

1. [10 pts] Integrate the function

$$f(x, y, z) = z(x^2 + y^2 + z^2)^{-3/2}$$

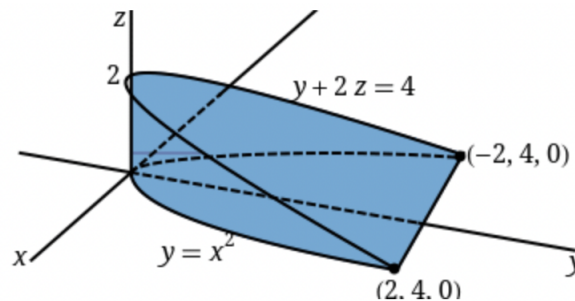
over the part of the ball  $x^2 + y^2 + z^2 \leq 16$  defined by  $z \geq 2$ .

2. [8 pts] Let  $E$  be the solid which lies inside both the sphere  $x^2 + y^2 + z^2 = 4$  and the cylinder  $(x - 1)^2 + y^2 = 1$ . Express the volume of  $E$  as a triple integral. Do **not** evaluate your expression.

3. Let  $E$  be the solid region bounded by the three surfaces in  $\mathbb{R}^3$ :

$$y = x^2, \quad z = 0, \quad y + 2z = 4$$

The solid  $E$  is pictured below:



By filling in the empty boxes with the appropriate limit of integration, express the volume of  $E$  as an iterated integral in two different ways.

(a) [5 pts]  $\int_0^{\boxed{\phantom{000}}} \int_0^{\boxed{\phantom{000}}} \int_{-\sqrt{y}}^{\boxed{\phantom{000}}} dx \, dz \, dy$

(b) [5 pts]  $\int_{\boxed{\phantom{000}}}^{\boxed{\phantom{000}}} \int_{\boxed{\phantom{000}}}^{\boxed{\phantom{000}}} \int_{\boxed{\phantom{000}}}^{\boxed{\phantom{000}}} dy \, dz \, dx$