```
Fri Oct 08 00:13:19 2021
heap.h
// heap.h
// a binary min heap
#ifndef HEAP_H
#define HEAP_H
#include <iostream>
#include <string>
const int DEFAULT_SIZE = 100;
template <class KeyType>
class MinHeap
 public:
                friend void testDefaultConstructor();
                friend void testInitConstructor();
                friend void testHeapify();
                friend void testBuildHeap();
                friend void testParentChilds();
                                             // default constructor
    MinHeap(int n = DEFAULT_SIZE);
    MinHeap(KeyType initA[], int n); // construct heap from array
    MinHeap(const MinHeap<KeyType>& heap); // copy constructor
                                             // destructor
    ~MinHeap();
    void heapSort(KeyType sorted[]); // heapsort, return result in sorted
    MinHeap<KeyType>& operator=(const MinHeap<KeyType>& heap); // assignment operator
                                    // return string representation
    std::string toString() const;
  private:
    KeyType *A;
                   // array containing the heap
    int heapSize; // size of the heap
    int capacity; // size of A
                                       // heapify subheap rooted at index
    void heapify(int index);
    void buildHeap();
                                       // build heap
    int leftChild(int index) { return 2 * index + 1; } // return index of left child
    int rightChild(int index) { return 2 * index + 2; } // return index of right child
    int parent(int index) { return (index - 1) / 2; } // return index of parent
    void heapifyR(int index);
                                               // recursive heapify
    void heapifyI(int index);
                                               // iterative heapify
    void swap(int index1, int index2);
                                               // swap elements in A
    void swap(int indexi, int indexi, void copy(const MinHeap<KeyType>& heap); // copy heap to this heap
void destrov(); // deallocate heap
};
template <class KeyType>
std::ostream& operator<<(std::ostream& stream, const MinHeap<KeyType>& heap);
```

#include "heap.cpp"

#endif

```
heap.cpp
               Fri Oct 08 00:21:12 2021
Class: CS 271, Fall 2021
Professor: Jessen Havill
Name: Tung Luu, Wilson Le
Date: October 4, 2021
Purpose: Answers to project 3
// heap.cpp
#include <sstream>
/*
The default constructor. Allocate the array A of the heap with size n, set heapSize = 0 a
nd capacity to n.
Preconditions: the parameter n is either missing, or n must be a non-negative integer.
Postconditions: Return a new instance of MinHeap whose heapSize is 0 and capacity is eith
er n or DEFAULT_SIZE if no parameter n is provided
template <class KeyType>
MinHeap<KeyType>::MinHeap(int n) {
    A = new KeyType[n];
    heapSize = 0;
    capacity = n;
}
Allocate new array A of the heap, copy the content from initA to A and the call buildHeap
to build a correct heap from A.
Preconditions: n must be a non-negative integer
Postconditions: Return a new instance of MinHeap whose internal array is the same as init
A and capacity is n.
*/
template <class KeyType>
MinHeap<KeyType>::MinHeap(KeyType initA[], int n) {
    A = new KeyType[n];
    capacity = n;
    for (int i = 0; i < capacity; i++) {
        A[i] = initA[i];
    buildHeap();
}
/*
Copy constructor
Preconditions: The parameter heap is a correct min heap
Postconditions: Return a new instance of MinHeap which is a copy of the parameter heap
*/
template <class KeyType>
MinHeap<KeyType>::MinHeap(const MinHeap<KeyType>& heap) {
    // Set A = nullptr so that copy method doesn't delete[] A
    A = nullptr;
    copy (heap);
}
/*
Destructor
Preconditions: None
Postconditions: Completely remove this min heap from memory.
*/
template <class KeyType>
MinHeap<KeyType>::~MinHeap() {
    destroy();
}
Perform heapsort, return result in the sorted array
Preconditions: This heap is a correct min heap.
Postconditions: The array sorted is sorted
*/
```

1

```
template<class KeyType>
void MinHeap<KeyType>::heapSort(KeyType sorted[]) {
    int initialHeapSize = heapSize;
    for(int i = heapSize - 1; i >= 1; i--) {
        swap(0, i);
        heapSize--;
        heapify(0);
    // Change the heapSize back into its initial value
    heapSize = initialHeapSize;
    // Now A is sorted in reverse order. We just need copy A to sorted in reverse order.
    for(int i = 0; i < heapSize; i++) {</pre>
        sorted[i] = A[heapSize - i - 1];
    // Reverse A to turn A back into a correct heap
    for(int i = 0; i < heapSize; i++) {</pre>
        A[i] = sorted[i];
}
Heapify subheap rooted at index
Preconditions: Two subtrees at root index are correct min heaps
Post conditions: The tree at root index is a correct min heap.
template < class KeyType >
void MinHeap<KeyType>::heapify(int index) {
    heapifyR(index);
Build heap from the array A
Preconditions: None
Postconditions: This heap is a correct min heap.
template <class KeyType>
void MinHeap<KeyType>::buildHeap() {
    heapSize = capacity;
    // Iterate from the node (capacity / 2) - 1 to 0, which is iterating in bottom-up met
hod, and call heapify in each iteration
    for (int i = (capacity / 2) - 1; i >= 0; i--) {
        heapify(i);
}
Heapify subheap rooted at index using recursive method
Preconditions: Two subtrees at root index are correct min heaps
Post conditions: The tree at root index is a correct min heap.
*/
template < class KeyType >
void MinHeap<KeyType>::heapifyR(int index) {
    int left = leftChild(index);
    int right = rightChild(index);
    int smallestChild = index;
    if(left < heapSize && A[left] < A[index]) {</pre>
        smallestChild = left;
    if(right < heapSize && A[right] < A[smallestChild]) {</pre>
        smallestChild = right;
```

```
if(smallestChild != index) {
        swap(index, smallestChild);
        heapifyR(smallestChild);
    }
}
Heapify subheap rooted at index using iterative method
Preconditions: Two subtrees at root index are correct min heaps
Post conditions: The tree at root index is a correct min heap.
*/
template<class KeyType>
void MinHeap<KeyType>::heapifyI(int index) {
    while(leftChild(index) < heapSize) {</pre>
        int left = leftChild(index);
        int right = rightChild(index);
        int smallestChild = index;
        if(left < heapSize && A[left] < A[index]) {</pre>
            smallestChild = left;
        if(right < heapSize && A[right] < A[smallestChild]) {</pre>
            smallestChild = right;
        if(smallestChild != index) {
            swap(index, smallestChild);
            index = smallestChild;
        }
        else {
            break;
    }
}
/*
Swap two elements at index1 and index2 in A
Preconditions: index1 and index2 are valid element in the array A
Postconditions: two elements at index1 and index2 are swapped
template <class KeyType>
void MinHeap<KeyType>::swap(int index1, int index2) {
    KeyType temp = A[index1];
    A[index1] = A[index2];
    A[index2] = temp;
}
Copy the parameter heap to this heap
Preconditions: The parameter heap is a correct min heap
Postconditions: This heap becomes a copy of the parameter heap
template <class KeyType>
void MinHeap<KeyType>::copy(const MinHeap<KeyType>& heap) {
    destroy();
    heapSize = heap.heapSize;
    capacity = heap.capacity;
    A = new KeyType[capacity];
    for(int i = 0; i < heapSize; i++) {
        A[i] = heap.A[i];
    }
}
Destroy is a function to deallocate this heap.
Preconditions: None.
Postconditions: The array A of this heap is removed from memory and instance variables he
apSize and capacity are set to 0.
```

```
heap.cpp
               Fri Oct 08 00:21:12 2021
*/
template <class KeyType>
void MinHeap<KeyType>::destroy() {
    if(A != nullptr) {
        delete[] A;
    heapSize = 0;
    capacity = 0;
}
/*
Assignment operator.
Preconditions: The parameter heap is a correct min heap.
Postconditions: if this heap and the parameter heap is not the same (having the same addr
ess), this heap becomes a copy of the parameter heap
template<class KeyType>
MinHeap<KeyType>& MinHeap<KeyType>::operator=(const MinHeap<KeyType>& heap) {
    if(this != &heap) {
        copy (heap);
    return *this;
// Use the following toString() for testing purposes.
template <class KeyType>
std::string MinHeap<KeyType>::toString() const
        std::stringstream ss;
        if (capacity == 0)
                ss << "[ ]";
        else
                ss << "[";
                if (heapSize > 0)
                {
                         for (int index = 0; index < heapSize - 1; index++)</pre>
                                 ss << A[index] << ", ";
                         ss << A[heapSize - 1];
                }
                ss << " | ";
                if (capacity > heapSize)
                         for (int index = heapSize; index < capacity - 1; index++)</pre>
                                 ss << A[index] << ", ";
                         ss << A[capacity - 1];
                ss << "]";
        return ss.str();
template <class KeyType>
std::ostream& operator<<(std::ostream& stream, const MinHeap<KeyType>& heap)
{
        return stream << heap.toString();</pre>
```

```
#include<sstream>
#include<string>
#include <assert.h>
#include "heap.h"
using namespace std;
void testDefaultConstructor() {
        MinHeap<int> heap1 = MinHeap<int>();
        assert (heap1.capacity == 100);
        assert(heap1.heapSize == 0);
        MinHeap<int> heap2 = MinHeap<int>(50);
        assert (heap2.capacity == 50);
        assert(heap2.heapSize == 0);
        cout << "Default Constructor Passed" << endl;</pre>
void testInitConstructor(){
        int initA[5] = \{0, 1, 2, 3, 4\};
        MinHeap<int> heap1 = MinHeap<int>(initA, 5);
        assert(heap1.capacity == 5);
        assert(heap1.heapSize == 5);
        cout << "Init Constructor Passed" << endl;</pre>
void testCopyConstructor(){
        int initA[5] = \{0, 1, 2, 3, 4\};
        MinHeap<int> heap1 = MinHeap<int>(initA, 5);
        MinHeap<int> heap2 = MinHeap<int>(heap1);
        assert(heap1.toString() == heap2.toString());
        cout << "Copy Constructor Passed" << endl;</pre>
void testAssignmentOperator(){
        int initA[5] = \{0, 1, 2, 3, 4\};
        MinHeap<int> heap1 = MinHeap<int>(initA, 5);
        MinHeap<int> heap2 = heap1;
        assert(heap1.toString() == heap2.toString());
        cout << "Assignment Operator Passed" << endl;</pre>
}
void testHeapSort(){
        int initA[10] = \{10, 8, 9, 1, 2, 4, 5, 3, 7, 6\};
        int n = 10;
        MinHeap<int> heap = MinHeap<int>(initA, n);
        heap.heapSort(initA);
        stringstream s;
        s << "[";
        for (int i = 0; i < n - 1; i++) {
                s << initA[i] << ", ";
        s << initA[n - 1] << "]";
        assert(s.str() == "[1, 2, 3, 4, 5, 6, 7, 8, 9, 10]");
        cout << "Heap Sort " << s.str() << " Passed" << endl;</pre>
}
void testHeapify() {
        int n = 4;
        int initA[4] = \{0, 1, 2, 3\};
        MinHeap<int> heap = MinHeap<int>(initA, n);
        heap.capacity++;
        heap.A[n] = 4;
        heap.heapSize++;
        heap.heapify(1);
        stringstream s;
        s << "[";
        for (int i = 0; i < heap.heapSize - 1; i++) {
                s << heap.A[i] << ", ";
        s << heap.A[heap.heapSize - 1] << "]";
        assert(s.str() == "[0, 1, 2, 3, 4]");
```

```
Fri Oct 08 00:20:28 2021
test_heap.cpp
        cout << "Heapify " << s.str() << " Passed" << endl;</pre>
}
void testBuildHeap(){
        int n = 5;
        int initA[5] = \{0, 2, 3, 5, 7\};
        MinHeap<int> heap = MinHeap<int>(initA, n);
        heap.capacity++;
        heap.A[n] = 1;
        heap.heapSize++;
        heap.buildHeap();
        stringstream s;
        s << "[";
        for (int i = 0; i < heap.heapSize - 1; i++) {
                s << heap.A[i] << ", ";
        s << heap.A[heap.heapSize - 1] << "]";</pre>
        assert(s.str() == "[0, 2, 1, 5, 7, 3]");
        cout << "Build Heap " << s.str() << " Passed" << endl;</pre>
void testParentChilds() {
        int initA[3] = \{0, 1, 2\};
        MinHeap<int> heap = MinHeap<int>(initA, 3);
        assert(heap.parent(1) == 0);
        assert(heap.parent(2) == 0);
        assert(heap.leftChild(0) == 1);
        assert(heap.rightChild(0) == 2);
        cout << "Test Parent Childs Passed" << endl;</pre>
}
int main(){
        testDefaultConstructor();
        testInitConstructor();
        testCopyConstructor();
        testAssignmentOperator();
        testHeapSort();
        testBuildHeap();
        testHeapify();
```

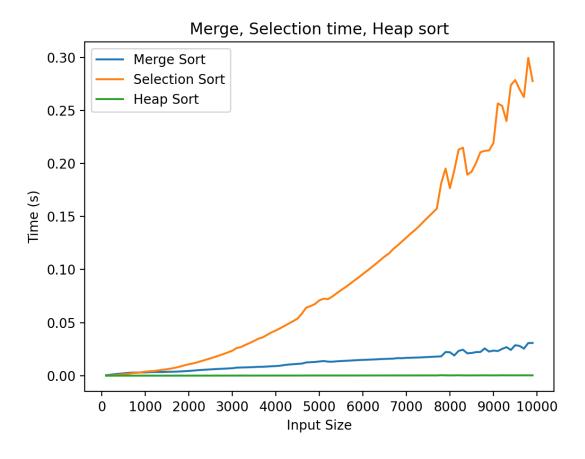
testParentChilds();

return 0;

}

CS271 Project 3 Wilson Le, Tung Luu

October 2021



- Asymptotic time complexity of the heap sort algorithm on an array that is already sorted:
  - $-\Theta(n\log n)$
- Asymptotic time complexity on an array that is in reverse order:
  - $-\Theta(n\log n)$
- Best case asymptotic time complexity of heap sort
  - $-\Theta(n\log n)$
- What kind of input does the best case asymtotic time complexity occur
  - Asymtotic time complexity of heap sort will always be  $\Theta(n \log n)$ , because the algorithm will carry on regardless of the order of the input list.