

Problem Set 8  
 Econ 312, Spring 2019  
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 Due May 30th, 2019  
 This draft, May 24, 2019

1. [30 pts] Answer all of the questions in the posted handout “*Causality in Econometrics and Statistics: Structural Models are Causal Models.*”
2. [20 pts] Answer all the questions in the posted handout “*The Principles Underlying Evaluation Estimators.*”
3. [10 pts] Compare ITT with TOT and PRTE. Consider two versions of ITT; conditional on  $D = 1$  and unconditional on  $D$ .
4. [20 pts] Answer all of the questions in the posted handout “*The Roy Model and the Generalized Roy Model.*” Specifically, how can the price of one skill rise but the wage associated with the skill decline if person  $i$ ,

$$(\text{wages})\ i = \underset{\substack{\uparrow \\ \text{price of} \\ \text{skill}}}{\pi} (\text{skill})\ i \quad ?$$

(Skill prices are uniform across people)

5. [20 pts] Read the posted handout “*LATE and the Generalized Roy Model: Some Relationships.*”
  - (a) Answer the questions embedded throughout the handout.
  - (b) Compare LATE and MTE for an instrument  $Z$ .

- (c) What is the role of  $Pr(D = 1|X, Z)$  in (i) LATE, (ii) MTE, (iii) selection bias models, and (iv) in propensity score matching estimators? Relate the parameters if you can.
- (d) How does  $Pr(D = 1|X, Z)$  naturally emerge as a key variable in LATE and MTE?
6. Continuation of 5. **Bonus – 20 pts:** Under what conditions is the Generalized Roy model identified nonparametrically?
7. [**Bonus: 30 pts**] Read the posted handout “Simultaneous Causality.” Consider equations (2a) and (2b). Suppose that
- $$(X_1, X_2) \perp\!\!\!\perp (U_1, U_2)$$
- $$U_1 \not\perp\!\!\!\perp U_2$$
- $$\gamma_{12} \neq 0 \quad \gamma_{21} \neq 0$$
- (a) Define the causal effect of  $Y_2$  on  $Y_1$ ; of  $Y_1$  on  $Y_2$ .
- (b) Are these causal effects identified?
- (c) Suppose now that  $\beta_{12} = 0$  and  $\beta_{21} = 0$ ; are they identified?
- (d) Suppose instead of (c) that  $U_1 \perp\!\!\!\perp U_2$ . Are the effects identified? Why or why not?
- (e) Suppose  $U_1 = U_2 = 0$ , but  $\beta_{12} \neq 0, \beta_{21} \neq 0$ . Is the model identified?