

1. [6 pts] Consider the double integral

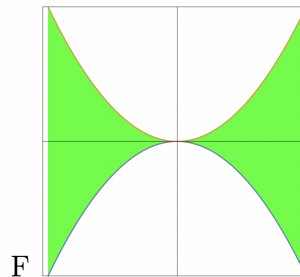
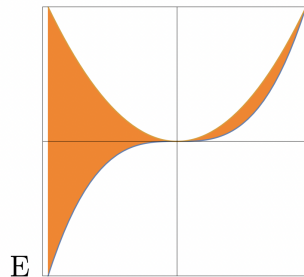
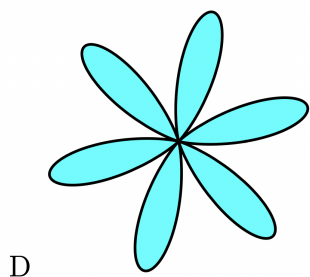
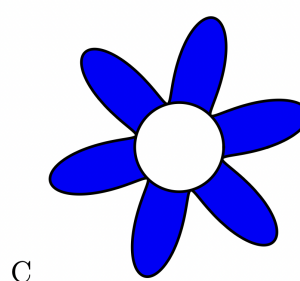
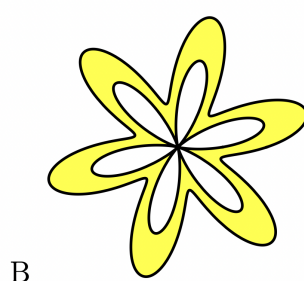
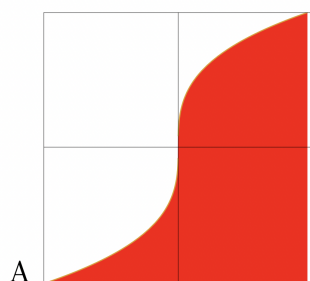
$$\mathbf{I} = \int_{-1}^1 \int_0^{1-x^2} \sqrt{1-y} \, dy \, dx$$

- (a) [3 pts] Sketch the region R of integration.

- (b) [3 pts] Switch the order of integration and rewrite the integral \mathbf{I} with the y -variable being outermost and x -variable being innermost.

- (c) [3 pts] Evaluate the integral \mathbf{I} .

2. [12 pts] Match each picture below with the double integral that computes the area of the region.



Enter A – F	Integral
	$\int_0^{2\pi} \int_0^{1+\sin(6\theta)} r dr d\theta$
	$\int_{-1}^1 \int_{y^3}^1 dx dy$
	$\int_{-1}^1 \int_{x^3}^{x^2} dy dx$
	$\int_{-1}^1 \int_{-x^2}^{x^2} dy dx$
	$\int_0^{2\pi} \int_{1+\sin(6\theta)}^{2+\sin(6\theta)} r dr d\theta$
	$\int_0^{2\pi} \int_1^{2+\sin(6\theta)} r dr d\theta$