Wavelet-Based Dual-Branch Network for Image Demoiréing

Lin Liu 1,2 Jianzhuang Liu 2 Shanxin Yuan 2* Gregory Slabaugh 2 Aleš Leonardis 2 Wengang Zhou 1 Qi $Tian^3$

University of Science and Technology of China
 Noah's Ark Lab, Huawei Technologies
 Huawei Cloud BU

Abstract. When smartphone cameras are used to take photos of digital screens, usually moiré patterns result, severely degrading photo quality. In this paper, we design a wavelet-based dual-branch network (WDNet) with a spatial attention mechanism for image demoiréing. Existing image restoration methods working in the RGB domain have difficulty in distinguishing moiré patterns from true scene texture. Unlike these methods, our network removes moiré patterns in the wavelet domain to separate the frequencies of moiré patterns from the image content. The network combines dense convolution modules and dilated convolution modules supporting large receptive fields. Extensive experiments demonstrate the effectiveness of our method, and we further show that WDNet generalizes to removing moiré artifacts on non-screen images. Although designed for image demoiréing, WDNet has been applied to two other low-level vision tasks, outperforming state-of-the-art image deraining and deraindrop methods on the Rain100h and Raindrop800 data sets, respectively.

Keywords: Deep learning, Image demoiréing, Wavelet

1 Introduction

A smartphone has become an indispensable tool in daily life, and the popularity of mobile photography has grown supported by advancements in photo quality. It has become increasingly common to take photos of digital screens in order to quickly save information. However, when a photo is taken of a digital screen, moiré patterns often appear and contaminate the underlying clean image. These moiré patterns are caused by the interference between the camera's color filter array (CFA) and the screen's subpixel layout. In general, moiré patterns are likely to appear when two repetitive patterns interfere with each other. For example, moiré artifacts can appear when the repetitive patterns in textiles and building's bricks interfere with camera's CFA. Removing moiré patterns is challenging, as moiré patterns are irregular in shape and color, and can span a large range of frequencies. Unlike other image restoration tasks, such as image denoising

^{*} Corresponding author

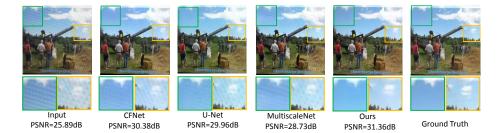


Fig. 1: Qualitative comparison among CFNet [32], U-Net [42], MultiscaleNet [53] and our network on the TIP2018 data set [53]. Ours is trained in the wavelet domain and removes the moiré patterns significantly better.

[67,27,54], image demosaicing [9,34] and super resolution [69,22,19,20], where the challenge is mainly in removing high-frequency noise and recovering details, image demoiréing requires not only recovering high frequency image details, but also removing moiré patterns with frequencies spanning a large range.

Most existing image restoration methods [42,21,69] working in the RGB domain are not tailored to image demoiréing, though a few attempts [53,32,14] have been made to tackle it recently. Sun et al. [53] proposed a multi-resolution network to remove moiré patterns of different frequencies/scales. Liu et al. [32] developed a coarse-to-fine network and trained it on a synthetic dataset and refined real images with GAN. He et al. [14] utilized the edge information and appearance attributes of moiré patterns to demoiré. However, all the existing methods (working in the RGB domain) have difficulty in distinguishing moiré patterns from the real image content, and in dealing with low-frequency moiré patterns [53]. Fig. 1 shows some qualitative comparisons among four methods (including ours). We argue that image demoiréing can be more easily handled in the frequency domain. Wavelet-based methods have been explored in computer vision and shown good performance, e.g., in classification [7,38], network compression [28,11], and face super-resolution [19]. However, due to their task-specific design, these methods cannot be directly used for image demoiréing.

In this paper, we propose to remove moiré patterns in the frequency domain, where the input image with moiré patterns is first decomposed into different frequency bands using a wavelet transform. After the wavelet transform, moiré patterns are more apparent in certain wavelet subbands, where they can be more easily removed (see Fig. 3 for example). Our model, working in the frequency domain, is a dual-branch network with dense branches and dilated branches, which are responsible for restoring the close-range and far-range information, respectively. We also design a spatial attention mechanism called a direction perception module in the dense branches to highlight the areas with moiré patterns.

In this paper, we make following contributions:

1. We propose a novel wavelet-based and dual-branch neural network for image demoiréing. We also propose a spatial attention mechanism called direction perception module (DPM) to highlight the areas with moiré patterns.

- 2. Our network achieves the best results on the demoiréing task. Our trained model can also remove moiré artifacts on non-screen images.
- 3. Our new architecture generalises well to other low-level vision tasks, such as deraining and deraindrop, where we also obtain state-of the-art results.
- 4. In addition, we built a new urban-scene data set with more types of moiré patterns, which will be made publicly available.

2 Related Work

In this section, we give a brief review of the most relevant work for image demoiréing.

Moiré Pattern Removal. Early image demoiréing work [48,43,46,33,61] focused on certain specific moiré patterns. Sidorov et al. [48] presented a spectral model to address monotonous and monochrome moiré patterns. Other work tried to remove striped moiré artifacts [43,56,47] or dotted artifacts [46,51,25] in scanned or X-ray images. Yang et al. [61] and Liu et al. [33] removed moiré artifacts using low-rank and sparse matrix decomposition. But their methods focus on textile moiré patterns and cannot handle low-frequency moiré patterns. Compared to these methods, our approach can deal with a much larger range of moiré patterns as we do not make presumptions about the moiré patterns. Contemporary models [53,32,14,70] and recent challenges [65,66,64] cast image demoiréing as an image restoration problem addressed using deep learning. Recently Liu et al. [32] built a coarse-to-fine convolutional neural network to remove moiré patterns from photos taken of screens. But the method mainly used synthetic data for network training and focuses on removing moiré patterns in text scenes. Sun et al. [53] proposed a multi-resolution convolutional neural network for demoiréing and released an associated dataset. He et al. [14] labeled the data set in [53] with three attribute labels of moiré patterns, which is beneficial to learn diverse patterns. This method, along with [32,53], works in the RGB domain and in a multi-scale manner. Such a strategy has limited capacity to correctly distinguish moiré patterns from true image content. In contrast, our method works in the wavelet domain, and we introduce a novel network design, resulting in stronger moiré pattern removal while restoring image details.

Wavelet-based Methods. Wavelet-based methods have been explored in some computer vision tasks, including classification [7,38,29,57], network compression [28,11], face aging [36], super-resolution [19,35], style transfer [63], etc. Fujieda et al. [7] proposed wavelet CNNs that utilize spectral information to classify the textures. Liu et al. [36] used a wavelet-based method to capture agerelated texture details at multiple scales in the frequency domain. Our work is the first to use a wavelet transform to remove moiré patterns in the frequency domain. Compared with Fourier transform and discrete cosine transform, wavelet transform considers both spatial domain information and frequency domain information. With the wavelet composition, different wavelet bands represent such a broad range of frequencies, which can not be achieved by a few convolutional layers even with large kernels.

The most relevant in the above studies is [19] for using wavelets for face superresolution, where a neural network is deployed to predict the wavelet coefficients. But predicting the wavelet coefficients of a moiré-free image from its moiré image in the RGB domain is difficult. Moiré patterns cover a wide range in both space and frequency domains, making it hard to distinguish moiré patterns from true scene textures. For photo-realistic style transfer, Yoo et al. [63] regarded the wavelet transform and wavelet inverse transform as a pooling layer and an unpooling layer respectively, with the aim of preserving their structural information. However, this technique [63] may not be suitable for image demoiréing, where moiré patterns can have strong structural information overlaid with true image contents. Our work runs directly in the wavelet domain. Wavelet transform and inverse wavelet transform are used outside of the network.

Dual-branch Design. Dual-branch network structure design makes use of two branches, complementing each other [8,40,6,45]. It has been used in image super-resolution [40], classification [8], segmentation [6] and person-re-ID [45]. Gao et al. [8] proposed a dual-branch network for polarimetric synthetic aperture radar image classification. One branch is used to extract the polarization features and the other to extract the spatial features. Fu et al. [6] proposed a dual attention network with a position attention module and a channel attention module for scene segmentation. For image super-resolution, the dual branch in [40] can give consideration to easy image regions and hard image regions at the same time. All existing dual-branch networks have different branches, each focusing on certain image features, which only merge at the end of the network. In our design, the two branches iteratively communicate with each other to achieve a better representation.

Texture Removal. Texture removal [50,13,68] is related to demoiréing, as moiré patterns can be viewed as a special type of texture. Methods using local filters attempted to remove certain textures while maintaining other high-frequency structures [50,13,68]. Subr et al. [50] smoothed texture by averaging two manifolds from local minima and maxima. Both Ham et al. [13] and Zhang et al. [68] used dynamic guidance and a fidelity term for image filtering. Multiple strategies to smooth texture were used in [49,24,1]. Optimization-based methods were also exploited [52,59,58]. Sun et al. [52] and Xu et al. [58] used l_0 minimization to retrieve structures from images. Xu et al. [59] optimized a global function with relative total variation regularization. However, these texture removal methods focus on the structure of the image and remove some repeated and identical or similar patterns. They do not address moiré patterns that span a much wider range of frequencies and appear in varied shapes and directions.

3 Our Method

The architecture of **WDNet** is shown in Fig. 2. The original RGB image input is first transformed into the **W**avelet domain, where a **D**ual-branch **Net**work is used to remove the moiré patterns. The final RGB image output is obtained by applying the inverse wavelet transform to the network's output. The dual-

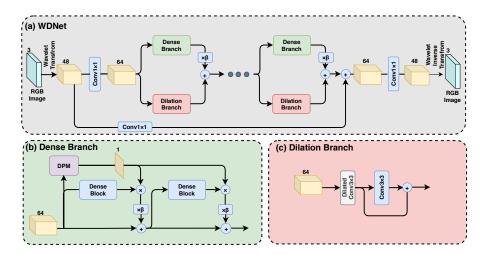


Fig. 2: The architecture of the proposed WDNet (a) consisting of two kinds of branches, the dense branch (b) for restoring the close-range information and the dilation branch (c) for restoring the far-range information. Working in the wavelet domain can better remove the moiré patterns and retain the details. The numbers of channels are given in the figure.

branch network has seven dual-branch modules, each including a dense branch and a dilation branch. A ResNet [15] style skip connection is made. The dense and dilation branches are responsible for acquiring moiré information in different frequency ranges; the former detects close-range patterns and the latter detects far-range patterns.

3.1 Working in the Wavelet Domain

Our network operates in the wavelet domain to remove moiré patterns. We employ 2D fast wavelet transform (FWT) to decompose the input RGB image into a sequence of wavelet subbands (coefficients) of a common smaller size, but with different frequency content. We choose the simplest Haar wavelet as the basis for the wavelet transform. A Haar wavelet transform can be efficiently computed and suitable for our task. The FWT iteratively applies low-pass and high-pass decomposition filters along with downsampling to compute the wavelet coefficients where the low-pass filter = $(1/\sqrt{2}, 1/\sqrt{2})$ and the high-pass filter = $(1/\sqrt{2}, -1/\sqrt{2})$. In each level of the transform, we use the high-pass filter and the low-pass filter along the rows to transform an image to two images, and then we apply the same filters along the columns of these two images, obtaining four images in total. The equations to derive the subbands can be found in [10].

As shown in Figs. 3(c) and (d), the wavelet subbands at different levels correspond to different frequencies. Moiré patterns are conspicuous only in certain wavelet subbands. For example, in Fig. 3(e), the difference between (c) and (d)

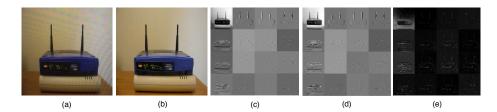


Fig. 3: (a) An image with moiré patterns. (b) The ground truth of (a). (c) Wavelet subbands transformed from the gray-level image of (a). (d) Wavelet subbands transformed from the gray-level image of (b). (e) Difference between (c) and (d).

shows that the first three wavelet subbands of the first column in Fig. 3(c) contain obvious and different moiré patterns. From our experiments, we find that wavelet subbands with higher frequencies usually contain fewer moiré patterns. These wavelet subbands provide important information to recover the details for moiré pattern-free images.

In our method, the wavelet transform level is set to 2. The original RGB input is transformed into 48 subbands, with 16 subbands for each color channel. As such, another benefit of working in the wavelet domain is that the spatial size of the original image $(H \times W \times 3)$ is reduced by a quarter in both the width and height $((H/4) \times (W/4) \times 48)$. The reduced spatial size consequently reduces the computation in the deep network. Besides, we concatenate all the 48 channels instead of processing the high and low frequency bands individually, because moire patterns for each image vary a lot, it is difficult to find a threshold to manually separate them.

3.2 Dense Branch

DenseNet [18] can alleviate the problem of vanishing gradient and reduce the number of network parameters through the design of bypass connections and feature reuse. In low-level vision, dense blocks have been used in deraining and dehazing [44,12], and image super-resolution with the Residual Dense Network (RDN) [69] or other networks [22].

As shown in Fig. 2(b), we design each dense branch by adding a new Direction Perception Module (DPM) to the residual dense module borrowed from RDN [69]. The residual dense module has two small dense blocks each with 5 convolutional layers. In the same dense block, the input of each layer contains the output of all previous layers. DPM is used to find the directions of moiré patterns and will be explained in Section 3.4 in detail. The output of DPM and each dense block are multiplied, weighted by a factor β , and then the result is added to the input. This design can effectively find the locations of close-range moiré patterns.

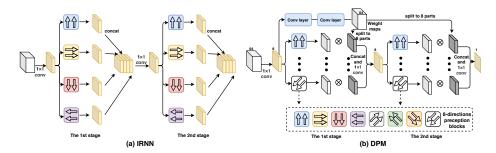


Fig. 4: (a) Image recurrent neural network (IRNN). (b) Our direction perception module (DPM) with two stages, each with 8 directions.

3.3 Dilation Branch

Subsampling or pooling feature maps can enlarge receptive fields, but loses some details. Dilated convolution is used to overcome this problem. In each of our dilation branches (Fig. 2(c)), there are two layers: a 3×3 dilated convolution layer with a dilation rate $d_{k+2} = d_k + d_{k+1}$, followed by a traditional 3×3 convolution, where k is the index of a dilation branch with $d_1 = 1$ and $d_2 = 2$. The rationale for this design is explained below.

When multiple dilated convolutions with a fixed dilation rate (say, 2) are applied successively, many pixels are not involved in the convolutions and a special kind of artifact called *gridding* appears [55]. Alternatively, a hybrid design using dilation rates (1,2,3,1,2,3,...) [55] is not suitable for our task because these dilations are not large enough to cover general moiré patterns. Therefore, we design our dilation rates according to the Fibonacci series (e.g., (1,2,3,5,8,13,21)) when there are 7 dilation branches). Additionally, we apply a traditional 3×3 convolution on the output of the dilated convolution to further reduce any gridding artifact (Fig. 2(c)).

3.4 Direction Perception Module

We propose a Direction Perception Module (DPM) by improving the Image Recurrent Neural Network (IRNN) [2,60,17], as shown in Fig. 4. The two-stage four-directional IRNN (Fig. 4(a)) architecture enhances the use of contextual information, where the first stage in IRNN aims to produce feature maps that acquire neighboring contextual information and the second stage in IRNN further gathers the global information. However, in IRNN, in the feature maps at the end of the first stage, a pixel can only obtain information in the vertical and horizontal directions, but not in other directions.

As shown in Fig. 4(b), we improve IRNN in two aspects. First, we extend the 4-direction perception to 8-direction perception by including 4 more diagonal directions to enhance the detection ability of slanting moiré patterns. The moiré patterns in other directions are detected in the second stage. Second, the weight maps are used to distinguish the importance of information in different

directions. Unlike IRNN which learns direction-aware features in the embedded space, we use DPM to generate the attention map which highlights moiré pattern spatial distributions and is supervised by L_a discussed in Sec. 3.6. The combination of the two convolution layers and the eight-direction perception blocks is equivalent to an attention operation.

Loss Function. The loss function of the whole network is defined as follows:

$$L = \lambda_1 L_a + \lambda_2 L_{l_1} + \lambda_3 L_p + \lambda_4 L_w, \tag{1}$$

where L_{l_1} is the l_1 loss between the image and its ground-truth in the RGB domain, L_p is the perceptual loss [23], and the other parts are described below.

Wavelet Loss. Let $C = (c_1, c_2, ..., c_N)$ and $\hat{C} = (\hat{c}_1, \hat{c}_2, ..., \hat{c}_N)$ be the ground-truth and the estimated wavelet subbands, respectively. Two wavelet-based losses, MSE loss l_{MSE} and detail loss l_{detail} , are defined as follows:

$$l_{\text{MSE}} = \gamma_1 \sum_{i=1}^{3} \|\hat{c}_i - c_i\|^2 + \gamma_2 \sum_{i=4}^{N} \|\hat{c}_i - c_i\|^2,$$
 (2)

where the first term is for the low-frequency components, and the second for the high-frequency ones, and γ_1 and γ_2 are two weighting factors.

$$l_{detail} = \sum_{i=4}^{N} \max \left(\alpha |c_i|^2 - |\hat{c}_i|^2, 0 \right),$$
 (3)

which is inspired by the work in super-resolution [19] to prevent the wavelet coefficients from converging to 0 and therefore retaining the high-frequency details of the image. α is a positive number and set to 1.2 in this work. Setting α to a value greater than 1 can effectively prevent \hat{c}_i from converging to 0. Different from the loss function in [19], ours does not have a bias value ϵ , because we found that ϵ has little effect on the final results. Besides, the value of ϵ in [19] was set to 0 in their source code. The network's wavelet loss L_w is then:

$$L_w = l_{\text{MSE}} + l_{detail}. \tag{4}$$

Attention Loss. We further apply the attention loss L_a as:

$$L_a = ||A - d(M)||_2^2, (5)$$

where A is the output of the DPM in the network and M is the mask of the moiré patterns, which is computed by thresholding the difference between the moiré-contaminated image and the ground-truth. $d(\cdot)$ is a downsampling operation to ensure that the mask and A have the same size. The threshold is set to 15 in this work.

4 Experiments

We compare WDNet with state-of-the-art methods, and conduct user studies for image demoiréing. We also demonstrate that WDNet when trained only for screen image demoiréing can also remove moiré artifacts on non-screen images. Finally, we apply WDNet to two other tasks, deraining and de-raindrop, to show that our method generalizes well to other frequency-based low-level vision tasks.

4.1 Implementation Details

Throughout our experiments, the input is a $256 \times 256 \times 3$ RGB image, which is then transformed into 48 different-level wavelet subbands with the size of 64×64 by a Haar wavelet transform. We use seven dual-branch modules and add DPM into the 4th dense branch to perceive moiré patterns. Our model is implemented in PyTorch and runs on a NVIDIA Tesla V100 GPU. The batch size is set to 16 during training. Adam [26] is used to search the minimum of the loss function. The learning rate of the generator is 0.0002 and reduced by one-tenth for every 20 epochs. In Eqns. (1) and (2), the parameters λ_1 , λ_2 , λ_3 , λ_4 , γ_1 and γ_2 are empirically set to 1, 5, 10, 200, 0.01 and 1.1 respectively. The method of eye initialization in [69] is used to initialize the weights of WDNet. The value of β throughout the paper is set to 0.2. The dense branch has more parameters than the dilation branch. Setting β to 0.2 makes the weights of the dilation branchs parameters larger, which can maintain the details of the original image.

4.2 Datasets and State-of-the-Art Methods

We perform experiments on two datasets, TIP2018 [53] and a new London's Buildings. The TIP2018 dataset contains 100,000+ image pairs with about 800×800 resolution and the moiré-free images come from the ImageNet ISVRC 2012 dataset. The new dataset London's Buildings was built by us recently and will be publicly released. It is an urban-scene data set and its images contain bricks, windows and other regular patterns which are prone to generate moiré patterns. We use mobile phones and screens different from those used in the TIP2018 data set and thus provide additional diversity of moiré patterns. London's Buildings includes 400 training pairs and 60 testing pairs with about 2300×1700 resolution. The 256×256 images used in training are resized (in TIP2018) or cropped (in London's buildings) from the original higher-resolution images. We conduct two experiments on the TIP2018 data set, TestA and TestB. TestB follows the same setting as in [53]. TestA is a subset of TestB and this subset contains 130 hard samples from the same camera.

We compare our model with MuiltiscaleNet [53], CFNet [32], Pix2pix [21], U-Net [42], MopNet [14], and ResNet-34 [15]. For fair comparison, when a network is trained on the TIP2018 data set, we use the same setting as in [53]. We faithfully reimplement MuiltiscaleNet [53] and CFNet [32] based on their papers. Note that since MopNet is very recent work without its code released, we can only compare with it in one experiment where [14] gives its result on TIP2018.

Table 1: Quantitative comparison on TIP2018. The best results are in **bold**.

Test set		Pix2pix	U-Net	CFNet	${\bf Multiscale Net}$	MopNet	WDNet
TestA	PSNR/SSIM	25.32/0.756	25.80/0.803	25.52/0.810	26.11/0.801	-/-	27.88/0.863
TestB	PSNR/SSIM	25.74/0.825	26.49/0.864	26.09/0.863	26.99/0.871	27.75/0.895	28.08/0.904

Table 2: Quantitative comparison on London's Building.

	U-Net	MultiscaleNet	ResNet	CFNet	WDNet
PSNR/SSIM	23.48/0.790	23.64/0.791	23.87/0.780	23.22/0.764	25.41/0.839

Table 3: User study. The preference rate shows the percentage of comparisons in which the users prefer our results.

	WDNet>CFNet	${\rm WDNet}{>}{\rm U}\text{-Net}$	${\bf WDNet}{>}{\bf MultiscaleNet}$
Preference rate	83.7%	82.1%	80.5%

4.3 Comparison with the State-of-the-Art

For quantitative comparison, we choose the PSNR and SSIM. As shown in Tables 1 and 2, our method outperforms the state-of-the-art on both datasets. Note that our model outperforms the most recent MopNet [14] by 0.33dB, even though MopNet uses additional annotation (labelling TIP2018 with three attribute labels of moiré patterns) for training. We show some qualitative results in Figs. 5 and 6, where there are different kinds of moiré patterns appearing in the input images. Our WDNet most effectively removes the moiré patterns. For the computation consumption, CFNet, MultiscaleNet, U-Net, MopNet and WDNet take $58.2 \, \mathrm{ms}$, $5.7 \, \mathrm{ms}$, $3.8 \, \mathrm{ms}$, $71.8 \, \mathrm{ms}$ and $14.6 \, \mathrm{ms}$, respectively, to restore a 256×256 image on one NVIDIA Tesla P100 GPU.

User Studies We also conduct a user study with 10 users to compare the visual quality of the results generated by the models. During the study, two images I_1 and I_2 , respectively obtained by our model and another model, and the corresponding moiré-free image (ground truth) I, are shown to a user who is asked to choose one from I_1 and I_2 which is closer to I. There are 100 triplets of these images randomly selected from TIP2018 to compare two models and the results are reported in Table 3.

Removal of Moiré Artifacts on Non-screen Images Moiré artifacts may also appear on objects with dense repetitive textures, such as buildings and clothes. This kind of moiré artifacts usually does not always appear on the whole image. In Fig. 7, we show some results of directly applying our WDNet model trained on TIP2018 without fine-tuning on non-screen images. It shows that our method is effective in removing this kind of moiré patterns as well.

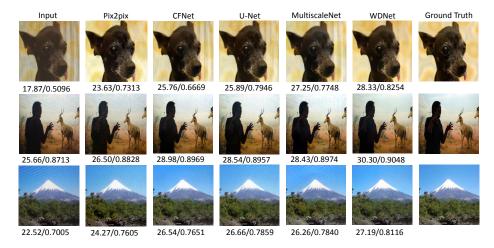


Fig. 5: Visual comparison among Pix2pix [21], CFNet [32], U-Net [42], MuiltiscaleNet [53] and our model WDNet, evaluated on images from the TIP2018 data set. The numbers under the images are PSNR/SSIM.



Fig. 6: Visual comparison on an image from the London's Building data set.



Fig. 7: Some results on non-screen images.

4.4 Ablation Studies

To conduct ablation studies to quantify the contributions of the components of WDNet, the TestA dataset is used in the experiments. To understand the restoration strategy between the two branches in the dual-branch architecture, we examine the feature maps of WDNet. At layer six, we normalize each channel of the feature map, and then sum up the values channel-wise to obtain a heat map. As shown in Fig. 8, the dense branch focuses on the local moiré patterns (interlaced bright and dark areas), while the dilation branch focuses on the

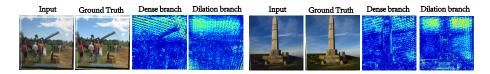


Fig. 8: The heat maps of the feature maps outputted from the two branches of the 6th layer.

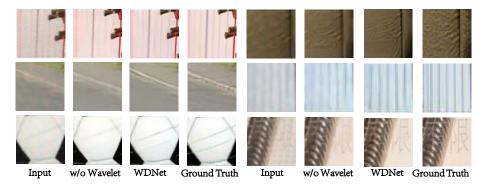


Fig. 9: Visual comparison between WDNet and WDNet without wavelet transform. These patches show that the former restores the details better and removes more moiré patterns.

whole areas contaminated by the moiré patterns due to its larger receptive field. It demonstrates that the two types of branches are responsible for the acquisition of the close-range and far-range information and jointly restore the image.

To test the effectiveness of the dense branches, we replace the dense blocks of them with ResNet blocks. To test the dilation branches, we replace the dilated convolutions with normal convolutions. As shown in Table 4, both the dense and dilation branches play an important role in WDNet. When the dense branches or the dilation branches are replaced, the PSNR decreases by 0.52dB or 1.05dB, respectively. The PSNR decreases by 0.41dB when we remove the DPM module and the attention loss, and by 0.27dB when we remove the weight maps in DPM. In addition, to compare the 8-directional DPM with the 4-directional IRNN, using the latter makes the PSNR decrease by 0.19dB.

In order to verify whether working in the wavelet domain is better than in the RGB domain, we design a network by removing the wavelet transform and wavelet inverse transform from WDNet, without the wavelet loss during training. These two networks are compared at the same computation amount and the results are shown in Table 4. A visual comparison is shown in Fig. 9. From Table 4 and Fig. 9, we can see that the complete model best achieves moiré pattern removal. The wavelet transform can help to keep the edges and prevent the details from blurring.

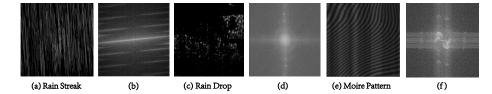


Fig. 10: Frequency spectra of images of rain streak, rain drop and moiré pattern.

Table 4: Ablation study on TestA. (a) Replace dilated convolutions with normal convolutions. (b) Replace the dense blocks with the residual blocks. (c) Without the wavelet and inverse wavelet transfrom. (d) Without DPM. (e) Replace the 8-directional DPM with the 4-directional IRNN.

Network	a	b	c	d	e	Complete model
PSNR/SSIM	26.83/0.858	27.36/0.856	27.03/0.859	27.47/0.853	27.69/0.857	27.88/0.863

The above studies clearly demonstrate that all the WDNet's components and the network design have their contributions to the excellent performance of WDNet. We also perform an experiment to explore the effect of different wavelet transform levels on the network's performance with the same network parameters. For levels 1, 2 and 3, the PSNR/SSIM are 27.24/0.866, 27.88/0.863, and 27.94/0.843, respectively. As the number of levels increases, the PSNR increases, but the SSIM decreases. The reason for such an interesting phenomenon will be left as the future work. Some recent related work such as [3] shows that perceptual quality and distortion (PSNR) may conflict with each other, particularly for image restoration tasks.

4.5 Extension to Deraining and Deraindrop

We show that our network also has advantages over the state-of-the-art methods in some other low-level vision tasks, such as deraining and deraindrop. Deraining methods can be divided into traditional methods and deep-learning methods. Traditional methods [37,4] remove rain streaks in images by designing some hand-crafted priors. Deep-learning methods [62,30,16] use convolutional neural networks to learn the rain streak features automatically. Yang et al. [62] created a multi-task network to jointly detect and remove rain. And Li et al. [30] proposed a recurrent neural network, where useful information in previous stages is beneficial to the rain removal in later stages. However, few deep-learning methods study how to use the feature of the rain streaks in the frequency domain to derain. In Fig. 10, similar to moiré patterns, rain streaks include high-frequency and low-frequency patterns, depending on the severity of the rain and distance to the camera. However, unlike moiré patterns, which can have different orientations in the same image, the directions of rain streaks are more consistent, resulting in an easier image restoration task. Like demoiréing, after the wavelet

Table 5: Quantitative comparison on Rain100h.

Method	DSC [37]	${\rm JORDER_R}~[62]$	DID_MDN $[69]$	RESCAN $[30]$	DAFNet [16]	$\mathrm{WDNet}(\mathrm{Ours})$
PSNR/SSIM	15.6/0.5446	23.45/0.749	24.53/0.799	26.45/0.845	28.44/0.874	28.60/0.878

Table 6: Quantitative comparison on Raindrop800.

Method	Eigen [5]	Pix2pix~[21]	A^2 Net [31]	AttentiveGAN [39]	Quan's $[41]$	WDNet (Ours)
PSNR/SSIM	23.90/0.80	28.85/0.84	30.79/0.93	31.52/0.92	31.44/ 0.93	31.75/0.93

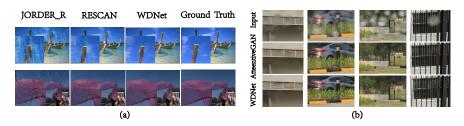


Fig. 11: (a) Visual deraining comparison among JORDER_R, RESCAN and WD-Net. (b) Visual deraindrop comparison between AttentiveGAN and WDNet.

transform, different types of rain steaks in the RGB domain are easier to distinguish in the wavelet domain.

We train WDNet on the Rain100h data set [62] for deraining and on the Raindrop800 data set [39] for deraindrop, and test it on the corresponding test sets. Though the textures of the rain/raindrop and moir patterns are very different in color and structure, our WDNet method can also remove them well. The results are given in Table 5, Table 6 and Fig. 11, which show that our WDNet performs better than the state-of-the-art. More visual results are given in the supplementary material.

5 Conclusion

We have proposed a novel wavelet-based dual-branch network (WDNet) to remove moiré patterns. Working in the wavelet domain can restore more details and is more effective at moiré pattern removal than in the RGB domain. WDNet's dense branches and dilation branches are responsible for the acquisition of close-range and far range information, respectively. The new DPM module inside some dense branches can better perceive slanting moiré patterns. WDNet substantially outperforms other state-of-the-art models. Moreover, it obtains the best results in two other low-level vision tasks, deraining and deraindrop. In addition, we built a new urban-scene data set with challenging types of moiré patterns, which will be made publicly available. Our future work includes applications of WDNet on other vision tasks such as denoising and demosaicing.

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