

1. Multiple choice. Circle all that apply.

(a) [3 pts] If a particle moves along a straight line, what can you say about its acceleration vector?

- (i) The acceleration vector is parallel to the tangent vector.
- (ii) The acceleration vector has magnitude equal to one.
- (iii) The acceleration vector equals the velocity vector.
- (iv) The acceleration vector is parallel to the unit normal vector.
- (v) The acceleration vector has a magnitude equal to zero.

(b) [3 pts] If a particle moves with constant speed along a curve, what can you say about its acceleration vector?

- (i) The acceleration vector is parallel to the tangent vector.
- (ii) The acceleration vector has a magnitude of one.
- (iii) The acceleration vector equals the velocity vector.
- (iv) The acceleration vector is parallel to the unit normal vector.
- (v) The acceleration vector has a magnitude of zero.

(c) [3 pts] Let  $\mathbf{r}_1(t)$  and  $\mathbf{r}_2(t)$  be two parametrizations of the same space curve  $\mathcal{C}$ . Then at any time  $t$  the velocity vectors  $\mathbf{v}_1(t)$  and  $\mathbf{v}_2(t)$  are equal.

- (i) True.
- (ii) False.
- (iii) Indeterminable.

2. A leaf tumbles down following the curve of intersection between the hyperbolic paraboloid  $z = x^2 - y^2$  and the cylinder  $x^2 + y^2 = 64$ .

(a) [3 pts] Find a vector-valued function  $\mathbf{r}(t)$  that parametrizes the path taken by the falling leaf.

(b) [3 pts] How far does the *shadow* (i.e. the projection of the space curve  $\mathbf{r}(t)$  onto the  $xy$ -plane) of the leaf travel from  $t = 0$  to  $t = \pi$ ?

3. [4 pts] Consider the space curve  $\mathcal{C}$  parametrized by

$$\mathbf{r}(t) = \begin{bmatrix} 3\sin(t) \\ \cos(t) - \sin(t) \\ -3\cos(t) + 6 \end{bmatrix} \quad -\infty < t < \infty$$

Show that  $\mathcal{C}$  lies entirely in a single plane. Provide an equation for the plane.