The First 100 Prime Empirical Proof in Long Division

P₁ 2

Prime numbers are defined as numbers greater than 1 that have no positive divisors other than 1 and themselves. 1 is self-Prime. The sequence of Prime numbers starts with 2, 3, 5, 7, 11, and so on.

A Prime is any number only divisible by 1 and itself searching first that a number is not even if it divides by 2, optimising using a Vignette Sieve that if not only up to n/2 needs to be tested as a divisor, then 3 if not only up to n/3 needs to be tested as divisor, n/5, n/7, n/11, n/13, n/17, n/19, n/23, n/29, n/31 & so on so that only divisibility by a Prime needs to be checked up to \sqrt{n} for to prove not Prime & since for example we have ruled out that the number is a factor of three or two so there is no natural number greater than n/3 that can be a divisor.

Explanation: This prime is only divisible by 1 and itself. No division required.

https://github.com/Willtech/Prime

P₂ 3

3 ÷ 2 = 1 remainder 1

P₃ 5

5 ÷ 2 = 2 remainder 1

P₄ 7

7 ÷ 2 = 3 remainder 1

P₅ 11

11 ÷ 2 = 5 remainder 1

11 ÷ 3 = 3 remainder 2

P₆ 13

 $13 \div 2 = 6$ remainder 1

 $13 \div 3 = 4$ remainder 1

P₇ 17

17 ÷ 2 = 8 remainder 1

 $17 \div 3 = 5$ remainder 2

P₈ 19

19 ÷ 2 = 9 remainder 1

 $19 \div 3 = 6$ remainder 1

$$\begin{array}{c|c}
 & -6 \\
 & 19 \\
 & 18 \\
 & -1 \\
 & 1 \leftarrow \text{remainder}
\end{array}$$

P₉ 23

23 ÷ 2 = 11 remainder 1

 $23 \div 3 = 7 \text{ remainder } 2$

P₁₀ 29

 $29 \div 2 = 14 \text{ remainder } 1$

 $29 \div 3 = 9 \text{ remainder } 2$

 $29 \div 5 = 5$ remainder 4

P₁₁ 31

 $31 \div 2 = 15$ remainder 1

 $31 \div 3 = 10$ remainder 1

 $31 \div 5 = 6$ remainder 1

$P_{12} 37$

 $37 \div 2 = 18 \text{ remainder } 1$

 $37 \div 3 = 12 \text{ remainder } 1$

 $37 \div 5 = 7 \text{ remainder } 2$

P₁₃ 41

 $41 \div 2 = 20 \text{ remainder } 1$

$$\begin{array}{c|c}
 & \underline{20}_{-} \\
2 & 41 \\
 & 40 \\
 & -1 \\
\hline
 & 1 \leftarrow \text{remainder}
\end{array}$$

 $41 \div 3 = 13 \text{ remainder } 2$

$$\begin{array}{c|c}
 & -13 \\
3 & 41 \\
39 \\
-- \\
2 & \leftarrow \text{ remainder}
\end{array}$$

 $41 \div 5 = 8 \text{ remainder } 1$

$$\begin{array}{ccc}
 & -8 \\
5 & 41 \\
 & 40 \\
 & -1 \\
 & 1 & \leftarrow \text{ remainder}
\end{array}$$

$P_{14} 43$

 $43 \div 2 = 21 \text{ remainder } 1$

 $43 \div 3 = 14 \text{ remainder } 1$

 $43 \div 5 = 8 \text{ remainder } 3$

P₁₅ 47

 $47 \div 2 = 23 \text{ remainder } 1$

 $47 \div 3 = 15 \text{ remainder } 2$

$$\begin{array}{c|c}
 & 15 \\
 & 47 \\
 & 45 \\
 & - \\
 & 2 \leftarrow \text{remainder}
\end{array}$$

 $47 \div 5 = 9 \text{ remainder } 2$

P₁₆ 53

 $53 \div 2 = 26 \text{ remainder } 1$

 $53 \div 3 = 17 \text{ remainder } 2$

 $53 \div 5 = 10$ remainder 3

 $53 \div 7 = 7$ remainder 4

P₁₇ 59

 $59 \div 2 = 29 \text{ remainder } 1$

 $59 \div 3 = 19 \text{ remainder } 2$

 $59 \div 5 = 11 \text{ remainder } 4$

 $59 \div 7 = 8 \text{ remainder } 3$

$$\begin{array}{ccc}
 & \underline{}8_{-} \\
7 & 59 \\
 & 56 \\
 & - \\
 & 3 \leftarrow \text{remainder}
\end{array}$$

P₁₈ 61

 $61 \div 2 = 30 \text{ remainder } 1$

 $61 \div 3 = 20 \text{ remainder } 1$

$$\begin{array}{c|c}
 & \underline{} 20 \\
3 & 61 \\
 & 60 \\
 & -- \\
 & 1 \leftarrow \text{remainder}
\end{array}$$

 $61 \div 5 = 12 \text{ remainder } 1$

 $61 \div 7 = 8 \text{ remainder } 5$

$$\begin{array}{ccc}
 & -8 \\
7 & | 61 \\
 & 56 \\
 & -7 \\
5 & \leftarrow \text{ remainder}
\end{array}$$

P₁₉ 67

 $67 \div 2 = 33 \text{ remainder } 1$

 $67 \div 3 = 22 \text{ remainder } 1$

 $67 \div 5 = 13 \text{ remainder } 2$

$$\begin{array}{ccc}
 & \underline{} & 13 \\
5 & | & 67 \\
 & 65 \\
 & \underline{} & \\
 & 2 & \leftarrow \text{ remainder}
\end{array}$$

 $67 \div 7 = 9 \text{ remainder } 4$

$P_{20} 71$

 $71 \div 2 = 35 \text{ remainder } 1$

 $71 \div 3 = 23 \text{ remainder } 2$

$$\begin{array}{c|c}
 & 23 \\
 \hline
 & 71 \\
 & 69 \\
 & -- \\
 & 2 \leftarrow \text{remainder}
\end{array}$$

 $71 \div 5 = 14 \text{ remainder } 1$

 $71 \div 7 = 10 \text{ remainder } 1$

P₂₁ 73

 $73 \div 2 = 36 \text{ remainder } 1$

 $73 \div 3 = 24 \text{ remainder } 1$

 $73 \div 5 = 14 \text{ remainder } 3$

 $73 \div 7 = 10 \text{ remainder } 3$

$P_{22} 79$

 $79 \div 2 = 39 \text{ remainder } 1$

 $79 \div 3 = 26 \text{ remainder } 1$

 $79 \div 5 = 15 \text{ remainder } 4$

 $79 \div 7 = 11 \text{ remainder } 2$

P₂₃ 83

 $83 \div 2 = 41$ remainder 1

 $83 \div 3 = 27 \text{ remainder } 2$

$$\begin{array}{c|c}
 & \underline{}27_{\underline{}}\\
3 & 83 \\
 & 81 \\
 & \underline{}\\
2 & \leftarrow \text{remainder}
\end{array}$$

 $83 \div 5 = 16 \text{ remainder } 3$

 $83 \div 7 = 11 \text{ remainder } 6$

$P_{24} 89$

 $89 \div 2 = 44$ remainder 1

1 ← remainder

 $89 \div 3 = 29 \text{ remainder } 2$

 $89 \div 5 = 17 \text{ remainder } 4$

 $89 \div 7 = 12 \text{ remainder } 5$

P₂₅ 97

 $97 \div 2 = 48 \text{ remainder } 1$

1 ← remainder

 $97 \div 3 = 32 \text{ remainder } 1$

 $97 \div 5 = 19 \text{ remainder } 2$

 $97 \div 7 = 13 \text{ remainder } 6$

P₂₆ 101

 $101 \div 2 = 50 \text{ remainder } 1$

1 ← remainder

 $101 \div 3 = 33 \text{ remainder } 2$

$$\begin{array}{c|c}
 & 33 \\
3 & 101 \\
99 \\
 & 2 \leftarrow \text{remainder}
\end{array}$$

101 ÷ 5 = 20 remainder 1

 $101 \div 7 = 14 \text{ remainder } 3$

$$\begin{array}{c|c}
 & -14 \\
7 & 101 \\
 & 98 \\
 & --- \\
 & 3 \leftarrow \text{remainder}
\end{array}$$

P₂₇ 103

 $103 \div 2 = 51 \text{ remainder } 1$

2 |
$$\frac{-51}{103}$$

102

1 ← remainder

103 ÷ 3 = 34 remainder 1

1 ← remainder

 $103 \div 5 = 20 \text{ remainder } 3$

103 ÷ 7 = 14 remainder 5

$$\begin{array}{c|c}
 & -14 \\
7 & 103 \\
 & 98 \\
 & --- \\
 & 5 \leftarrow \text{remainder}
\end{array}$$

$P_{28} 107$

 $107 \div 2 = 53 \text{ remainder } 1$

2 |
$$\frac{_{-}53_{-}}{107}$$

106

1 ← remainder

 $107 \div 3 = 35 \text{ remainder } 2$

$$\begin{array}{c|c}
 & 35 \\
 & 107 \\
 & 105 \\
 & --- \\
 & 2 \leftarrow \text{remainder}
\end{array}$$

107 ÷ 5 = 21 remainder 2

 $107 \div 7 = 15 \text{ remainder } 2$

P₂₉ 109

 $109 \div 2 = 54 \text{ remainder } 1$

2 |
$$\frac{_{-}54_{-}}{109}$$

108

1 ← remainder

 $109 \div 3 = 36 \text{ remainder } 1$

109 ÷ 5 = 21 remainder 4

 $109 \div 7 = 15 \text{ remainder } 4$

P₃₀ 113

 $113 \div 2 = 56 \text{ remainder } 1$

2 |
$$\frac{_{-}56_{-}}{113}$$

112

1 ← remainder

 $113 \div 3 = 37 \text{ remainder } 2$

$$\begin{array}{c|c}
 & 37 \\
3 & 113 \\
 & 111 \\
 & \cdots \\
2 & \leftarrow \text{remainder}
\end{array}$$

113 ÷ 5 = 22 remainder 3

 $113 \div 7 = 16 \text{ remainder } 1$

P₃₁ 127

 $127 \div 2 = 63 \text{ remainder } 1$

1 ← remainder

 $127 \div 3 = 42 \text{ remainder } 1$

3 |
$$\overline{127}$$

126

1 ← remainder

 $127 \div 5 = 25 \text{ remainder } 2$

2 ← remainder

 $127 \div 7 = 18 \text{ remainder } 1$

127 ÷ 11 = 11 remainder 6

P₃₂ 131

 $131 \div 2 = 65 \text{ remainder } 1$

2 |
$$\frac{-65}{131}$$

130

- - -

1 ← remainder

 $131 \div 3 = 43 \text{ remainder } 2$

2 ← remainder

 $131 \div 5 = 26 \text{ remainder } 1$

1 ← remainder

 $131 \div 7 = 18 \text{ remainder } 5$

131 ÷ 11 = 11 remainder 10

$$\begin{array}{r}
 -11 \\
 11 \mid 131 \\
 121 \\
 \hline
 10 \leftarrow remainder$$

P₃₃ 137

 $137 \div 2 = 68 \text{ remainder } 1$

1 ← remainder

 $137 \div 3 = 45 \text{ remainder } 2$

2 ← remainder

 $137 \div 5 = 27 \text{ remainder } 2$

137 ÷ 7 = 19 remainder 4

137 ÷ 11 = 12 remainder 5

P₃₄ 139

 $139 \div 2 = 69 \text{ remainder } 1$

2 |
$$\frac{_{-}69_{-}}{139}$$

138

1 ← remainder

139 ÷ 3 = 46 remainder 1

1 ← remainder

 $139 \div 5 = 27 \text{ remainder } 4$

 $139 \div 7 = 19 \text{ remainder } 6$

139 ÷ 11 = 12 remainder 7

P₃₅ 149

 $149 \div 2 = 74 \text{ remainder } 1$

2 |
$$\frac{_{-}74_{-}}{149}$$

148

1 ← remainder

149 ÷ 3 = 49 remainder 2

149 ÷ 5 = 29 remainder 4

 $149 \div 7 = 21 \text{ remainder } 2$

149 ÷ 11 = 13 remainder 6

P₃₆ 151

 $151 \div 2 = 75 \text{ remainder } 1$

2 |
$$\frac{_{-}75_{-}}{151}$$

150

- - -

1 ← remainder

 $151 \div 3 = 50 \text{ remainder } 1$

1 ← remainder

 $151 \div 5 = 30 \text{ remainder } 1$

1 ← remainder

 $151 \div 7 = 21 \text{ remainder } 4$

151 ÷ 11 = 13 remainder 8

P₃₇ 157

 $157 \div 2 = 78 \text{ remainder } 1$

1 ← remainder

 $157 \div 3 = 52 \text{ remainder } 1$

$$\begin{array}{c|c}
 & 52 \\
 & 157 \\
 & 156 \\
 & --- \\
 & 1 \leftarrow \text{remainder}
\end{array}$$

157 ÷ 5 = 31 remainder 2

 $157 \div 7 = 22 \text{ remainder } 3$

 $157 \div 11 = 14 \text{ remainder } 3$

P₃₈ 163

 $163 \div 2 = 81 \text{ remainder } 1$

2 |
$$\frac{.81}{163}$$

162

1 ← remainder

 $163 \div 3 = 54 \text{ remainder } 1$

$$\begin{array}{c|c}
 & 54_{-} \\
3 & 163 \\
 & 162 \\
 & --- \\
1 & \leftarrow remainder
\end{array}$$

163 ÷ 5 = 32 remainder 3

 $163 \div 7 = 23 \text{ remainder } 2$

 $163 \div 11 = 14 \text{ remainder } 9$

$$\begin{array}{r}
-14 \\
11 \mid 163 \\
154 \\
--- \\
9 \leftarrow \text{remainder}
\end{array}$$

P₃₉ 167

 $167 \div 2 = 83 \text{ remainder } 1$

2 |
$$\frac{-83}{167}$$

166

1 ← remainder

167 ÷ 3 = 55 remainder 2

167 ÷ 5 = 33 remainder 2

 $167 \div 7 = 23 \text{ remainder } 6$

 $167 \div 11 = 15 \text{ remainder } 2$

$P_{40} 173$

 $173 \div 2 = 86 \text{ remainder } 1$

2 |
$$\frac{_{86}_{-}}{173}$$

172

1 ← remainder

 $173 \div 3 = 57 \text{ remainder } 2$

2 ← remainder

 $173 \div 5 = 34 \text{ remainder } 3$

3 ← remainder

 $173 \div 7 = 24 \text{ remainder } 5$

173 ÷ 11 = 15 remainder 8

173 ÷ 13 = 13 remainder 4

$$\begin{array}{rcl}
 & -13_{-1} \\
 & 173 \\
 & 169 \\
 & --- \\
 & 4 & \leftarrow \text{ remainder}
\end{array}$$

P₄₁ 179

 $179 \div 2 = 89 \text{ remainder } 1$

2 |
$$\frac{-89}{179}$$

178

- - -

1 ← remainder

 $179 \div 3 = 59 \text{ remainder } 2$

2 ← remainder

 $179 \div 5 = 35 \text{ remainder } 4$

4 ← remainder

 $179 \div 7 = 25 \text{ remainder } 4$

 $179 \div 11 = 16 \text{ remainder } 3$

179 ÷ 13 = 13 remainder 10

P₄₂ 181

 $181 \div 2 = 90 \text{ remainder } 1$

1 ← remainder

 $181 \div 3 = 60 \text{ remainder } 1$

1 ← remainder

181 ÷ 5 = 36 remainder 1

181 ÷ 7 = 25 remainder 6

181 ÷ 11 = 16 remainder 5

181 ÷ 13 = 13 remainder 12

$$\begin{array}{rrr}
 & -13 \\
 & 181 \\
 & 169 \\
 & --- \\
 & 12 & \leftarrow \text{ remainder}
\end{array}$$

P₄₃ 191

 $191 \div 2 = 95 \text{ remainder } 1$

1 ← remainder

 $191 \div 3 = 63 \text{ remainder } 2$

$$\begin{array}{c|c}
 & -63 \\
 & | 191 \\
 & 189 \\
 & --- \\
 & 2 \leftarrow \text{remainder}
\end{array}$$

191 ÷ 5 = 38 remainder 1

191 ÷ 7 = 27 remainder 2

$$\begin{array}{c|c}
 & -27 \\
7 & 191 \\
 & 189 \\
 & --- \\
2 & \leftarrow \text{remainder}
\end{array}$$

191 ÷ 11 = 17 remainder 4

191 ÷ 13 = 14 remainder 9

$$\begin{array}{r}
 -14 \\
 13 \mid 191 \\
 182 \\
 \hline
 9 \leftarrow remainder$$

P₄₄ 193

 $193 \div 2 = 96 \text{ remainder } 1$

1 ← remainder

193 ÷ 3 = 64 remainder 1

1 ← remainder

 $193 \div 5 = 38 \text{ remainder } 3$

 $193 \div 7 = 27 \text{ remainder } 4$

193 ÷ 11 = 17 remainder 6

193 ÷ 13 = 14 remainder 11

P₄₅ 197

 $197 \div 2 = 98 \text{ remainder } 1$

1 ← remainder

 $197 \div 3 = 65 \text{ remainder } 2$

197 ÷ 5 = 39 remainder 2

 $197 \div 7 = 28 \text{ remainder } 1$

197 ÷ 11 = 17 remainder 10

197 ÷ 13 = 15 remainder 2

$$\begin{array}{rrr}
 & -15 \\
 & 197 \\
 & 195 \\
 & --- \\
 & 2 & \leftarrow \text{ remainder}
\end{array}$$

P₄₆ 199

 $199 \div 2 = 99 \text{ remainder } 1$

- - -

1 ← remainder

 $199 \div 3 = 66 \text{ remainder } 1$

1 ← remainder

 $199 \div 5 = 39 \text{ remainder } 4$

199 ÷ 7 = 28 remainder 3

199 ÷ 11 = 18 remainder 1

199 ÷ 13 = 15 remainder 4

$$-_{15}^{-}$$
13 | 199
195

4 ← remainder

P₄₇ 211

 $211 \div 2 = 105 \text{ remainder } 1$

2 |
$$\frac{105}{211}$$

210

1 ← remainder

 $211 \div 3 = 70 \text{ remainder } 1$

$$\begin{array}{r}
 -70 \\
 3 \mid 211 \\
 210 \\
 \hline
 1 \leftarrow remainder$$

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211 ÷ 5 = 42 remainder 1

 $211 \div 7 = 30 \text{ remainder } 1$

211 ÷ 11 = 19 remainder 2

211 ÷ 13 = 16 remainder 3

P₄₈ 223

 $223 \div 2 = 111 \text{ remainder } 1$

2 |
$$\frac{111}{223}$$

222

1 ← remainder

 $223 \div 3 = 74 \text{ remainder } 1$

$$\begin{array}{c|c}
 & -74 \\
3 & 223 \\
 & 222 \\
 & --- \\
 & 1 \leftarrow \text{remainder}
\end{array}$$

 $223 \div 5 = 44 \text{ remainder } 3$

223 ÷ 7 = 31 remainder 6

 $223 \div 11 = 20 \text{ remainder } 3$

223 ÷ 13 = 17 remainder 2

$P_{49} 227$

 $227 \div 2 = 113 \text{ remainder } 1$

1 ← remainder

 $227 \div 3 = 75 \text{ remainder } 2$

 $227 \div 5 = 45 \text{ remainder } 2$

 $227 \div 7 = 32 \text{ remainder } 3$

 $227 \div 11 = 20 \text{ remainder } 7$

227 ÷ 13 = 17 remainder 6

P₅₀ 229

 $229 \div 2 = 114 \text{ remainder } 1$

2 |
$$\overline{229}$$

228

1 ← remainder

 $229 \div 3 = 76 \text{ remainder } 1$

1 ← remainder

 $229 \div 5 = 45 \text{ remainder } 4$

229 ÷ 7 = 32 remainder 5

$$\begin{array}{r}
 -32_{-} \\
7 \mid 229 \\
 224 \\
 --- \\
5 \leftarrow remainder$$

229 ÷ 11 = 20 remainder 9

$$\begin{array}{r}
-20_{-} \\
11 \mid 229 \\
220 \\
--- \\
9 \leftarrow \text{remainder}
\end{array}$$

229 ÷ 13 = 17 remainder 8

$$\begin{array}{rrr}
 & -17_{-} \\
 & 13 & 229 \\
 & 221 \\
 & --- \\
 & 8 & \leftarrow \text{ remainder}
\end{array}$$

P₅₁ 233

233 ÷ 2 = 116 remainder 1

1 ← remainder

 $233 \div 3 = 77 \text{ remainder } 2$

$$\begin{array}{r}
 -77_{-} \\
3 \mid 233 \\
 231 \\
 --- \\
2 \leftarrow remainder$$

 $233 \div 5 = 46 \text{ remainder } 3$

 $233 \div 7 = 33 \text{ remainder } 2$

233 ÷ 11 = 21 remainder 2

233 ÷ 13 = 17 remainder 12

P₅₂ 239

 $239 \div 2 = 119 \text{ remainder } 1$

2 |
$$\frac{119}{239}$$

238

1 ← remainder

 $239 \div 3 = 79 \text{ remainder } 2$

$$\begin{array}{r}
 -79_{-} \\
3 \mid 239 \\
 237 \\
 --- \\
2 \leftarrow remainder$$

 $239 \div 5 = 47 \text{ remainder } 4$

 $239 \div 7 = 34 \text{ remainder } 1$

239 ÷ 11 = 21 remainder 8

$$\begin{array}{r}
-21 \\
11 \mid 239 \\
231 \\
--- \\
8 \leftarrow \text{remainder}
\end{array}$$

239 ÷ 13 = 18 remainder 5

5 ← remainder

P₅₃ 241

 $241 \div 2 = 120 \text{ remainder } 1$

1 ← remainder

241 ÷ 3 = 80 remainder 1

241 ÷ 5 = 48 remainder 1

 $241 \div 7 = 34 \text{ remainder } 3$

241 ÷ 11 = 21 remainder 10

$$\begin{array}{r}
-21 \\
11 \mid 241 \\
231 \\
-- \\
10 \leftarrow \text{remainder}
\end{array}$$

241 ÷ 13 = 18 remainder 7

$$\begin{array}{r}
-18_{-} \\
13 \mid 241 \\
234 \\
-- \\
7 \leftarrow \text{remainder}
\end{array}$$

P₅₄ 251

 $251 \div 2 = 125 \text{ remainder } 1$

2 |
$$\frac{125}{251}$$

250

1 ← remainder

 $251 \div 3 = 83 \text{ remainder } 2$

251 ÷ 5 = 50 remainder 1

$$50_{-}$$
 $5 \mid 251$
 250
 $- 1 \leftarrow remainder$

 $251 \div 7 = 35 \text{ remainder } 6$

251 ÷ 11 = 22 remainder 9

251 ÷ 13 = 19 remainder 4

P₅₅ 257

 $257 \div 2 = 128 \text{ remainder } 1$

1 ← remainder

 $257 \div 3 = 85 \text{ remainder } 2$

 $257 \div 5 = 51 \text{ remainder } 2$

$$51_{-}$$
 $5 \mid 257$
 255
 $- 2 \leftarrow remainder$

 $257 \div 7 = 36 \text{ remainder } 5$

 $257 \div 11 = 23 \text{ remainder } 4$

257 ÷ 13 = 19 remainder 10

$$\begin{array}{rrr}
 & -19 \\
 & 257 \\
 & 247 \\
 & --- \\
 & 10 & \leftarrow \text{ remainder}
\end{array}$$

P₅₆ 263

 $263 \div 2 = 131 \text{ remainder } 1$

2 |
$$\frac{-131}{263}$$

262

1 ← remainder

 $263 \div 3 = 87 \text{ remainder } 2$

263 ÷ 5 = 52 remainder 3

$$\begin{array}{r}
-52\\
5 \mid 263\\
260\\
---\\
3 \leftarrow \text{remainder}
\end{array}$$

 $263 \div 7 = 37 \text{ remainder } 4$

263 ÷ 11 = 23 remainder 10

$$\begin{array}{r}
-23_{-} \\
11 \mid 263 \\
253 \\
-- \\
10 \leftarrow \text{remainder}
\end{array}$$

263 ÷ 13 = 20 remainder 3

P₅₇ 269

 $269 \div 2 = 134 \text{ remainder } 1$

2 |
$$\frac{-134}{269}$$

268

1 ← remainder

 $269 \div 3 = 89 \text{ remainder } 2$

$$\begin{array}{c|c}
 & \underline{}89\underline{}\\
 & 269\\
 & 267\\
 & \underline{}\\
 & 2 \leftarrow \text{remainder}
\end{array}$$

 $269 \div 5 = 53 \text{ remainder } 4$

 $269 \div 7 = 38 \text{ remainder } 3$

$$\begin{array}{r}
 -38 \\
7 \mid 269 \\
 266 \\
 --- \\
 3 \leftarrow remainder$$

269 ÷ 11 = 24 remainder 5

269 ÷ 13 = 20 remainder 9

P₅₈ 271

 $271 \div 2 = 135 \text{ remainder } 1$

1 ← remainder

271 ÷ 3 = 90 remainder 1

1 ← remainder

 $271 \div 5 = 54 \text{ remainder } 1$

1 ← remainder

 $271 \div 7 = 38 \text{ remainder } 5$

271 ÷ 11 = 24 remainder 7

271 ÷ 13 = 20 remainder 11

P₅₉ 277

 $277 \div 2 = 138 \text{ remainder } 1$

2 |
$$\overline{277}$$

276

1 ← remainder

277 ÷ 3 = 92 remainder 1

$$\begin{array}{c|c}
 & 92 \\
 & 277 \\
 & 276 \\
 & --- \\
 & 1 \leftarrow \text{remainder}
\end{array}$$

277 ÷ 5 = 55 remainder 2

 $277 \div 7 = 39 \text{ remainder } 4$

277 ÷ 11 = 25 remainder 2

277 ÷ 13 = 21 remainder 4

$$\begin{array}{rcl}
 & -21 \\
 & 277 \\
 & 273 \\
 & & \\
 & & \leftarrow \text{ remainder}
\end{array}$$

$P_{60} 281$

 $281 \div 2 = 140 \text{ remainder } 1$

2 |
$$\frac{-140}{281}$$

280

1 ← remainder

 $281 \div 3 = 93 \text{ remainder } 2$

281 ÷ 5 = 56 remainder 1

$$56_{-}$$
 $5 \mid 281$
 280
 $- 1 \leftarrow remainder$

 $281 \div 7 = 40 \text{ remainder } 1$

281 ÷ 11 = 25 remainder 6

281 ÷ 13 = 21 remainder 8

P₆₁ 283

283 ÷ 2 = 141 remainder 1

2 |
$$\frac{-141}{283}$$

282

1 ← remainder

 $283 \div 3 = 94 \text{ remainder } 1$

283 ÷ 5 = 56 remainder 3

 $283 \div 7 = 40 \text{ remainder } 3$

283 ÷ 11 = 25 remainder 8

283 ÷ 13 = 21 remainder 10

P₆₂ 293

293 ÷ 2 = 146 remainder 1

2 |
$$\frac{-146}{293}$$

292

1 ← remainder

 $293 \div 3 = 97 \text{ remainder } 2$

 $293 \div 5 = 58 \text{ remainder } 3$

293 ÷ 7 = 41 remainder 6

293 ÷ 11 = 26 remainder 7

293 ÷ 17 = 17 remainder 4

$P_{63} 307$

 $307 \div 2 = 153 \text{ remainder } 1$

2 |
$$\frac{153}{307}$$

306

1 ← remainder

 $307 \div 3 = 102 \text{ remainder } 1$

1 ← remainder

 $307 \div 5 = 61 \text{ remainder } 2$

2 ← remainder

 $307 \div 7 = 43 \text{ remainder } 6$

307 ÷ 11 = 27 remainder 10

 $307 \div 13 = 23 \text{ remainder } 8$

$$\begin{array}{r}
-23 \\
13 \mid 307 \\
299 \\
--- \\
8 \leftarrow \text{remainder}
\end{array}$$

307 ÷ 17 = 18 remainder 1

$$\begin{array}{rrr}
 & -18 \\
 & 17 & | & 307 \\
 & & 306 \\
 & & --- \\
 & 1 & \leftarrow \text{ remainder}
\end{array}$$

$P_{64} 311$

 $311 \div 2 = 155 \text{ remainder } 1$

2 |
$$\frac{155}{311}$$

310

1 ← remainder

311 ÷ 3 = 103 remainder 2

2 ← remainder

 $311 \div 5 = 62 \text{ remainder } 1$

311 ÷ 7 = 44 remainder 3

311 ÷ 11 = 28 remainder 3

$$\begin{array}{r}
-28 \\
11 \mid 311 \\
308 \\
-- \\
3 \leftarrow \text{remainder}
\end{array}$$

311 ÷ 13 = 23 remainder 12

$$\begin{array}{r}
-23 \\
13 \mid 311 \\
299 \\
--- \\
12 \leftarrow \text{remainder}
\end{array}$$

311 ÷ 17 = 18 remainder 5

$P_{65} 313$

 $313 \div 2 = 156 \text{ remainder } 1$

2 |
$$\frac{156}{313}$$

312

1 ← remainder

 $313 \div 3 = 104 \text{ remainder } 1$

1 ← remainder

 $313 \div 5 = 62 \text{ remainder } 3$

313 ÷ 7 = 44 remainder 5

 $313 \div 11 = 28 \text{ remainder } 5$

$$\begin{array}{r}
-28_{-} \\
11 \mid 313 \\
308 \\
--- \\
5 \leftarrow \text{remainder}
\end{array}$$

313 ÷ 13 = 24 remainder 1

$$\begin{array}{r}
-24 \\
13 \mid 313 \\
312 \\
-- \\
1 \leftarrow \text{remainder}
\end{array}$$

313 ÷ 17 = 18 remainder 7

$P_{66} 317$

 $317 \div 2 = 158 \text{ remainder } 1$

2 |
$$\frac{158}{317}$$

316

1 ← remainder

 $317 \div 3 = 105 \text{ remainder } 2$

2 ← remainder

 $317 \div 5 = 63 \text{ remainder } 2$

2 ← remainder

 $317 \div 7 = 45 \text{ remainder } 2$

317 ÷ 11 = 28 remainder 9

317 ÷ 13 = 24 remainder 5

317 ÷ 17 = 18 remainder 11

$$\begin{array}{rrr}
 & -18 \\
 & 317 \\
 & 306 \\
 & --- \\
 & 11 & \leftarrow \text{ remainder}
\end{array}$$

P₆₇ 331

 $331 \div 2 = 165 \text{ remainder } 1$

2 |
$$\frac{-165}{331}$$

330

1 ← remainder

331 ÷ 3 = 110 remainder 1

1 ← remainder

 $331 \div 5 = 66 \text{ remainder } 1$

 $331 \div 7 = 47 \text{ remainder } 2$

 $331 \div 11 = 30 \text{ remainder } 1$

$$\begin{array}{r}
 -30 \\
 11 \mid 331 \\
 330 \\
 \hline
 1 \leftarrow remainder$$

 $331 \div 13 = 25 \text{ remainder } 6$

331 ÷ 17 = 19 remainder 8

$P_{68} 337$

 $337 \div 2 = 168 \text{ remainder } 1$

2 |
$$\frac{_{-1}168_{--}}{337}$$

1 ← remainder

337 ÷ 3 = 112 remainder 1

1 ← remainder

 $337 \div 5 = 67 \text{ remainder } 2$

 $337 \div 7 = 48 \text{ remainder } 1$

 $337 \div 11 = 30 \text{ remainder } 7$

337 ÷ 13 = 25 remainder 12

$$\begin{array}{r}
-25 \\
13 \mid 337 \\
325 \\
-- \\
12 \leftarrow \text{remainder}
\end{array}$$

 $337 \div 17 = 19 \text{ remainder } 14$

$$\begin{array}{r}
-19_{-1} \\
17 \mid 337 \\
323 \\
--- \\
14 \leftarrow \text{remainder}
\end{array}$$

P₆₉ 347

 $347 \div 2 = 173 \text{ remainder } 1$

2 |
$$\frac{173}{347}$$

346

1 ← remainder

 $347 \div 3 = 115 \text{ remainder } 2$

347 ÷ 5 = 69 remainder 2

 $347 \div 7 = 49 \text{ remainder } 4$

347 ÷ 11 = 31 remainder 6

347 ÷ 13 = 26 remainder 9

$$\begin{array}{r}
 -26 \\
 13 \mid 347 \\
 338 \\
 --- \\
 9 \leftarrow remainder
 \end{array}$$

 $347 \div 17 = 20 \text{ remainder } 7$

P₇₀ 349

 $349 \div 2 = 174 \text{ remainder } 1$

2 |
$$\frac{174}{349}$$

348

1 ← remainder

 $349 \div 3 = 116 \text{ remainder } 1$

1 ← remainder

 $349 \div 5 = 69 \text{ remainder } 4$

 $349 \div 7 = 49 \text{ remainder } 6$

349 ÷ 11 = 31 remainder 8

349 ÷ 13 = 26 remainder 11

$$\begin{array}{r}
-26 \\
13 \mid 349 \\
338 \\
-- \\
11 \leftarrow \text{remainder}
\end{array}$$

349 ÷ 17 = 20 remainder 9

P₇₁ 353

 $353 \div 2 = 176 \text{ remainder } 1$

2 |
$$\frac{176}{353}$$

352

1 ← remainder

 $353 \div 3 = 117 \text{ remainder } 2$

2 ← remainder

 $353 \div 5 = 70 \text{ remainder } 3$

3 ← remainder

 $353 \div 7 = 50 \text{ remainder } 3$

3 ← remainder

 $353 \div 11 = 32 \text{ remainder } 1$

1 ← remainder

 $353 \div 13 = 27 \text{ remainder } 2$

353 ÷ 17 = 20 remainder 13

P₇₂ 359

 $359 \div 2 = 179 \text{ remainder } 1$

2 |
$$\frac{179}{359}$$

358

1 ← remainder

 $359 \div 3 = 119 \text{ remainder } 2$

2 ← remainder

 $359 \div 5 = 71 \text{ remainder } 4$

4 ← remainder

 $359 \div 7 = 51 \text{ remainder } 2$

359 ÷ 11 = 32 remainder 7

359 ÷ 13 = 27 remainder 8

$$\begin{array}{r}
 -27 \\
 13 \mid 359 \\
 351 \\
 \hline
 8 \leftarrow remainder$$

359 ÷ 17 = 21 remainder 2

P₇₃ 367

 $367 \div 2 = 183 \text{ remainder } 1$

1 ← remainder

367 ÷ 3 = 122 remainder 1

1 ← remainder

 $367 \div 5 = 73 \text{ remainder } 2$

367 ÷ 7 = 52 remainder 3

367 ÷ 11 = 33 remainder 4

$$367 \div 13 = 28 \text{ remainder } 3$$

367 ÷ 17 = 21 remainder 10

$$\begin{array}{r}
-21 \\
17 \mid 367 \\
357 \\
--- \\
10 \leftarrow \text{remainder}
\end{array}$$

 $367 \div 19 = 19 \text{ remainder } 6$

P₇₄ 373

 $373 \div 2 = 186 \text{ remainder } 1$

2 |
$$\overline{373}$$

372

1 ← remainder

373 ÷ 3 = 124 remainder 1

3 |
$$\frac{124}{373}$$

372

1 ← remainder

 $373 \div 5 = 74 \text{ remainder } 3$

 $373 \div 7 = 53 \text{ remainder } 2$

373 ÷ 11 = 33 remainder 10

 $373 \div 13 = 28 \text{ remainder } 9$

$$\begin{array}{r}
 -28_{-} \\
 13 \mid 373 \\
 364 \\
 --- \\
 9 \leftarrow remainder$$

373 ÷ 17 = 21 remainder 16

$$\begin{array}{r}
-21_{-} \\
17 \mid 373 \\
357 \\
--- \\
16 \leftarrow \text{remainder}
\end{array}$$

 $373 \div 19 = 19 \text{ remainder } 12$

P₇₅ 379

 $379 \div 2 = 189 \text{ remainder } 1$

2 |
$$\frac{189}{379}$$

378

1 ← remainder

379 ÷ 3 = 126 remainder 1

1 ← remainder

 $379 \div 5 = 75 \text{ remainder } 4$

4 ← remainder

 $379 \div 7 = 54 \text{ remainder } 1$

1 ← remainder

 $379 \div 11 = 34 \text{ remainder } 5$

5 ← remainder

$$379 \div 13 = 29 \text{ remainder } 2$$

379 ÷ 17 = 22 remainder 5

 $379 \div 19 = 19 \text{ remainder } 18$

P₇₆ 383

 $383 \div 2 = 191 \text{ remainder } 1$

2 |
$$\frac{191}{383}$$

382

1 ← remainder

383 ÷ 3 = 127 remainder 2

2 ← remainder

 $383 \div 5 = 76 \text{ remainder } 3$

3 ← remainder

 $383 \div 7 = 54 \text{ remainder } 5$

383 ÷ 11 = 34 remainder 9

383 ÷ 17 = 22 remainder 9

 $383 \div 19 = 20 \text{ remainder } 3$

P₇₇ 389

 $389 \div 2 = 194 \text{ remainder } 1$

1 ← remainder

389 ÷ 3 = 129 remainder 2

2 ← remainder

 $389 \div 5 = 77 \text{ remainder } 4$

389 ÷ 7 = 55 remainder 4

 $389 \div 11 = 35 \text{ remainder } 4$

$$\begin{array}{r}
-29 \\
13 \mid 389 \\
377 \\
--- \\
12 \leftarrow \text{remainder}
\end{array}$$

$$\begin{array}{r}
 -22 \\
 17 \mid 389 \\
 374 \\
 \hline
 15 \leftarrow remainder$$

P₇₈ 397

 $397 \div 2 = 198 \text{ remainder } 1$

1 ← remainder

397 ÷ 3 = 132 remainder 1

3 |
$$\frac{132}{397}$$

396

1 ← remainder

 $397 \div 5 = 79 \text{ remainder } 2$

397 ÷ 7 = 56 remainder 5

 $397 \div 11 = 36 \text{ remainder } 1$

$$397 \div 13 = 30 \text{ remainder } 7$$

 $397 \div 17 = 23 \text{ remainder } 6$

 $397 \div 19 = 20 \text{ remainder } 17$

P₇₉ 401

 $401 \div 2 = 200 \text{ remainder } 1$

2 |
$$\frac{200}{401}$$

400

1 ← remainder

401 ÷ 3 = 133 remainder 2

2 ← remainder

 $401 \div 5 = 80 \text{ remainder } 1$

401 ÷ 7 = 57 remainder 2

 $401 \div 11 = 36 \text{ remainder } 5$

$$401 \div 13 = 30 \text{ remainder } 11$$

$$\begin{array}{r}
-30 \\
13 \mid 401 \\
390 \\
-- \\
11 \leftarrow \text{remainder}
\end{array}$$

401 ÷ 17 = 23 remainder 10

$$\begin{array}{r}
-23_{-} \\
17 \mid 401 \\
391 \\
--- \\
10 \leftarrow \text{remainder}
\end{array}$$

 $401 \div 19 = 21 \text{ remainder } 2$

P₈₀ 409

 $409 \div 2 = 204 \text{ remainder } 1$

- - -

1 ← remainder

 $409 \div 3 = 136 \text{ remainder } 1$

1 ← remainder

 $409 \div 5 = 81 \text{ remainder } 4$

$$409 \div 7 = 58 \text{ remainder } 3$$

409 ÷ 11 = 37 remainder 2

$$\begin{array}{r}
-37_{-1} \\
11 \mid 409 \\
407 \\
--- \\
2 \leftarrow \text{remainder}
\end{array}$$

$$409 \div 13 = 31 \text{ remainder } 6$$

6 ← remainder

$$409 \div 17 = 24 \text{ remainder } 1$$

$$\begin{array}{rcr}
 & -24 \\
 & 17 & | & 409 \\
 & & 408 \\
 & & & --- \\
 & 1 & \leftarrow \text{ remainder}
\end{array}$$

 $409 \div 19 = 21 \text{ remainder } 10$

$$\begin{array}{rrr}
 & -21 \\
 & 19 & | & 409 \\
 & & 399 \\
 & & & --- \\
 & & 10 & \leftarrow \text{ remainder}
\end{array}$$

P₈₁ 419

 $419 \div 2 = 209 \text{ remainder } 1$

2 |
$$\frac{209}{419}$$

418

1 ← remainder

419 ÷ 3 = 139 remainder 2

419 ÷ 5 = 83 remainder 4

 $419 \div 7 = 59 \text{ remainder } 6$

419 ÷ 11 = 38 remainder 1

$$\begin{array}{r}
-38_{-} \\
11 \mid 419 \\
418 \\
-- \\
1 \leftarrow \text{remainder}
\end{array}$$

 $419 \div 13 = 32 \text{ remainder } 3$

419 ÷ 17 = 24 remainder 11

$$\begin{array}{rrr}
 & -24 \\
17 & 419 \\
 & 408 \\
 & --- \\
 & 11 & remainder
\end{array}$$

419 ÷ 19 = 22 remainder 1

$$\begin{array}{rrr}
 & -22 \\
 & 19 & | & 419 \\
 & & 418 \\
 & & & --- \\
 & 1 & \leftarrow \text{ remainder}
\end{array}$$

$P_{82} 421$

 $421 \div 2 = 210 \text{ remainder } 1$

1 ← remainder

421 ÷ 3 = 140 remainder 1

1 ← remainder

421 ÷ 5 = 84 remainder 1

421 ÷ 7 = 60 remainder 1

$$\begin{array}{c|c}
 & -60 \\
7 & 421 \\
 & 420 \\
 & --- \\
 & 1 & \leftarrow \text{ remainder}
\end{array}$$

421 ÷ 11 = 38 remainder 3

$$\begin{array}{r}
-38_{-} \\
11 \mid 421 \\
418 \\
-- \\
3 \leftarrow \text{remainder}
\end{array}$$

 $421 \div 13 = 32 \text{ remainder } 5$

421 ÷ 17 = 24 remainder 13

 $421 \div 19 = 22 \text{ remainder } 3$

$$\begin{array}{r}
-22 \\
19 \mid 421 \\
418 \\
-- \\
3 \leftarrow \text{remainder}
\end{array}$$

P₈₃ 431

 $431 \div 2 = 215 \text{ remainder } 1$

2 |
$$\frac{-215}{431}$$

430

1 ← remainder

431 ÷ 3 = 143 remainder 2

2 ← remainder

 $431 \div 5 = 86 \text{ remainder } 1$

 $431 \div 7 = 61 \text{ remainder } 4$

 $431 \div 11 = 39 \text{ remainder } 2$

$$\begin{array}{r}
-39_{-} \\
11 \mid 431 \\
429 \\
-- \\
2 \leftarrow \text{remainder}
\end{array}$$

 $431 \div 13 = 33 \text{ remainder } 2$

2 ← remainder

431 ÷ 17 = 25 remainder 6

431 ÷ 19 = 22 remainder 13

$$\begin{array}{rrr}
 & -22 \\
19 & | & 431 \\
 & & 418 \\
 & & & -- \\
 & & 13 & \leftarrow \text{ remainder}
\end{array}$$

$P_{84} 433$

 $433 \div 2 = 216 \text{ remainder } 1$

1 ← remainder

433 ÷ 3 = 144 remainder 1

1 ← remainder

 $433 \div 5 = 86 \text{ remainder } 3$

433 ÷ 7 = 61 remainder 6

 $433 \div 11 = 39 \text{ remainder } 4$

 $433 \div 13 = 33 \text{ remainder } 4$

433 ÷ 17 = 25 remainder 8

433 ÷ 19 = 22 remainder 15

P₈₅ 439

 $439 \div 2 = 219 \text{ remainder } 1$

1 ← remainder

439 ÷ 3 = 146 remainder 1

1 ← remainder

 $439 \div 5 = 87 \text{ remainder } 4$

 $439 \div 7 = 62 \text{ remainder } 5$

439 ÷ 11 = 39 remainder 10

$$\begin{array}{r}
-39_{-} \\
11 \mid 439 \\
429 \\
-- \\
10 \leftarrow \text{remainder}
\end{array}$$

$$\begin{array}{r}
 -25 \\
 17 \mid 439 \\
 425 \\
 \hline
 14 \leftarrow remainder$$

P₈₆ 443

 $443 \div 2 = 221 \text{ remainder } 1$

1 ← remainder

 $443 \div 3 = 147 \text{ remainder } 2$

2 ← remainder

 $443 \div 5 = 88 \text{ remainder } 3$

443 ÷ 7 = 63 remainder 2

 $443 \div 11 = 40 \text{ remainder } 3$

 $443 \div 13 = 34 \text{ remainder } 1$

1 ← remainder

 $443 \div 17 = 26 \text{ remainder } 1$

443 ÷ 19 = 23 remainder 6

P₈₇ 449

 $449 \div 2 = 224 \text{ remainder } 1$

1 ← remainder

 $449 \div 3 = 149 \text{ remainder } 2$

449 ÷ 5 = 89 remainder 4

449 ÷ 7 = 64 remainder 1

 $449 \div 11 = 40 \text{ remainder } 9$

 $449 \div 13 = 34 \text{ remainder } 7$

449 ÷ 17 = 26 remainder 7

449 ÷ 19 = 23 remainder 12

$$\begin{array}{rrr}
 & -23 \\
 & 19 & | & 449 \\
 & & 437 \\
 & & & --- \\
 & & 12 & \leftarrow \text{ remainder}
\end{array}$$

P₈₈ 457

 $457 \div 2 = 228 \text{ remainder } 1$

1 ← remainder

457 ÷ 3 = 152 remainder 1

1 ← remainder

 $457 \div 5 = 91 \text{ remainder } 2$

457 ÷ 7 = 65 remainder 2

457 ÷ 11 = 41 remainder 6

$$457 \div 13 = 35 \text{ remainder } 2$$

457 ÷ 17 = 26 remainder 15

457 ÷ 19 = 24 remainder 1

P₈₉ 461

 $461 \div 2 = 230 \text{ remainder } 1$

1 ← remainder

461 ÷ 3 = 153 remainder 2

2 ← remainder

461 ÷ 5 = 92 remainder 1

 $461 \div 7 = 65 \text{ remainder } 6$

461 ÷ 11 = 41 remainder 10

 $461 \div 13 = 35 \text{ remainder } 6$

461 ÷ 17 = 27 remainder 2

461 ÷ 19 = 24 remainder 5

$$\begin{array}{rrr}
 & -24 \\
 & 19 & | & 461 \\
 & & 456 \\
 & & & --- \\
 & 5 & \leftarrow \text{ remainder}
\end{array}$$

P₉₀ 463

 $463 \div 2 = 231 \text{ remainder } 1$

1 ← remainder

463 ÷ 3 = 154 remainder 1

1 ← remainder

 $463 \div 5 = 92 \text{ remainder } 3$

463 ÷ 7 = 66 remainder 1

 $463 \div 11 = 42 \text{ remainder } 1$

463 ÷ 13 = 35 remainder 8

 $463 \div 17 = 27 \text{ remainder } 4$

463 ÷ 19 = 24 remainder 7

P₉₁ 467

 $467 \div 2 = 233 \text{ remainder } 1$

1 ← remainder

467 ÷ 3 = 155 remainder 2

2 ← remainder

 $467 \div 5 = 93 \text{ remainder } 2$

 $467 \div 7 = 66 \text{ remainder 5}$

 $467 \div 11 = 42 \text{ remainder } 5$

$$\begin{array}{r}
 -35_{-} \\
 13 \mid 467 \\
 455 \\
 --- \\
 12 \leftarrow remainder
 \end{array}$$

P₉₂ 479

 $479 \div 2 = 239 \text{ remainder } 1$

1 ← remainder

479 ÷ 3 = 159 remainder 2

 $479 \div 5 = 95 \text{ remainder } 4$

 $479 \div 7 = 68 \text{ remainder } 3$

479 ÷ 11 = 43 remainder 6

479 ÷ 13 = 36 remainder 11

$$\begin{array}{r}
-36 \\
13 \mid 479 \\
468 \\
-11 \leftarrow \text{remainder}
\end{array}$$

 $479 \div 17 = 28 \text{ remainder } 3$

$$\begin{array}{r}
-28 \\
17 \mid 479 \\
476 \\
--- \\
3 ← remainder$$

 $479 \div 19 = 25 \text{ remainder } 4$

P₉₃ 487

 $487 \div 2 = 243 \text{ remainder } 1$

1 ← remainder

487 ÷ 3 = 162 remainder 1

1 ← remainder

 $487 \div 5 = 97 \text{ remainder } 2$

 $487 \div 7 = 69 \text{ remainder } 4$

 $487 \div 11 = 44 \text{ remainder } 3$

$$487 \div 13 = 37 \text{ remainder } 6$$

487 ÷ 17 = 28 remainder 11

$$\begin{array}{rrr}
 & -28 \\
 & 17 & | & 487 \\
 & & 476 \\
 & & & --- \\
 & & 11 & \leftarrow \text{ remainder}
\end{array}$$

 $487 \div 19 = 25 \text{ remainder } 12$

P₉₄ 491

 $491 \div 2 = 245 \text{ remainder } 1$

1 ← remainder

 $491 \div 3 = 163 \text{ remainder } 2$

2 ← remainder

 $491 \div 5 = 98 \text{ remainder } 1$

1 ← remainder

 $491 \div 7 = 70 \text{ remainder } 1$

491 ÷ 11 = 44 remainder 7

$$491 \div 13 = 37 \text{ remainder } 10$$

$$\begin{array}{r}
-28_{-} \\
17 \mid 491 \\
476 \\
--- \\
15 \leftarrow \text{remainder}
\end{array}$$

P₉₅ 499

 $499 \div 2 = 249 \text{ remainder } 1$

1 ← remainder

 $499 \div 3 = 166 \text{ remainder } 1$

1 ← remainder

 $499 \div 5 = 99 \text{ remainder } 4$

 $499 \div 7 = 71 \text{ remainder } 2$

 $499 \div 11 = 45 \text{ remainder } 4$

$$499 \div 13 = 38 \text{ remainder } 5$$

5 ← remainder

499 ÷ 17 = 29 remainder 6

499 ÷ 19 = 26 remainder 5

$$-26_{-}$$
19 | 499
494

5 ← remainder

P₉₆ 503

503 ÷ 2 = 251 remainder 1

1 ← remainder

503 ÷ 3 = 167 remainder 2

2 ← remainder

 $503 \div 5 = 100 \text{ remainder } 3$

3 ← remainder

 $503 \div 7 = 71 \text{ remainder } 6$

503 ÷ 11 = 45 remainder 8

$$503 \div 13 = 38 \text{ remainder } 9$$

$$\begin{array}{r}
 -38 \\
 13 \mid 503 \\
 494 \\
 \hline
 9 \leftarrow remainder$$

$$\begin{array}{r}
-29_{-} \\
17 \mid 503 \\
493 \\
--- \\
10 \leftarrow \text{remainder}
\end{array}$$

$$503 \div 19 = 26 \text{ remainder } 9$$

$$-26_{-}$$
19 | 503
494

9 ← remainder

P₉₇ 509

509 ÷ 2 = 254 remainder 1

- - -

1 ← remainder

 $509 \div 3 = 169 \text{ remainder } 2$

2 ← remainder

 $509 \div 5 = 101 \text{ remainder } 4$

4 ← remainder

 $509 \div 7 = 72 \text{ remainder } 5$

 $509 \div 11 = 46 \text{ remainder } 3$

$$509 \div 13 = 39 \text{ remainder } 2$$

$$\begin{array}{r}
-29_{-} \\
17 \mid 509 \\
493 \\
--- \\
16 \leftarrow \text{remainder}
\end{array}$$

$$\begin{array}{r}
-26 \\
19 \mid 509 \\
494 \\
--- \\
15 \leftarrow \text{remainder}
\end{array}$$

P₉₈ 521

 $521 \div 2 = 260 \text{ remainder } 1$

2 |
$$\frac{260}{521}$$

520

1 ← remainder

 $521 \div 3 = 173 \text{ remainder } 2$

521 ÷ 5 = 104 remainder 1

 $521 \div 7 = 74 \text{ remainder } 3$

 $521 \div 11 = 47 \text{ remainder } 4$

1 ← remainder

 $521 \div 17 = 30 \text{ remainder } 11$

$$\begin{array}{r}
-30_{-1} \\
17 \mid 521 \\
510_{-1} \\
11 \leftarrow \text{remainder}
\end{array}$$

521 ÷ 19 = 27 remainder 8

P₉₉ 523

523 ÷ 2 = 261 remainder 1

2 |
$$\frac{-261}{523}$$

522

1 ← remainder

523 ÷ 3 = 174 remainder 1

1 ← remainder

 $523 \div 5 = 104 \text{ remainder } 3$

 $523 \div 7 = 74 \text{ remainder } 5$

523 ÷ 11 = 47 remainder 6

$$523 \div 13 = 40 \text{ remainder } 3$$

$$\begin{array}{r}
-30_{-1} \\
17 \mid 523 \\
510 \\
--- \\
13 \leftarrow \text{remainder}
\end{array}$$

$P_{100} 541$

541 ÷ 2 = 270 remainder 1

1 ← remainder

541 ÷ 3 = 180 remainder 1

1 ← remainder

 $541 \div 5 = 108 \text{ remainder } 1$

1 ← remainder

541 ÷ 7 = 77 remainder 2

 $541 \div 11 = 49 \text{ remainder } 2$

541 ÷ 13 = 41 remainder 8

8 ← remainder

541 ÷ 17 = 31 remainder 14

$$\begin{array}{r}
-31 \\
17 \mid 541 \\
527 \\
-- \\
14 \leftarrow \text{remainder}
\end{array}$$

541 ÷ 19 = 28 remainder 9

 $541 \div 23 = 23$ remainder 12