training, so that the two models can improve each other, and finally make the retrieved documents more accurate. The full score paper won the nomination award for the best paper of SIGIR2017, which is both very innovative and very practical. Just like GAN in other fields, it has brought a change in the research paradigm of information retrieval [[9](#_bookmark21)].

At present, a small amount of work has improved or extended IRGAN. Deshpande et al. [[10](#_bookmark22)] proposed two models influenced by self- contrastive estimation and co-training to improve the performance of IRGAN. Jain et al. [[11](#_bookmark23)] improved the convergence of IRGAN through a novel optimization objective based on Proximal Policy Optimiza- tion (PPO) and a sampling technique based on Gumbel-Softmax. Lu et al. [[12](#_bookmark24)] proposed a personalized adversarial training framework PSGAN for personalized search with limited and noisy click data to alleviate the problems of scarcity of high-quality user data and noisy data in personalized search. The PSGAN framework is extended on the basis of IRGAN, the generated model is enhanced to train the attention of those hard-to-distinguish training data through adversarial training, the discriminator is used to evaluate the personalized relevance of documents, and the generator is used to learn the distribution of relevant documents. Two models are proposed in this framework: a model based on the document selection and a model based on the query generation to effectively improve the quality of personalized search. Park et al. [[13](#_bookmark25)] proposed an adversarial sampling and training framework different from IRGAN to learn Ad-hoc retrieval models with implicit feedback, and applied adversarial training to the pairwise learning to rank framework.

Although there have been some improved methods for IRGAN, its performance still has some room for improvement due to the instability of IRGAN training and its simple network model.

* 1. *Learning to rank methods based on attention mechanisms*

Applying attention mechanisms to the learning to rank task, which has been proven that it can successfully focus on different aspects of the input [[14](#_bookmark26)]. Wang et al. [[14](#_bookmark26)] applied the attention mechanism to

the list problem of learning to rank and proposed a new attention- based deep neural network for the learning to rank problem, which applied the attention mechanism to merge different embeddings of query and search results, and used the list approach to sort the search results. Jiang et al. [[15](#_bookmark27)] proposed a learning framework for explicit result diversification using the attention mechanism, recurrent neural networks and max pooling technology, which used the attention mech- anism to capture the subtopics to be concerned while selecting the next document. Zhang et al. [[16](#_bookmark28)] proposed an attention-based learning-to- rank model for structured map search, which was a novel deep neural network architecture of learning-to-rank. Qin et al. [[17](#_bookmark29)] proposed a method of learning to rank based on self-attention network for search result diversification task. This method used self-attention to model the interactions between all candidate documents and subtopics, which can comprehensively measure the relationships between the whole candi- date documents and the coverage degrees of candidate documents to different subtopics. Sun et al. [[18](#_bookmark30)] explored modeling the interactions between documents for learning to rank by employing regularized self-attention. Pobrotyn et al. [[19](#_bookmark31)] studied context-aware learning to rank with self-attention mechanism, and proposed a learnable, context- aware, and scoring function based on self-attention, which allows for modeling of inter-item dependencies not only at the loss level but also in the computation of items’ scores.

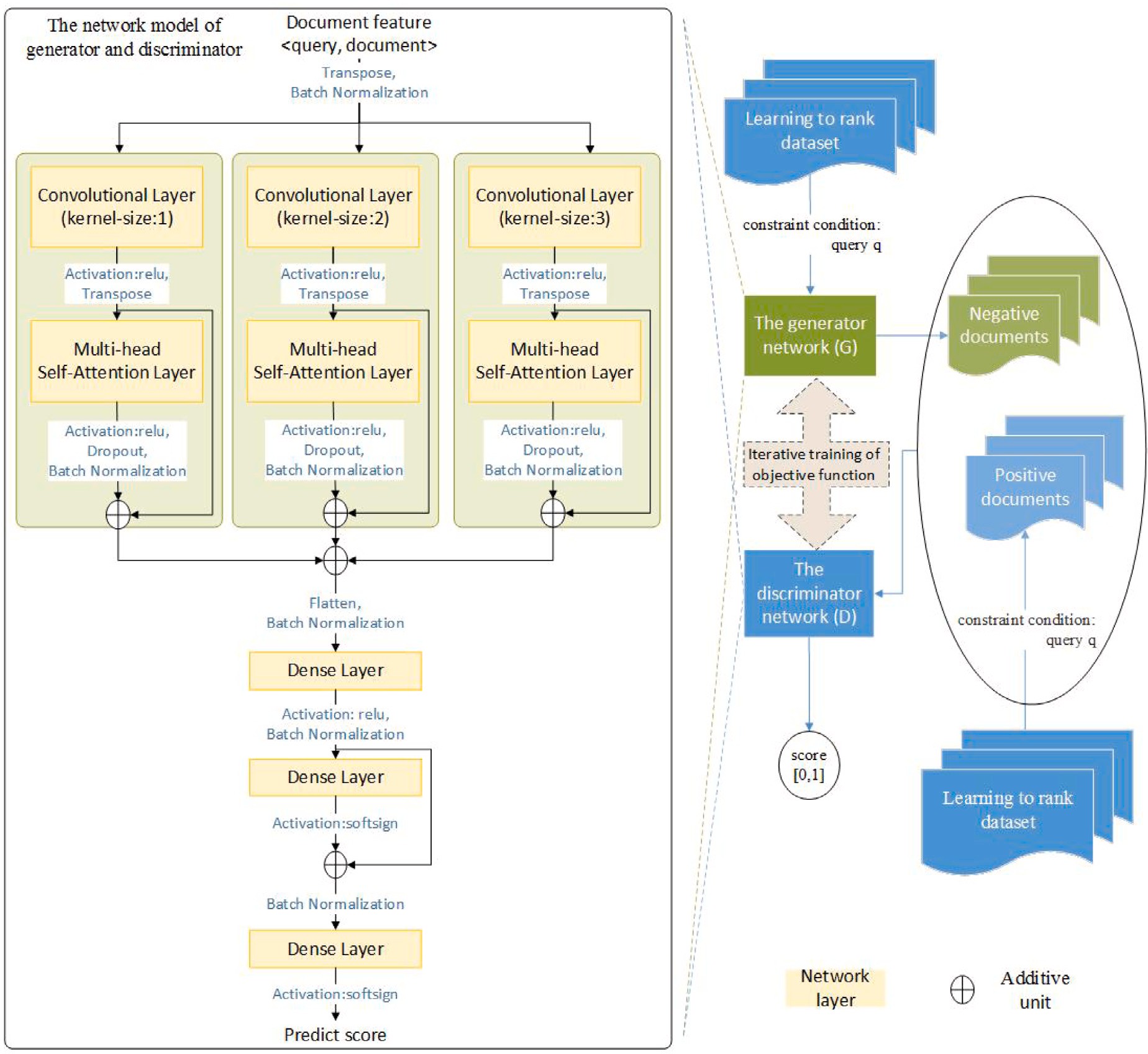
The above research shows that integrating attention mechanism into learning to rank method helps to improve the performance of learning to rank method.

* 1. *Generative adversarial networks based on attention mechanisms*

At present, due to some excellent characteristics of attention mech- anism, the study of applying attention mechanism to generative adver- sarial networks has become a hot spot pursued by some researchers, and some good research results have been gradually formed. Zhang et al. [[20](#_bookmark32)] proposed Self-Attention Generative Adversarial Networks (SAGANs), which integrated the self-attention mechanism into the convolutional GANs framework. The self-attention module is comple- mentary to the convolutional structure so that each pixel was associated with other pixels, and helps to model the long-range, multi-level de- pendencies across different image regions. Xu et al. [[21](#_bookmark33)] added the attention mechanism to GANs and proposed the attentional generative adversarial networks model, named AttnGAN, for synthesizing images from text descriptions. Emami et al. [[22](#_bookmark34)] proposed a novel spatial attention GAN model, i.e. SPA-GAN, which introduced the attention mechanism into the generative adversarial network architecture to help the generator focus more on the most discriminative regions between the source and target domains, resulting in more realistic output images. Jiang et al. [[23](#_bookmark35)] proposed a super-resolution magnetic resonance image reconstruction method by using self-attention based generative adversarial networks, which integrated the self-attention mechanism into the super-resolution GAN framework to calculate the weight parameters of the input features.

The above research shows that incorporating the attention mech- anism into GAN helps GAN to focus on some important and critical information, thereby improving the performance of GAN.

Therefore, based on these research foundations described above, and inspired by their ideas, this paper intends to integrate the attention mechanism and the generative adversarial networks to design the learning to rank method, that is, to propose a method of learning to rank, named \*GAN-LTR, which combines multi-head self-attention with Conditional Generative Adversarial Nets (CGAN) [[24](#_bookmark36)]. \*GAN-LTR method will improve some design ideas of IRGAN framework applied to web search, that is to say, this method integrates the convolutional layer, multi-head self-attention layer, residual layer, fully connected layer, batch normalization and dropout technology into the genera- tor and discriminator of the CGAN framework. Moreover, it uses the softsign activation function to replace the tanh activation function in IRGAN to construct a new network model, so as to further improve the performance of the learning to rank method.



**/ig. 1.** The overall framework of \*GAN-LTR.

# A learning to rank approach combining multi-head self-attent- ion mechanisms with conditional generative adversarial nets

The overall framework of learning to tank method \*GAN-LTR, which integrates multi-head self-attention mechanisms and conditional generative adversarial nets (CGAN), is shown in [Fig.](#_bookmark4) [1](#_bookmark4). In this figure,

documents by setting query *𝑞* as the constraint of CGAN; the left the right side is the framework of CGAN, which controls the generated

side is a new network model reconstructed for the generator and discriminator in CGAN, and the generator and discriminator use the same network model. In the new network model, Transpose is the transpose operation of the input matrix, and Batch Normalization (BN) is the batch normalization operation, which is used several times in the model to alleviate the problem of gradient vanishing, so as to improve the stability of the network. Flatten is a flattening operation for the input matrix to transform the matrix into a one-dimensional vector. Activation represents the activation function, and relu and softsign are used as the activation function, where relu is used as the activation function for the output of the previous layers of the network model, and softsign is used as an alternative to tanh activation function in the last two layers to better alleviate the problem of gradient vanishing. Dropout represents that hidden neurons are deactivated randomly, and

L2 regularization is used to prevent over-fitting of the model. The network model includes convolutional layer, multi-head self-attention layer, residual layer and fully connected layer, etc, where the addition

operation *⊕* represents the residual layer, and Dense Layer represents

the fully connected layer.

The generator network and the discriminator network use the same network model, and the main process of its network model is as follows:

Firstly, several convolution kernels of size 1 × *𝑘*, 2 × *𝑘*, 3 × *𝑘* are

respectively used to convolve the input features in order to achieve

the local feature extraction of the input features; Secondly, the multi- head self-attention layer and the residual layer are used to achieve the global feature extraction for the different convolution results; Thirdly, the output of the multi-headed self-attention layer is spread into a one-dimensional vector, and the results after batch normalization and residual layer accumulation are input into the full connection layer to obtain new features with the same dimensionality as the ranking features; Then, the output of the fully connected layer is performed a fully connected layer and residual layer operations; Finally, the output documents belong to the prediction scores of positive and negative examples respectively after a fully connected layer.

The main layers of the network model of the generator and dis- criminator in \*GAN-LTR are described in detail below: convolutional

layer, multi-head self-attention layer, residual layer, and fully con- nected layer.

* 1. *Convolutional layer*

The convolutional network has the characteristics of local correla- tion and weight sharing. The local correlation feature can avoid the excessive amount of parameters of the fully connected network, and can extract the correlation between local features, a single convolu- tional kernel for weight sharing on feature extraction also avoids the disadvantage of the excessive number of parameters.

Kim [[25](#_bookmark37)] explores the convolutional neural network for sentence classification. Inspired by the idea of its convolutional layer, we apply

it to the network model of \*GAN-LTR. Suppose that *𝑓𝑖* ∈ *𝑅𝑘* is the *𝑖*th

feature vector of document *𝑑*, where *𝑘* is the feature vector dimension

of each feature in the document, then the document vector with length

*𝑛* can be represented as *𝑓𝑖*∶*𝑛* = *𝑐𝑜𝑛𝑐𝑎𝑡*([*𝑓*1*, 𝑓*2*,* … *, 𝑓𝑛*]), where the function

According to the idea of multi-head attention in the literature [[26](#_bookmark38)], we divide the calculation process of multi-head self-attention into three steps as follows.

layer is activated and transposed, matrices *𝑄*, *𝐾* and V required to cal- Step 1: Linear transformation. After the output of the convolutional

of them are set to *𝑊 𝑄*, *𝑊 𝐾* and *𝑊 𝑉* respectively. Then, perform linear culate the self-attention scores are obtained and the parameter matrices transformation on three matrices *𝑄*, *𝐾* and *𝑉* with the same dimensions but different initial parameters, that is, perform *ℎ* different projections on *𝑄*, *𝐾*, and *𝑉* .

of *𝑄* and *𝐾* are calculated by the scaled dot product method, and Step 2: Self-attention calculation. For each head, the attention scores

the attention scores and its corresponding matrix *𝑉* are weighted and the attention scores are normalized by the Softmax function, then summed to obtain the self-attention result of the *𝑖*th head, as shown in

Eqs. ([1](#_bookmark5)) and ([2](#_bookmark6)).

*𝑄𝐾𝑇*

*𝑐𝑜𝑛𝑐𝑎𝑡*() is the splicing function. More generally, let *𝑓𝑖*∶*𝑖*+*𝑗* be as the

splicing feature vector of the document *𝑓𝑖,𝑖*+1*,*…*,𝑖*+*𝑗* . The convolution

operation is to apply a convolutional kernel *𝑤* ∈ *𝑅𝑥𝑘* with the window

*𝑆𝑒𝑙𝑓 𝐴𝑡𝑡𝑒𝑛𝑡𝑖𝑜𝑛*(*𝑄, 𝐾, 𝑉* ) = *𝑠𝑜𝑓 𝑡𝑚𝑎𝑥*( √

*𝑑𝑘*

)*𝑉* (1)

*ℎ𝑒𝑎𝑑𝑖* = *𝑆𝑒𝑙𝑓 𝐴𝑡𝑡𝑒𝑛𝑡𝑖𝑜𝑛*(*𝑄𝑊 𝑄, 𝐾𝑊 𝐾 , 𝑉 𝑊 𝑉* ) (2)

size of *𝑥* to the document features *𝑓𝑖*∶*𝑖*+*𝑥*−1 to produce a new feature

*𝑖 𝑖 𝑖*

*𝑐𝑖*, i.e. *𝑐𝑖* = *𝑆*(*𝑤𝑓𝑖*∶*𝑖*+*𝑥*−1 + *𝑏*), where the bias value *𝑏* ∈ *𝑅*, and *𝑆* is a

document features {*𝑓*1∶*𝑥, 𝑓*2∶*𝑥*+1*,* … *, 𝑓𝑛*−*𝑥*+1∶*𝑛*} to generate a new feature linear function. The kernel function acts on all possible windows in the mapping *𝑐* = [*𝑐*1*, 𝑐*2*,* … *, 𝑐𝑛*−*𝑥*+1] of dimension *𝑅𝑛*−*𝑥*+1, where padding is

the final features are mapped *𝑐* = [*𝑐*1*, 𝑐*2*,* … *, 𝑐𝑛*]. valid. When padding is the same, the blank area will be added so that

For the convolutional layer in \*GAN-LTR, we first transpose the

document features into column vectors and perform a batch normal- ization operation, and then convolve the processed document features

of the *ℎ* heads are spliced and then linearly transformed to obtain the Step 3: Splicing and linear transformation. The self-attention results

final multi-head self-attention output, as shown in Eq. ([3](#_bookmark7)).

*𝑀𝑢𝑙𝑡𝑖𝐻 𝑒𝑎𝑑𝑆𝑒𝑙𝑓 𝐴𝑡𝑡𝑒𝑛𝑡𝑖𝑜𝑛*(*𝑄, 𝐾, 𝑉* ) = *𝐶𝑜𝑛𝑐𝑎𝑡*(*ℎ𝑒𝑎𝑑*1*,* … *, ℎ𝑒𝑎𝑑𝑘*)*𝑊* 0 (3) In each of the above steps, the scaling factor *𝑑𝑘* represents the

dimensionality of the key *𝐾*, and *𝑊 𝑄* ∈ *𝑅𝑑𝑚𝑜𝑑𝑒𝑙* ×*𝑑𝑘* , *𝑊 𝐾* ∈ *𝑅𝑑𝑚𝑜𝑑𝑒𝑙* ×*𝑑𝑘* ,

*𝑖 𝑖*

*𝑊*

using *𝑚* convolutional kernels of size 1 × *𝑘*, 2 × *𝑘*, 3 × *𝑘* respectively,

three feature matrices with *𝑚* × *𝑛*, where *𝑚* denotes the number of where the convolution step is 1 and the padding is the same, to obtain convolutional kernels, *𝑛* denotes the dimension of the document feature vector, and *𝑘* is the dimension of the feature vector. After each feature

matrix is activated and transposed, it is used as the input of the multi-head self-attention layer.

* 1. *Multi-head self-attention layer*

The multi-head self-attention mechanism originates from the Trans- former model proposed by Google [[26](#_bookmark38)]. It is a special internal attention mechanism for modeling the dependencies between elements, which can directly calculate the attention on a sequence itself and reassign the weights at each position to obtain a more reasonable feature representation.

The multi-head self-attention layer is composed of multiple self- attention layers which can be computed in parallel. The queries, keys,

and values matrices are denoted by *𝑄*, *𝐾*, and *𝑉* , respectively, and

*𝑄*, *𝐾*, and *𝑉* are all the same. Suppose that there are *ℎ* heads, and each head transforms *𝑄*, *𝐾*, and *𝑉* into a subspace through a linear

transformation during computation. The parameters of the linear trans- formation of each head are different and learnable, so as to ensure that the model learns relevant features from different representation sub- spaces [[26](#_bookmark38)]. The proposed method \*GAN-LTR in this paper incorporates the multi-head self-attention layer to model the internal dependencies among the ranking features and aggregate these features to obtain higher-level features.

For the multi-head self-attention layer in \*GAN-LTR, its core idea is to calculate the relationships between each ranking feature and all other ranking features, and these feature-to-feature relationships reflect the correlation and importance degree between different features to a

certain extent. Its input is composed of three matrices of query *𝑄*, key

*𝐾* and value *𝑉* , and its output is the multi-head self-attention matrix

after multi-head splicing and linear transformation.

*𝑉* ∈ *𝑅𝑑𝑚𝑜𝑑𝑒𝑙* ×*𝑑𝑣* and *𝑊* 0 ∈ *𝑅ℎ𝑑𝑣* ×*𝑑𝑚𝑜𝑑𝑒𝑙* are the parameter matrixes

respectively, *𝑑𝑚𝑜𝑑𝑒𝑙* denotes the dimensionality of the element vector.

*𝑖*

* 1. *Residual layer*

A residual network simply adds a skip connection between the input and output, and does not add a new type of network layer. In the

residual network, the input *𝑥* is transformed through the network layer

*𝐹* to obtain the output value *𝐹* (*𝑥*), and then the output value *𝐹* (*𝑥*) is summed with the input *𝑥* to get the final output *𝐻* (*𝑥*), i.e. *𝐻* (*𝑥*) =

*𝑥* + *𝐹* (*𝑥*). By stacking the residual modules, the whole network training

can be stabilized with the deepening of network depth.

Xie et al. [[27](#_bookmark39)] explores the aggregated residual transformation of deep neural networks. Inspired by its idea of aggregated residual transformation, we apply it to the network model of \*GAN-LTR. In order to take into account the properties of the residual layer and

result, we add influence factors *𝑎* and *𝑏* to the residual network such consider the overall impact of each part of the residuals on the final that *𝐻* (*𝑥*) = *𝑎𝑥* + *𝑏𝐹* (*𝑥*), where *𝑎* and *𝑏* are trainable hyper-parameters with gradient descent, and 0 ≤ *𝑎* ≤ 1 and 0 ≤ *𝑏* ≤ 1. when *𝑎* = 1 and

*𝑏* = 1, *𝐻* (*𝑥*) will degenerate into a general residual network, otherwise

it will become a weighted residual network. More generally, if there

are multiple networks with outputs of the same dimensional size, then

*𝐻* (*𝑥*) = ∑*𝑛 𝑤𝑖𝐻𝑖*(*𝑥*), where *𝑛* denotes the number of networks, *𝑤𝑖*

*𝑖*=1

denotes the weight of the *𝑖*th network *𝐻𝑖*(*𝑥*), and 0 ≤ *𝑤𝑖* ≤ 1.

For the residual layer in \*GAN-LTR, it is used in the network

the following three cases, i.e., the additive operations *⊕*: Firstly, the model of the generator and discriminator of CGAN respectively in

output of the convolution layer and the output of the multi-head self- attention layer are connected to improve the stability of downstream tasks; Secondly, the outputs of three multi-head self-attention layers are connected to linearly superimpose different outputs; Thirdly, the fully connected layers with the same dimensional outputs are concatenated to further encode useful upstream features and downstream features.

* 1. *Fully connected layer*

The fully connected layer, realizes the mutual mapping of different linear spaces through linear functions. The activation function is added to enhance the classification effect of the fully connected layer and avoid the gradient vanishing.

For the fully connected layer in \*GAN-LTR, that is, the Dense layer in [Fig.](#_bookmark4) [1](#_bookmark4) is used in three spaces in the network model of the generator and discriminator of CGAN, which are: (1) The results of flattening and batch normalization for the output of the second case in the residual layer are input to a fully connected layer, and they are mapped to a linear space with the same dimensional size as the input feature’s dimension for mapping from the high-dimensional space to the low- dimensional space. Here, the relu function is used as the activation function. (2) The last two layers of the network model are two fully connected layers, which correspond to the two fully connected layers in IRGAN. But here, the softsign function is used as the activation function, the activation function of tanh hyperbolic tangent in IRGAN is modified to a softsign activation function with a smoother curve to avoid gradient vanishing.

# Experimental comparison and analysis

To verify the performance of our proposed learning to rank method

\*GAN-LTR that combines the multi-head self-attention mechanism and conditional generative adversarial nets, we re-code the IRGAN ex- perimental code[1](#_bookmark8) and perform experiments on the same dataset of learning to rank MQ2008-semi applied to the web search experiments of IRGAN, then compare and analyze the experimental results with IRGAN applied to the dataset in web search. For other representa- tive methods of learning to rank, i.e., RankNet, LambdaRank and LambdaMART, since IRGAN has been compared with them in the literature [[2](#_bookmark14)] in terms of performance, their experimental results show that IRGAN method has brought significant performance improvements

in all metrics (including *𝑁𝐷𝐶𝐺*@*𝑁* , *𝑃 𝑟𝑒𝑐𝑖𝑠𝑖𝑜𝑛*@*𝑁* , *𝑀𝐴𝑃* and *𝑀𝑅𝑅*).

Therefore, \*GAN-LTR is only compared with IRGAN, and the compari-

son with these methods will not be repeated in this paper. We use the same evaluation metrics in IRGAN [[2](#_bookmark14)] to compare the performance of

\*GAN-LTR and IRGAN, namely *𝑃 𝑟𝑒𝑐𝑖𝑠𝑖𝑜𝑛*@*𝑁* , Mean Average Precision

(*𝑀𝐴𝑃* ), Normalized Discounted Cumulative Gain (*𝑁𝐷𝐶𝐺*@*𝑁* ) and Mean Reciprocal Ranking (*𝑀𝑅𝑅*), which are the generally used stan-

dard ranking performance indicators for learning to rank in information retrieval field. Therefore, for the calculation methods and formulas of these evaluation indicators, please refer to the relevant literature [[28](#_bookmark40)], which are ignored here.

* 1. *Experimental setup*

Following some experimental settings of IRGAN applied to Web search, we preprocess the MQ2008-semi dataset of learning to rank, that is, all query-document pairs with relevance values greater than

with relevance values of 0 or −1 are regarded as unlabeled samples. 0 are regarded as positive samples, and all query-document pairs

Meanwhile, the MQ2008-semi dataset is randomly split into training set and test set according to 4:1, and the sampling method and training process of IRGAN are also adopted, etc.

The experimental results of IRGAN applied to Web search found that IRGAN-Pointwise training was in a stable state when epoch > 100, so the value of epoch was set to 100 to reduce the training time, while other parameters remain consistent with IRGAN’ parameters in the orig- inal paper. For the training of IRGAN-Pairwise, we set the learning rate of the generator of GAN to 0.0003 and the number of training epochs of discriminator and generator to be 30 and 25 respectively by parameter tuning. On the basis of this parameter setting, the experimental results of \*GAN-LTR and IRGAN are compared and analyzed.

1 <https://github.com/geek-ai/irgan>

**Table 1**

Ranking performance comparison of \*GAN-LTR and IRGAN on the MQ2008-semi dataset.

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| Learning to rank methods | Precision@3 | Precision@5 | Precision@10 | MAP |
| IRGAN-pointwise | 0.1873 | 0.1619 | 0.1190 | 0.1801 |
| \*GAN-LTR-pointwise | 0.1968 | 0.1771 | 0.1314 | 0.1936 |
| IRGAN-pairwise | 0.1968 | 0.1657 | 0.1248 | 0.1923 |
| \*GAN-LTR-pairwise | 0.2000 | 0.1752 | 0.1276 | 0.2036 |
| Learning to rank methods | NDCG@3 | NDCG@5 | NDCG@10 | MRR |
| IRGAN-pointwise | 0.2087 | 0.2163 | 0.2377 | 0.3487 |
| \*GAN-LTR-pointwise | 0.2192 | 0.2304 | 0.2484 | 0.3407 |
| IRGAN-pairwise | 0.2204 | 0.2208 | 0.2440 | 0.3497 |
| \*GAN-LTR-pairwise | 0.2274 | 0.2348 | 0.2565 | 0.3573 |

* 1. *Results and discussion*

In order to facilitate the performance comparison with IRGAN,

\*GAN-LTR also follows the same settings on some performance metrics and learning curves of IRGAN applied to web search on the MQ2008- semi dataset of learning to rank. [Table](#_bookmark9) [1](#_bookmark9) shows the comparison of the ranking performance metrics of pointwise and pairwise learning to

for *𝑃 𝑟𝑒𝑐𝑖𝑠𝑖𝑜𝑛*@*𝑁* , *𝑁𝐷𝐶𝐺*@*𝑁* , *𝑀𝐴𝑃* , and *𝑀𝑅𝑅*. As the results are rank methods of \*GAN-LTR and IRGAN on the MQ2008-semi dataset

shown in [Table](#_bookmark9) [1](#_bookmark9), it can be seen that in the vast majority of cases,

\*GAN-LTR is better than IRGAN in each corresponding evaluation metrics. The reasons are mainly due to the integration of convolutional neural networks and multi-head self-attention mechanisms, which can

effectively extract the implicit ranking features of <query *𝑞*, document

*𝑑*>, obtain the correlation between the ranking features, and assign

different weights to different ranking features. Due to the existence

of the multi-head self-attention mechanism, the weight assignments within multiple vector subspaces can be obtained, and the weights of

ranking feature within *𝑞, 𝑑* can be assigned more reasonably, and

⟨ ⟩

the contribution of important ranking features is enhanced, thereby

improving the performance of the learning to rank method \*GAN-LTR.

[Fig.](#_bookmark10) [2](#_bookmark10) shows the changes of the non-adversarial learning curve of the pre-trained models of \*GAN-LTR and IRGAN before adversarial training on the MQ2008-semi dataset, and [Figs.](#_bookmark11) [3](#_bookmark11) and [4](#_bookmark12) show the changes of learning curve of pointwise and pairwise learning to rank methods of \*GAN-LTR and IRGAN during adversarial training on the MQ2008-semi dataset, respectively. They are all the results obtained under the same hyper-parameters (including the number of training epochs, learning rate, batch size, etc.). Specifically, the results shown in [Fig.](#_bookmark10) [2](#_bookmark10) reflect the performance’s changes of the non-adversarial learning curves of the pre-trained models of \*GAN-LTR and IRGAN

before adversarial training on the evaluation criteria *𝑁𝐷𝐶𝐺*@5 and

*𝑃 𝑟𝑒𝑐𝑖𝑠𝑖𝑜𝑛*@5, which is iteratively evolved with the number of rounds.

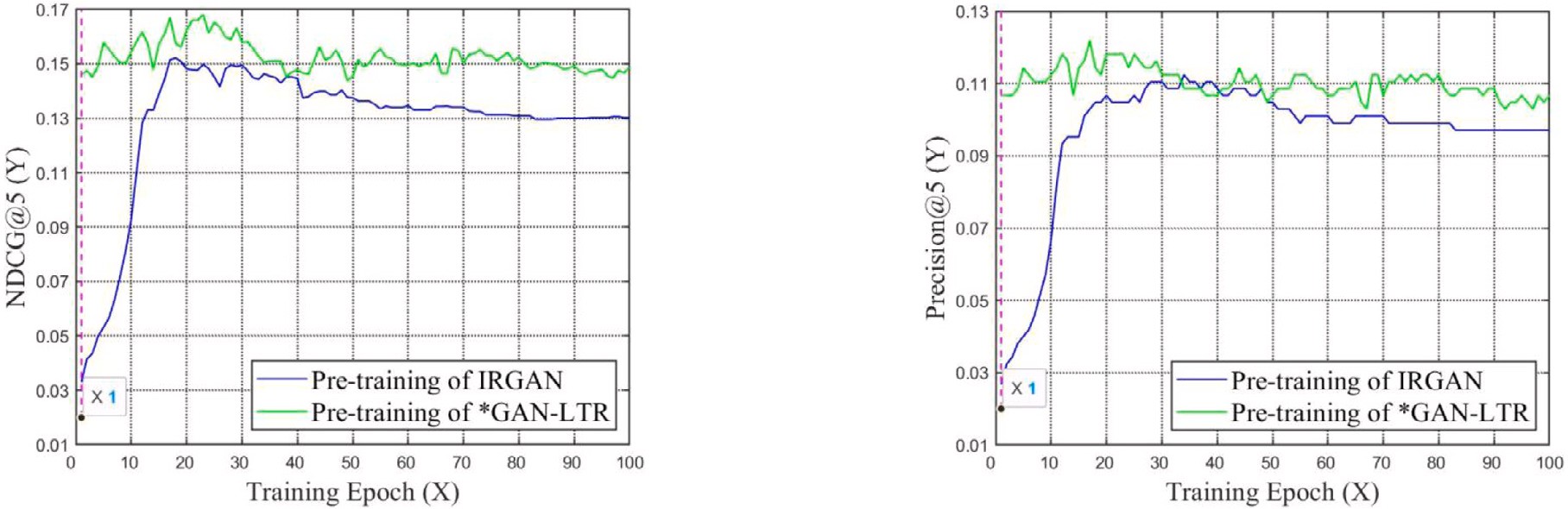
It can be seen from this figure that the pre-training model of \*GAN-

evaluation metrics *𝑃 𝑟𝑒𝑐𝑖𝑠𝑖𝑜𝑛*@5 and *𝑁𝐷𝐶𝐺*@5. Furthermore, we can LTR performs better than the pre-training model of IRGAN for the

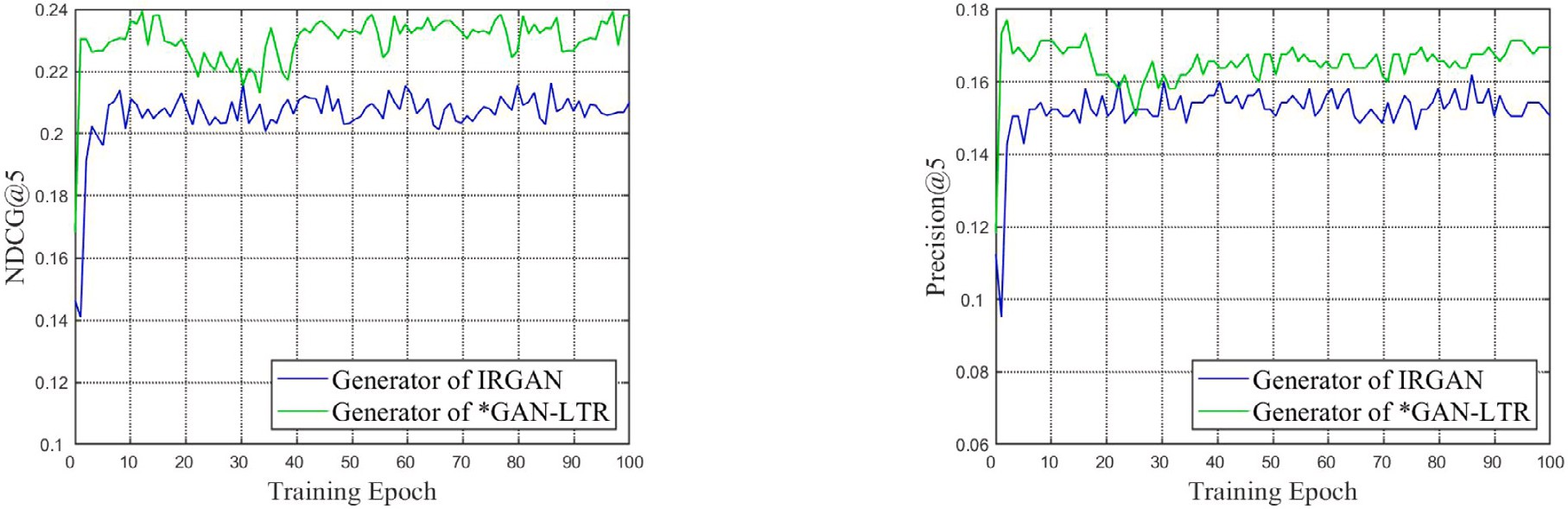
also see that the convergence of our proposed method \*GAN-LTR is faster compared with IRGAN. So our proposed method \*GAN-LTR is better than IRGAN in evaluation metrics and convergence. The main reason is that the multi-head self-attention layer is integrated into the pre-training model of \*GAN-LTR, which can capture the attention weights of ranking features and assign higher weights to important ranking features, thereby improving the performance of the \*GAN-LTR method as a whole. The results shown in [Fig.](#_bookmark11) [3](#_bookmark11) reflect the perfor- mance’s changes of the adversarial learning curves of the respective

IRGAN on the evaluation criteria *𝑃 𝑟𝑒𝑐𝑖𝑠𝑖𝑜𝑛*@5 and *𝑁𝐷𝐶𝐺*@5, which generators in the pointwise learning to rank methods of \*GAN-LTR and

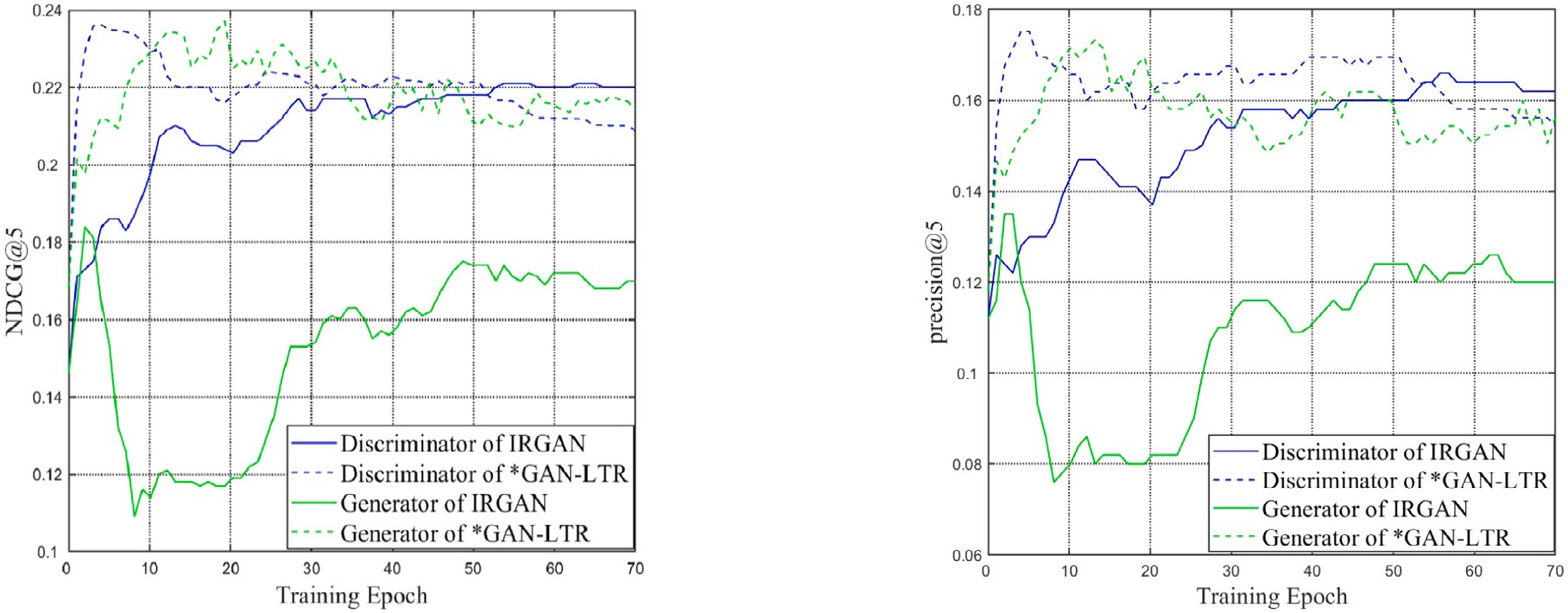
are iteratively evolved with the number of epochs. The results shown in [Fig.](#_bookmark12) [4](#_bookmark12) reflect the evolution of the adversarial learning curves of the respective generators and discriminators in the pairwise learning to rank methods of IRGAN and \*GAN-LTR on the evaluation criteria



**/ig. 2.** Learning curves of the pre-trained models of \*GAN-LTR and IRGAN before the adversarial training on the MQ2008-semi dataset.



**/ig. 3.** Pointwise learning curves of \*GAN-LTR and IRGAN on the MQ2008-semi dataset.



**/ig. 4.** Pairwise learning curves of \*GAN-LTR and IRGAN on the MQ2008-semi dataset.

*𝑃 𝑟𝑒𝑐𝑖𝑠𝑖𝑜𝑛*@5 and *𝑁𝐷𝐶𝐺*@5 with the number of iterations. It can be

iterative training, the values of the evaluation criteria *𝑁𝐷𝐶𝐺*@5 and seen from the results in these two figures that in the early stage of

*𝑃 𝑟𝑒𝑐𝑖𝑠𝑖𝑜𝑛*@5 obtained by the respective pointwise and pairwise learning

to rank methods of \*GAN-LTR and IRGAN show a increasing trend with

the iterative training. The main reason is that the generator network and the discriminator network in \*GAN-LTR and IRGAN methods lead to the improvement of the generative ability and the discriminative ability in the continuous adversarial game, thus increasing the value of each evaluation metric. In the later stage of iterative training, the value of each evaluation metric tends to be stable and fluctuate up and down, indicating that the adversarial training of each method has reached a stable state. Furthermore, from the overall point of view, [Figs.](#_bookmark11) [3](#_bookmark11)

and [4](#_bookmark12) also show that the curves of various performance indicators of \*GAN-LTR are roughly above those of IRGAN, indicating that the corresponding performance indicators obtained by \*GAN-LTR training have obtained better results, that is, \*GAN-LTR has better performance than IRGAN. In the same way, the main reason for such results is still due to the incorporation of technologies such as convolutional neural networks and multi-head self-attention mechanisms in CGAN. Finally,

compared with the results of the performance criteria *𝑁𝐷𝐶𝐺*@5 and

*𝑃 𝑟𝑒𝑐𝑖𝑠𝑖𝑜𝑛*@5 of the pre-trained model shown in [Fig.](#_bookmark10) [2](#_bookmark10), the results of the

performance criteria shown in [Figs.](#_bookmark11) [3](#_bookmark11) and [4](#_bookmark12) show superior performance,

indicating that the iterative adversarial training of CGAN can improve the performance of pre-trained models (here, non-adversarially trained models) to a certain extent.

# Conclusion

Aiming at the fact that the existing learning to rank methods often ignore the relationship between ranking features, this paper proposes a new method of learning to rank, named \*GAN-LTR, that combines a multi-head self-attention mechanism with Conditional Generative Adversarial Nets (CGAN). This method adopts the sampling method and training process of IRGAN, and improves some design ideas of applying the IRGAN framework to web search. \*GAN-LTR has made the following improvements on the basis of IRGAN: In the network model of CGAN, the convolutional layer and multi-head self-attention layer are added to extract the local features and global combined features of the documents and assign appropriate weights to different ranking features, the residual layer is added to avoid the gradient vanishing and degradation problems caused by the network being too deep, batch normalization is added to enhance the stability of the network, the dropout technique is added to randomly deactivate the hidden units to avoid over-fitting, and the activation function hyperbolic tangent tanh function is modified to a softsign activation function with a smoother curve to avoid gradient vanishing. The experimental results on the MQ2008-semi learning to rank dataset show that: compared with the experimental results of IRGAN applied to web search, the learning to rank method \*GAN-LTR proposed in this paper obtains better results in various performance indicators. As a whole, \*GAN-LTR has certain performance advantages.

# CRediT authorship contribution statement

**Jinzhong Li:** Conceptualization, Methodology, Software, Formal analysis, Investigation, Resources, Writing – original draft, Writing – review & editing, Project administration, Funding acquisition. **Huan Zeng:** Conceptualization, Methodology, Software, Validation, Formal analysis, Data curation, Writing – original draft, Writing – review & editing, Visualization. **Lei Peng:** Writing – review & editing, Supervi- sion. **Jingwen Zhu:** Investigation, Supervision, Project administration, Funding acquisition. **Zhihong Liu:** Validation, Visualization.

# Declaration of competing interest

The authors declare that they have no known competing finan- cial interests or personal relationships that could have appeared to influence the work reported in this paper.

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