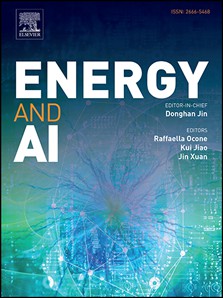
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# Highlights

* Investigated CSP integrated sCO2 Brayton cycles' thermal performance and optimization
* Analysed solar irradiance's and climate temperature impact on the system extensively
* Explored TES dynamic operation at night and seasonal power generation patterns.
* Utilized a hybrid approach: machine learning with genetic algorithm for optimization.
* Achieved 16.985 MW power and 54.708% thermal efficiency with optimized condition



**Multi-Objective Performance Optimization & Thermodynamic Analysis of Solar Powered Supercritical CO2 Power Cycles Using Machine Learning Methods & Genetic Algorithm**

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# Abstract

The present study is focused on multi-objective performance optimization & thermodynamic analysis from the perspectives of energy and exergy for Recompression, Partial Cooling & Main Compression Intercooling supercritical CO2 (sCO2) Brayton cycles for concentrated solar power (CSP) applications using machine learning algorithms. The novelty of this work lies in the integration of artificial neural networks (ANN) and genetic algorithms (GA) for optimizing the performance of advanced sCO2 power cycles considering climatic variation, which has significant implications for both the scientific community and engineering applications in the renewable energy sector. The methodology employed includes thermodynamic analysis based on energy, exergy & environmental factors including system performance optimization. The system is modelled for net power production of 15 MW thermal output utilizing equations for the energy and exergy balance for each component. Subsequently, thermodynamic model extracted dataset used for prediction & evaluation of Random Forest, XGBoost, KNN, AdaBoost, ANN and LightGBM algorithm. Finally, considering climate conditions, multi-objective optimization is carried out for the CSP integrated sCO2 Power cycle for optimal power output, exergy destruction, thermal and exergetic efficiency. Genetic algorithm and TOPSIS (technique for order of preference by similarity to ideal solution), multi-objective decision-making tool, were used to determine the optimum operating conditions. The major findings of this work reveal significant improvements in the performance of the advanced sCO2 cycle by 1.68% and 7.87% compared to conventional recompression and partial cooling cycle, respectively. This research could advance renewable energy technologies, particularly concentrated solar power, by improving power cycle designs to increase system efficiency and economic feasibility. Optimized advanced supercritical CO2 power cycles in concentrated solar power plants might increase renewable energy use and energy generation infrastructure, potentially opening new research avenues.

# Keywords

Supercritical CO2; Concentrated solar power; Thermodynamic analysis; Machine Learning; Artificial Neural Network; Multi-objective optimization.

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# Nomenclature

*A* area, m2

*Cp* specific heat at constant pressure, J/kg K

*E* exergy, kW

*h* specific enthalpy, kJ/kg

*ṁ* mass flow rate, kg/s

1. pressure, MPa
2. heat capacity, kW

*s* specific entropy, kJ/kg K

*T* temperature, ºC or K

*W* power output, MW

*x* split ratio

# Greek symbols

*ε* recuperator effectiveness

*η*

# Subscripts

*cyc cos ex hel in net out rec ref s*

*s&h 0*

*1, 2, 3, …*

# Abbreviations

ANN CSP DP DNI DT GA H HTR INT ICL KNN

LGBM LTR MCIT

Efficiency

cycle cosine exergy heliostat inlet

net power outlet receiver reflectivity supercritical

shading & blocking environment state state points

artificial neural network concentrated solar power design point

direct normal irradiance decision tree

genetic algorithm heater

high temperature recuperator

main compression intercooling cycle intercooler

k-nearest neighbor

light gradient boosting machine low temperature recuperator

main compressor inlet temperature

MC ML MSE PAR PC PCL RC REC RF RH RMSE RPR R2 sCO2

sCO2BC TES TIT TOPSIS

XGBoost

main compressor machine learning mean square error partial cooling cycle pre-compressor

pre-cooler recompressor recompression cycle random forest reheater

root mean square error ratio of pressure ratios coefficient of determination supercritical carbon dioxide

supercritical carbon dioxide Brayton cycle thermal energy storage

turbine inlet temperature

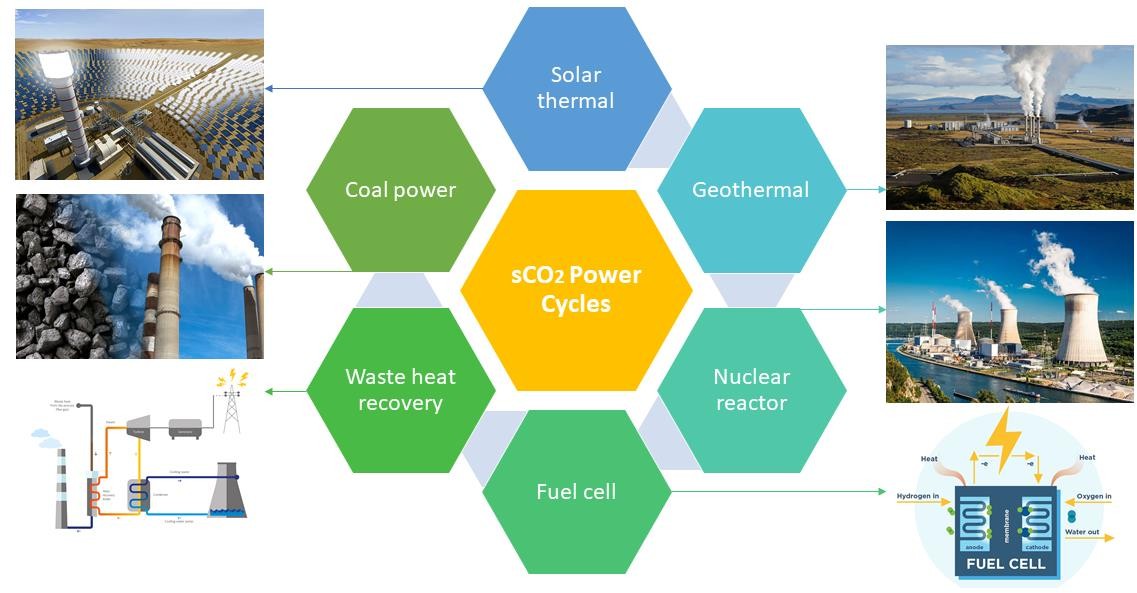
technique for order preference by similarity to ideal solution extreme gradient boosting

# Introduction

In the current context of the energy and environmental challenges, it is imperative to enhance the effectiveness as well as affordability of energy conversion systems. Environmentalists have expressed long-standing concerns regarding climate change and the depletion of the ozone layer due to their potential threats to the sustainability of ecosystems [1]. In response to the increasing per capita energy demands, the global energy sectors are actively engaged in the progression and improvement of clean and efficient power production systems. The Supercritical CO2 Brayton cycle (sCO2BC) has garnered significant attention due to its high thermodynamic efficiency. The Brayton cycle's operating fluid reaches the turbine at an extremely high temperature after receiving heat from the source, contributing to the high efficiency of the energy system [2]. The petroleum industry, mining processes, concentrating solar systems, electricity generation, waste heat recovery, geothermal power, nuclear power, and fossil fuels are only a few industries and energy applications where the sCO2 is utilized [3]. This technology exhibits distinctive benefits in concentrated solar power (CSP) as energy sources, in which thermal energy storage enables prolonged operation beyond sunset, thereby mitigating temperature fluctuations and presenting CSP plants as a feasible alternative for fulfilling energy requirements in desert regions [4]. This study presents a methodology that utilizes Machine Learning techniques to predict performance, conduct parametric analysis, and optimize results. Thermodynamic analysis and multi-objective optimization are carried on the sCO2BC system utilizing artificial neural network (ANN) and regression models. This approach enables performing optimization processes that are relatively simple, efficient, and accurate.

# Superiority and Potential Benefits of sCO2 cycles

Supercritical CO2 Brayton cycles, including comparisons of simple, recompression, and partial cooling are described and compared by Besarati et al. [5]. The concept of a bottoming cycle refers to a thermodynamic process in which waste heat from an existing power generation system is used. To utilize heat as effectively as possible, Organic Rankine Cycles (ORC) are included into each design. In some setups, Efficiency levels over 50% are attainable with the sCO2 Brayton cycle. When combined with an ORC, the recompression cycle has enhanced potential. Persichilli et al. [6] discovered that sCO2 technology can replace steam in gas turbines to produce more power, reduce installation, maintenance, and operating costs, and lower life cycle cost of ownership by 10–20%. According to Ehsan et al. [7], sCO2 technologies outperform heat recovery steam generators in industrial applications due to their higher energy density, smaller component size, higher efficiency, lower environmental impact, and ease of installation.



***Fig. 1.*** *Application of supercritical CO2 cycle.*

**Fig. 1** depicts solar thermal, geothermal, nuclear, fuel cell, waste heat recovery, and coal as heat sources for the application of supercritical CO2 cycles. Combining the advantages of steam Rankine cycles and gas turbines is possible with supercritical CO2 Brayton cycles. A greater turbine input temperature can be used without causing material issues because, compared to the steam Rankine cycle, the fluid is compressed in the incompressible region. Supercritical CO2, at the same temperature, which causes less corrosion comparing to steam, may increase turbine inlet temperature [8]. Because of the characteristics of the working fluid, sCO2BC have exceptional advantages over conventional thermodynamic systems [9]:

* Supercritical CO2 has a lower compression coefficient than working fluids such as air and water which indicates the system requires to carry out less compression energy.
* Systems heat exchangers and turbomachinery and are compact and ten times smaller than a standard power plant while producing an equal amount of power due to the increased density of sCO2 [10].
* The CO2 critical pressure (7.38 MPa) must be exceeded to avoid air intrusion. This simplifies power conversion. Low condenser pressure allows gas into the steam cycle, necessitating complex purification systems.
* Dry cooling could be used to cool the system, potentially saving water since the critical temperature of CO2 is near to the ambient temperature [11].
* Because of these advantages, sCO2 power systems are growing in popularity in a range of application scenarios like solar energy, waste heat utilization [12] & nuclear power plants [13,14].

# CSP Plant Integrated with sCO2

For a 25 MW CSP plant, Ehsan et al. [15] examined the operation and design of the dry cooling system. Reyes-Belmonte et al. [16] reported on a single-stage sCO2BC in recompression in central receiver CSP plants that has a great deal of potential because of its remarkable thermodynamic features. Solar field- using dense particle suspension (DPS) receivers are suitable for sCO2 power cycles from their high temperatures and stability. The power cycle efficiency ranges from 43% to 49% at turbine inlet temperatures between 630˚C and 680˚C, with a performance threshold of 75% fraction split ratio. Osorio et al. [17] simulated the fluctuating behavior of a central receiver CSP technique under various variations in the seasons and investigated the impacts of variables like intermediate pressures, mass flow rate, recuperator effectiveness, and number of compression-expansion phases on cycle efficiency. Process efficiency improved by 0.7% points across all four seasons, while average net power output increased by 12.6%, 14.3%, 16.2%, and 15.5% in the winter, spring, summer, and autumn, respectively.

# CSP Plant Equipped with Thermal Energy Storage

Thermal energy storage (TES) systems are essential for increasing energy efficiency and integrating renewable energy sources. CSP facilitates cost-effective dry cooling [18] and efficient TES through the conversion of solar energy into heat prior to generating electricity. Yu et al.[19] proposes universal TES models for thermal storage technologies using the aggregated parameter method. According to the findings, all three systems charging and discharging capabilities are comparable, and that the dynamic characteristics of steam discharge temperature vary with critical parameters. In contemporary cost- efficient configurations of CSP systems, a two-tank TES system and a steam accumulator are integrated. The exergetic efficiency of a system decreases when the discharge temperature falls below the system's charged state. To enhance the operational capabilities and reduce the limitations on outlet temperature for the straightforward implementation of TES utilizing enclosed phase change material (PCM). A hybrid thermal energy storage system design and operation is suggested by Ma et al. [20]. Its reduced unit cost and increased utility factor make it a preferable alternative for encapsulated PCM for a variety of outlet temperature constraints.

# Machine Learning Implementation on Power Cycle

Siddique et al. [21] analyzed five machine learning algorithms for Combined Cycle Power plant (CCPP) net power prediction using a six-year data set. The dataset evaluates output power based on input parameters such as temperature, humidity, and pressure. Gradient boosted Regression Tree performs better than all others, with 450 trees having the lowest RMSE and AE. Tufekci et al. [22] demonstrated a feasible model for predicting a base load operated power output. The CCPP is utilizing the Bagging technique with the REPTree predictor to predict the following day's hourly energy production. Wang et al.



[23] introduced a new Machine Learning-based method for predicting and optimizing ORC performance. BPNN and SVR models provided accurate predictions, proving research feasibility and effectiveness. SVR improves cycle operating parameter and reverse prediction. The approach has replaced the thermodynamic optimization, making it more rapid, precise, and efficient.

# Multi-Objective Performance Optimization

Besarati et al. [24] describes a multi-objective genetic algorithm (NSGA II) for Pareto approach optimization of cycle outputs in combined Brayton and inverse Brayton cycles. Saeed et al. [25] enhances the efficiency of a C-shaped PCHE by optimizing the channel design. Processing of dataset is done to train ML regression models, and a trained regression model is combined with a GA to determine the optimum set of design variables. For heat source conditions with variable temperature, Jin et al. [26] present an irreversible system and an ANN model for cycle performance optimization and assessment. Following the completion of the nonlinear ML model training and generalization, the systems and energy efficiencies are increased by changing the geometrical input variables. In science and engineering, it resolves multivariable problems. Similar to a chromosome in GA, each solution in particle swarm optimization (PSO) is represented by an avian. When it comes to analyzing cycle performance, Shannon Entropy is far superior; however, TOPSIS or LINMAP methods are more appropriate for making decisions.

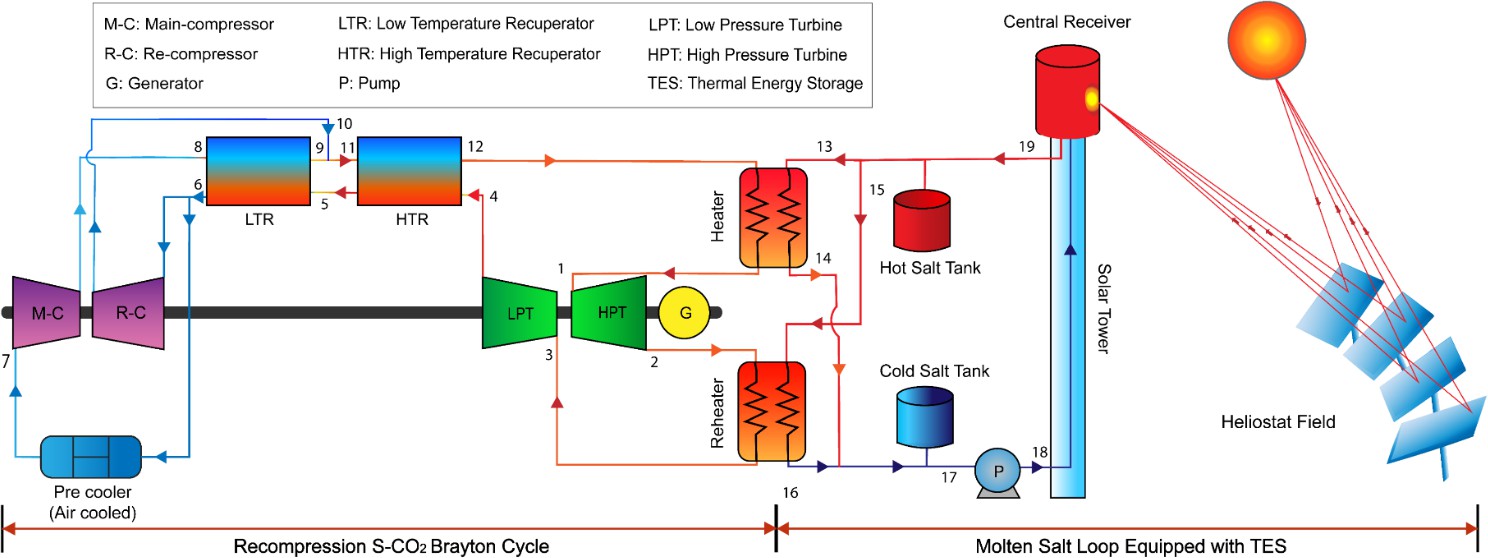
# Research Scope & Problem Statement

The key contribution of this study involves thorough examination of the optimal MCIT, TIT, and climate conditions for sCO2 Brayton cycles and optimization using advanced optimization framework to attain optimal thermal performance of the system. This analysis is conducted by employing machine learning algorithms and a creative approach to optimization using the Genetic Algorithm (GA) method. In addition to the comprehensive analysis and parametric optimization, this study also underscores the critical role of hyperparameter optimization for the machine learning algorithms, specifically the Artificial Neural Network (ANN), ensuring their optimal performance in modeling and optimization tasks. This study examines the optimization technique of sCO2BC, which incorporates concentrated solar power (CSP) and utilizes solar irradiance as the major source of heat. This study examines the impact of several factors on net power output, cycle thermal efficiency, and net energy utilization. The system design and performance are significantly influenced by climate conditions. Furthermore, an investigation has been performed for potential application of a Pre-compressor inside a recompression cycle, specifically in the context of partial cooling and main compression intercooling sCO2BC. This investigation also explores the inclusion of an additional cooler to enhance cooling at intermediate pressure, hence improving overall system performance. The scope of this work is outlined in the section below:

* Physical state reconstruction and thermodynamic characteristic prediction for three different sCO2 power cycles (recompression, partial cooling and main compression intercooling cycle) validate the framework.
* The MCIT design-point at different temperatures is determined depending on the year-round ambient temperature profile to develop systems for distinct situations. Based on optimal MCIT conditions, the temperature of the hot & cold tank, and heliostat field design of TES are evaluated.
* The contribution of TES at night and its resulting patterns in power generation are shown for each season (summer, winter, autumn, and spring).
* To facilitate the DNI variation calculation, GA was used to optimize the variables to acquire the optimal design of the overall system & customized algorithmic strategies are created to reduce model complexity and accelerate model convergence.
* Extensive analysis and parametric optimization are performed to determine the effects of solar irradiance on the efficiency of the system.

# System Description

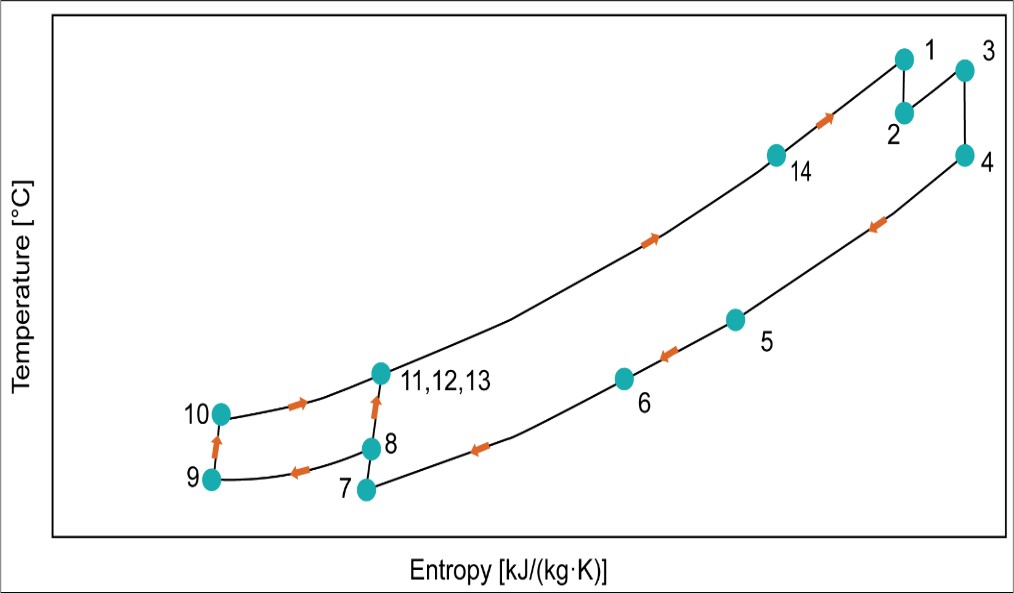
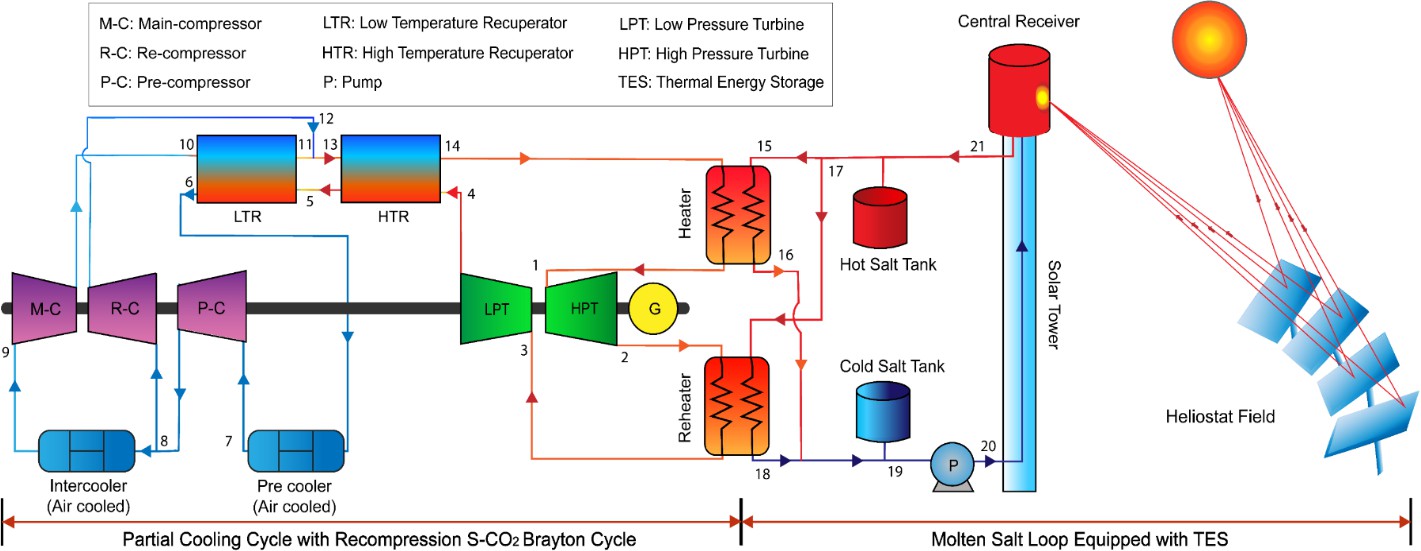
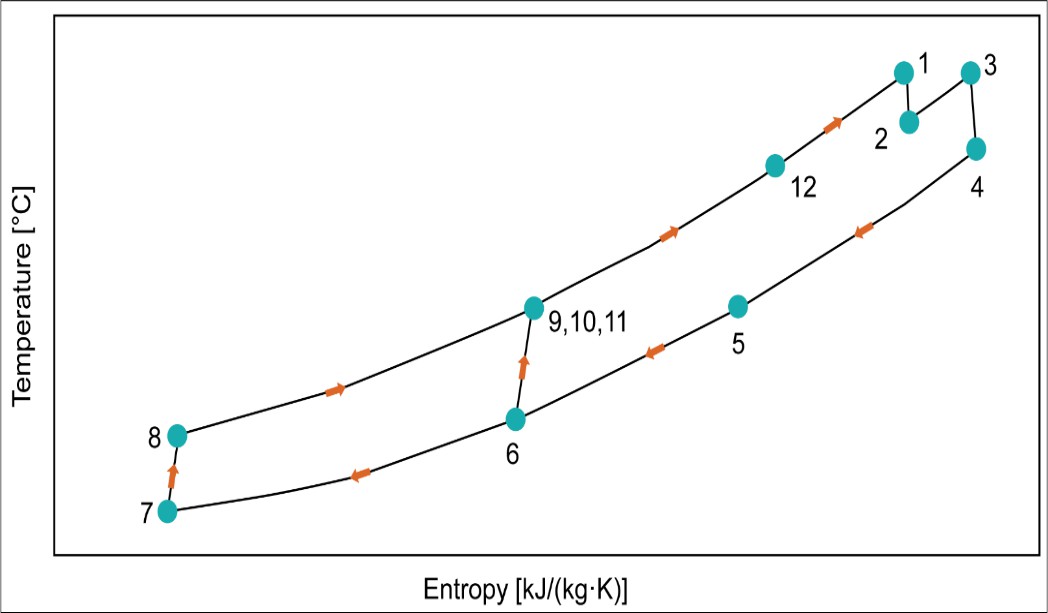
**Fig. 2** depicts a schematic diagram of Recompression sCO2BC equipped with molten salt loop, which is considered as the base of this study. The Simple Brayton recuperation cycle has a pinch point issue, which reduces cycle efficiency, since the hot and cold fluid streams have different heat capacities. To solve this



problem, the recompression cycle also includes LTR and the recompression compressor [27]. The recompression compressors receive a fraction of total mass flow rate of sCO2 [28]. The recompression cycle lowers mass flow through the stream at high pressure. Consequently, the low-pressure stream is split after the low-temperature recuperator and compressed in the precooler and main compressor. **Fig. 3** shows the *T-s* diagram of Recompression sCO2 cycle.

***Fig. 2.*** *Schematic diagram of Recompression sCO2 cycle equipped with TES.*

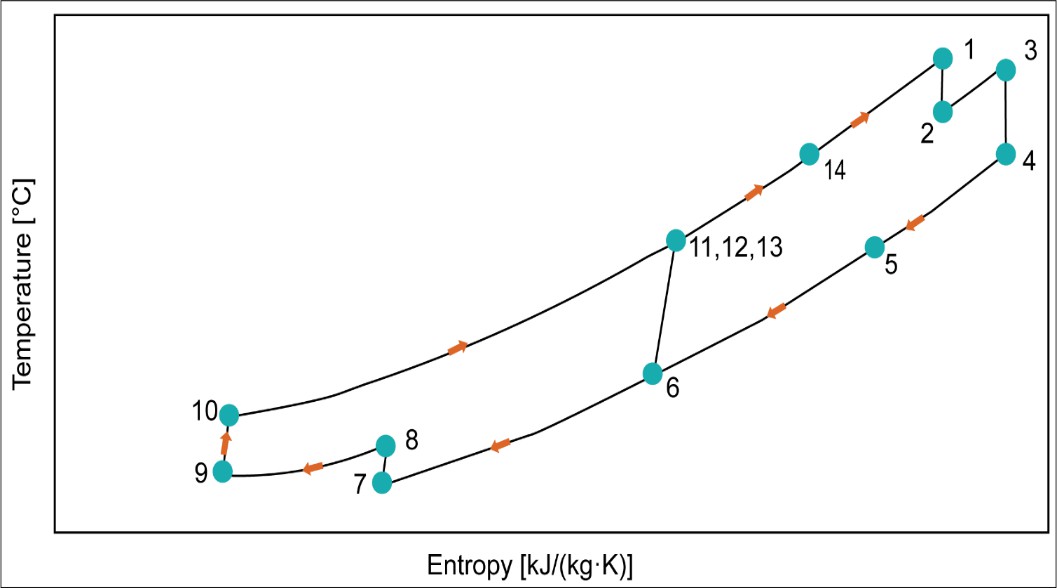
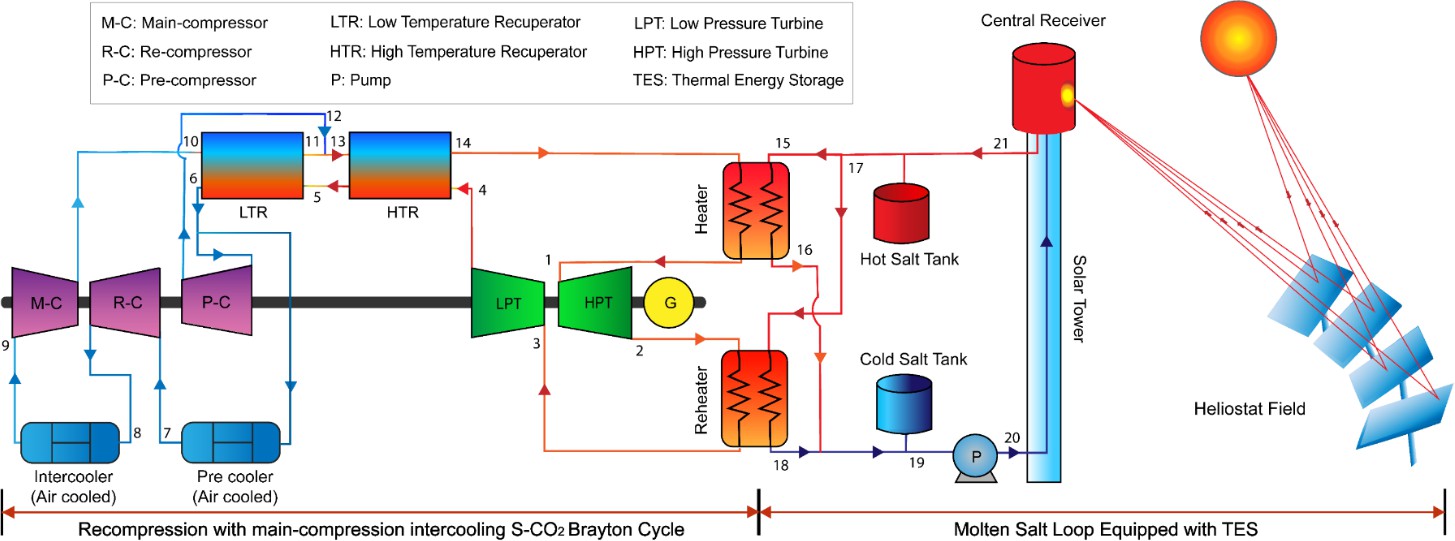
***Fig. 3.*** *T-s diagram of Recompression sCO2 cycle.*



***Fig. 4.*** *Schematic diagram of Partial cooling sCO2 cycle equipped with TES.*

***Fig. 5.*** *T-s diagram of Partial cooling sCO2 cycle.*

***Fig. 6.*** *Schematic diagram of Main-compression intercooling sCO2 cycle equipped with TES.*



***Fig. 7.*** *T-s diagram of Main-compression intercooling sCO2 cycle.*

**Fig. 4** represents a modified recompression cycle by adding an extra compressor and an intercooler known as the partial cooling layout. The sCO2 Simple Brayton cycle's efficiency can also be increased by partial cooling. The partial cooling cycle is analogous to the intercooling cycle in terms of the parts of the turbomachinery and the number of heat exchangers. A low-temperature recuperator's working fluid stream flows mostly in the precooler's direction during partial cooling [29]. The stream is split in a single possible intercooling recompression configuration following the pre-compressor [30]. Before it enters the pre-compressor, a precooler is used to cool the turbine exhaust flow. Thus, the pre-compressor's input pressure is intermediate, and the re-compressor contributes to the turbine pressure ratio [27]. **Fig. 5** shows the *T-s* diagram of partial cooling sCO2 cycle.

***Table 1:*** *Description of the sCO2 Brayton cycles.*

Cycle

Compressor intercooling

Recuperators/ Turbines

Cooler

Compressor

Key Features

Recompression

sCO2BC (REC)

No HTR & LTR

HPT & LPT

Precooler

(Air-cooled)

Main Compressor,

Re-compressor

* Modified Simple Brayton cycle. An
* An additional compressor is used.
* Splitting the LTR's hot steam

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
|  | | | | | reduces the cold stream's heat  capacity. |
| Partial Cooling sCO2BC  (PAR) | Yes | HTR & LTR HPT & LPT | Precooler (Air-cooled),  Intercooler | Main Compressor, Re-compressor, and  Pre-compressor | * Modified REC sCO2 Brayton cycle. * Pree-compressor is utilized in this configuration. |
|  |  |  | (Air-cooled) |  | * Splitting the stream exiting the |
|  |  |  |  |  | main compressor reduces the cold |
|  |  |  |  |  | stream's heat capacity. |
|  |  |  |  |  | * To minimize compressor input |
|  |  |  |  |  | power, an intercooling phase is |
|  |  |  |  |  | added to the split fraction sent to |
|  |  |  |  |  | the LTR. |
| Main  Compression | Yes | HTR & LTR  HPT & LPT | Precooler  (Air-cooled), | Main Compressor,  Re-compressor, and | * A modified PAR sCO2 Brayton   cycle. |
| Intercooling |  |  | Intercooler | Pre-compressor | * After the MC is introduced, an |
| sCO2BC  (INT) |  |  | (Air-cooled) |  | intercooling step is added to lower  the power input to the compressors. |

In **Fig. 6**, the schematic diagram of Main-compression intercooling sCO2 cycle is presented. In main- compression intercooling cycle, two intercooling stages are separated from the primary compressor. The main compressor gets working fluid at high pressure and temperature. Before entering the main compressor, the stream from the precooler flows via an intercooling stage and a low-pressure compressor. Since the compressor input temperature significantly affects system performance, cooling system design is crucial [31]. In this configuration, the re-compressor operates over the entire pressure ratio since the inlet pressure is at the turbine outlet pressure [27]. What unites them is the idea that both the intercooling cycle and the recompression cycle involve multistage compression with intercooling [32]. **Fig. 7** shows the *T-s* diagram of Main Compression Intercooling sCO2 cycle.

All heat exchangers and devices (compressors and turbines) are mass, energy, and exergy balanced for the thermodynamic study of the sCO2BC designs. An effectiveness factor for the whole hot stream was taken into account for setups with the LTR, and the HTR is simulated through presuming the effectiveness of a heat exchanger [5]. In sCO2BC with LTR, split ratio is the ratio of the sCO2's total mass flow rate to the cold stream's mass flow rate. Split ratio is calculated from the LTR's energy balance, which is used to compute thermal performance and compression power. **Table 1** demonstrates the key features of three sCO2BC layouts.

# Research Methodology

* 1. **Assumptions**

The first and second laws of thermodynamics are applied to the different devices under analysis to create a mathematical model of the 3 layouts of sCO2 Brayton cycles. Python programming is used to execute the simulation. The primary presumptions made in order to streamline the simulation of the system are as follows:

* The steady-state condition is considered to be attained by all three cycles.
* Except for the solar field components, there are negligible heat losses from the cycle components to the ambient air.
* A 360° external cylinder receiver is used to collect more of the light that is reflected from the edge of the solar field.
* All heat recuperators and pipelines ignore pressure drops and friction losses.
* The system's kinetic and potential energy hardly change over time.
* Solar salt split ratio to thermal energy storage is considered 0.5 for molten salt loop.
* For the two primary compression stages, it is assumed that the input temperatures are the same.

# Energy Analysis

In this article, recompression, partial cooling & main-compression intercooling sCO2BC configurations coupled with CSP loop are utilized in order to examine the performance under off-design conditions. When analyzing all of the components, both energy and mass conservation principles from the first law of thermodynamics was utilized. Ratio of pressure ratios, net work output & cycle thermal efficiency can be calculated using Equations (1)-(3).

 𝑃ℎ𝑖𝑔ℎ −1

Ratio of pressure ratios[27] , 𝑅𝑃𝑅 = 𝑃𝑖𝑛𝑡𝑒𝑟𝑚𝑒𝑑𝑖𝑎𝑡𝑒

𝑃ℎ𝑖𝑔ℎ−1

𝑃𝑙𝑜𝑤

*(1)*

Net work output, 𝑊̇ 𝑛𝑒𝑡 = 𝑊̇ 𝑇 − 𝑊̇ 𝑃 *(2)*

Thermal efficiency of the cycle, 𝑛

𝑐𝑦𝑐

= 𝑊̇ 𝑛𝑒𝑡

𝑄𝐻

*(3)*

The energy equation of each component for 3 layouts of sCO2 cycles are presented in **Table 2, Table 3,**

and **Table 4.**

***Table 2:*** *Components-wise energy equation of recompression cycle.*

Component Equation

Compressor isentropic efficiency 𝑛𝐶

ℎ8,𝑠 − ℎ7

=

ℎ8 − ℎ7

ℎ1 − ℎ2

Turbine isentropic efficiency 𝑛𝑇 =

ℎ

1

− ℎ2,𝑠

Work input to the compressor 𝑊̇ 𝐶 = 𝑚̇ 𝐶𝑂2 (ℎ8 – ℎ7) Work output from the turbine 𝑊̇ 𝑇 = 𝑚̇ 𝐶𝑂2 (ℎ4 – ℎ5) Heat input by the heater 𝑄𝐻 = 𝑚̇ 𝐶𝑂2 (ℎ1 – ℎ12)

Recuperator effectiveness 𝜀𝑅

𝑚̇ 𝐶𝑂2(ℎ4 − ℎ5)

=

𝑄 𝑚𝑎𝑥

𝑚̇ 9

Split ratio 𝑆𝑅 =

𝑚̇ 9 + 𝑚̇ 10

***Table 3:*** *Components-wise energy equation of partial cooling cycle.*

Component Equation

Main Compressor isentropic efficiency 𝑛𝐶

ℎ10,𝑠 − ℎ9

=

ℎ10 − ℎ9

ℎ1 − ℎ2

Turbine isentropic efficiency 𝑛𝑇 =

ℎ

1

− ℎ2,𝑠

Work input to the compressor 𝑊̇ 𝐶 = 𝑚̇ 𝐶𝑂2 (ℎ10 – ℎ9) Work output from the turbine 𝑊̇ 𝑇 = 𝑚̇ 𝐶𝑂2 (ℎ4 – ℎ5) Heat input by the heater 𝑄𝐻 = 𝑚̇ 𝐶𝑂2 (ℎ1 – ℎ14)

Recuperator effectiveness 𝜀𝑅

𝑚̇ 𝐶𝑂2(ℎ4 − ℎ5)

=

𝑄 𝑚𝑎𝑥

Split ratio 𝑆𝑅 = 𝑚̇ 11

𝑚̇ 11 + 𝑚̇ 12

***Table 4:*** *Components-wise energy equation of main compression intercooling cycle.*

Component Equation

Main Compressor isentropic efficiency 𝑛𝐶

ℎ10,𝑠 − ℎ9

=

ℎ10 − ℎ9

ℎ1 − ℎ2

Turbine isentropic efficiency 𝑛𝑇 =

ℎ

1

− ℎ2,𝑠

Work input to the compressor 𝑊̇ 𝐶 = 𝑚̇ 𝐶𝑂2 (ℎ10 – ℎ9) Work output from the turbine 𝑊̇ 𝑇 = 𝑚̇ 𝐶𝑂2 (ℎ4 – ℎ5) Heat input by the heater 𝑄𝐻 = 𝑚̇ 𝐶𝑂2 (ℎ1 – ℎ14)

Recuperator effectiveness 𝜀𝑅

𝑚̇ 𝐶𝑂2(ℎ4 − ℎ5)

=

𝑄 𝑚𝑎𝑥

Split ratio 𝑆𝑅 = 𝑚̇ 11

𝑚̇ 11 + 𝑚̇ 12

***Table 5:*** *CSP field and TES equations.*

Parameter Equation

Heliostat field efficiency [33] 𝑠&𝑏 ∙ 𝜂𝑖𝑛𝑡 ∙ 𝜂𝑎𝑡𝑡 ∙ 𝜂𝑟𝑒𝑓

Solar receiver heat input [33] 𝑄̇𝑟𝑒𝑐,𝑖𝑛 = 𝜂𝑐𝑜𝑠 ∙ 𝑄̇𝑠𝑢𝑛 = 𝜂𝑓𝑖𝑒𝑙𝑑 ∙ (𝐷𝑁𝐼) ∙ 𝐴ℎ𝑒𝑙 ∙ 𝑁ℎ𝑒𝑙

Solar receiver efficiency [33] 𝜂

𝑟𝑒𝑐

𝑄̇𝑟𝑒𝑐,𝑛𝑒𝑡

= 𝑄̇

𝑟𝑒𝑐,𝑖𝑛

Heliostat field efficiency [33] 𝜂𝑐𝑜𝑠 ∙ 𝜂𝑠&𝑏 ∙ 𝜂𝑖𝑛𝑡 ∙ 𝜂𝑎𝑡𝑡 ∙ 𝜂𝑟𝑒𝑓

𝐸stored

TES capacity ratio [34] 𝜎 =

𝐸𝑚𝑎𝑥, stored

Maximum theoretical storage capacity [34] 𝐸max , stored = 𝑚𝑝𝑐𝑚𝑐𝑝,𝑠(𝑇ain − 𝑇𝑏𝑖𝑛) + 𝑚𝑝𝑐𝑚𝐿

# Exergy Analysis

Exergy may be defined as an energy stream's maximum work potential when compared to its surroundings. The exergy balance equation in a steady-state controlled volume system is presented as:

𝑋̇

𝑑𝑒𝑠𝑡,𝑖

= ∑(𝑚˙

𝑖𝑛

× 𝑥𝑖𝑛

) − ∑(𝑚˙

𝑜𝑢𝑡

× 𝑥𝑜𝑢𝑡

) + ∑𝑄˙ × (1 − 𝑇0)

𝑇 in

− ∑𝑄˙ × (1 − 𝑇0)

𝑇 𝑜𝑢𝑡

+ ∑𝑊˙ *(04)*

Where the term ‘*x*’ refers to the exergy of an energy stream in a controlled volume steady-state system, which is defined as:

𝑥𝑖 = ℎ𝑖 − ℎ𝑜 − 𝑇𝑜 × (𝑠𝑖 − 𝑠𝑜) (*05*)

The ratio of energy yield to energy input is used to determine the second law of efficiency. The exergetic efficiency of the entire cycle can be determined by:

𝑛𝑒𝑥𝑒𝑟𝑔𝑦

= (1 − 𝑋𝑑𝑒𝑠𝑡 ) *(06)*

𝑋𝑖𝑛

Components-wise exergy destruction equation of each component for 3 layouts of sCO2 cycles are demonstrated in **Table 6, Table 7,** and **Table 8**.

***Table 6:*** *Components-wise exergy destruction equation of recompression cycle.*

Component

Equation

Heater 𝑋 = 𝑚̇ [(ℎ – ℎ ) − 𝑇

(𝑠 – 𝑠 )] + 𝑚̇

𝑇

[1 − ( )] 𝑄

0 ̇

𝐻 𝐶𝑂2 12 1

0 12 1

𝐶𝑂2

𝑇𝐻 𝐻

Reheater 𝑋

= 𝑚̇

[(ℎ – ℎ ) − 𝑇

(𝑠 – 𝑠 )] + 𝑚̇

𝑇

[1 − ( )] 𝑄

0 ̇

𝑅𝐻

𝐶𝑂2 2 3

0 2 3

𝐶𝑂2

𝑇𝑅𝐻

𝑅𝐻

HTR 𝑋𝐻𝑇𝑅 = 𝑚̇ 𝐶𝑂2 [(ℎ4 – ℎ5) − 𝑇0 (𝑠4– 𝑠5)] + 𝑚̇ 𝐶𝑂2 [(ℎ10 – ℎ12) −𝑇0 (𝑠10– 𝑠12)]

LTR 𝑋𝐿𝑇𝑅 = 𝑚̇ 𝐶𝑂2 [(ℎ5 – ℎ6) − 𝑇0 (𝑠5– 𝑠6)] + 𝑚̇ 𝐶𝑂2 (1 − 𝑆𝑅)[(ℎ8 – ℎ10) −𝑇0 (𝑠8– 𝑠10)]

Main compressor 𝑋𝑀𝐶 = 𝑆𝑅. 𝑚̇ 𝐶𝑂2 [(ℎ7 – ℎ8) − 𝑇0 (𝑠7– 𝑠8)] + 𝑊𝑀𝐶

Re-compressor 𝑋𝑅𝐶 = (1– 𝑆𝑅). 𝑚̇ 𝐶𝑂2 [(ℎ6 – ℎ10) − 𝑇0 (𝑠6– 𝑠10)] + 𝑊𝑅𝐶

HPT 𝑋𝐻𝑃𝑇 = 𝑚̇ 𝐶𝑂2 [(ℎ1 – ℎ2) − 𝑇0 (𝑠1– 𝑠2)] − 𝑊𝐻𝑃𝑇

LPT 𝑋𝐿𝑃𝑇 = 𝑚̇ 𝐶𝑂2 [(ℎ3 – ℎ4) − 𝑇0 (𝑠3– 𝑠4)] − 𝑊𝐿𝑃𝑇

Pre-cooler 𝑋𝑃𝐶𝐿 = 𝑆𝑅. 𝑚̇ 𝐶𝑂2 [(ℎ6 – ℎ7) − 𝑇0 (𝑠6– 𝑠7)]

Exergy input 𝑋𝑖𝑛

= 𝑚̇

𝐶𝑂2

𝑇

[1 − ( )] 𝑄𝐻

0 ̇

𝑇1

+ 𝑚̇

𝐶𝑂2

𝑇

[1 − ( )] 𝑄

0 ̇

𝑇3

𝑅𝐻

Total Exergy

destruction 𝑋𝑑𝑒𝑠𝑡 = 𝑋𝐻 + 𝑋𝑅𝐻 + 𝑋𝐻𝑇𝑅 + 𝑋𝐿𝑇𝑅 + 𝑋𝑀𝐶 + 𝑋𝑅𝐶 + 𝑋𝐻𝑃𝑇 + 𝑋𝐿𝑃𝑇 + 𝑋𝑃𝐶𝐿

***Table 7:*** *Components-wise exergy destruction equation of partial cooling cycle.*

Component Equation

Heater 𝑋 = 𝑚̇ [(ℎ – ℎ ) − 𝑇

(𝑠 – 𝑠 )] + 𝑚̇

𝑇

[1 − ( )] 𝑄

0 ̇

𝐻 𝐶𝑂2 14 1

0 14 1

𝐶𝑂2

𝑇𝐻 𝐻

Reheater 𝑋

= 𝑚̇

[(ℎ – ℎ ) − 𝑇

(𝑠 – 𝑠 )] + 𝑚̇

𝑇

[1 − ( )] 𝑄

0 ̇

𝑅𝐻

𝐶𝑂2 2 3

0 2 3

𝐶𝑂2

𝑇𝑅𝐻

𝑅𝐻

HTR 𝑋𝐻𝑇𝑅 = 𝑚̇ 𝐶𝑂2 [(ℎ4 – ℎ5) − 𝑇0 (𝑠4– 𝑠5)] + 𝑚̇ 𝐶𝑂2 [(ℎ12 – ℎ14) −𝑇0 (𝑠12– 𝑠14)]

LTR 𝑋𝐿𝑇𝑅 = 𝑚̇ 𝐶𝑂2 [(ℎ5 – ℎ6) − 𝑇0 (𝑠5– 𝑠6)] + 𝑚̇ 𝐶𝑂2 (1 − 𝑆𝑅)[(ℎ10 – ℎ12) −𝑇0 (𝑠10– 𝑠12)]

Main compressor 𝑋𝑀𝐶 = 𝑆𝑅. 𝑚̇ 𝐶𝑂2 [(ℎ9 – ℎ10) − 𝑇0 (𝑠9– 𝑠10)] + 𝑊𝑀𝐶

Re-compressor 𝑋𝑅𝐶 = (1– 𝑆𝑅). 𝑚̇ 𝐶𝑂2 [(ℎ8 – ℎ12) − 𝑇0 (𝑠8– 𝑠12)] + 𝑊𝑅𝐶

Pre-compressor 𝑋𝑃𝐶 = 𝑚̇ 𝐶𝑂2 [(ℎ7 – ℎ8) − 𝑇0 (𝑠7– 𝑠8)] + 𝑊𝑃𝐶 HPT 𝑋𝐻𝑃𝑇 = 𝑚̇ 𝐶𝑂2 [(ℎ1 – ℎ2) − 𝑇0 (𝑠1– 𝑠2)] − 𝑊𝐻𝑃𝑇 LPT 𝑋𝐿𝑃𝑇 = 𝑚̇ 𝐶𝑂2 [(ℎ3 – ℎ4) − 𝑇0 (𝑠3– 𝑠4)] − 𝑊𝐿𝑃𝑇

Pre-cooler 𝑋𝑃𝐶𝐿 = 𝑚̇ 𝐶𝑂2 [(ℎ6 – ℎ7) − 𝑇0 (𝑠6– 𝑠7)]

Intercooler 𝑋𝐼𝐶𝐿 = 𝑆𝑅. 𝑚̇ 𝐶𝑂2 [(ℎ8 – ℎ9) − 𝑇0 (𝑠8– 𝑠9)]

Exergy input 𝑋𝑖𝑛

= 𝑚̇

𝐶𝑂2

𝑇

[1 − ( )] 𝑄𝐻

0 ̇

𝑇1

+ 𝑚̇

𝐶𝑂2

𝑇

[1 − ( )] 𝑄

0 ̇

𝑇3

𝑅𝐻

Total Exergy

destruction 𝑋𝑑𝑒𝑠𝑡 = 𝑋𝐻 + 𝑋𝑅𝐻 + 𝑋𝐻𝑇𝑅 + 𝑋𝐿𝑇𝑅 + 𝑋𝑀𝐶 + 𝑋𝑅𝐶 + 𝑋𝑃𝐶 + 𝑋𝐻𝑃𝑇 + 𝑋𝐿𝑃𝑇 + 𝑋𝑃𝐶𝐿 + 𝑋𝐼𝐶𝐿

***Table 8:*** *Components-wise exergy destruction equation of main compression intercooling cycle.*

Component

Equation

Heater 𝑋 = 𝑚̇ [(ℎ – ℎ ) − 𝑇

(𝑠 – 𝑠 )] + 𝑚̇

𝑇

[1 − ( )] 𝑄

0 ̇

𝐻 𝐶𝑂2 14 1

0 14 1

𝐶𝑂2

𝑇𝐻 𝐻

Reheater 𝑋

= 𝑚̇

[(ℎ – ℎ ) − 𝑇

(𝑠 – 𝑠 )] + 𝑚̇

𝑇

[1 − ( )] 𝑄

0 ̇

𝑅𝐻

𝐶𝑂2 2 3

0 2 3

𝐶𝑂2

𝑇𝑅𝐻

𝑅𝐻

HTR 𝑋𝐻𝑇𝑅 = 𝑚̇ 𝐶𝑂2 [(ℎ4 – ℎ5) − 𝑇0 (𝑠4– 𝑠5)] + 𝑚̇ 𝐶𝑂2 [(ℎ12 – ℎ14) −𝑇0 (𝑠12– 𝑠14)]

LTR 𝑋𝐿𝑇𝑅 = 𝑚̇ 𝐶𝑂2 [(ℎ5 – ℎ6) − 𝑇0 (𝑠5– 𝑠6)] + 𝑚̇ 𝐶𝑂2 (1 − 𝑆𝑅)[(ℎ10 – ℎ12) −𝑇0 (𝑠10– 𝑠12)]

Main compressor 𝑋𝑀𝐶 = 𝑆𝑅. 𝑚̇ 𝐶𝑂2 [(ℎ9 – ℎ10) − 𝑇0 (𝑠9– 𝑠10)] + 𝑊𝑀𝐶

Re-compressor 𝑋𝑅𝐶 = (1– 𝑆𝑅). 𝑚̇ 𝐶𝑂2 [(ℎ6 – ℎ12) − 𝑇0 (𝑠6– 𝑠12)] + 𝑊𝑅𝐶

Pre-compressor 𝑋𝑃𝐶 = 𝑚̇ 𝐶𝑂2 [(ℎ7 – ℎ8) − 𝑇0 (𝑠7– 𝑠8)] + 𝑊𝑃𝐶 HPT 𝑋𝐻𝑃𝑇 = 𝑚̇ 𝐶𝑂2 [(ℎ1 – ℎ2) − 𝑇0 (𝑠1– 𝑠2)] − 𝑊𝐻𝑃𝑇 LPT 𝑋𝐿𝑃𝑇 = 𝑚̇ 𝐶𝑂2 [(ℎ3 – ℎ4) − 𝑇0 (𝑠3– 𝑠4)] − 𝑊𝐿𝑃𝑇

Pre-cooler 𝑋𝑃𝐶𝐿 = 𝑆𝑅. 𝑚̇ 𝐶𝑂2 [(ℎ6 – ℎ7) − 𝑇0 (𝑠6– 𝑠7)]

Intercooler 𝑋𝐼𝐶𝐿 = 𝑆𝑅. 𝑚̇ 𝐶𝑂2 [(ℎ8 – ℎ9) − 𝑇0 (𝑠8– 𝑠9)]

Exergy input 𝑋𝑖𝑛

= 𝑚̇

𝐶𝑂2

𝑇

[1 − ( )] 𝑄𝐻

0 ̇

𝑇1

+ 𝑚̇

𝐶𝑂2

𝑇

[1 − ( )] 𝑄

0 ̇

𝑇3

𝑅𝐻

Total Exergy

destruction 𝑋𝑑𝑒𝑠𝑡 = 𝑋𝐻 + 𝑋𝑅𝐻 + 𝑋𝐻𝑇𝑅 + 𝑋𝐿𝑇𝑅 + 𝑋𝑀𝐶 + 𝑋𝑅𝐶 + 𝑋𝑃𝐶 + 𝑋𝐻𝑃𝑇 + 𝑋𝐿𝑃𝑇 + 𝑋𝑃𝐶𝐿 + 𝑋𝐼𝐶𝐿

# Framework of the Mathematical Model

A simulation model is executed in the Python programming language using the equations for energy balance and exergy destruction. The integrated CoolProp library is used for obtaining sCO2's properties. **Table 9** and **Table 10** shows the operational parameters that are taken into consideration for cycle simulation. The controllable variable ranges are selected from published literatures [35,36] that investigated the parametric impacts of variables on various configurations of the sCO2 Brayton cycle.

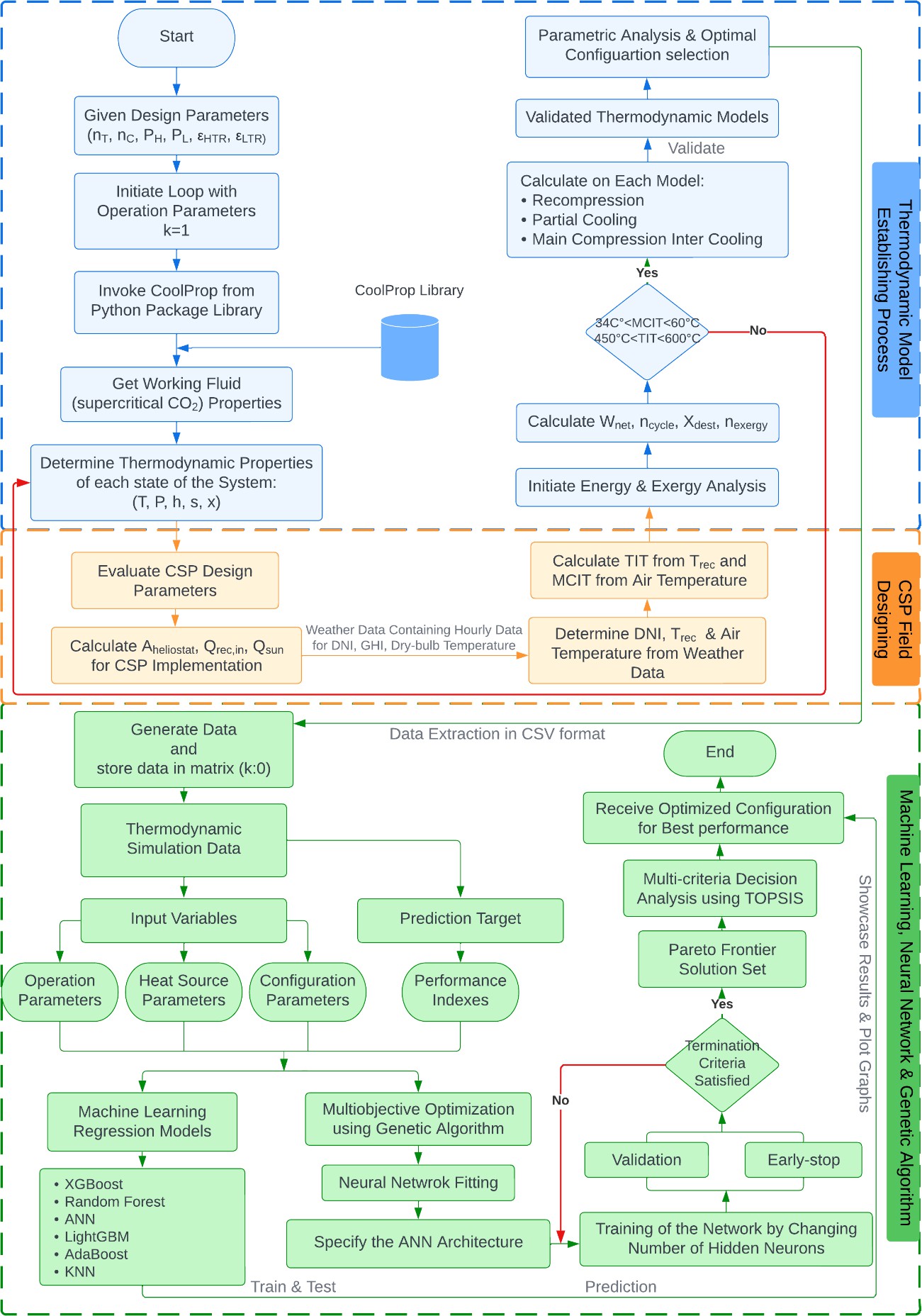
**Fig. 8** depicts the simulation model's stages. In order to provide a thorough understanding of the effects of each controllable variable, graphs are generated by changing one controllable variable within the acceptable range while keeping the others constant. Weather data is utilized to analyze cycle performance on different seasons throughout a year. Multiple machine learning model performance have been compared to find best-fit model for this study. Additionally, using a genetic algorithm, multi-objective optimization has been performed to provide an ideal set of data for optimal cycle performance. The results of this research are graphically assessed in the following sections.

***Table 9:*** *Initial parameters for simulation and analysis of system performance.*

|  |  |  |
| --- | --- | --- |
| Parameters | Values | Unit |
| Maximum pressure, *Pmax* | 25 | *MPa* |
| Minimum pressure, *Pmin* | 8 | *MPa* |
| Turbine inlet temperature, *TIT* | 600 | *°C* |
| Main compressor inlet temperature, *MCIT* | 34 | *°C* |
| Pinch temperature, *Tpinch* | 7 | *°C* |
| Mass flow rate of the sCO2 cycle, ṁCO2 | 1 | *kg/s* |
| Effectiveness of HTR | 0.97 | *-* |
| Effectiveness of LTR | 0.88 | *-* |
| Compressor isentropic efficiency, *ηC* | 0.89 | *-* |
| Turbine isentropic efficiency, *ηt* | 0.90 | *-* |

***Table 10:*** *CSP loop Design Parameters.*

|  |  |  |  |
| --- | --- | --- | --- |
| Parameters | Symbol | Values | Unit |
| Direct normal irradiance | *DNI* | 0.6 | kW/m2 |
| Cosine effect efficiency | *ηcos* | 0.8267 | - |
| Shading and blocking efficiency | *ηs&b* | 0.9698 | - |
| Interception efficiency | *ηint* | 0.971 | - |
| Atmospheric attenuation efficiency | *ηatt* | 0.9383 | - |
| Reflectivity efficiency of heliostat | *ηref* | 0.88 | - |
| Number of heliostats | *Nhel* | 624 | - |
| Reflective area of each heliostat | *Ahel* | 9.45 × 12.84 m2 | |
| Receiver aperture area | *Arec* | 68.1 m2 | |



***Fig. 8.*** *Flow chart demonstrating cycle modelling, data extraction & performance optimization for sCO2BC.*

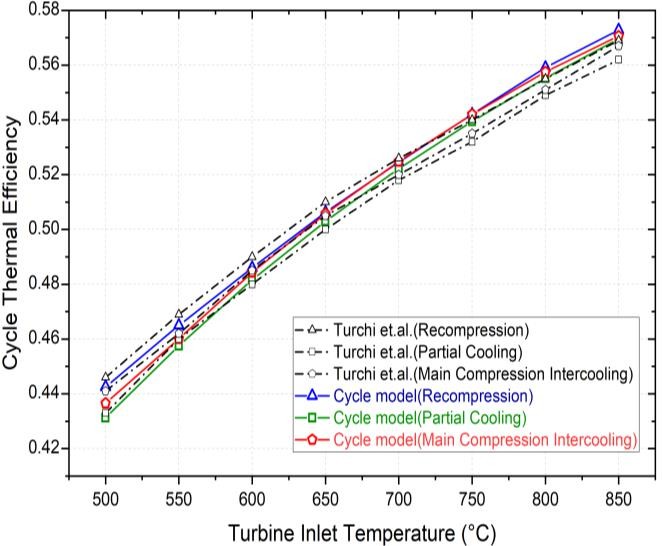
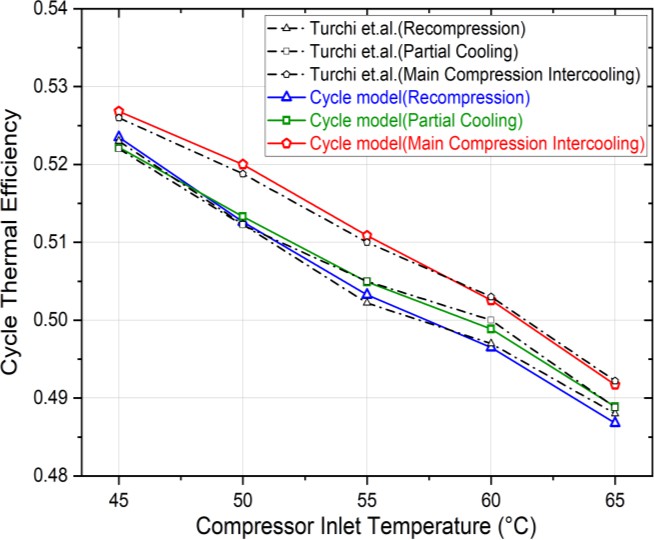
# Boundary Conditions

CoolProp library is utilized to determine the working fluid's thermal characteristics and each cycle's thermodynamic performance. The base model's initial conditions are illustrated in **Table 9** and **Table 10**. The results of this research are graphically assessed in the next section.

# Model Validation

Earlier research from the literature has been used to verify the layout of recompression, partial cooling and main compression intercooling sCO2 cycles. **Fig. 9** compares the cycle thermal efficiency obtained by the current model and from the previous data [27] for the variation of MCIT (45°C– 65°C) & TIT (500°C- 850°C). The figure exhibits very strong model agreement. Fig. 8 illustrates the entire model development process. **Table 11** demonstrates the boundary conditions at which the validation is performed.

***Table 11:*** *Cycle model validation boundary conditions.*



|  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- |
| Cycles | Turbine efficiency | Compressor efficiency | HTR  effectiveness | LTR  effectiveness | Pinch temperature | Maximum pressure | RPR | Pressure ratio |
| Recompression | 93% | 89% | 97% | 88% | 5 K | 25 MPa | - | 2.7 |
| Partial cooling | 93% | 89% | 97% | 88% | 5 K | 25 MPa | 0.97 | 5.0 |
| Main compression  intercooling | 93% | 89% | 97% | 90% | 5 K | 25 MPa | 0.60 | 3.6 |

***Fig. 9.*** *Cycle model validation for MCIT & TIT variation.*

# Results and Discussion

* 1. **Thermodynamic Analysis**

To illustrate the thermodynamic state attributes of recompression sCO2BC, **Table 12** is developed provided the cited configurations in **Table 9**. In addition, thermodynamic state properties for partial cooling & main-compression intercooling sCO2BC are displayed in **Table 13** and **Table 14**, respectively.

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| ***Table 12:*** *Recompression sCO2 cycle pressure, temperature, enthalpy & entropy for each state point.* | | | | |
| State (i) | T (°C) | P (MPa) | h (kJ/kg) | s (kJ/kg·K) |
| 1 | 600 | 25 | 1094.689 | 2.767 |
| 2 | 546.108 | 16.5 | 1032.902 | 2.775 |
| 3 | 600 | 16.5 | 1099.484 | 2.854 |
| 4 | 509.777 | 8 | 996.47 | 2.869 |
| 5 | 200.327 | 8 | 640.034 | 2.291 |
| 6 | 82.934 | 8 | 495.911 | 1.939 |
| 7 | 34 | 8 | 320.691 | 1.391 |
| 8 | 75.834 | 25 | 350.18 | 1.401 |
| 9 | 192.324 | 25 | 572.98 | 1.957 |
| 10 | 192.327 | 25 | 572.98 | 1.957 |
| 11 | 192.327 | 25 | 572.98 | 1.957 |
| 12 | 468.0952 | 25 | 929.416 | 2.562 |
| ***Table 13:*** *Partial cooling sCO2 cycle pressure, temperature, enthalpy & entropy for each state point.* | | | | |

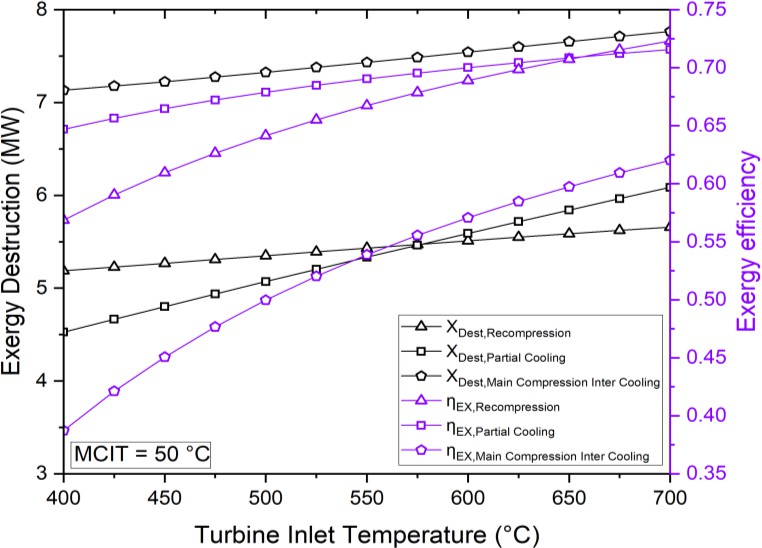
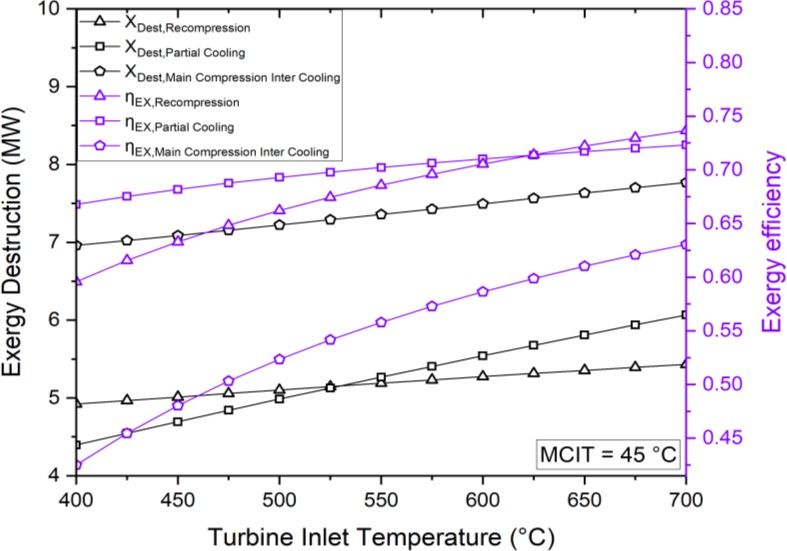
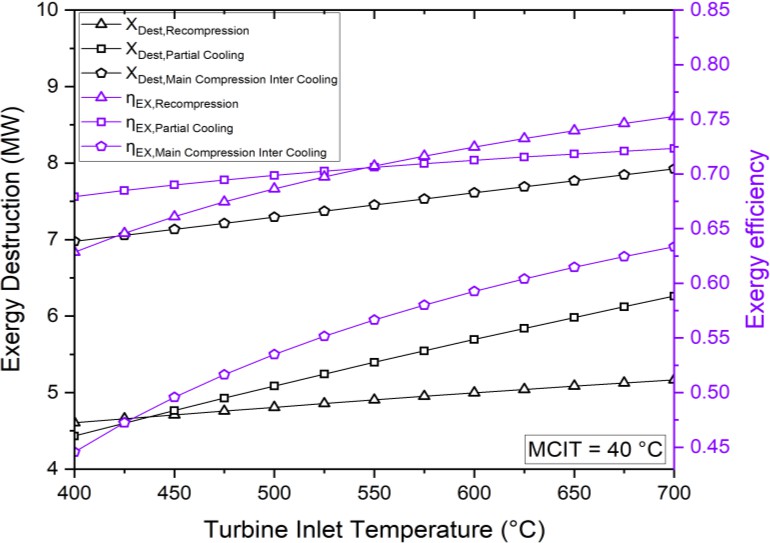
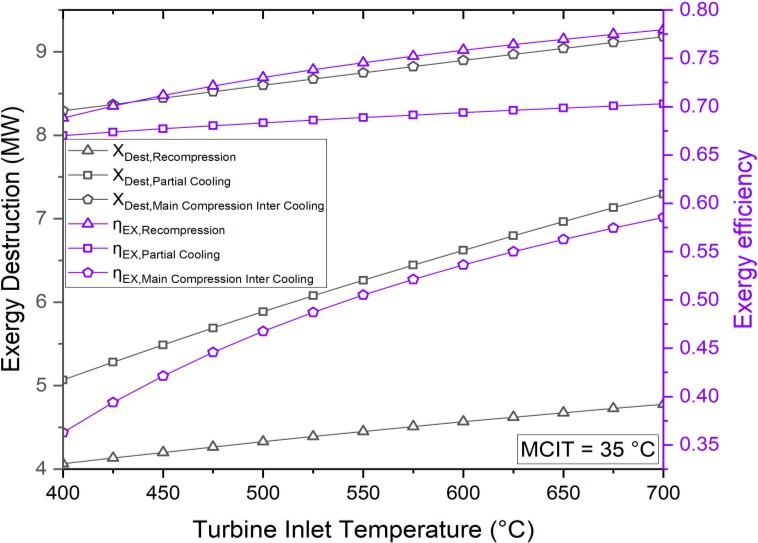
|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| State (i) | T (°C) | P (MPa) | h (kJ/kg) | s (kJ/kg·K) |
| 1 | 600 | 25 | 1094.689 | 2.767 |
| 2 | 544.433 | 16.5 | 30.842 | 2.773 |
| 3 | 600 | 16.5 | 1099.484 | 2.854 |
| 4 | 506.897 | 8 | 993.036 | 2.864 |
| 5 | 103.09 | 8 | 523.998 | 2.016 |
| 6 | 60.936 | 8 | 459.916 | 1.834 |
| 7 | 35 | 8 | 352.291 | 1.494 |
| 8 | 48.558 | 10.498 | 358.523 | 1.496 |
| 9 | 35 | 10.498 | 286.459 | 1.268 |
| 10 | 56.523 | 25 | 307.531 | 1.275 |
| 11 | 92.35 | 25 | 387.409 | 1.505 |
| 12 | 92.35 | 25 | 387.409 | 1.505 |
| 13 | 92.35 | 25 | 387.409 | 1.505 |
| 14 | 409.56 | 25 | 856.447 | 2.459 |

***Table 14:*** *Main Compression Intercooling sCO2 cycle pressure, temperature, enthalpy & entropy for every state point.*

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| State (i) | T (°C) | P (MPa) | h (kJ/kg) | s (kJ/kg·K) |
| 1 | 600 | 25 | 1094.689 | 2.767 |
| 2 | 544.433 | 16.5 | 1030.842 | 2.773 |
| 3 | 600 | 16.5 | 1099.484 | 2.854 |
| 4 | 506.897 | 8 | 993.0367 | 2.864 |
| 5 | 178.593 | 8 | 615.201 | 2.237 |
| 6 | 64.746 | 8 | 446.908 | 1.855 |
| 7 | 34 | 8 | 320.691 | 1.391 |
| 8 | 43.582 | 10.5 | 325.598 | 1.393 |
| 9 | 34 | 10.5 | 282.898 | 1.256 |
| 10 | 54.746 | 25 | 303.707 | 1.263 |

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| 11 | 168.462 | 25 | 534.376 | 1.872 |
| 12 | 168.462 | 25 | 534.376 | 1.872 |
| 13 | 168.462 | 25 | 534.376 | 1.872 |
| 14 | 454.293 | 25 | 912.211 | 2.538 |

# Effect of TIT



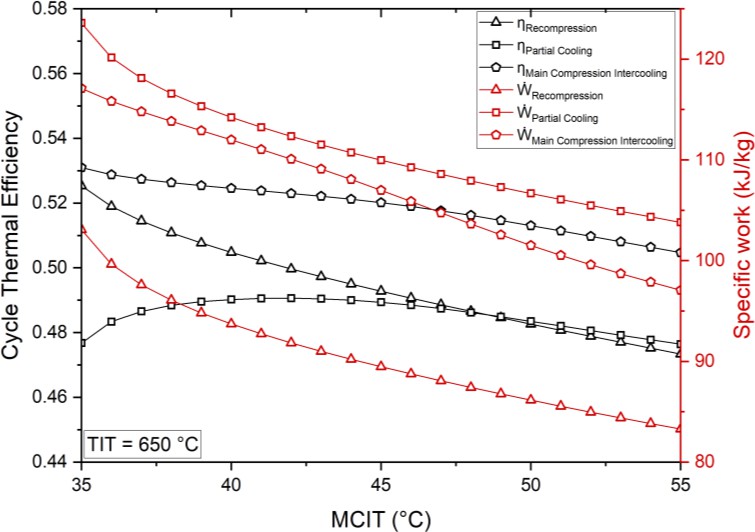
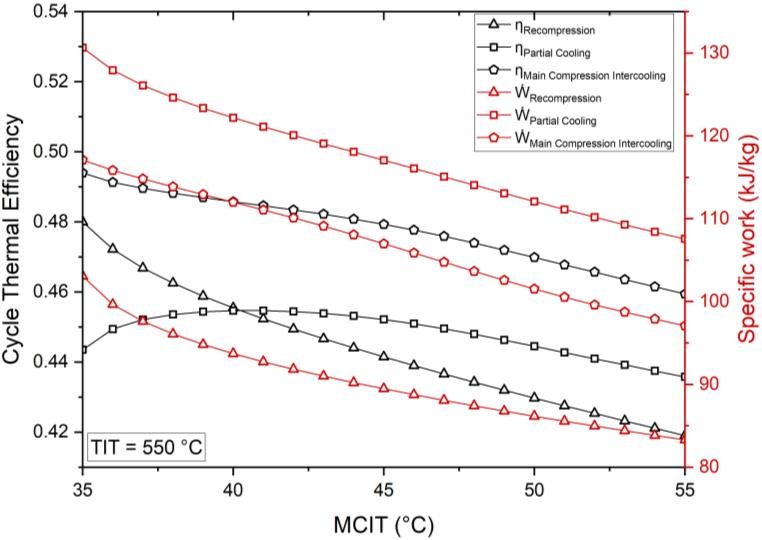
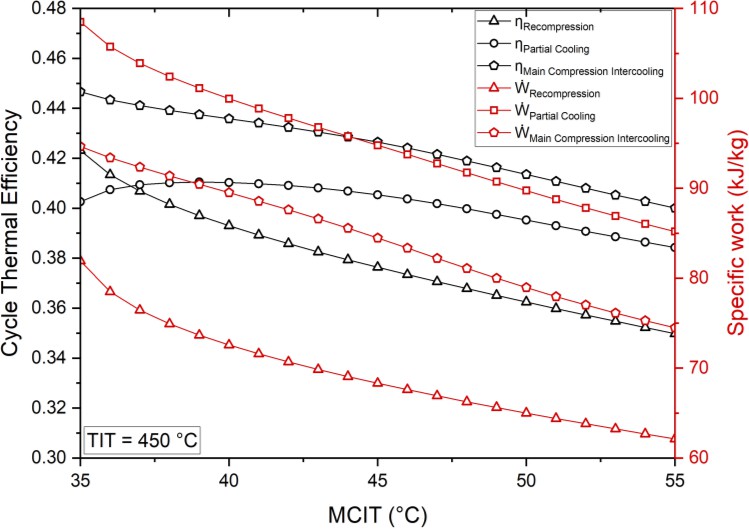
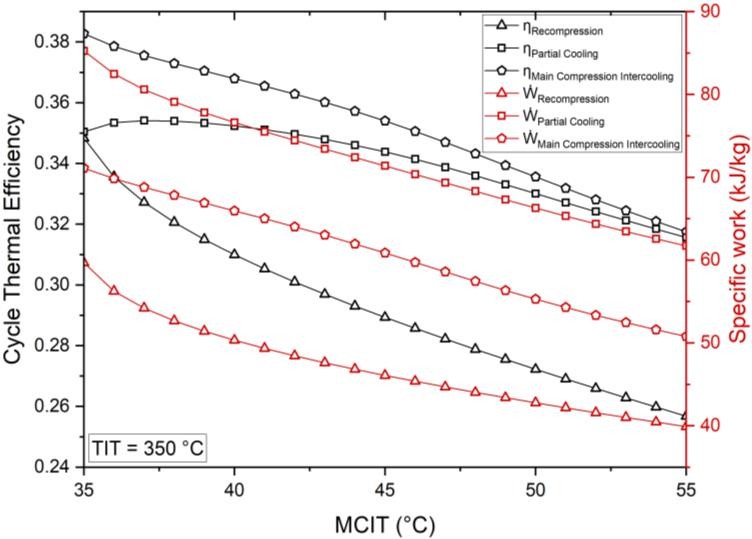
***Fig. 10.*** *Exergy destruction & exergy efficiency comparison for recompression, partial cooling &*

*intercooling cycle with the variation of the TIT at different compressor inlet temperature of 35°C, 40°C, 45°C and 50°C.*

According to previous studies and the laws of thermodynamics, increasing TIT causes the sCO2 power cycles' thermal efficiency to increase. **Fig. 10** depicts exergy destruction & energetic efficiency comparison of all three cycle configurations with the changes in turbine inlet temperature. During the comparative analysis, the MCIT is maintained constant, while the TIT is systematically adjusted within the range of 400°C to 700°C. Based on this comparison, it can be seen that the recompression sCO2BC

exhibits better exergetic efficiency at lower MCIT values. Conversely, the partial cooling sCO2BC demonstrates better performance at higher MCIT circumstances. When MCIT ≥ 45°C, there is noticeable rise in the amount of exergy destruction occurring within the recompression cycle. Nevertheless, the influence of this rise on the trend of increasing TIT is rather insignificant. Observable differences in efficiency can be observed when intercooling is employed in the main compression process at temperatures of 40°C, 45°C, and 50°C. These fluctuations usually relate to the irreversibility of the main compressor when it operates at high temperatures.

# Effect of Main Compressor Inlet Temperature (MCIT)



***Fig. 11.*** *Cycle thermal efficiency & specific work comparison for recompression, partial cooling & intercooling cycle with the variation of the MCIT at different turbine inlet temperature of 350°C, 450°C,*

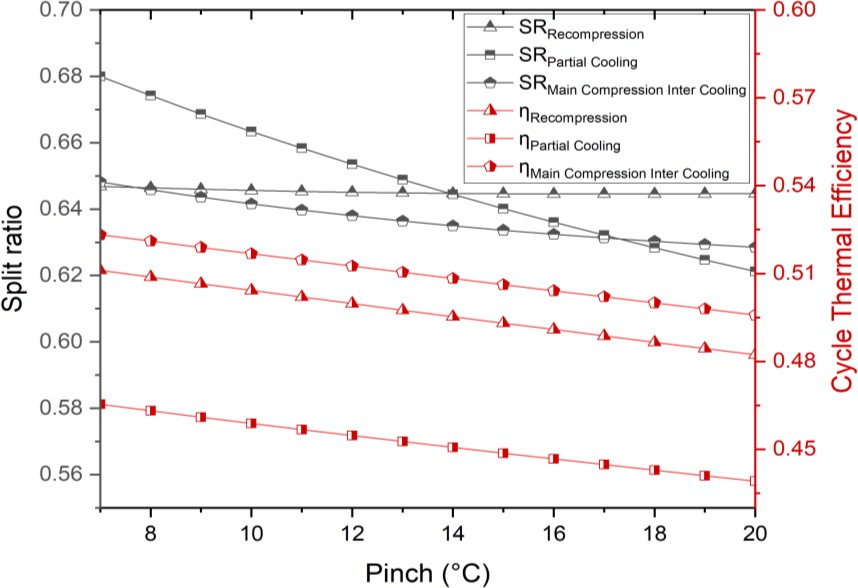
*550°C and 650°C.*

**Fig. 11** illustrates comparison of sCO2 cycles thermal efficiency & specific work varying MCIT from 35°C to 55°C while keeping TIT fixed at certain temperatures to be investigated. In accordance with the Carnot efficiency, cycles that reject heat at a lower weighted average temperature will have higher efficiencies. Thus, reduction of MCIT results of increase *ηcycle* and as well as, *Wne*t. It also demonstrates

that when temperature rises, work output and cycle efficiency decrease. Partial cooling cycle *ηcycle* increases at 40°C MCIT and then decreases due to the ideal cooling level that maximizes *ηcycle*. The precooler's failure to maintain ideal conditions causes a temperature drop when a threshold is reached. From the comparison, it is evident that main-compression intercooling sCO2BC provides better cycle thermal efficiency (53.2% at 650°C TIT), comparing to other two cycles.

# Impact of Pinch Temperature of Recuperator

The effect of the pinch temperature for the recuperator on the performance of sCO2 Brayton cycles are also investigated. For recuperator *Tpinch* in the range of 7°C to 20°C, the cycles are optimized to obtain maximum cycle efficiency. **Fig. 12** shows the optimal split ratio and pinch temperature to produce the maximum *ηcycle*. As recuperator *Tpinch* increases, the ideal split ratio decreases from 0.65 to 0.632. Accordingly, *ηcycle* decreases steadily with increasing recuperator *Tpinch*. From an economic point of view, the main-compression intercooling cycle has an advantage over the recompression & partial cooling cycle, which has different splitting location of the working fluid.

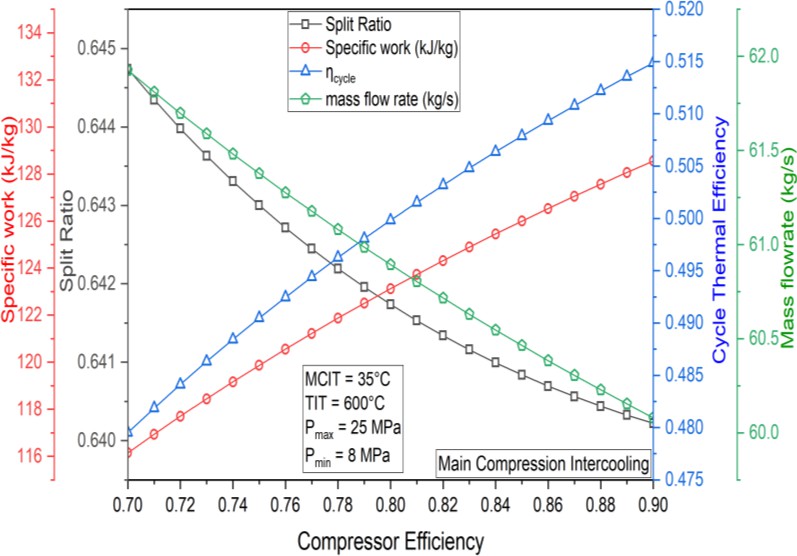
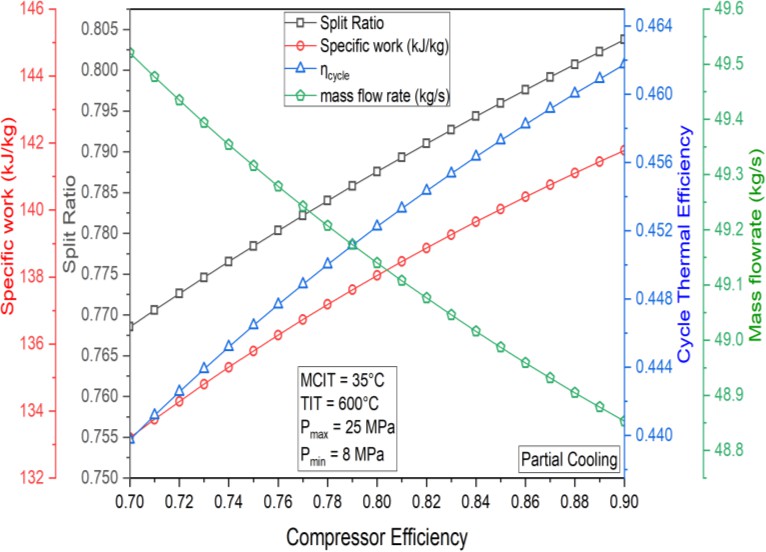
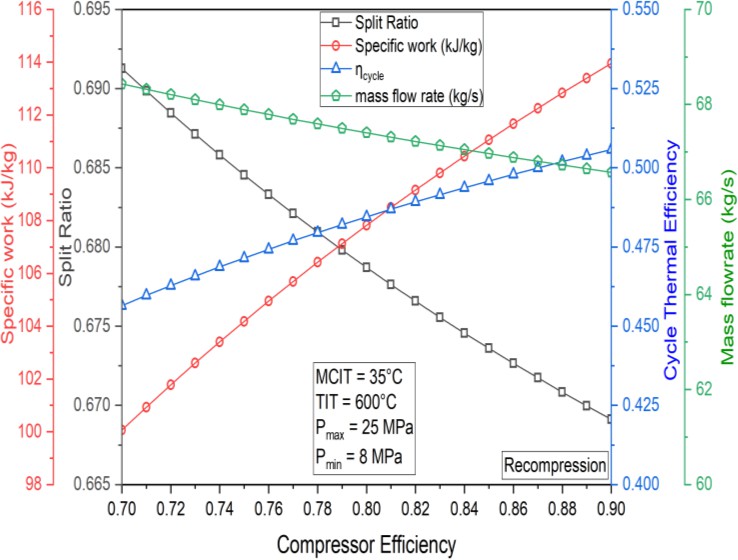


***Fig. 12.*** *Comparison of split ratio & cycle thermal efficiency with variation of recuperator pinch temperature.*

# Impact of Isentropic Efficiency of Main Compressor

Although it was presumed that the compressor efficiency for all three cycles was 89%, the effect of main compressor efficiency on each cycle's performance should be investigated to make a fair comparison of the three cycles. **Fig. 13** shows the specific work, split ratio, *ηcycle* & *ṁ* of the recompression, partial cooling, and main-compression intercooling cycle for *ηc* ranging from 70% to 90% and a constant isentropic turbine efficiency (*ηt* = 90%). In the cases of the recompression and main-compression intercooling cycles, SR increases steadily with increasing isentropic efficiency of the main compressor. However, in the case of the partial cooling cycle, the split ratio has a decreasing curve. The main- compression intercooling cycle has a higher efficiency than the recompression and partial cooling cycles over a wide range of *ηc*, especially in the region of low *ηc*. Therefore, the main-compression intercooling cycle can achieve a higher efficiency at a lower main compressor efficiency.

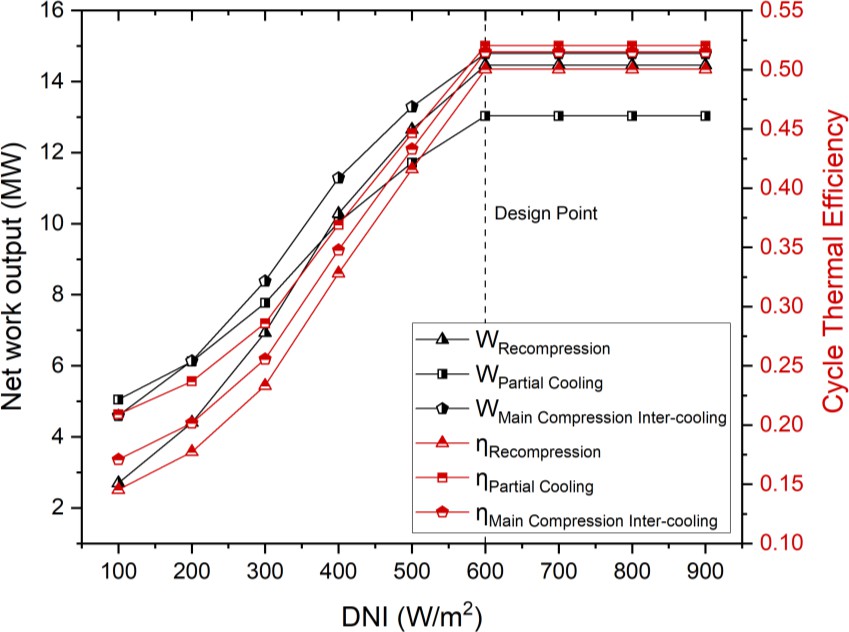
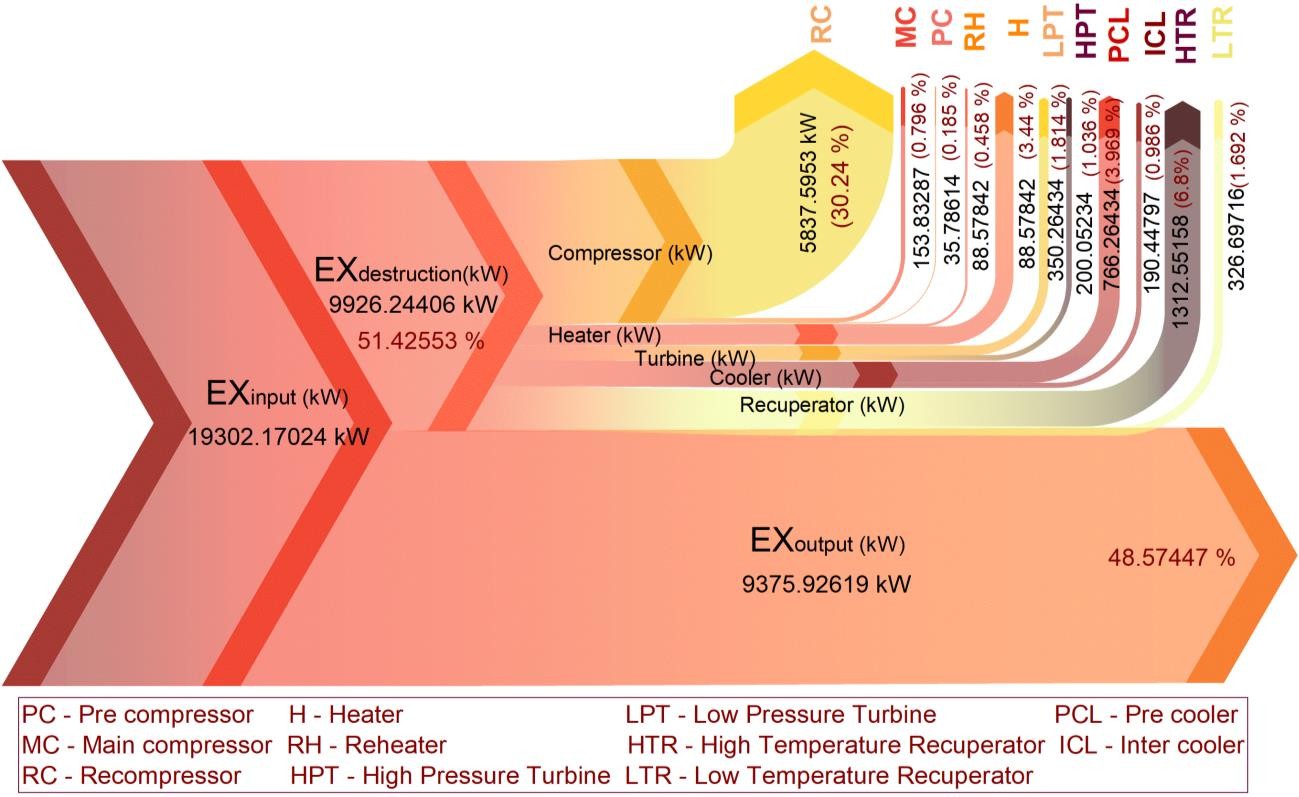
***Fig. 13.*** *Specific work, split ratio, cycle efficiency & mass flowrate of different sCO2 cycle with the variation of compressor efficiency.*



# Exergy Destruction

**Fig. 14** illustrates Grassmann diagram representing each component's exergy destruction in an operational state of 25 MPa cycle *Pmax*, 8 MPa cycle *Pmin*, 600°C *TIT* and 34°C *MCIT*. The arrows represent the components and the width of the lines connecting the components was varied to visually represent the quantity of exergy flow. From the results, it can be seen that maximum exergy destruction of 5837.5953 kW (30.24%) occurs in the compressor, whereas insignificant exergy destruction is seen in the turbines.

***Fig. 14.*** *Exergy destruction in different components in main compression intercooling sCO2 cycle.*

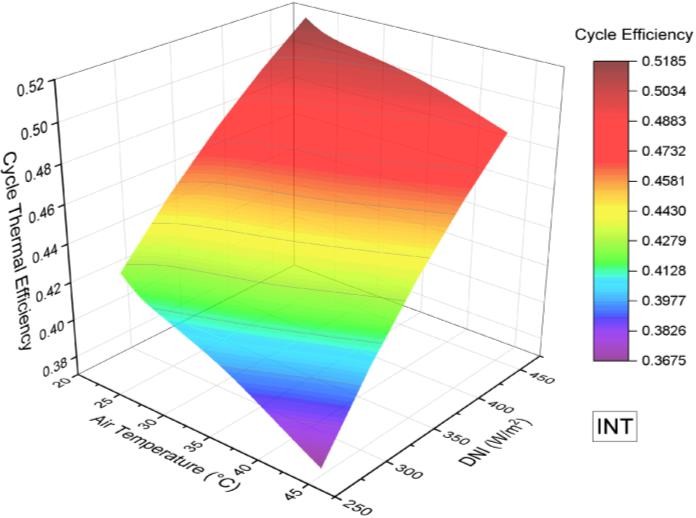
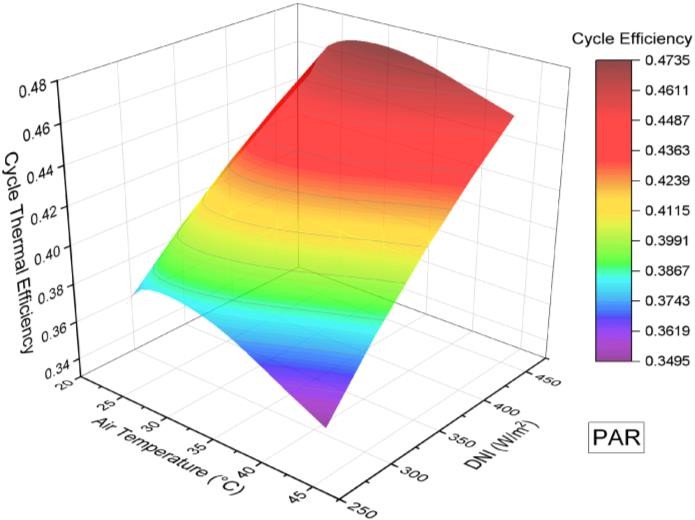
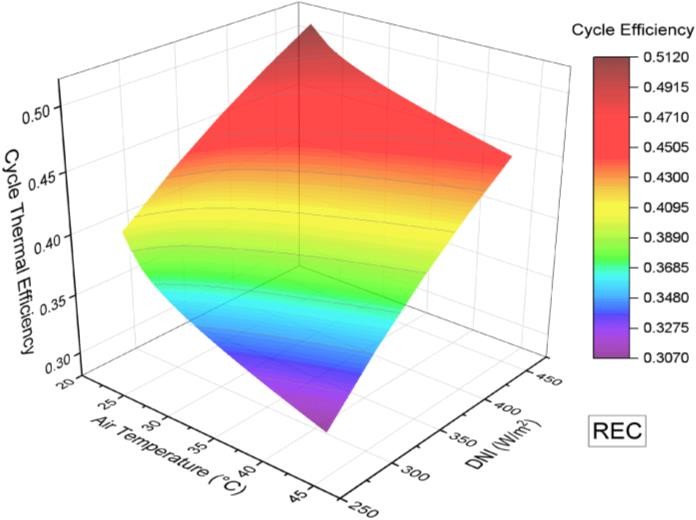


# Effect of Air Temperature and DNI

***Fig. 15.*** *Power output and cycle thermal efficiency at different DNI conditions.*

Power output for recompression, partial cooling, and main-compression intercooling cycle at different DNI conditions is demonstrated in **Fig. 15**. Without TES arrangement, when the ambient temperature falls under the design point (MCIT=34°C & DNI=0.6 kW/m2), the CSP plant overcools. At critically lower air

temperatures, portion of heat from CSP loop is used in the cycle, to keep MCIT at 34°C throughout. When DNI rises above 600 W/m2, TIT is expected to increase as well resulting in more Wnet, however, this would make the turbines vulnerable due to metallurgical limitations. Hence, TIT is limited to 600°C regardless increase in DNI after the design point, providing constant thermal power output.

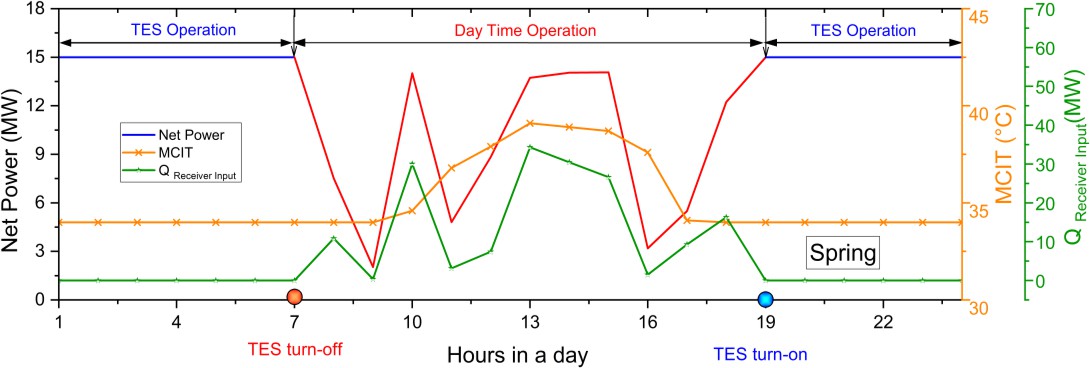
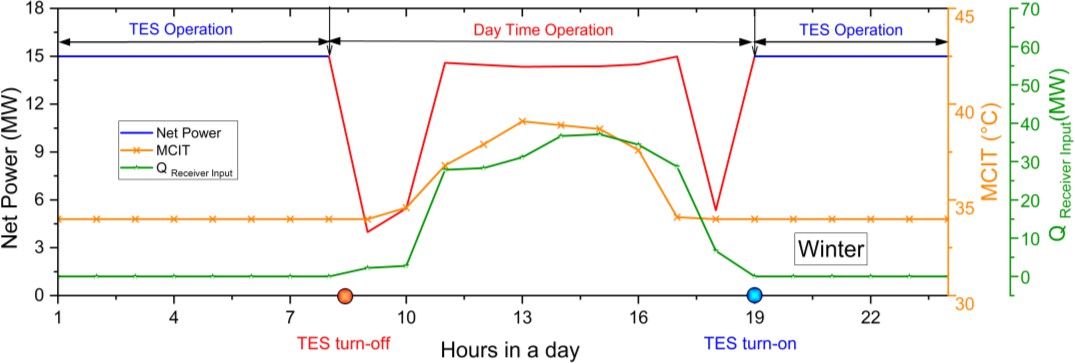
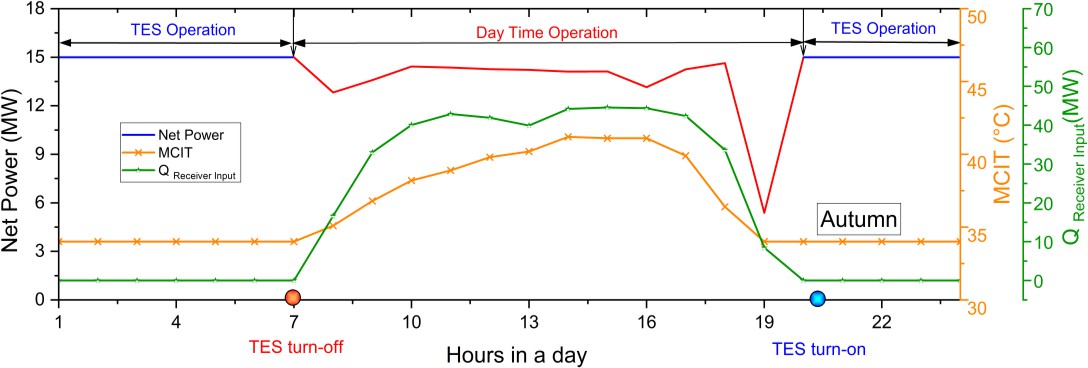


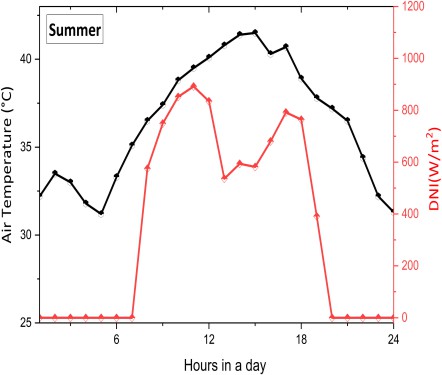
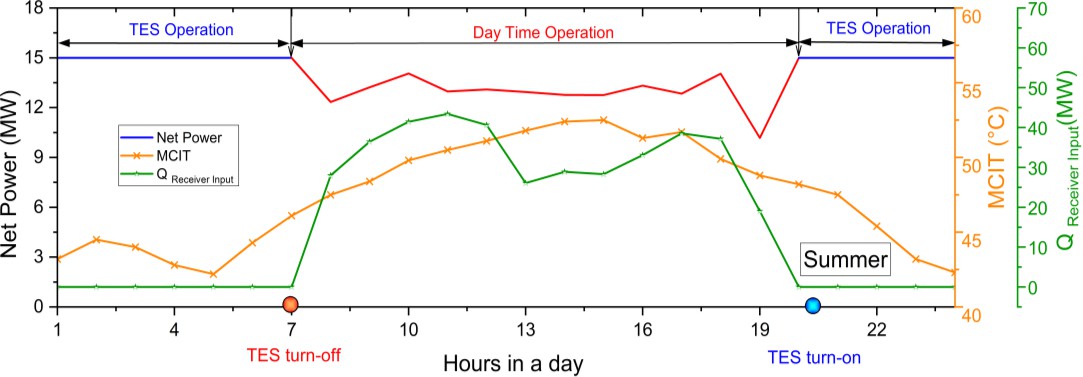
***Fig. 16.*** *The effect of air temperature and DNI on cycle thermal efficiency (a) Recompression sCO2BC,*

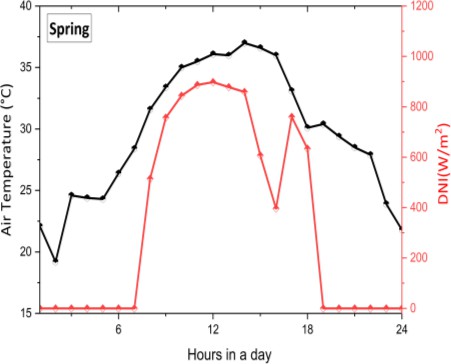
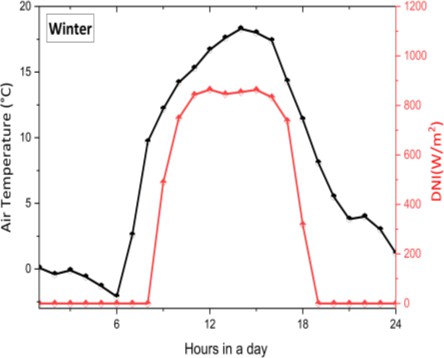
*(b) Partial cooling sCO2BC, (c) Main compression intercooling sCO2BC.*

**Fig. 16**. illustrates the trend between cycle thermal efficiency, air temperature, and DNI for three distinct functional cycles. The color gradients serve as visual representations of the varying levels of cycle efficiency. The efficiency of the cycle is negatively impacted by an increase in air temperature, with the optimal conditions being characterized by the lowest possible air temperature and the DNI values. The area exhibiting the lowest cycle efficiency for the INT cycle is observed when the air temperature falls between the range of 37 to 45˚C, while the Direct Normal Irradiance (DNI) varies from 250 to 300 W/m2. However, for PAR cycle, an improvement in efficiency to 47.35% was initially observed when DNI rose and air temperature declined. Finally, these 3D plots indicate that the REC, PAR, and INT sCO2 cycles achieve optimal cycle performance when operating under conditions characterized by low air temperatures and high DNI.

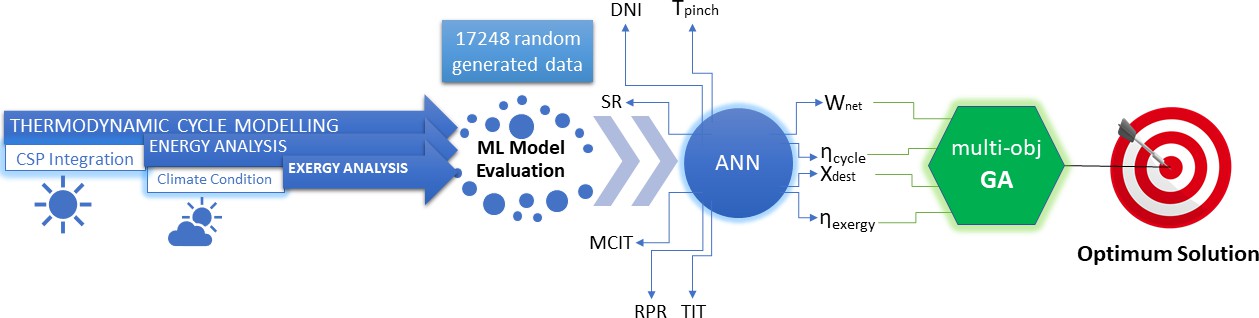
# Dynamic Attributes of Plant Operation Under Various Climate Condition





***Fig. 17.*** *Main compression intercooling sCO2 cycle hourly CSP plant performance for supplemented with TES at various seasonal climates.*

**Fig. 17** shows hourly performance for sCO2 cycle at varied seasonal climates, TES was incorporated. Since the temperature during the day consistently exceeds the design point, the core flow splitter alters the split ratio to increase energy output. Since the air temperature is consistently below the intended limit in autumn, the Natural Draft Dry Cooling Tower (NDDCT) flow divider is constantly in operation [37]. Similar performance is shown in the winter and spring, although because of the very low ambient temperature, the winter bypass percentage changes significantly. The primary flow divider is essentially constant throughout the autumn, winter, and spring. TES is switched off at 7:00 a.m., and the cycle is thereafter powered by solar energy. Power output is limited by variations in the temperature of the turbine caused by variations in solar energy. Additionally, the quantity of solar salt that flows between the power block and the central receiver is constantly regulated by changes in DNI. Since solar energy is irregular a key characteristic that constantly changes is the bulk flow of molten salt. When there is no solar energy available in the evening around 19:00, using the molten salt in the heated reservoir TES switches to discharge mode. The CSP plant built for DP (15MW) demonstrates increased steadiness in power output while running under TES as almost constant heat is supplied to the turbine. The performance fluctuates greatly on other days throughout each season; therefore, the graph above does not really assess the best seasonal environment for maximizing power output. The steam cycle's thermal efficiency increases as MCIT decreases. For sCO2 power cycles, however, this is not true since lowering the operating fluid's temperature below the pseudocritical point can seriously damage the compressor's ability to operate properly. Furthermore, according to earlier studies, a cold climate requires a higher thermal input for the sCO2 power cycle. A broader solar field is thus required for CSP applications to run the power cycle when the air is cooler and collect more thermal energy from the central receiver. In this study, it is avoided that the sCO2 power cycle's subcritical operation and NDDCT design. Operation instability of the compressor results from the sCO2 power cycle operating in subcritical state.



# Multi-objective Optimization

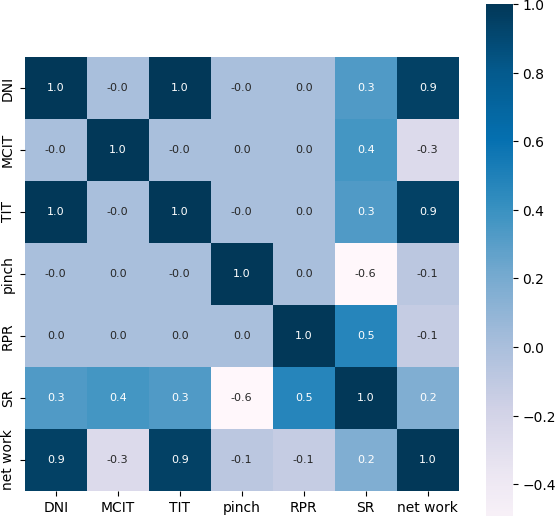
***Fig. 18****: Optimization methodology framework.*

Main-compression intercooling sCO2BC is chosen for optimization as this system outperforms recompression & partial cooling cycle in terms of thermal performance at different operating conditions. **Fig. 18**. shows the outline of the optimization methodology used in this study. Once the data required has been calculated, to find the sensitivity of the input parameters, the generated values are initially analyzed with a sensitivity analysis. Based on computing requirements and ML model prediction accuracy, the most optimal model is chosen. The use of artificial neural networks (ANNs) into the optimization of advanced sCO2 power cycles presents numerous benefits in comparison to conventional thermodynamic models. ANNs have been shown to enhance accuracy through their ability to capture intricate, non-linear

interactions. Additionally, ANNs enable adaptability in accommodating diverse situations and complexities within a given system. They have exceptional proficiency in managing complex systems, enabling quick adjustments in response to changing circumstances, leveraging data-driven analysis to inform decision-making, and expediting the process of software development. ANNs have the potential to significantly improve energy efficiency, rendering them highly valuable in various domains, including power generation. Nevertheless, it is imperative to utilize these tools along with thermodynamic models in order to optimally utilize their capabilities while effectively addressing their limits. To optimize design parameters, multi-objective GA is integrated with the best machine learning model. MATLAB software is used for setting up neural network & GA- gamultiobj was set as solver for multi-obj optimization. The following subsections provide insights regarding the adopted framework for this study.

# Sensitivity Analysis

Using the Weighted Least Square (WLS) technique, a sensitivity analysis has been conducted. A heat map, **Fig. 19,** depicts sensitivity and correlation between the input and output parameters. A greater number indicates that the column's parameters are more sensitive to changes in the row's values[2]. Conversely, the trends of the output numbers are caused by the input parameters are shown by positive and negative signs as being direct or inverse. The output parameter, net work is sensitive to all input factor where, DNI is the most sensitive input parameter.



***Fig. 19:*** *Heat map showing the sensitivity of cycle parameters to the variation in output variables.*

# Methodology of ML based Algorithms

In the current work, six machine learning algorithms, specifically XGBoost, Random forest, LightGBM, AdaBoost, KNN, and ANN are used to train the data. On the basis of prediction accuracy, the best model is chosen for next stage of optimization. The following subsections present details about the theoretical framework used in the study.

## *XGBoost Algorithm*

The supervised learning algorithm XGBoost, accurately predicts a target variable by combining the values of simpler variables. It implements regression trees as weak learners and minimizes the objective function by means of a convex loss function and penalty clause. The training procedure is iterative, with the addition of new trees for forecasting residues and errors and the execution of gradient boosting to minimize loss. Instead of selecting the best model based on the data, XGBoost parallelizes the dataset's boosting by training hundreds of models on diverse subsets[38].

*Fn (X) = Fn-1 (X) + αn-1 gj (X, qn-1)* (07)

Here,

αj, qj = regularization parameters and residual computing jth tree. gj = function used to train the prediction of residuals

For computing αj we first compute the residual then use this function

arg min(α) = ∑𝑛 𝐿(𝑌𝑗, 𝐹𝑗−1(𝑋𝑗) + 𝛼𝑔𝑗(𝑋𝑗,𝑞𝑗−1))

𝑗=1

where *L (Y, F(X))* differentiable loss function

## *Random Forest Algorithm*

The RF approach, which combines multiple independent decision trees to precisely anticipate new input data, is a key part of machine learning's supervised learning strategy. Ensemble learning solves classification and regression problems. Using each tree's projections and predictions, Optuna hyperparameter tweaking minimizes overfitting and maintains accuracy [39]. Least squares create the decision tree, *x(n)* was separated into *R1* and *R2* after choosing the separation point (sp). Calculating the minimal output *y* value by calculating *c1* and *c2*. This means that *(n)* is this ap's optimal separation point from *x*.

𝑚𝑖𝑛𝑠𝑝 [𝑚𝑖𝑛𝑐1 ∑𝑥𝑖∈𝑅1

(𝑦𝑖 − 𝑐1)2 +

𝑚𝑖𝑛𝑐1 ∑𝑥𝑖∈𝑅2 (𝑦𝑖 − 𝑐1)2]

(*08*)

The value of the output will be calculated for each node. Here, *R1* is shown as an example. The output value of this node will be:

𝐶0= 1

𝑁1

∑ 𝑦𝑖

𝑥𝑖∈𝑅1

(*09*)

## *LightGBM Algorithm*

LightGBM is a data structure that applies the GBDT algorithm, combines weak learners, and sets up a regression tree. It enhances accuracy and efficiency by splitting continuous eigenvalues into k-intervals and avoiding overfitting through regularization. Also, the objective function is efficiently approximated using Newton's approach. [40]. The objective function can be expressed as

𝑚

1

𝑂𝑏𝑗(𝑛) ≅ ∑ [𝑔𝑛𝑓𝑛(𝑥𝑛) +  ℎ

𝑓2(𝑥𝑛)] + ∑ 𝛺(𝑓𝑘)

(*10*)

𝑛=1

2 𝑛 𝑛

𝑘

Where, 𝑔𝑛& ℎ𝑛 denotes two loss functions: a first-order loss function and a second-order loss function, respectively.

𝑔𝑛 = 𝜕𝐹𝑛−1(𝑥𝑖)𝛹(𝑦𝑛, 𝐹𝑛−1(𝑥𝑖)) (*11)*

ℎ𝑛 = 𝜕2 ( )𝛹(𝑦𝑛, 𝐹𝑛−1(𝑥𝑖)) (*12*)

𝐹𝑛−1 𝑥𝑖

The algorithm implements a leaf-wise generation strategy to minimize training data and eliminate overfitting. By integrating high-dimensional data features in a sparse feature space, the EFB algorithm of LightGBM prevents redundant features[41].

## *AdaBoost*

AdaBoost's classifier or regression functions use an array of stumps that are iteratively trained using feature data (x) and target data (y). The algorithm's overall predictions are obtained immediately after training using a weighted average of the predictions from the stumps. Weak classifiers {*φµ(x)*: µ = 1, ..., M}. Known data X = {(xi, yi): i = 1, ..., N} where yi ∈ {±1}. here 𝜆𝜇 weights that must be developed. AdaBoost's final regression solution is asymptotic. This is partially accurate due to technological issues and data growth. AdaBoost Regression improves results but requires additional computations. Furthermore, it necessitates the execution of the sparsity requirement that the diversity of *λ's* be zero.[42]

𝑒𝑦 ∑𝜇 𝜆𝜇𝜙𝜇(𝑥)

𝑃(𝑦 ∣ 𝑥) = 𝑒∑𝜇 𝜆𝜇𝜙𝜇(𝑥) + 𝑒− ∑𝜇 𝜆𝜇𝜙𝜇(𝑥)

(*13*)

## *K Nearest Neighbor (KNN) Algorithm*

KNN is a popular regression technique that calculates distances between neighbors using weighting techniques. It provides more accuracy but is time-consuming. However, it necessitates adaptive neighbors and weighting to accommodate dataset properties, and traditional KNN may not be accurate due to dataset density variations.[43]. Let {*N j*}*k* represent the target values of an instance's k nearest neighbors. After that, the conventional KNN prediction Yi for the i-th instance is calculated as shown below:

*i*

𝑌𝑖 =

𝑘

1 ∑ 𝑁𝑗

𝑖

𝑘

𝑗=1

(*14*)

## *Artificial Neural Network (ANN)*

The configuration of the ANN algorithm is shown in **Table 15**. A feedforward net neural network integrated into MATLAB was utilized, and the inputs were divided at random (dividerand), as shown **Fig.**

**20**. Ideally, the number of neurons for the analysis should be set to 10. The feedforward neural network is a versatile tool that can be employed for various types of input-output mappings. The performance metric employed in this study is the Mean Squared Error (MSE), whereas the training method utilized is Bayesian regularization (trainbr). Although the trainbr approach normally takes longer, it may provide a high degree of generalization for difficult, constrained, or noisy datasets and adaptive weight minimization determines when training ends.

***Fig. 20.*** *Artificial neural network.*

***Table 15:*** *ANN algorithm setup.*

**6.3 Optimization Methodology**

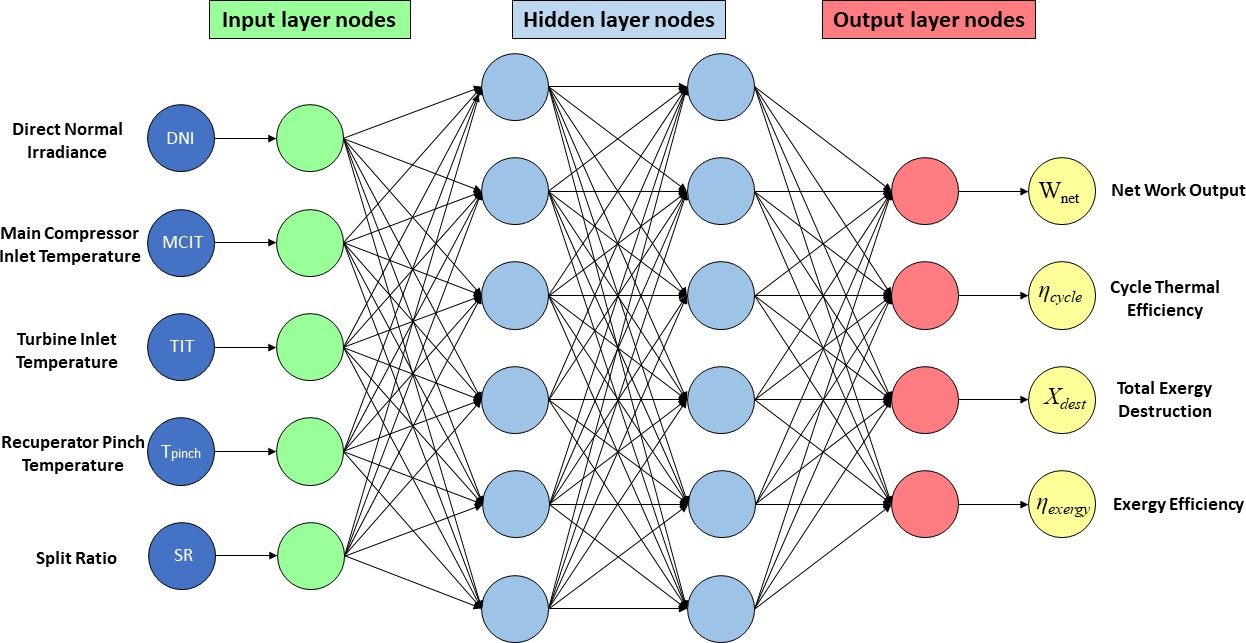
A genetic algorithm is a population-based feature selection method that chooses from a variety of solutions instead of limiting to just a single. The genetic algorithm's fundamental objective is to find the optimal solution from the population in the shortest amount of time [44]. MATLAB in-built neural network tool is used to train the model and generate the function that is utilized in multi-obj GA to carry out the optimization process using the input parameters included in **Table 16**. The GA evaluates the population using the objective function. **Table 17** outlines the range of input parameters (LB-lower bounds & UB-upper bounds) for multi-objective optimization for REC, PAR & INT sCO2BC.

***Table 16:*** *GA problem setup parameter options.*

|  |  |  |  |
| --- | --- | --- | --- |
| Data Division | Training | Performance | Calculations |
| dividerand | trainbr | MSE | MEX |

|  |  |  |
| --- | --- | --- |
| Parameters | Options | Values |
| Population | Type: Double vector | Population size: 200 |
| Selection | Function: Tournament | Size: 2 |
| Mutation | Constraint dependent | - |
| Migration | Direction: Forward | Fraction: 0.2, Interval: 20 |
| Multiobjective problem settings | Function: @distancecrowding | Fraction: 0.35 |
| Stopping criteria | Function tolerance | Specify: 0 |
| Plot functions | Pareto front | - |

***Table 17:*** *Range of input parameters for optimization.*



UB

LB

UB

LB

UB

LB

Parameters

INT

PAR

REC

Cycle

DNI (kW/m2) 0.27187 0.65312 0.271875 0.653125 0.27187 0.65312

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| MCIT(°C) | 34 | 55 | 34 | 55 | 34 | 55 |
| TIT (°C) | 400 | 700 | 400 | 700 | 400 | 700 |
| Tpinch (K) | 5 | 20 | 5 | 20 | 5 | 20 |
| RPR | - | - | 0.3 | 0.9 | 0.3 | 0.9 |
| SR (x) | 0.6445 | 0.7968 | 0.23 | 0.98 | 0.5566 | 0.8 |

# TOPSIS Method

In multi-criteria decision-making, ranking reversal is a problem when a selection method or alternative set shifts. This issue is fundamental to decision-making and multi-criteria decision-making discussions. According to Alirahmi et al.[45] assuming K decision-makers are evaluating *m* decisions based on *n* criteria and weights combined using the arithmetic mean or other methods, i.e., the traditional TOPSIS method's appropriate approach, the sum of the ratings and weights is then utilized to generate the decision

(*D*) and weight (*W*) matrix depicted below [46]:

𝑥11 𝑥12 ⋯ 𝑥1𝑛

𝐷 = [ 𝑥21 𝑥22 ⋯ 𝑥2𝑛 ]

⋮ ⋮ ⋯ ⋮

𝑥𝑚1 𝑥𝑚2 ⋯ 𝑥𝑚𝑛

𝑊 = [𝑤1 𝑤2 ⋯ 𝑤𝑛]

Subjected to

*xij* = aggregate rating of *ith* alternative for *jth* criterion

*wj* = the weight for *jth* criterion

Vector or linear normalization is used to scale up diverse criteria to a similar level. Decision matrix (*R*) that has been normalized by[46]:

Subjected to

𝑟11 𝑟12 ⋯ 𝑟1𝑛

𝑅 = [ 𝑟21 𝑟22 ⋯ 𝑟2𝑛 ]

⋮ ⋮ ⋯ ⋮

𝑟𝑚1 𝑟𝑚2 ⋯ 𝑟𝑚𝑛

*rij* = normalized rating of *ith* alternative for *jth* criterion

Chen el al.[47] suggested a linear method to construct a decision matrix, which illustrates how the alternatives perform against each criterion. To maintain impartiality, raw data is normalized into dimensionless values. To weight decision-making aspects, many weighing methods are investigated.

𝐸𝐷+

𝑜𝑝𝑡 { 𝑖 }

𝑖 ∈ 𝑚𝑎𝑥

𝐸𝐷+ + 𝐸𝐷−

(*15*)

𝑖 𝑖

𝑚

(*16*)

𝐵𝑖𝑗 = 𝐹𝑖𝑗 /√∑ 𝐹2 , 𝐺𝑖𝑗 = 𝑤𝑇𝑂𝑃𝑆𝐼𝑆 ⋅ 𝐵𝑖𝑗

𝑖𝑗 𝑗

𝑖=1

𝑚

(*17*)

)

𝐸𝐷− = √∑ (𝐺

− 𝐺negative 2

𝑖

𝑗=1

𝑖𝑗 𝑗

In Equation (16), w TOPSIS is the weight of the *j*-th optimization objective, G negative is the value of the *jth* target with an NIP (negative ideal point) after normalization, and Distance *i* is the Euclidean distance between the *ith* feasible option and (NIP) [48]. For a simple computation, *w TOPSIS* = 1 is utilized in this study.

*j*

j j

The ideal (*P+*) & negative-ideal (*P-*) strategies are determined as Equations (18) and (19), respectively[49]:

𝑃+ = {𝑣+, … , 𝑣+} = {(𝑚𝑎𝑥 𝑣

∣ 𝑖 ∈ 𝑅′) , (𝑚𝑖𝑛𝑣

∣ 𝑖 ∈ 𝑅−} (*18*)

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𝑗 𝑖𝑗

𝑗 𝑖𝑗

𝑃− = {𝑣−, … , 𝑣−} = {(𝑚𝑖𝑛𝑣

∣ 𝑖 ∈ 𝑅′) , (𝑚𝑎𝑥 𝑣

∣ 𝑖 ∈ 𝑅−} (*19*)

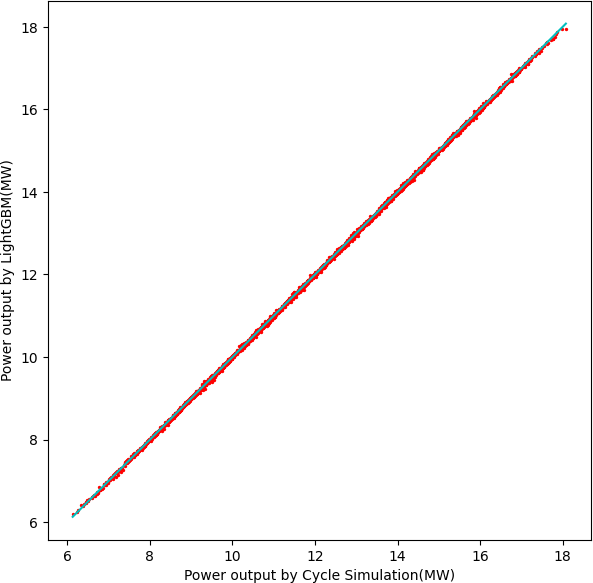
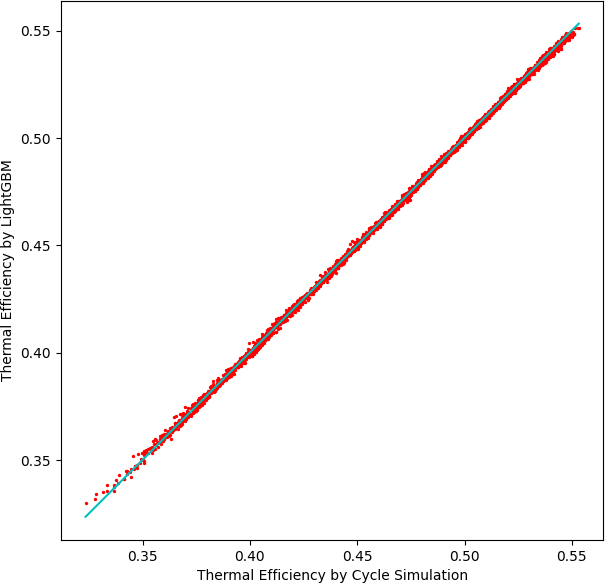
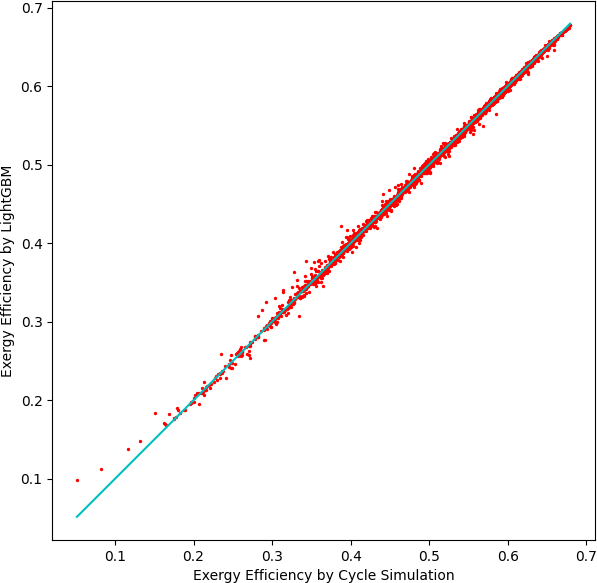
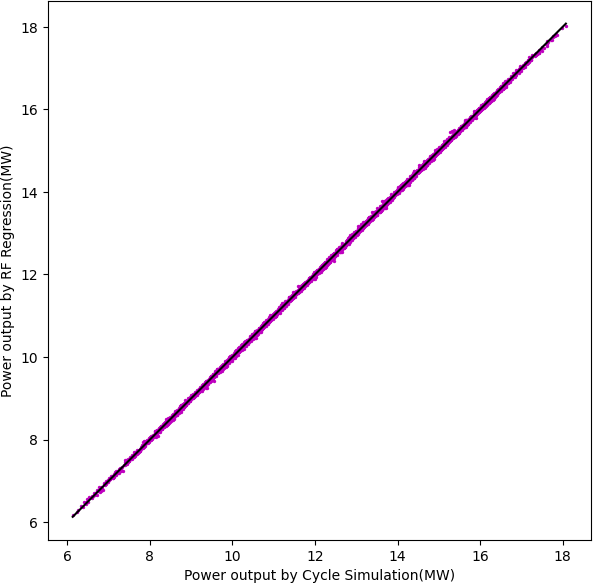
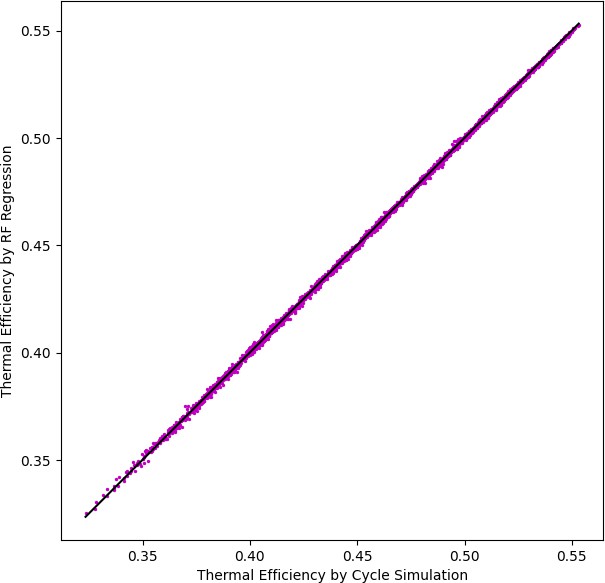
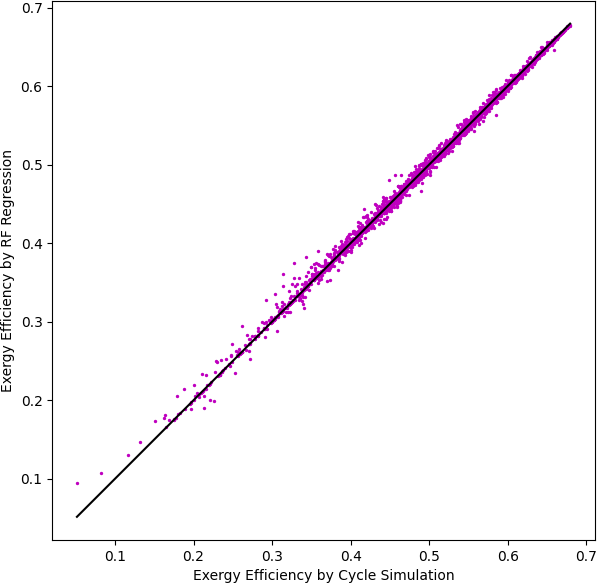
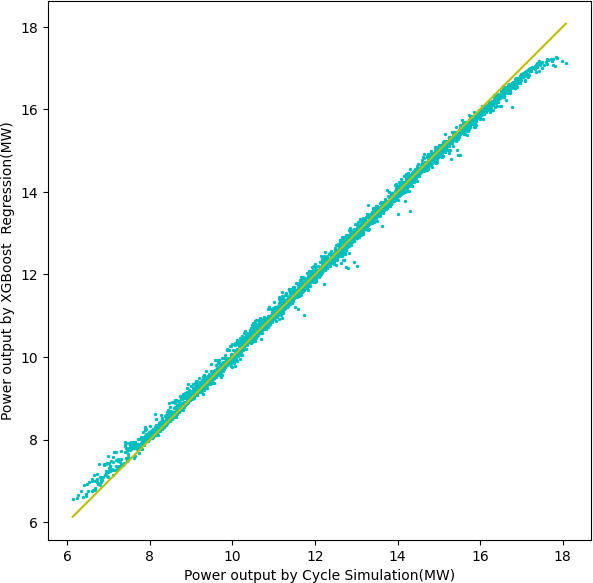
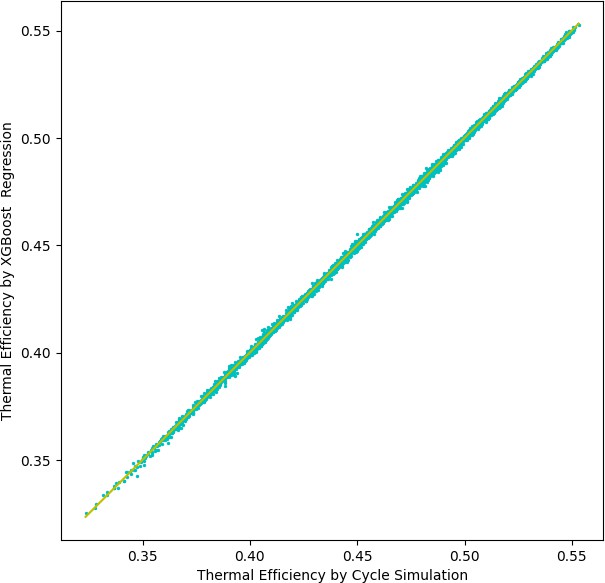
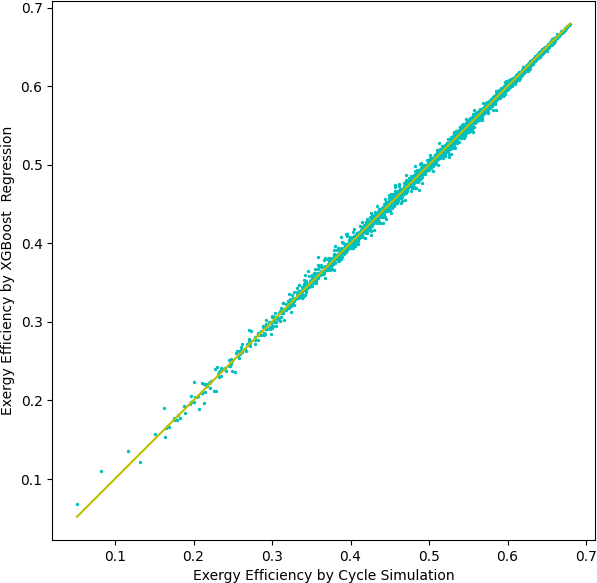
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# ML Model Accuracy Check & Error Evaluation

Machine learning models are evaluated by comparing their performance using metrics such as R2 and RMSE values. For dataset sizes greater than 3500 samples, a significant drop in the RMSE values for the three objective functions may be seen[50]. **Fig. 21**, **Fig. 22** and **Fig. 23** illustrates prediction result curve for cycle thermal efficiency, power output, exergetic efficiency and comparison between ML algorithms R2 score for both train & test datasets, respectively. Machine learning issues encompass the phenomena of overfitting and underfitting. A model exhibit overfitting on the training data, as it tends to incorporate irrelevant or random fluctuations, hence reducing its ability to generalize to unknown data. The occurrence of underfitting emerged prominently in the case of K-nearest neighbors (KNN), indicating that this particular model is extremely simplistic and lacks the ability to effectively capture crucial patterns present in the dataset. ANN shows best prediction score (Test = 0.99941 & test = 0.99855) compared to other models: ANN > XGBoost > RF> LightGBM > AdaBoost > Ridge > KNN > ElasticNet > Lasso.

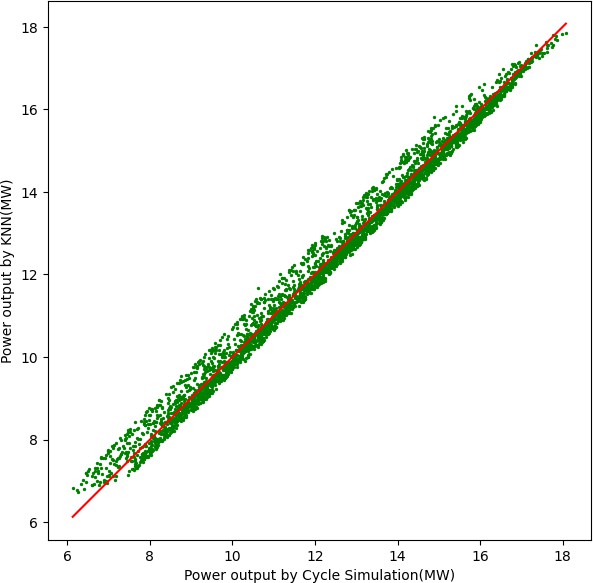
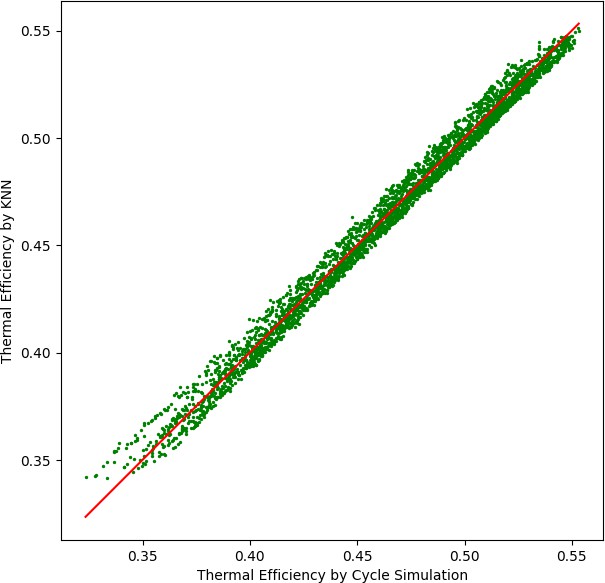
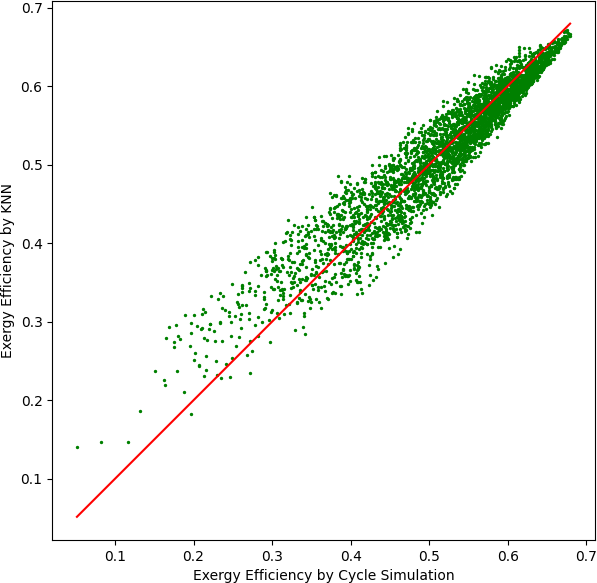
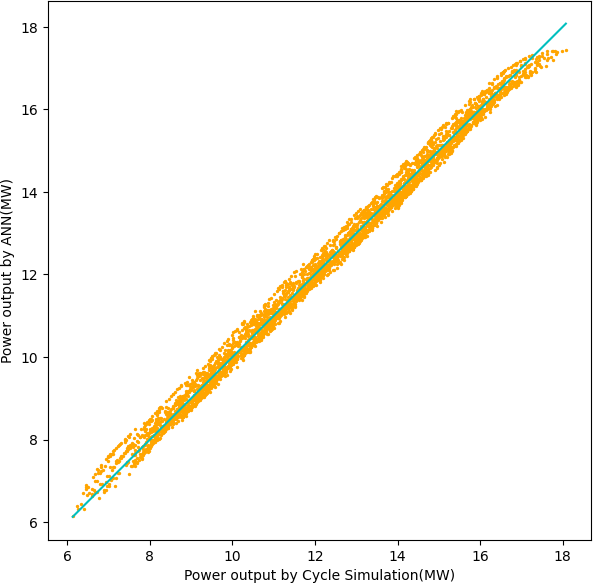
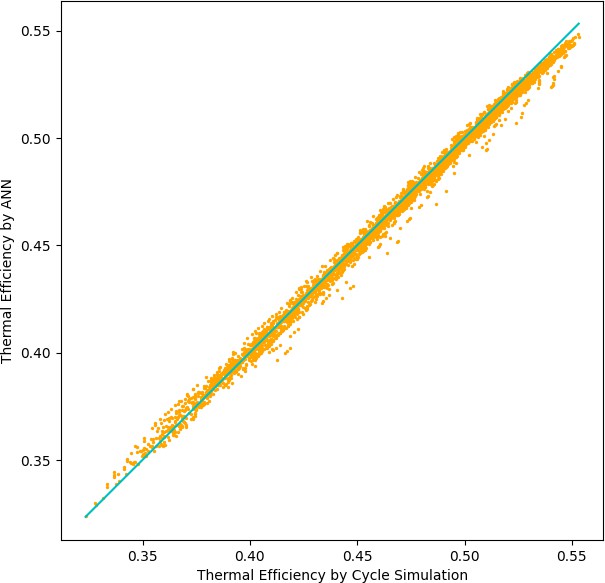
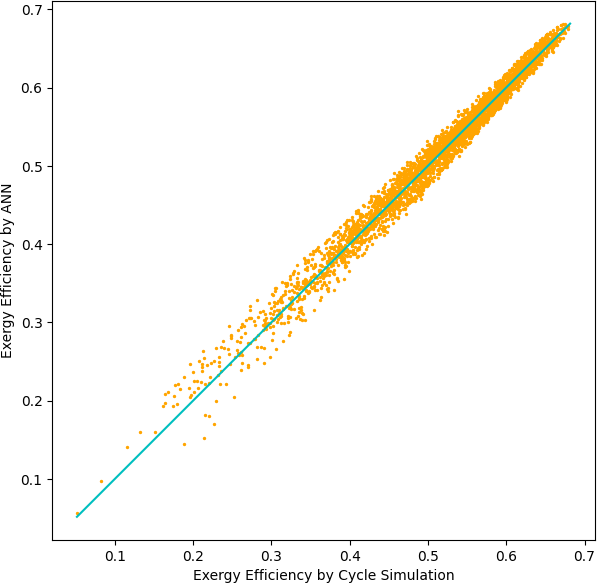
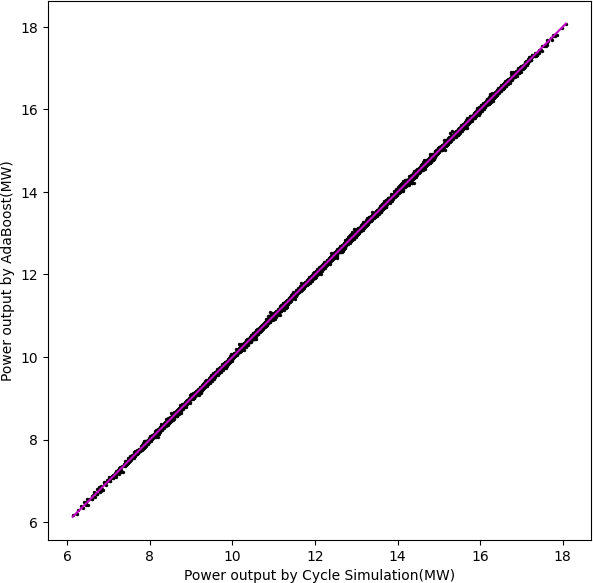
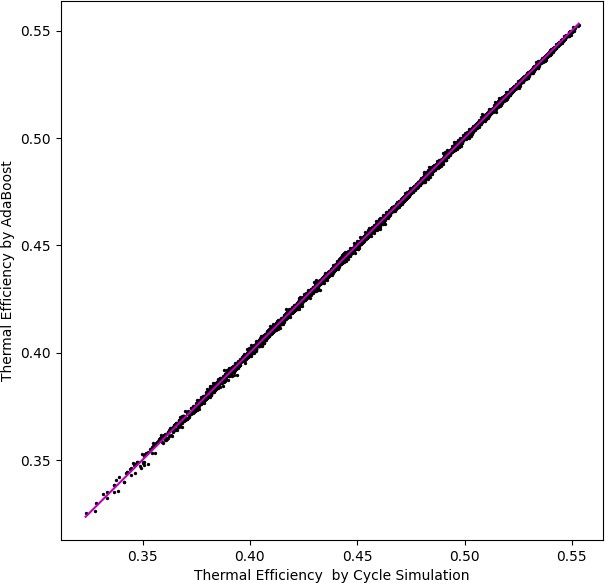
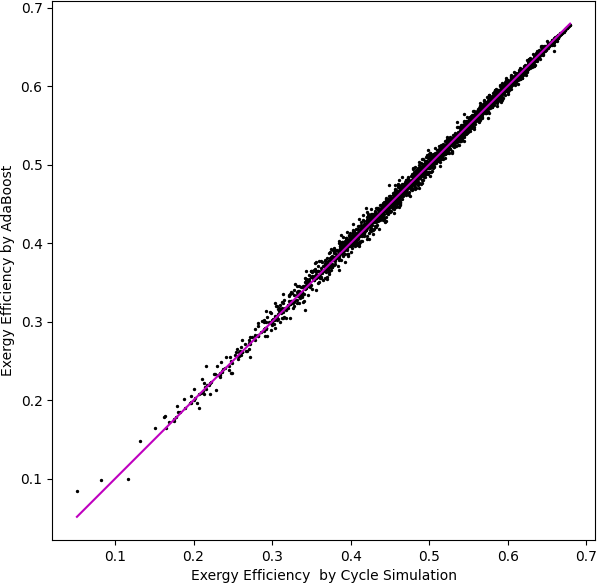


(a)

(b)

(c)

***Fig. 21.*** *Prediction result by for thermal efficiency(left), power output(mid) and exergy(right) efficiency of main compression intercooling cycle for (a)XGBoost, (b)RF, (c)LightGBM.*

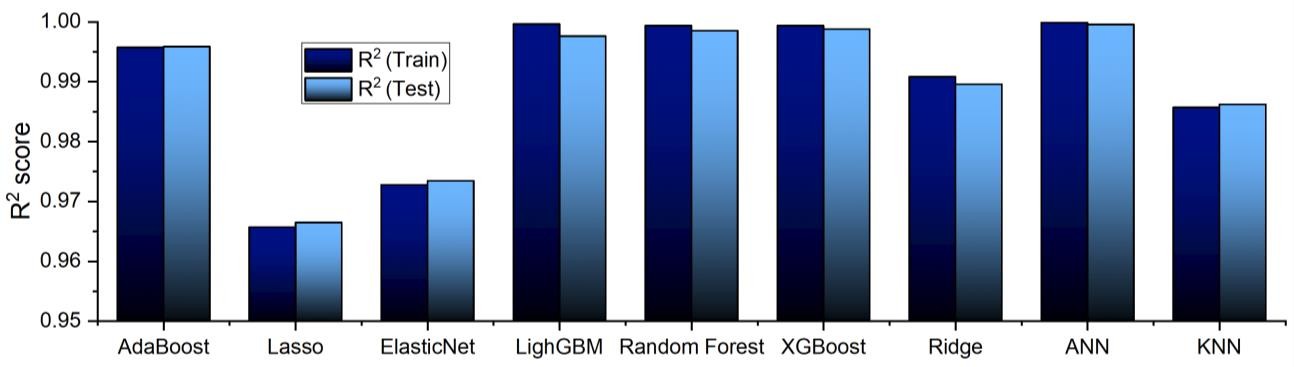


(d)

(e)

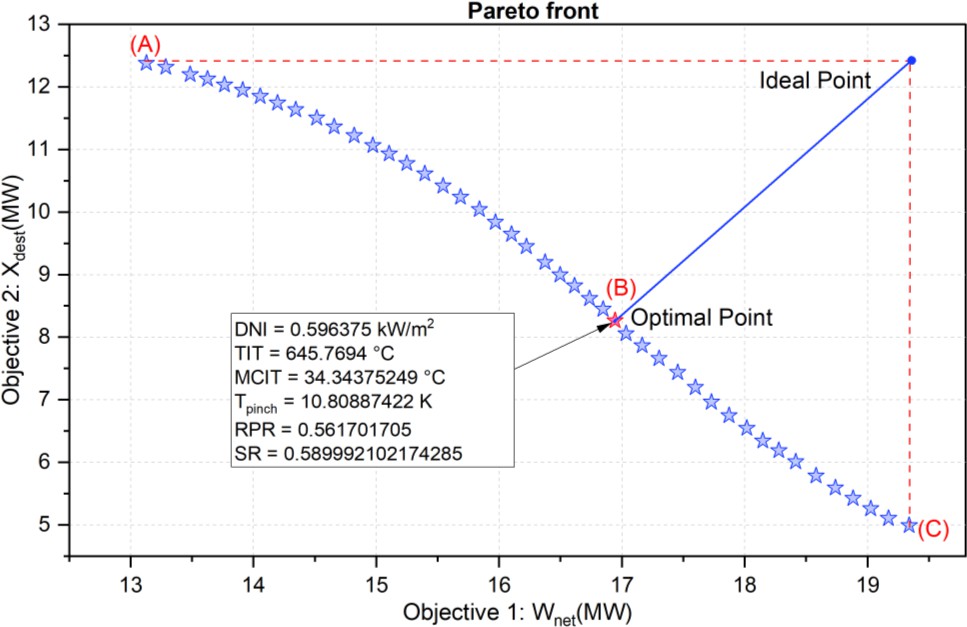
(f)

***Fig. 22.*** *Prediction result by for thermal efficiency(left), power output(mid) and exergy(right) efficiency of main compression intercooling cycle for (d)AdaBoost, (e)ANN, (f)KNN.*



***Fig. 23.*** *Prediction score (test & train) comparison of different machine learning models.*

# Optimization Result



The comprehensive list of the optimal design conditions generating the Pareto front for main-compression intercooling cycle (**Fig. 24**) is included in **Table 17**. Pareto front shows a reasonable compromise between Objective-1 (*Wnet*) and Objective-2 (*Xdest*) and displays the greatest ranges of the net power output. TOPSIS decision making tool is utilized for choosing optimized configurations. **Table 18** shows the conditions for (A) maximum exergy destruction, (B) optimal point & (C) maximum work output, obtained from pareto front diagram.

***Fig. 24.*** *Pareto front calculated by coupling ANN with a multi-objective genetic algorithm for INT sCO2BC.*

***Table 18:*** *Pareto front input & output variables for optimal & maximum points.*

|  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| Points | Condition | *DNI,*  *kW/m2* | MCIT,  *°C* | TIT,  *°C* | *Tpinch, K* | *RPR* | *SR* | *Wnet, MW* | *Xdest, MW* |
| (A) | Max. Exergy  Destruction | 0.565852 | 34.19028 | 629.6794 | 19.7702 | 0.883539 | 0.646379 | 13.12637 | 12.38015 |
| (B) | Optimal | 0.596375 | 34.34375 | 645.7694 | 10.80887 | 0.561702 | 0.589992 | 16.985 | 8.167 |
| (C) | Max. Work  Output | 0.653125 | 34.12277 | 660.998 | 9.078243 | 0.49408 | 0.566457 | 19.33925 | 4.99355 |

***Table 19:*** *Values of the input layer functions corresponding to the optimal solution obtained using TOPSIS.*

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| Optimization variables | Unit | Recompression | Partial cooling | Main compression  intercooling |
| Direct normal irradiance, *DNI* | *kW/m2* | 0.608273 | 0.621001 | 0.596375 |
| MCIT | *°C* | 40.328 | 34.047 | 34.344 |
| TIT | *°C* | 662.414 | 687.4 | 645.769 |
| Pinch temperature, *Tpinch* | *K* | 11.12 | 12.19 | 10.81 |
| Ratio of pressure ratios, *RPR* | *-* | - | 0.825 | 0.562 |
| Split ratio, *SR* | *-* | 0.6531 | 0.7106 | 0.5899 |
| Net power output, *Wnet* | *MW* | 15.561 | 16.902 | 16.985 |
| Thermal efficiency, ηcycle | *%* | 53.028 | 46.833 | 54.708 |
| Exergy destruction, *Xdest* | *MW* | 4.697 | 7.961 | 8.167 |
| Exergetic efficiency, *ηexergy* | *%* | 77.896 | 67.533 | 63.619 |

**Table 19** highlights the optimized parameters (DNI, MCIT, TIT, Tpinch, RPR, SR) obtained from this study using different tools for best cycle performance (*Wnet, ηcycle, Xdest, ηexergy*) for Recompression, Partial cooling & Main compression intercooling sCO2 cycle. The thermal efficiency of the optimized concentrated solar power (CSP) integrated main compression intercooling system exhibits an enhancement from 50.845% to 54.708%, resulting in a substantial increase of 7.59%. This improvement facilitates the generation of a greater amount of energy. Simultaneously, a reduction in the turbine inlet temperature from 675 K to 645.769 K is observed, indicating a better utilization of the heat source, while achieving a net power output of 16.985 MW. Furthermore, the optimized power cycle exhibits enhanced efficiency, as indicated by a notable 15.67% increase in exergy efficiency under the specified conditions. In regard to the recompression and partial cooling cycle, the optimized net power production is determined to be 15.561 MW and 16.902 MW, respectively. The aforementioned data provide evidence that the utilization of the optimization approach has shown to be effective in determining the ideal parametric values of the power plant, resulting in enhanced thermodynamic performance. However, it is worth noting that a slight variation in input data may yield different optimized values.

# Conclusion

In this study, an optimization method is proposed based on GA for predicting the physical state and thermodynamic performance of sCO2 power cycles from their design parameters. A comprehensive framework for numerical analysis and optimization is stated, considering CSP as heat source. To improve continuous power production when there is no solar insolation, the power block is equipped with TES. In addition, performance evaluations are made between three cycles in this work for solar power towers at the same solar subsystem (heliostats + receiver) conditions. The process of data collecting involves conducting calculations on recompression, partial cooling, and main compression intercooling in a sCO2 cycle. These calculations are performed to assess the effectiveness of machine learning models. A total of 17,248 cases were collected by altering the important parameters. Out of these cases, 70% were allocated for use in training. The determination of the optimum set of the design parameters is achieved through the integration of a trained artificial neural network (ANN) with a multi-objective genetic algorithm. According to the preceding work, the following are the conclusions:

* + - Thermodynamic analysis reveals that under specific operating conditions, main compression intercooling sCO2BC thermodynamic performance is better than the recompression and partial cooling cycle.
    - Exergy analysis reveals that that component with the greatest exergy destruction is the compressor (5837.5953 kW), making the compressor a crucial component of the sCO2 cycle and optimization procedure.
    - The impact of TES at night and the resulting system dynamic response is investigated as well. Heat rejection in the tower, tower outlet temperature, and net power generation are evaluated year-round under a variety of solar insolation and ambient temperature.
    - ANN outperformed Random Forest, XGBoost, LightGBM, AdaBoost, and KNN in predicting *ηcycle* and *Wnet*. ANN predicted 99% thermal efficiency and net power production data with 98% accuracy. When training sizes for complex systems are compared, the model still performs well when training sizes are reduced (from 70% to 50%), demonstrating that the model may lower the expense of sampling complicated systems.
    - Thermodynamic optimization has shown that the suggested system is capable of achieving the best power production and thermal efficiency, 16.985 MW and 54.708%, respectively, at 34.344°C of MCIT.

The sCO2 cycles presented in this paper can be investigated for use in waste heat recovery systems and nuclear reactors. Novel cycle configuration and operating conditions-independent models can be developed by global sensitivity analysis and optimization. Subsequently, the model needs previous sampling by modelling calculation in the design space, and research including active learning and transfer learning could reduce data required. These investigations would improve the efficiency and generalizability of ANN-GA based models for digital thermodynamic systems.

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# Declaration of interests

☒The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

☐The authors declare the following financial interests/personal relationships which may be considered as potential competing interests:

**Graphical Abstract**

