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Specifying and Executing Reactive Scenarios With Lutin

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**Abstract**

This paper presents the language Lutin and its operational semantics. This language specifically targets the domain of reactive systems, where an execution is a (virtually) infinite sequence of input/output reactions. More precisely, it is dedicated to the description and the execution of constrained random scenarios. Its first use is for test sequence specification and generation. It can also be useful for early simulation of huge systems, where Lutin programs can be used to describe and simulate modules that are not yet fully developed.

The programming style mixes relational and imperative features. Basic statements are input/output re- lations, expressing constraints on a single reaction. Those constraints are then combined to describe non deterministic sequences of reactions. The language constructs are inspired by regular expressions, and pro- cess algebra (sequence, choice, loop, concurrency). Moreover, the set of statements can be enriched with user defined operators. A notion of stochastic directive is also provided, in order to finely influence the selection of a particular class of scenarios.

*Keywords:* Reactive systems, synchronous programming, language design, test, simulation.

# Introduction

The targeted domain is the one of reactive systems, where an execution is a (vir- tually) infinite sequence of input/output reactions. Examples of such systems are control/command in industrial process, embedded computing systems in transporta- tion.

Testing reactive software raises specific problems. First of all, a single execution may require thousands of atomic reactions, and thus as many input vector values. It is almost impossible to write input test sequences by hand: they must be auto- matically generated according to some concise description. More specifically, the relevance of input values may depend on the behavior of the program itself: the program influences the environment which in turn influences the program. As a

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matter of fact, the environment behaves itself as a reactive system, whose environ- ment is the program under test. This feed-back aspect makes off-line test generation impossible: testing a reactive system requires to run it in a simulated environment. All these remarks have led to the idea of defining a language for describing random reactive systems. Since testing is the main goal, the programming style should be close to the intuitive notion of test scenarios, which means that the

language is mainly control-flow oriented.

Note that, even if testing is the main goal, such a language can be useful for other purposes. In particular, for early prototyping and simulation, where constrained random programs can implement missing modules.

For programming random systems, one solution is to use a classical (determin- istic) language together with a random procedure. In some sense, non-determinism is achieved by relaxing deterministic behaviors. We have adopted an opposite solu- tion where non-determinism is achieved by constraining chaotic behaviors; in other terms, the proposed language is mainly relational, not functional.

In the language Lutin, non-predictable atomic reactions are expressed as in- put/output relations. Those atomic reactions are combined using statements like sequence, loop, choice or parallel composition. Since simulation (execution) is the goal, the language also provides stochastic constructs to express that some scenarios are more interesting/realistic than others.

Since the first version [[10](#_bookmark15)], the language has evolved with the aim of being a user- friendly, powerful programming language. The basic statements (inspired by regular expressions), have been completed with more sophisticated control structures (par- allel composition, exceptions) and a functional abstraction has been introduced in order to provide modularity and reusability.

This work is indeed related to synchronous programming languages [[3](#_bookmark8)]. Some constructs of the language (traps and parallel composition) are directly inspired by the imperative synchronous language Esterel [[2](#_bookmark6)], while the relational part (con- straints) is inspired by the declarative language Lustre [[4](#_bookmark9)].

Related works are abundant in the domain of models for non-deterministic (or stochastic) concurrent systems: Input/Output automata [[7](#_bookmark11)], and their stochastic extension [[14](#_bookmark19)]; stochastic extension of process algebra [[6](#_bookmark12),[1](#_bookmark7)]. There are also relations with concurrent constraint programming [[12](#_bookmark17)], in particular with works that adopt a synchronous approach of time and concurrency [[13](#_bookmark18),[8](#_bookmark13)]. A general characteristic of these models is that they are defined to perform analysis of stochastic dynamic systems (e.g., model checking, probabilistic analysis). On the contrary, Lutin is designed with the aim of being a user-friendly programming language. On one hand, the language allows to concisely describe, and then execute a large class of scenarios. On the other hand, it is in general impossible to decide if a particular behavior can be generated and even less with which probability.

The paper is organized as follows: it starts with an informal presentation of the language. Then the operational semantics is formally defined in terms of constraints generator. Some important aspects, in particular constraints solving, are parameters of this formal semantics: they can be adapted to favor the efficiency or the expressive

power. These aspects are presented in the implementation section. Finally, we conclude by giving some possible extensions of this work.

# Overview of the language

* 1. *Reactive, synchronous systems*

The language is devoted to the description of reactive systems. Those systems have a cyclic behavior: they react to input values by producing output values and updating their internal state. We adopt the synchronous approach, which in this case simply means that the execution is viewed as a sequence of pairs “input values/output values”.

Such a system is declared with its input and output variables; they are called the *support variables* of the system.

**Example 2.1** We illustrate the language with a simple program that receives a Boolean input (c) and a real input (t) and produces a real output x. The high-level specification is that x should get closer to t when c is true, or should tend to zero otherwise. The header of the program is:

system foo(c: bool; t: real) returns (x: real) = *statement* The core of the program consists of a *statement* describing the program behavior. The definition of *statement* is developed later.

During the execution, inputs are provided by the environment: they are called *uncontrollable variables*. The program reacts by producing outputs: they are called *controllable variables*.

* 1. *Variables, reactions and traces*

The core of the system is a statement describing a sequence of atomic reactions. In Lutin, a reaction is not deterministic: it does not define precisely the out-

put values, but states *constraints* on these values. For instance, the constraint

((x > 0.0) and (x < 10.0)) states that the current output should be some value comprised between 0 and 10.

Constraints may involve inputs, for instance: ((x > t - 2.0) and (x < t)). In this case, during the execution, the actual value of t is substituted, and the resulting constraint is solved.

In order to express temporal constraints, *previous values* can be used: pre *id* de- notes the value of the variable *id* at the previous reaction. For instance (x > pre x)

states that x must increase in the current reaction. Like inputs, pre variables are uncontrollable: during the execution, their values are inherited from the past and cannot be changed: this is the *non-backtracking principle*.

Performing a reaction consists in producing, if it exists, a particular solution of the constraint. Such a solution may not exist.

**Example 2.2** Consider the constraint:

(c and (x > 0.0) and (x < pre x + 10.0))

where c (input) and pre x (past value) are uncontrollable. During the execution, it may appear that c is false and/or that pre x is less than *−*10*.*0. In those cases, the constraint is unsatisfiable: we say that the constraint *deadlocks*.

Local variables may be useful auxiliaries for expressing complex constraints.

They can be declared within a program:

local *ident* : *type* in *statement*

A local variable behaves as a hidden output: it is controllable and must be produced as long as the execution remains in its scope.

* 1. *Composing reactions*

A constraint (Boolean expression) represents an atomic reaction: it defines the rela- tions between the current values of the variables. Scenarios are built by combining such atomic reactions *temporal statements*. We introduce the type trace for typing expressions made of temporal statements. A single constraint obviously denotes a trace of length 1; in other terms, expressions of type bool are implicitly cast to type trace when combined with temporal operators.

The basic trace statements are inspired by regular expression:

* + - sequence (fby: trace *×* trace *→* trace),
    - unbounded loop (loop: trace *→* trace)
    - non-deterministic choice (|: trace *×* trace *→* trace).

Because of this design choice, the notion of sequence differs from the one of Esterel, which is certainly the reference in control-flow oriented synchronous language[[2](#_bookmark6)]. In Esterel, the sequence (semicolon) is instantaneous, while the Lutin construct fby “takes” one instant of time, just like in classical regular expressions.

**Example 2.3** With those operators, we can propose a first version for our example. In this version, the output tends to 0 or t according to a first order filter. The non- determinism resides in the initial value, and also in the fact that the system is subject to failure and may miss the c command.

((-100.0 < x) and (x < 100.0)) fby *-- initial constraint*

loop {

(c and (x = 0.9\*(pre x) + 0.1\*t)) *-- x gets closer to t*

| ((x = 0.9\*(pre x)) *-- x gets closer to 0*

}

Initially, the value of x is (randomly) chosen between -100 and +100, then, forever, it may tend to t or to 0.

Note that, inside the loop, the first constraint (x tends to t) is not satisfiable unless c is true, while the second is always satisfiable. If c is false, the first constraint *deadlocks*. In this case, the second branch (x gets closer to 0) is necessarily taken. If c is true, both branches are feasible: one is randomly selected, and the corresponding constraint is solved.

This illustrates an important principle of the language: the *reactivity principle*

states that a program may only deadlock if all its possible behaviors deadlock.

* 1. *Traces, termination and deadlocks*

Because of non-determinism, a behavior has in general several possible first reactions (constraints). According to the reactivity principle, it deadlocks only if all those constraints are not satisfiable. If at least one reaction is satisfiable, it must “do something”: we say that it is *startable*.

Termination, startability and deadlocks are important concepts of the language; here is a more precise definition of the basic statements according to these concepts:

* + - A constraint *c*, if it is satisfiable, generates a particular solution and terminates, otherwise it deadlocks.
    - *st1* fby *st2* executes *st1*, and, if and when it terminates, executes *st2*. If *st1*

deadlocks, the whole statement deadlocks.

* + - loop *st*, if *st* is startable, behaves as *st* fby loop *st*, otherwise it terminates. Intuitively, the meaning is “loop as long as possible”.
    - {*st1* |... |*stn* } randomly chooses one of the *startable* statements from *st1*...*stn*. If none of them are startable, the whole statement deadlocks.
    - The priority choice {*st1* |>... |>*stn* } behaves as *st1* if *st1* is startable, otherwise behaves as *st2* if *st2* is startable, etc. If none of them are startable, the whole statement deadlocks.
    - try *st1* do *st2* catches any deadlock occurring *during the execution* of *st1* (not only at the first step). In case of deadlock, the control passes to *st2*.
  1. *Well-founded loops*

Let’s denote by *ε* the identity element for fby (i.e. the unique behavior such that b fby *ε* = *ε* fby b = b). Although this “empty” behavior is not provided by the language, it is helpful for illustrating a problem raised by nested loops.

As a matter of fact, the simplest way to define the loop is to state that “loop c” is equivalent to “c fby loop c |>*ε*”, that is, try in priority to perform one iteration, and if it fails, stop. According to this definition, nested loops may generate infinite, instantaneous loops, as shown in the following example:

**Example 2.4** loop {loop *c*}

Performing an iteration of the outer loop consists in executing the inner loop loop *c*. If *c* is not currently satisfiable, loop *c* terminates immediately, and thus, the iter- ation is actually “empty”: it generates no reaction. However, since it is not a deadlock, this strange behavior is considered by the outer loop as a normal itera- tion. As a consequence, another iteration is performed, which is also empty, and so on: the outer loop keeps the control forever but does nothing.

One solution is to state that such programs are incorrect. Statically checking whether a program will infinitely loop or not is undecidable: it may depend on

arbitrarily complex conditions. Some over-approximation is necessary, which will (hopefully) reject all the incorrect programs, but also lots of correct ones. For instance, a program as simple as: “loop *{ {*loop a*}* fby *{*loop b *} }*” will certainly be rejected as potentially incorrect.

We think that such a solution is too much restrictive and tedious for the user, and we prefer to slightly modify the semantics of the loop. The solution retained is to introduce the *well-founded loop principle*: a loop statement may stop or continue, but if it continues it must do something. In other terms, empty iterations are dynamically forbidden.

The simplest way to explain this principle is to introduce an auxiliary operator *st \ε*: if *st* terminates immediately, *st \ε* deadlocks, otherwise it behaves as *st*. The correct definition of loop *st* follows:

* + - if *st \ε* is startable, behaves as *st \ε* fby loop *st*,
    - otherwise terminates.
  1. *Influencing non-determinism*

When executing a non-deterministic statement, the problem of which choice should be preferred arises. The default is that, if *k* out of the *n* choices are startable, each of them is chosen with a probability 1*/k*.

In order to influence this choice, the language provides a mechanism of *relative weights*:

{*st1* weight *w1* |... |*stn* weight *wn* }

Weights are basically integer constants, and their interpretation is straightforward: a branch with a weight 2 has twice the chance to be tried than a branch with weight

1. More generally, a weight can depend on the environment and on the past: it is given as a integer expression depending on uncontrollable variables. In this case, weight expressions are dynamically evaluated before performing the choice.

**Example 2.5** In a first version (example [2.3](#_bookmark1)), our example system may ignore the command c with a probability 1*/*2. This case can be made less probable by using weights (when omitted, a weight is implicitly 1):

loop {

(c and (x = 0.9\*(pre x) + 0.1\*t)) weight 9

| ((x = 0.9\*(pre x))

}

In this new version, a true occurrence of c is missed with the probability 1*/*10.

Note that weights are not only directives. Even with a big weight, a non startable branch has a null probability to be chosen, which is the case in the example when c is false.

* 1. *Random loops*

We want to define some loop structure where the number of iterations is not fully determined by deadlocks. Such a construct can be based on weighted choices, since a loop is nothing but a binary choice between stopping and continuing. However, it seems more natural to define it in terms of expected number of iterations. Two loop “profiles” are provided:

* + - loop[*min*,*max*]: the number of iterations should be between the constants *min*

and *max*

* + - loop~*av*:*sd*: the average number of iteration should be *av*, with a standard devi- ation *sd*.

Note that random loops, just like other non-deterministic choices, follow the *re-* *activity principle*: depending on deadlocks, looping may sometimes be required or impossible. As a consequence, during an execution, the actual number of iterations may significantly differ from the “expected” one (see *§*[3](#_bookmark2),*§*[4.2](#_bookmark5)).

Moreover, just like the basic loop, they follow the *well-founded loop principle*, which means that, even if the core contains nested loops, it is impossible to perform “empty” iterations.

* 1. *Parallel composition*

The parallel composition of Lutin is synchronous: each branch produces, at the same time, its local constraint. The global reaction must satisfy the conjunction of all those local constraints. This approach is similar to the one of temporal concurrent constraint programming [[8](#_bookmark13)].

The termination of the concurrent execution is directly inspired by the language Esterel. During the execution:

* + - if one or more branches abort (deadlock), the whole statement aborts,
    - otherwise, the parallel composition terminates if and when all the branches have terminated.

The concrete syntax suggests a non-commutative operator, this choice is explained in the next section.

{ *st1* &> ... &>*stn* }

* 1. *Parallel composition versus stochastic directives*

It is impossible to define a parallel composition which is fair according to the stochas- tic directives (weights), as shown in the following example.

**Example 2.6** Consider the statement:

{ {*X* weight 1000 |*Y* } &> {*A* weight 1000 |*B* } } where *X*, *A*, *X∧B*, *A∧Y* are all startable, but not *X∧A*. The higher priority can be given to:

* + - *X∧B*, but it does not respect the stochastic directive of the second branch,
    - *A∧Y*, but it does not respect the stochastic directive of the first branch.

In order to solve the problem, the stochastic directives are not treated in parallel, but in *sequence*, from left to right:

* + - the first branch “plays” first, according its local stochastic directives,
    - the second one makes its choice, according to what has been chosen by the first one etc.

In the example, the priority is then given to *X∧B*.

The concrete syntax (&>) has been chosen to reflect the fact that the operation is not commutative: the treatment is parallel for the constraints (conjunction), but sequential for stochastic directives (weights).

* 1. *Exceptions*

User-defined exceptions are mainly a means for by-passing the normal control flow. They are inspired by exceptions in classical languages (Ocaml, Java, Ada) and also by the trap signals of Esterel.

Exceptions can be globally declared outside a system ( exception *ident* ) or

locally within a statement, in which case the standard binding rules hold:

exception *ident* in *st*

An existing exception *ident* can be raised with the statement:

raise *ident*

and caught with the statement:

catch *ident* in *st1* do *st2*

If the exception is raised in *st1*, the control immediately passes to *st2*. The do part may be omitted, in which case the control passes in sequence.

* 1. *Modularity*

An important point is that the notion of system is not a sufficient modular abstrac- tion. In some sense, systems are similar to main programs in classical languages: they are entry point for the execution but are not suitable for defining “pieces” of behaviors.

## Data combinators.

A good modular abstraction would be one that allows to enrich the set of com- binators. Allowing the definition of data combinators is achieved by providing a functional-like level in the language. For instance, one can program the useful “within an interval” constraint:

let within(x, min, max : real) : bool = (x >= min) and (x <= max)

Once defined, this combinator can be instantiated, for instance:

within(a, 0.8, 0.9)

or

within(a + b, c - 1.0, c + 1.0)

Note that such a combinator is definitively not a function in the sense of com- puter science: it actually computes nothing. It is rather a well typed *macro* defining how to build a Boolean expression with three real expressions.

## Reference arguments.

Some combinators specifically require support variables as argument (input, out- put, local). This is the case for the operator pre, and, as a consequence, for any combinator using a pre. This situation is very similar to the distinction between “by reference” and “by value” parameters in imperative languages. We classically solve the problem by adding the flag ref to the type of such parameters.

**Example 2.7** The following combinator defines the generic first order filter con- straint. The parameter y must be a real support variable (bool ref) since its previous value is required. The other parameters can be any expressions of type real.

let fof (y: real ref; gain, x: real) : bool = (y = gain\*(pre y) + (1.0-gain)\*x)

## Trace combinators.

User-defined temporal combinators are simply macros of type trace.

**Example 2.8** The following combinator is a binary parallel composition where the termination is enforced when the second argument terminates:

let as long as(X, Y : trace) : trace = exception Stop in

catch Stop in {

X &> {Y fby raise Stop}

}

## Local combinators.

A macro can be declared within a statement, in which case the classical binding rules hold; in particular, a combinator may have no parameter at all.

let *id* (*params*): *type* = *statement* in *statement*

**Example 2.9** We can now write more elaborated scenarios for the system of ex- ample [2.3](#_bookmark1). In this new version, the system works almost properly for about 1000 reactions: if c is true, x tends to t 9 times out of 10, otherwise it tends to 0. During this phase, the gain for the filters (a) randomly changes each 30 to 40 reactions. At last, the system breaks down and x quickly tends to 0.

system foo(c: bool; t: real) returns (x: real) = within(x, -100.0, 100.0) fby

local a: real in

let gengain() : trace = loop {

within(a, 0.8, 0.9) fby loop[30,40] (a = pre a)

} in aslongas (

gengain(), loop~1000:100 {

(c and fof(x, a, t)) weight 9

| fof(x, a, 0.0)

}

) fby

loop fof(x, 0.7, 0.0)

The following timing diagram shows an execution of this program. Inputs values are provided by the environment (i.e., us) according to the following specification:

* the input t is constant (150),
* the command c toggles each about 100 steps.

160

140

120

100

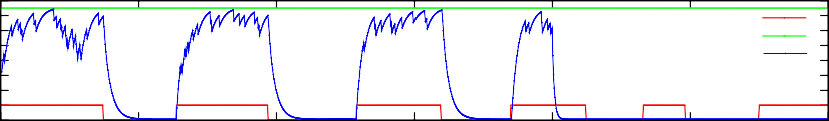
80

60

40

20

0



\_c

\_t

\_x

0 200 400 600 800 1000 1200

steps

# Operational semantics

* 1. *Abstract syntax*

For the sake of simplicity, the semantics is given on the flat language (user defined macros are inlined). We use the following abstract syntax for trace expression, where the intuitive meaning of each construct is given as a comment:

*t* ::= *c (constraint) | ε (empty behavior) | t \ ε (empty filter) | t · t (sequence)*

*| t∗ (priority loop) | t*(*ωc,ωs*) *(random loop) |*

*k*

*i*=1

*x* *x*

*(raise) | t ‹→*

*‹→*

[

*i*=1

*t'*] *(catch)*

*n i*=1

*| >*

*ti (priority) | |n*

*ti/wi (choice) |* &*n*

*ti (parallel)*

This abstract syntax slightly differs from the concrete one on the following points:

* the empty behavior (*ε*) and the empty behavior filter (*t\ε*) are internal constructs that will ease the definition of the semantics,
* random loops are *normalized* by making explicit their weight functions:
  + the stop function *ωs* takes the number of already performed iterations and returns the relative weight of the “stop” choice,
  + the continue function *ωc* takes the number of already performed iterations and returns the relative weight of the “continue” choice.

These functions are completely determined by the loop profile in the concrete program (interval or average, together with the corresponding static arguments). See *§*[4.2](#_bookmark5) for a precise definition of these weight functions.

* the number of already performed iterations (*k*) is syntactically attached to the loop; this is convenient to define the semantics in terms of rewriting (in the initial program, this number is obviously set to 0).

**Definition 3.1** *T* denotes the set of trace expressions (as defined above), and *C*

the set of constraints.

* 1. *The execution environment*

The execution takes place within an environment which stores the variable values (inputs and memories). Constraint resolution, weight evaluation and random selec- tion are also performed by the environment. We keep this environment abstract. As a matter of fact, resolution capabilities and (pseudo)random generation may vary from one implementation to another, and they are not part of the reference semantics.

The semantics is given in term of constraints generator. In order to generate constraints, the environment should provide the two following procedures:

**Satisfiability.** The predicate *e |*= *c* is true iff the constraint *c* is satisfiable in the environment *e*.

**Priority sort.** Executing choices first requires to evaluate the weights in the envi- ronment. This is possible (and straightforward) because weights may dynamically depends on uncontrollable variables (memories, inputs), but not on controllable variables (outputs, locals). Some weights may be evaluated to 0, in which case the corresponding choice is forbidden. Then a random selection is made, according to the actual weights, to determine a total order between the choices.

For instance, consider the following list of pairs (trace/weight), where *x* and *y*

are uncontrollable variables:

(*t*1*/x* + *y*)*,* (*t*2*/*1)*,* (*t*3*/y*)*,* (*t*4*/*2)

In a environment where *x* = 3 and *y* = 0, weights are evaluated to:

(*t*1*/*3)*,* (*t*2*/*1)*,* (*t*3*/*0)*,* (*t*4*/*2)

The choice *t*3 is erased, and the remaining choices are randomly sorted according to their weights. The resulting (total) order may be:

* *t*1*, t*2*, t*4 with a probability 3*/*6 *×* 1*/*3 = 1*/*6
* *t*1*, t*4*, t*2 with a probability 3*/*6 *×* 2*/*3 = 1*/*3
* *t*4*, t*1*, t*2 with a probability 2*/*6 *×* 3*/*4 = 1*/*4
* etc.

All these treatments are “hidden” within the function *Sorte* which takes a list of pairs (choice/weights) and returns a totally ordered list of choices.

* 1. *The step function*

An execution step is performed by the function *Step*(*e, t*), taking an environment *e*

and a trace expression *t*. It returns an *action* which is either:

* + - a transition *→c n*, which means that *t* produces a *satisﬁable* constraint *c* and rewrite itself in the (next) trace *n*,

*‹→*

* + - a termination *x*, where *x* is a termination flag which is either *ε* (normal termi-

nation), *δ* (deadlock) or some user-defined exception.

**Definition 3.2** *A* denotes the set of actions, and *X* denotes the set of termination flags.

* 1. *The recursive step function*

The step function *Step*(*e, t*) is defined via a recursive function *Se*(*t, g, s*) where the parameters *g* and *s* are continuation functions returning actions:

* + - *g* : *C × T '→ A* is the *goto* function, defining how a local transition should be treated according to the calling context.
    - *s* : *X '→A* is the *stop* function, defining how a local termination should be treated

according to the calling context.

At the top-level, *Se* is called with the trivial continuations:

*Step*(*e, t*)= *Se*(*t, g, s*) with *g*(*c, v*) = *→c v* and *s*(*x*) = *x*

*‹→*

**Basic traces.** The empty behavior raises the termination flag in the current con- text. A raise statement terminates with the corresponding flag. At last, a constraint generates a goto or raises a deadlock, depending on its satisfiability.

*Se*(*ε, g, s*)= *s*(*ε*)

*Se*( *x, g, s*)= *s*(*x*)

*‹→*

*Se*(*c, g, s*)= if (*e |*= *c*) then *g*(*c, ε*) else *s*(*δ*)

**Sequence.** The rule is straightforward:

*Se*(*t · t', g, s*)= *Se*(*t, g', s'*) where:

*g'*(*c, n*)= *g*(*c, n · t'*)

*s'*(*x*)= if *x* = *ε* then *Se*(*t', g, s*) else *s*(*x*)

**Priority choice.** We only give the definition of the binary choice, since the operator is right-associative. This rule formalizes the reactivity principle: all possibilities in *t* must have failed before *t'* is taken into account.

*Se*(*t > t', g, s*) = if (*r /*= *δ*) then *r* else *Se*(*t', g, s*) where *r* = *Se*(*t, g, s*)

*‹→*

**Empty filter and priority loop.** The empty filter intercepts the termination of

*t* and replaces it by a deadlock:

*Se*(*t \ ε, g, s*) = *Se*(*t, g, s'*) where *s'*(*x*) = if (*x* = *ε*) then *s*(*δ*) else *s*(*x*) The semantics of the loop results from the equivalence:

*t∗ ⇔* (*t \ ε*) *· t∗ > ε*

**Catch.** This internal operator ([*n ‹z*

*→*

*t*]) covers the cases of try (*z* = *δ*) and catch

(*z* is a user-defined exception):

*S* ([*t ‹ t'*]*, g, s*)= *S* (*t, g', s'*) where:

*z*

*e → e*

*g'*(*c, n*)= *g*(*c,* [*n ‹z t'*])

*→*

*s'*(*x*)= if (*x* = *z*) then *Se*(*t', g, s*) else *s*(*x*)

**Parallel composition.** We only give the definition of the binary case, since the operator is right-associative.

*Se*(*t* & *t', g, s*)= *Se*(*t, g', s'*) where:

*s'*(*x*)= if (*x* = *ε*) then *Se*(*t', g, s*) else *s*(*x*)

and *g'*(*c, n*)= *Se*(*t', g'', s''*) where:

*s''*(*x*)= if (*x* = *ε*) then *g*(*c, n*) else *s*(*x*)

*g''*(*c', n'*)= *g*(*c ∧ c',n* & *n'*)

**Weighted choice.** The evaluation of the weights, and the (random) total ordering of the branches, are both performed by the function *Sorte* (cf. *§*[3.2](#_bookmark3)).

if *Sorte*(*{ti/wi}i*=1*···n*) = *∅*: *Se*(*|n*

*i*=1

otherwise: *Se*(*|n*

*i*=1

*ti/wi, g, s*)= *s*(*δ*)

*ti/wi, g, s*)= *Se*(*> Sorte*(*t*1*/w*1*, ··· , tn/wn*)*, g, s*)

**Random loop.** We recall that this construct is labelled by two weight functions (*ωc* for continue, *ωs* for stop) and by the current number of already performed iterations

(*i*). The weight functions are evaluated for *i*, and the statement is then equivalent to a binary weighted choice:

(*ωc,ωs*)

*t*

*i*

*⇔* (*t \ ε*) *· t*(*ωc,ωs*)*/ωc*(*i*) *| ε/ωs*(*i*)

Note that the semantics follows the well-founded loop principle.

*i*+1

* 1. *A complete execution*

**Solving a constraint.** The main role of the environment is to store the values of uncontrollable variables: it is a pair of stores “(past values, input values)”. For such an environment *e* = (*ρ, ι*), and a satisfiable constraint *c*, we suppose given a procedure able to produce a particular solution of *c*: *Solveρ,ι*(*c*) = *γ* (where *γ* is a store of controllable variables). We keep this *Solve* function abstract, since it may vary from one implementation to another (see *§*[4](#_bookmark4)).

**Execution algorithm.** A complete run is defined according to:

* + - a given sequence of input stores *ι*0*, ι*1*, ··· , ιn*,
    - an initial (main) trace *t*0,
    - an initial previous store (values of pre variables) *ρ*0

A run produces a sequence of (controllable variables) stores *γ*1*, γ*2*, ..., γk*, where *k ≤ n*. For defining this output sequence, we use intermediate sequences of traces (*t*1*, ··· , tk*+1), previous stores (*ρ*1*, ··· , ρk*), environments (*e*0*, ··· , ek*), and con- straints (*c*0*, ··· , ck*). The relation between those sequences are listed below, for all step *j* = 0 *··· k*:

* + - the current environment is made of previous and input values: *ej* = (*ρj, ιj*)
    - the current trace makes a transition: *e t cj t*

:

*j j→ j*+1

* + - a solution of the constraint is elected: *γj* = *Solveej* (*cj*)
    - the previous store for the next step is the union of current inputs/outputs: *ρj*+1 =

(*ιj ⊕ γj*)

At the end, we have:

* + - either *k* = *n*, which means that the execution has run to completion,

*‹→*

* + - or (*ρk*+1

*, ιk*+1

) : *t*

*k*+1

*x* which means that it has been aborted.

# Implementation

A prototype has been developed, which implements the operational semantics pre- sented in the previous section. This tool can:

* + - interpret/simulate Lutin programs in a file-to-file (or pipe-to-pipe) manner. This tool serves for simulation/prototyping: several Lutin simulation sessions can be combined with other reactive process in order to animate a complex system.
    - compile Lutin programs into the internal format of the testing tool Lurette. This format, called Lucky, is based on flat, explicit automata [[9](#_bookmark14)]. In this case, Lutin serves as a high-level language for designing test scenarios.
  1. *Notes on constraint solvers*

The core semantics only defines how constraints are generated, but not how they are solved. This choice is motivated by the fact that there is no “ideal” solver.

A required characteristic of such a solver is that it must provide a constructive, complete decision procedure: methods that can fail and/or that are not able to exhibit a particular solution are clearly not suitable. Basically, a constraint solver should provide:

* + - a syntactic analyzer for checking if the constraints are supported by the solver (e.g. linear arithmetics); this is necessary because the language syntax allows to write arbitrary constraints,
    - a decision procedure for the class of constraints accepted by the checker,
    - a precise definition of the election procedure which selects a particular solution (e.g. in terms of fairness).

Even with those restriction, there is no obvious best solver:

* + - it may be efficient but limited in terms of capabilities,
    - it may be powerful, but likely to be very costly in terms of time and memory.

The idea is that the user may choose between several solvers (or several options of a same solver) the one which best fits his needs.

Actually, we use the solver that have been developed for the testing tool Lurette [[11](#_bookmark16),[5](#_bookmark10)]. This solver is quite powerful, since it covers Boolean algebra and linear arithmetics. Concretely, constraints are solved by building a canonical repre- sentation mixing Binary Decision Diagrams and convex polyhedra.

Because it is very powerful, this method is also costly. However the solver ben- efits from several years of experimentation and optimizations (partitioning, switch form polyhedra to intervals whenever it is possible).

The election of a particular solution is also quite sophisticated:

* The basic rule is to ensure some fairness between the solutions. This is achieved by simulating a uniform choice among the set of solutions. Since uniform selection within a polyhedron is a complex problem, several options are available ranging from a simple, rough approximation to a very accurate, and thus costly one.
* The solver can also be parameterized to select some class of interesting solutions (e.g. limit values corresponding to the polyhedra vertices).
  1. *Notes on predeﬁned loop proﬁles*

In the operational semantics, loops with iteration profile are translated into bi- nary weighted choices. Those weights are dynamic: they depend on the number of (already) performed iterations *k*.

**Interval loops.** For the “interval” profile, those weights functions are formally defined, and thus, they could take place in the reference semantics of the language. For a given pair of integer (*min, max*), such that 0 *≤ min ≤ max*, and a number *k* of already performed iterations, we have:

* + - if *k < min* then *ωs*(*k*) = 0 and *ωc*(*k*) = 1 (loop is mandatory),
    - if *k ≥ max* then *ωs*(*k*) = 1 and *ωc*(*k*) = 0 (stop is mandatory),
    - if *min ≤ k < max* then *ωs*(*k*) = 1 and *ωc*(*k*) = 1 + *max − k*

**Average loops.** There is no obvious solution for implementing the “average” profile in terms of weights. A more or less sophisticated (and accurate) solution should be retained, depending on the expected precision.

In the actual implementation, for an average value *av* and a standard variation

*sv*, we use a relatively simple approximation:

* + - First of all, the underlying discrete repartition law is approximated by a contin- uous (Gaussian) law. As a consequence, the result will not be accurate if *av* is too close to 0, and/or if *st* is too big comparing to *av*. Concretely we must have 10 *<* 4 *∗ sv < av*.
    - It is well known that it does not exist any algebraic definition for the Gaussian repartition function. This function is then classically approximated by using an interpolation table (512 samples with a fixed precision of 4 digits).

# Conclusion

We propose a language for describing constrained-random reactive systems. Its first purpose is to describe test scenarios, but it may also be useful for prototyping and simulation.

We have developed a compiler/interpreter which strictly implements the oper- ational semantics presented here. Thanks to this tool, the language is integrated into the framework of the Lurette tool, where it is used to describe test scenar-

ios. Further works concerns the integration of the language within a more general prototyping framework.

Other works concern the evolution of the language. We plan to introduce a notion of signal (i.e. event), which is useful for describing values that are not always available (this is related to the notion of clocks in synchronous languages). We also plan to allow the definition of (mutually) tail-recursive traces. Concretely, that means that a new programming style would be allowed, based on explicit concurrent, hierarchic automata.

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