

Student Name: \_\_\_\_\_

Student ID: \_\_\_\_\_

### In-class Exercise 05 Schema Refinement

Q1. Please calculate  $A^+$ ,  $G^+$  and  $AG^+$  given  $F = \{A \rightarrow B, A \rightarrow C, CG \rightarrow H, CG \rightarrow I, B \rightarrow H\}$  and  $R = (A, B, C, G, H, I)$ . What is the key of  $R$ ?

Solution:

From the given  $F$ , we can obtain that

$$A^+ = ABCGH$$

$$G^+ = G$$

$$AG^+ = ABCGHI = R$$

Thus,  $AG$  is the key of  $R$ .

Q2. Given  $R = (A, B, C)$  and  $F = \{A \rightarrow B, C \rightarrow B\}$ , what is the key for  $R$ ? Is  $R$  in BCNF? Why?

Solution:

$$\text{From } F = \{A \rightarrow B, C \rightarrow B\},$$

$$\text{we can compute } AC^+ = ABC = R,$$

thus  $AC$  is the key of  $R$ .

$R$  is not in BCNF, since note that

$$f_1 = A \rightarrow B, B \text{ is not a subset of } A$$

and  $A$  is not the candidate key of  $R$ .

For  $f_2 = C \rightarrow B$ ,  $B$  is not a subset of  $C$  and  $C$  is not the candidate key of  $R$

Thus,  $R$  is not in BCNF.

Q3. Given a schema  $R = (A, B, C, D, E)$  and functional dependencies  $F = \{E \rightarrow A, E \rightarrow B, A \rightarrow BC, B \rightarrow C\}$ . What is the key of  $R$ ? Is  $R$  in 3NF? Why?

Solution:

Step 1: Find the candidate key of  $R$

$$\Rightarrow DE^+ = DEABC = R$$

Thus, Key =  $DE$

$$F_C = \{E \rightarrow A, E \rightarrow B, A \rightarrow BC, B \rightarrow C\}$$

$$= \{E \rightarrow A, E \rightarrow B, A \rightarrow B, A \rightarrow C, B \rightarrow C\}$$

$$= \{E \rightarrow A, A \rightarrow B, B \rightarrow C\}$$

$$\text{Let } f_1 = E \rightarrow A, f_2 = A \rightarrow B, f_3 = B \rightarrow C$$

For  $f_1$ ,  $A$  is not a subset of  $E$ ,  $E \neq \text{key}$ , and  $A \not\subseteq DE$

Thus,  $R$  is not in 3NF

Q4. Given  $R = \{A, B, C, D, E\}$  and  $F = \{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$ .

(1)  $R_1 = \{A, B, C\}$ ,  $R_2 = \{A, D, E\}$ . Is (1) a lossless join decomposition? Why?

Solution:

Find the candidate key of  $R$

$$A^+ = ABCDE = R$$

Thus,  $A$  is the key of  $R$

Verify given  $R_1$  and  $R_2$

①  $A \in R_1, A \in R_2$

$$\textcircled{2} \quad R_1 \bowtie R_2 = (A, B, C) \bowtie (A, D, E) = (A, B, C, D, E) = R$$

Thus, this is a

Verify the result of  $R_1 \bowtie R_2$

$$\Rightarrow R_1 \bowtie R_2 = (A, B, C) \bowtie (A, D, E) = (A, B, C, D, E) = R$$

Thus, this is a lossless join decomposition

(2)  $R_1 = \{A, B, C\}$ ,  $R_2 = \{C, D, E\}$ . Is (2) a lossless join decomposition? Why?

Solution:

Verify the result of  $R_1 \bowtie R_2$

$$\Rightarrow R_1 \bowtie R_2 = (A, B, C) \bowtie (C, D, E) = (A, B, C, D, E) = R$$

However,  $A \notin R_2$

Thus, this is not a lossless join decomposition

Q5. Given  $R = \{A, B, C, D, E\}$   $F = \{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$ , we have the following decomposition:

$$R1 = \{A, B, C\}, \quad R2 = \{A, D, E\}.$$

Is the above decomposition dependency-preserving? Why?

Solution:

To determine whether the above decomposition is dependency-preserving, we should figure out how it comes from.

$$R = \{A, B, C, D, E\}$$

$\diagup A \Rightarrow BC$ 
 $\diagdown$

$$R_1 = \{A, B, C\} \qquad R_2 = \{A, D, E\}$$

From the process of decomposition stated above, we can know that only  $f_1 = A \rightarrow BC$  is preserved, and the rest of the dependencies are lost.

thus, the above decomposition is not dependency-preserving.

Q6. Given  $R = (A, B, C, D)$  and  $F = \{C \rightarrow D, C \rightarrow A, B \rightarrow C\}$ .

(1) Identify all candidate keys for R.

Solnlich:

From  $F = \{C \rightarrow D, C \rightarrow A, B \rightarrow C\}$ , we can compute

$$\beta^+ = BCAD = R$$

$$\Rightarrow \text{key} = B$$

(2) Is R in BCNF? If not, please decompose R into BCNF.

## Solutions

We have obtained the key of R is B.

From the candidate key and dependency,

we can know that R is not in BCNF

## Decompose R into BNF

Thus, new relations  $R_1 = \{C, D\}$ ,  $R_2 = \{A, C\}$  and  $R_3 = \{B, C\}$  are in BCNF

Q7.  $R = (A, B, C, D, E)$  and  $F = \{AC \rightarrow E, ACD \rightarrow B, CE \rightarrow D, B \rightarrow E\}$ . Please give the canonical cover of  $F$ .

Solution:

From  $F = \{AC \rightarrow E, ACD \rightarrow B, CE \rightarrow D, B \rightarrow E\}$ ,  
we compute

$$F_C = \{AC \rightarrow E, ACD \rightarrow B, CE \rightarrow D, B \rightarrow E\}$$

$$= \{AC \rightarrow E, AC \rightarrow B, CE \rightarrow D, B \rightarrow E\}$$

$$= \{AC \rightarrow B, CE \rightarrow D, B \rightarrow E\}$$

A, B, C, D, E, G

Q8. R = (A, B, C, D, E, ~~G~~, G) and F = {AC → G, D → EG, BC → D, CG → BD, ACD → B, CE → AG}. What is the canonical cover of F? Please decompose R into 3NF.

Solution:

Compute  $F_C$  from the given F

$$\begin{aligned}F_C &= \{AC \rightarrow G, D \rightarrow EG, BC \rightarrow D, CG \rightarrow BD, ACD \rightarrow B, CE \rightarrow AG\} \\&= \{AC \rightarrow G, D \rightarrow E, D \rightarrow G, BC \rightarrow D, CG \rightarrow B, CG \rightarrow D, ACD \rightarrow B, CE \rightarrow A, CE \rightarrow G\} \\&= \{AC \rightarrow G, D \rightarrow E, D \rightarrow G, BC \rightarrow D, \underline{CG \rightarrow B}, \underline{CG \rightarrow D}, \underline{CD \rightarrow B}, \underline{CE \rightarrow A}, \underline{CE \rightarrow G}\} \\&= \{AC \rightarrow G, D \rightarrow EG, BC \rightarrow D, CG \rightarrow D, CD \rightarrow B, CE \rightarrow A\}\end{aligned}$$

Find the candidate key of R

$$\Rightarrow AC^+ = ACGDEB = R$$

$$CD^+ = CDEGAB = R$$

$$BC^+ = BCDEGA = R$$

$$CG^+ = CGDBEA = R$$

$$CE^+ = CEAGDB = R$$

Thus, Key = {AC, CD, BC, CG, CE}

From the candidate key obtained and canonical cover,  
we can know that R is not in 3NF

Decompose R into 3NF

$$R_1 = (A, C, G), R_2 = (D, E, G), R_3 = (B, C, D), R_4 = (C, D, G), R_5 = (A, C, E)$$