

# LHC EFT WG, Area 1

## Truncation, validity, uncertainties

*Editors:* Ilaria Brivio, Sally Dawson, Jorge de Blas,  
Gauthier Durieux, Pierre Savard

*Proposal contributors:*

*A.* Roberto Contino, Adam Falkowski, Florian Goertz,  
Christophe Grojean, Fabio Maltoni, Giuliano Panico,  
Francesco Riva, Andrea Wulzer

*B.* Céline Degrande, Fabio Maltoni, Ken Mimasu,  
Eleni Vryonidou, Cen Zhang

*C.* William Shepherd

January 14, 2022

The truncation of the standard-model effective field theory (SMEFT), its validity and the associated uncertainties have been discussed in a dedicated meeting on [January 19, 2021](#). Answering a call issued beforehand, three proposals were presented: [A](#), [B](#), and [C](#). A preliminary version of the present note summarizing them was written by the editors, submitted for feedback to the proponents, and presented at the [May 3](#) general meeting. [Comments](#) from the wider community were collected in an online document. Experimental collaborations provided formal feedback during a second dedicated meeting on [June 28](#). Extensive discussions took place with the whole community at that occasion, but no consensus emerged. None of the proposals has been approved or validated. No recommendation is therefore put forward at this time and this note only aims at summarizing the different points raised at meetings. Further work is needed to establish a prescription.

## 1 Common ground

There are various points of agreement between proponents of various schemes for dealing with truncation uncertainties. Most participants agree that:

1. most near-future experimental analyses will not aim at probing simultaneously both dimension-six and dimension-eight operator contributions. The SMEFT truncation

of interest is then at the level of dimension-six operators.

2. although they only constitute a partial set of  $1/\Lambda^4$  corrections, the squares of amplitudes featuring a single dimension-six operator insertion provide a convenient proxy to estimate  $1/\Lambda^4$  corrections, as they are well defined and unambiguous. They are indeed gauge invariant and can be translated exactly from one dimension-six operator basis to the other. See [Appendix A](#) for more detailed statements.
3. estimating the relative contributions of dimension-six and dimension-eight operators requires a power counting covering a given range of new-physics scenarios and depends on its parameters (e.g. mass scales and couplings). Being able to compute the dimension-eight dependence of observables is insufficient, as a prescription determining the relative magnitude of dimension-six and dimension-eight operator contributions is still needed.

## 2 Proposals

Specific points made in each proposal are succinctly summarized under Arabic numbers. Additional considerations highlighting pros and cons are listed under Latin lowercases.

Experimental results obtained by following one of the proposals would not be sufficient to allow for the a-posteriori application of the other prescription.

### 2.1 Proposals *A* and *B*

Proposal *A* and *B* are similar thus discussed together. They advocate:

1. providing full multidimensional information on the constrained EFT parameter space, to allow for the proper interpretations in (classes of) new-physics scenarios, and therefore for the EFT validity assessment.
  - (a) Providing individual and marginalized constraints, on single coefficients and in two dimensions, is a first but insufficient step. Full likelihoods, or covariance matrices in Gaussian cases, should be published.
  - (b) Correlations between operator coefficients deriving from specific new-physics assumptions may exclude parameter-space region where linear and quadratic dimension-six truncations diverge significantly and therefore improve the EFT validity.
2. including squared dimension-six dependences by default and comparing results with those obtained in the linear SMEFT approximation.
  - (a) The conclusions drawn from this comparison are more qualitative than quantitative.

In case the two sets of results match each other, one can conclude on the general validity of the dimension-six truncation, as situations in which dimension-eight contributions would dominate over linear dimension-six ones are likely pathological. No additional assumption is required on new physics.

When the linear and quadratic results differ significantly, constraints can only be applied in scenarios where dimension-eight contributions are generically suppressed with respect to quadratic dimension-six ones.

- (b) The linear-quadratic comparison does not reflect the convergence of the EFT series when interference contributions suffer (accidental or understood) suppressions.
  - (c) The assignment of a truncation uncertainty is not prescribed.
  - (d) Purely linear fits can be technically more involved, as they formally allow event rates to turn negative.
3. providing experimental results as functions of the maximal energy probed in the data employed, introducing where necessary an upper cut (denoted e.g.  $E_{\text{cut}}$  or  $M_{\text{cut}}$ ). Data and prediction are compared in the same phase-space region. This procedure, often referred to as *clipping*, provides the necessary information to verify the EFT validity for (classes of) models and enhances the range of scenarios for which a valid EFT interpretation is possible.
- (a) For different cut values, different analysis strategies may be required. While rate measurements could provide the highest sensitivities at high energies, differential observables may be required to probe the relevant operators at moderate energies. Upper energy cuts should therefore be considered from the onset in the analysis design.
  - (b) The reconstruction of the relevant variable to cut on may complicate experimental analyses and result in additional systematic uncertainties (e.g. in final states featuring missing energy). Many EFT analyses (e.g. STXS in the Higgs sector) do however already measure suitable energy variables (e.g. bosons' transverse momenta, or jet invariant masses) as sensitivity arises from these. Example of experimental analyses having adopted such a clipping procedure include diboson measurements by CMS (in  $W\gamma$ ,  $WZ$ ,  $ZZ$  final states).
  - (c) Combining different observables from different processes, each using an upper cut on a different variable, may also raise questions. What variables and cut values are compatible in different processes? The study of specific scenarios may be informative in that regard. Conclusions are expected to be model dependent.
  - (d) Repeating global analyses for several upper cut values would be more costly both computationally and in term of manpower.
  - (e) Applying a cut on the EFT signal simulation instead of the data was proposed by experimental collaborations. As existing run-2 analyses will not be re-designed,

modifying only the signal simulation could in particular be used to incorporate, into EFT fits, analyses in which no good energy variable was measured. The proponents *A* and *B* however judge that comparing data in a given phase-space region (without energy cut) with predictions in a different one (with energy cut) is inconsistent. Further studies could clarify whether the two approaches are practically equivalent in cases of interest.

4. assessing, a posteriori (even after the combination of different measurements), the range of models for which the extracted constraints apply, using this  $E_{\text{cut}}$  information. The experimental results themselves would therefore not incorporate assumptions about new-physics models. This approach allows theorists to interpret the results in the context of specific (classes of) models.

- (a) Quantifying missing dimension-eight contributions would require more effort.

A posteriori, one could approximately reproduce the experimental analysis and include estimates of dimension-eight contributions in the relevant phase-space region to assess their impact.

A priori, one could consider treating linear and quadratic contributions as independent in experimental analyses and, in interpretations, rescale the quadratic contribution to estimate dimension-eight effects. The significant increase in the number of parameters to be fitted may however not be practical.

## 2.2 Proposal *C*

Proposal *C* advocates:

1. using squared dimension-six contributions, which can readily be computed with existing tools, as proxies for missing dimension-eight terms at order  $1/\Lambda^4$ .
  - (a) As the dimension-eight contributions at that order arise from interferences with SM amplitudes, the dimension-eight contributions could have different kinematic distributions or suffer some accidental suppressions.
  - (b) It is claimed (see online [comments](#)) that such contributions violate gauge invariance, in contradiction with [item 2](#) and [Appendix A](#).
2. employing a power-counting rule that would encompass many new-physics models, to estimate dimension-eight contributions from squared dimension-six ones.
  - (a) The line drawn between classes of models that are, and are not, covered by the chosen power-counting rule is somewhat arbitrary.
  - (b) For specific classes of scenarios, this will necessarily be overly conservative. Employing different power-counting rules for different classes of scenarios would permit to quote tighter constraints in the specific cases where they apply.

3. considering the known squared dimension-six terms together with the dimension-eight estimates as theoretical uncertainty on the linear dimension-six signal.
  - (a) As the dimension-six squared contributions are known, they may not need to be included in uncertainties.
  - (b) This uncertainty depends on the SMEFT parameter point and could therefore be practically difficult to include in analyses.
  - (c) Purely linear fits can be technically more involved, as they formally allow event rates to turn negative.
4. folding these uncertainties directly into experimental analyses.
  - (a) This renders experimental results model dependent, as they then rely on a specific scaling between dimension-six and dimension-eight operator coefficients.

5. multiplying the squared dimension-six terms by the following factor to obtain truncation uncertainties:

$$1 + \sqrt{N_8} \frac{g_{\text{SM}}^2}{\mathfrak{C}_6 \Lambda^2} \sqrt{1 + \frac{1}{\mathfrak{C}_6^2 \Lambda^4}} \quad (1)$$

where  $N_8$  is an estimate of the number of contributing dimension-eight operators,  $g_{\text{SM}}$  is the relevant SM coupling,  $\mathfrak{C}_6$  is a dimensionful dimension-six operator coefficient, and  $\Lambda$  is a scale (such that, if identified with the physical BSM mass scale in a two-to-two process, one expects  $\mathfrak{C}_6 \Lambda^2 \sim g_{\text{BSM}}^2$ ).

- (a) The classes of models which are covered by this choice is yet to be determined. Without motivation from new-physics models, the various factors may seem ad hoc.
6. in cases where dimension-eight contributions can be computed, the functional form of dimension-six contributions squared would not need to be used as proxy for the dimension-eight ones and a power counting could be used for dimension-eight (and dimension-six) coefficients directly.

## Appendix A Well-defined and unambiguous squares

In the  $1/\Lambda^2$  expansion of dimension-six amplitudes ( $S$ -matrix elements), the zeroth and first terms,  $A_{\text{SM}}$  and  $A_6/\Lambda^2$ , are separately gauge invariant. The  $A_6/\Lambda^2$  term contains all and only  $1/\Lambda^2$  contributions to the amplitude. The squares of those two terms —  $|A_{\text{SM}}|^2$ ,  $\text{Re}\{A_{\text{SM}}^* A_6\}/\Lambda^2$ ,  $|A_6|^2/\Lambda^4$  — are thus separately gauge invariant too. More terms do appear in the squared amplitude at order  $1/\Lambda^4$ : from dimension-eight operators, amplitudes with two dimension-six operator insertions, or field redefinitions expanded to  $1/\Lambda^4$  order. Each of these other subclasses of  $1/\Lambda^4$  contributions to the squared amplitude is in general not

separately gauge invariant: only the full  $\text{Re}\{A_{\text{SM}}^* A_8\}/\Lambda^4$  is, where  $A_8/\Lambda^4$  collects all and only  $1/\Lambda^4$  contributions to the amplitude and is itself separately gauge invariant.

As a consequence of the equivalence theorem, dimension-six operators related by classical equations of motion have identical amplitudes ( $S$ -matrix elements) to  $1/\Lambda^2$  order. Equivalent operator bases can be defined by exploiting this freedom, changing operator normalizations, or taking linear combinations of them. The linear dimension-six amplitude  $A_6/\Lambda^2$ , including all and only  $1/\Lambda^2$  contributions, can thus be translated exactly from one dimension-six operator basis to the other by a linear transformation between the two sets of operator coefficients  $\{c_6\}$  and  $\{c'_6\}$ . The same transformation can also be used to translate exactly the square of this linear dimension-six amplitude  $|A_6|^2/\Lambda^4$  from one dimension-six basis to the other.

For these two specific reasons, the square of the linear dimension-six amplitude  $|A_6|^2/\Lambda^4$ , where  $A_6/\Lambda^2$  contains all and only  $1/\Lambda^2$  contributions to the amplitude, can be qualified as *well-defined* and *unambiguous*. It can thus for instance be employed as a convenient proxy for estimating full  $1/\Lambda^4$  contributions.