

## Definition of Number Systems

$$\mathbb{N} = \{x \mid x = 1 \text{ or } (\exists i, j \in \mathbb{N} : x = i + j)\}$$

$$\mathbb{N}_0 = \mathbb{N} \cup \{0\}$$

$$\mathbb{Z} = \{a - b \mid a, b \in \mathbb{N}\}$$

$$\mathbb{Q} = \left\{ \frac{a}{b} \mid a \in \mathbb{Z} \text{ and } b \in \mathbb{Z} \setminus \{0\} \right\}$$

$$\mathbb{R} = \left\{ \lim_{n \rightarrow \infty} a(n) \mid a : \mathbb{N} \rightarrow \mathbb{Q} \text{ s.t. } \forall \epsilon > 0 : \exists \{N, n\} \subseteq \mathbb{N} \text{ s.t. } \forall n > N, |a(n) - a(N)| < \epsilon \right\}$$

$$\overline{\mathbb{R}} = \mathbb{R} \cup \{-\infty, +\infty\}$$

$$\mathbb{C} = \{a + bi \mid a, b \in \mathbb{R} \text{ and } i = \sqrt{-1}\}$$