

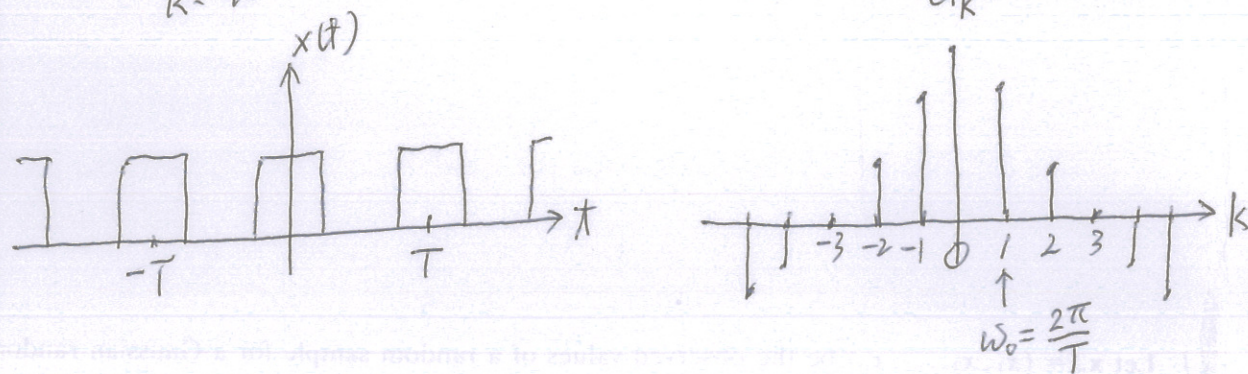
continuous

periodic

continuous-time Fourier series

$$x(t) = \sum_{k=-\infty}^{\infty} a_k e^{jk\omega_0 t} \longleftrightarrow a_k = \frac{1}{T} \int_T x(t) e^{-jk\omega_0 t} dt$$

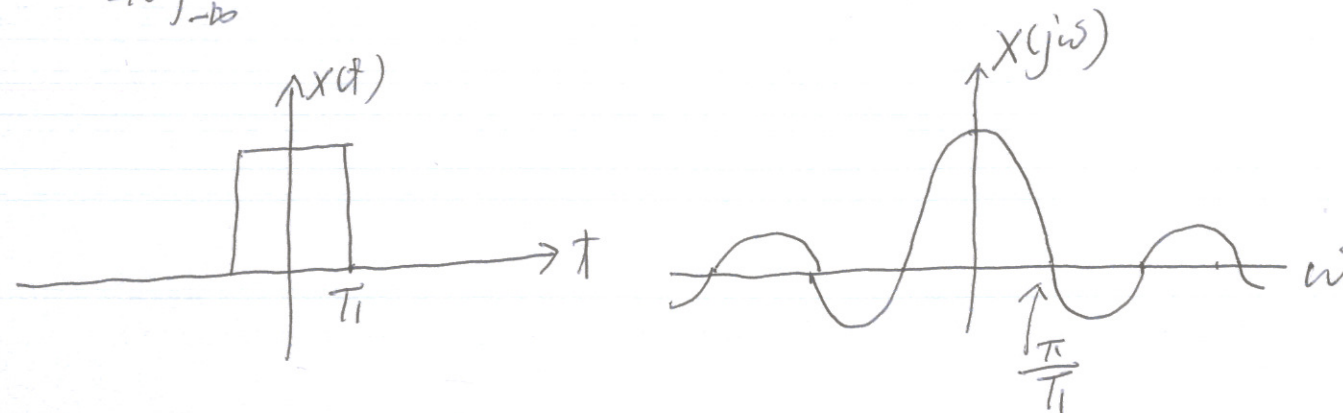
$$= \sum_{k=-\infty}^{\infty} a_k e^{jk \frac{2\pi}{T} t}$$



Non periodic

Fourier transform

$$x(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(j\omega) e^{j\omega t} d\omega \longleftrightarrow X(j\omega) = \int_{-\infty}^{\infty} x(t) e^{-j\omega t} dt$$

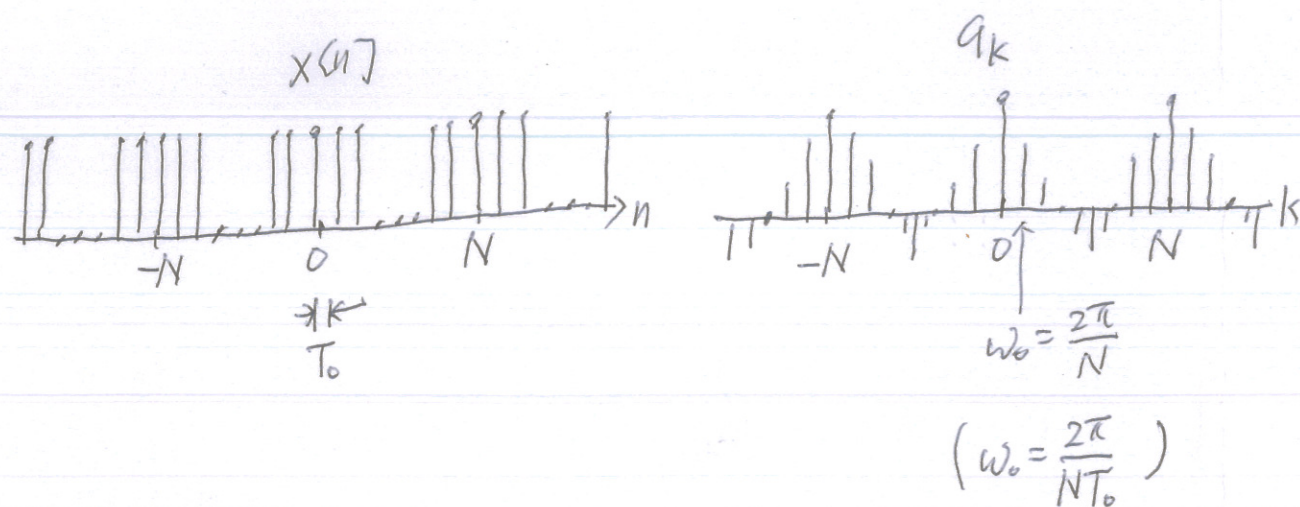


discrete

discrete-time Fourier series

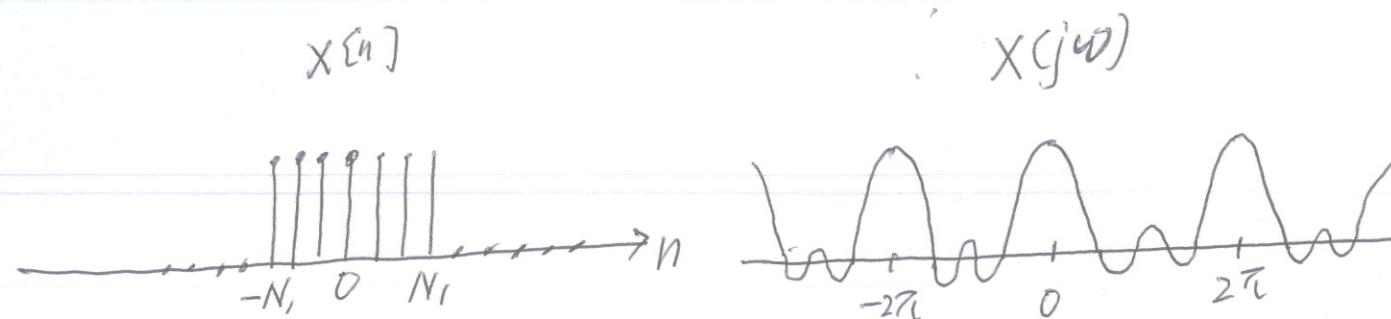
$$x[n] = \sum_{k=-\infty}^{\infty} a_k e^{jk\omega_0 n} \longleftrightarrow a_k = \frac{1}{N} \sum_{n=-\infty}^{\infty} x[n] e^{-jk\omega_0 n}$$

$$= \sum_{k=-\infty}^{\infty} a_k e^{jk \frac{2\pi}{N} n}$$



discrete-time Fourier transform (DTFT)

$$x[n] = \frac{1}{2\pi} \int_{2\pi} X(e^{j\omega}) e^{j\omega n} d\omega \longleftrightarrow X(e^{j\omega}) = \sum_{n=-\infty}^{\infty} x[n] e^{-j\omega n}$$



discrete-Fourier transform (DFT)

$$x[n] = \frac{1}{N} \sum_{k=0}^{N-1} X[k] e^{j \frac{2\pi}{N} kn} \longleftrightarrow X[k] = \sum_{n=0}^{N-1} x[n] e^{-j \frac{2\pi}{N} kn}$$

$$= \frac{1}{N} \sum_{k=0}^{N-1} X[k] W_N^{-kn} = \sum_{n=0}^{N-1} x[n] W_N^{kn}$$

$$W_N = e^{-j \frac{2\pi}{N}} \quad k, n = 0, 1, \dots, N-1$$