

instead of using backtracking, we can use Toptimized version; memorizing can use map with top down