

Generalized Fibonacci

Premchand S. Nair
pnair@miu.edu

November 1, 2021

Introduction

In this short note, a generalized version of Fibonacci series is presented along with its closed form solution. Define

$$G(n) = pG(n-1) + qG(n-2),$$

$p > 0, q > 0$ and $n \geq 0$.

Following steps similar to those we did today in the class you can show

$$G(n) = \frac{1}{p^2 + 4q} \left(\left(\frac{p + \sqrt{p^2 + 4q}}{2} \right)^n - \left(\frac{p - \sqrt{p^2 + 4q}}{2} \right)^n \right).$$