

CryptoCurrency and Blockchain (1)

金融科技導論

陳君明

jmchen@crypto.tw

國立臺灣大學 National Taiwan University

Status of Bitcoin

2











密碼貨幣市值

<http://coinmarketcap.com>

2018.12.03 12:00

Cryptocurrencies: 2073 • Markets: 15654 • Market Cap: \$130,682,200,032 • 24h Vol: \$14,229,263,166 • BTC Dominance: 53.5%

CryptoCurrency Market Capitalizations

#	Name	Market Cap	Price	Volume (24h)	Circulating Supply	Change (24h)	Price Graph (7d)
1	Bitcoin	\$69,951,279,963	\$4,019.21	\$5,241,643,436	17,404,250 BTC	-4.39%	
2	XRP	\$14,567,245,738	\$0.361225	\$344,113,652	40,327,341,704 XRP *	-3.29%	
3	Ethereum	\$11,766,015,799	\$113.61	\$1,844,499,814	103,567,766 ETH	-3.95%	
4	Stellar	\$3,005,747,705	\$0.156921	\$75,568,213	19,154,499,773 XLM *	-5.25%	
5	Bitcoin Cash	\$2,908,453,973	\$166.29	\$75,172,475	17,489,950 BCH	-4.36%	
6	EOS	\$2,588,177,828	\$2.86	\$752,240,466	906,245,118 EOS *	-3.97%	
7	Litecoin	\$1,931,761,461	\$32.52	\$411,205,200	59,406,663 LTC	-5.27%	
8	Tether	\$1,847,226,618	\$0.995047	\$3,249,760,147	1,856,421,736 USDT *	-0.44%	
9	Bitcoin SV	\$1,648,853,886	\$94.34	\$114,398,689	17,477,861 BSV	-0.83%	
10	Cardano	\$1,052,230,400	\$0.040584	\$20,895,294	25,927,070,538 ADA *	-3.41%	










密碼貨幣市值

<http://coinmarketcap.com>

2017.12.11 12:00

Cryptocurrencies: 1340 / Markets: 7241 Market Cap: \$441,691,960,448 / 24h Vol: \$23,412,353,847 / BTC Dominance: 63.6%

CryptoCurrency Market Capitalizations

#	Name	Market Cap	Price	Volume (24h)	Circulating Supply	Change (24h)	Price Graph (7d)
1	Bitcoin	\$281,060,655,096	\$16,796.50	\$14,441,100,000	16,733,287 BTC	23.34%	
2	Ethereum	\$44,200,888,612	\$459.16	\$1,423,510,000	96,264,047 ETH	4.09%	
3	Bitcoin Cash	\$23,529,360,581	\$1,396.51	\$910,319,000	16,848,688 BCH	9.15%	
4	IOTA	\$12,349,869,977	\$4.44	\$585,975,000	2,779,530,283 MIOTA *	11.71%	
5	Ripple	\$9,390,291,233	\$0.242398	\$201,596,000	38,739,144,847 XRP *	3.44%	
6	Litecoin	\$8,240,212,206	\$151.90	\$1,049,020,000	54,246,183 LTC	10.33%	
7	Dash	\$5,523,169,812	\$713.05	\$189,157,000	7,745,860 DASH	6.87%	
8	Bitcoin Gold	\$4,538,432,923	\$271.77	\$243,255,000	16,699,536 BTG	31.36%	
22	Zcash	\$861,969,134	\$306.91	\$122,975,000	2,808,531 ZEC	3.74%	

密碼貨幣市值

<http://coinmarketcap.com>

2017.04.12 11:00

#	Name	Symbol	Market Cap	Price	Circulating Supply	Volume (24h)	% 1h	% 24h	% 7d
1	Bitcoin	BTC	\$19,634,654,687	\$1206.88	16,268,937	\$204,585,000	0.23%	1.38%	6.67%
2	Ethereum	ETH	\$3,937,916,842	\$43.45	90,630,789	\$36,037,000	0.15%	-1.02%	-4.55%
3	Ripple	XRP	\$1,241,124,913	\$0.033082	37,516,282,515 *	\$11,861,100	-1.09%	-1.85%	-13.73%
4	Litecoin	LTC	\$455,699,318	\$9.01	50,593,457	\$47,189,300	-0.19%	1.17%	10.29%
5	Dash	DASH	\$437,184,554	\$60.51	7,225,522	\$11,717,000	-0.53%	-2.19%	-11.29%
6	Monero	XMR	\$305,452,960	\$21.39	14,278,507	\$4,956,310	0.24%	-0.87%	0.83%
7	Ethereum Classic	ETC	\$229,975,259	\$2.54	90,593,157	\$2,995,620	0.24%	-1.84%	-4.92%
8	NEM	XEM	\$182,873,700	\$0.020319	8,999,999,999 *	\$641,316	0.53%	-1.54%	13.89%
9	Augur	REP	\$110,849,200	\$10.08	11,000,000 *	\$435,094	-0.34%	-3.27%	-4.96%
10	MaidSafeCoin	MAID	\$88,125,079	\$0.194729	452,552,412 *	\$1,520,250	0.15%	-4.68%	-2.33%
11	VirtualCoin	VC	\$69,259,862	\$0.044471	1,557,409,332	\$113	0.20%	149.03%	293.03%
12	Zcash	ZEC	\$65,592,456	\$61.48	1,066,856	\$3,183,790	-0.43%	-4.13%	-1.90%
13	PIVX	PIVX	\$63,262,385	\$1.20	52,914,880 *	\$1,734,860	2.58%	28.56%	63.55%
14	Golem	GNT	\$57,562,770	\$0.070198	820,000,000 *	\$683,358	1.51%	-3.11%	-9.55%
15	Tether	USDT	\$54,941,255	\$0.999825	54,950,871 *	\$12,272,600	-0.01%	-0.01%	-0.02%

5

Bitcoin recognized by Germany as 'private money'

Matt Clinch | @mattclinch81
Monday, 19 Aug 2013 | 10:25 AM ET

Tomohiro Ohsumi | Bloomberg | Getty Images

Virtual currency bitcoin has been recognized by the German Finance Ministry as a "unit of account", meaning it is can be used for tax and trading purposes in the country.

Bitcoin is not classified as e-money or a foreign currency, the Finance Ministry said in a statement, but is rather a financial instrument under German banking rules. It is more akin to "private money" that can be used in "multilateral clearing circles", the Ministry said.

<http://www.cnn.com/id/100971898>

6

The UK Treasury Wants To Turn London Into A Bitcoin Capital

The Treasury has launched a review looking to turn the UK into a centre for virtual currency trade, the chancellor, George Osborne, announced at Canary Wharf in London.

Officials will study the benefits and threats unregulated digital currencies including bitcoin, which peaked with a market capitalisation of around \$14bn at the end of 2013 but has since declined to about \$8bn according to bitcoin market watcher BlockChain.



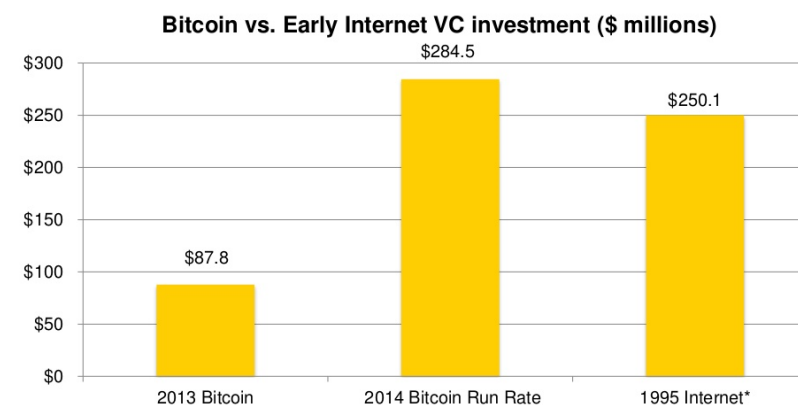
Enzo Figueira/ Getty Images

g SAMUEL GIBBS, THE GUARDIAN
AUG. 6, 2014, 7:05 AM | 1,373

The study, due in the autumn, will detail the role that cryptocurrencies could play in business, as part of the government's plan to stimulate innovation in the financial technology (fintech) sector.

<http://www.businessinsider.com/the-uk-treasury-wants-to-turn-london-into-a-bitcoin-capital-2014-8>

2014 VC Investment in Bitcoin Overtakes VC Early-Stage Internet Investments



<http://www.coindesk.com/state-of-bitcoin-q2-2014-report-expanding-bitcoin-economy>

8

Investor View on Bitcoin

“On the question of whether bitcoin will replace money, a good analogy is the postal service and email. Email didn't replace traditional mail, and we still send the same amount of mail today as we did before. But today we have totally new ways of communicating – chat, text, Facebook – things we didn't imagine when the Internet first arrived.”



Dan Morehead
Pantera Capital Management

<http://www.coindesk.com/state-of-bitcoin-q2-2014-report-expanding-bitcoin-economy>

9



Bitcoin is now a commodity according to the Commodity Futures Trading Commission (CFTC). On Thursday the organization publicly stated it had settled with a Bitcoin exchange for trading option contracts after an enforcement case against a Bitcoin operator.

“In this order, the CFTC for the first time finds that Bitcoin and other virtual currencies are properly defined as commodities,” according to the press release.



<https://www.cryptocoinsnews.com/cftc-bitcoin-commodity>

Top EU court rules Bitcoin exchange tax-free in Europe

AFP | Updated: Oct 22, 2015, 07.03 PM IST



EU's top court ruled that the exchange of Bitcoin and other virtual currencies should be treated just like traditional money in Europe and not incur any sales tax.

LUXEMBOURG: The EU's top court ruled today that the exchange of Bitcoin and other virtual currencies should be treated just like traditional money in Europe and not incur any sales tax.

According to **European Union** law, all transactions relating to currency, bank notes and coins used as legal tender across the 28-nation bloc are exempt from value-added tax (VAT).

<http://economictimes.indiatimes.com/news/international/business/top-eu-court-rules-bitcoin-exchange-tax-free-in-europe/articleshow/49495088.cms>

11

New Japan law recognizes bitcoin as method of payment

BY Jasmine Solana ON March 31, 2017

TAGS: **BITCOIN JAPAN**

Bitcoin's legal position in Japan is slowly—but surely—becoming clear.

After regulating digital currency exchanges in the country last year, the Japanese Diet has signed a landmark bill that will allow the use of digital currencies like bitcoin as a legal method of payment.

The long-awaited bill, which goes into effect on April 1, still does not recognize bitcoin as a currency, but it has accepted that bitcoin and other cryptocurrencies have “asset-like values” that can be used “as payment to indefinite parties for the cost of purchase or rent of items or receipt of services and which can be transferred by means of electronic data processing systems,” **explained** Bitflyer exchange.



<https://calvinayre.com/2017/03/31/bitcoin/new-japan-law-recognizes-bitcoin-method-payment>

Bitcoin exchange Coinbase ordered to hand over customer data to IRS

1 Comments / f Share / t Tweet / Stumble / @ Email

A federal court has ordered Coinbase, which operates the largest U.S. exchange for buying and selling Bitcoins, to hand over information to IRS on more than 14,000 customers suspected of evading taxes.

The ruling by U.S. Magistrate Judge Jacqueline Scott Corley, calls for Coinbase to provide the tax agency with the name, birth date, address and taxpayer identification number of customers who had the Bitcoin equivalent of \$20,000 or more in their accounts in any one year between 2013 and 2015.

According to Coinbase, the order will only affect its highest transacting clients, roughly 1 percent of its total customer base of roughly 6 million account holder. The IRS originally demanded records of all Coinbase customers.

<https://www.cbsnews.com/news/bitcoin-coinbase-ordered-to-hand-over-customer-data-to-irs/>

13

MARKETS

Bitcoin Futures Set to Start Trading as Regulator Gives Thumbs Up

CFTC says it will allow launches by Chicago exchanges CME Group and Cboe Global Markets

By [Alexander Osipovich](#)

Updated Dec. 1, 2017 3:43 p.m. ET



The U.S. Commodity Futures Trading Commission said it would allow two major Chicago exchanges to launch bitcoin futures.

<https://www.wsj.com/articles/regulator-opens-way-to-bitcoin-futures-1512133201>

14

Central bank keeping close eye on Bitcoin development: governor

Like 0 / f Share / t Tweet / G+ Share

By Central News Agency
2013/11/20 15:09

"At the moment, the CBC views Bitcoin trading the same way it views trading in precious metals," Perng said. "We are keeping track of changes in the development of Bitcoin and will prevent money laundering using this digital currency," Perng said.

CBC – Central Bank of the Republic of China (Taiwan)
Head : Perng Fai-nan 彭淮南

<http://www.taiwannews.com.tw/en/news/2349491>

15

Now you can buy bitcoin along with your snacks and sodas in 3,000 Taiwanese convenience stores

Josh Horwitz
2:00 PM at Oct 28, 2014 | 3 min read

45



<https://www.techinasia.com/now-you-can-buy-bitcoin-with-your-red-bull-and-chewing-gum-in-3000-taiwanese-convenience-stores-bitoex-family-mart>



<https://www.bitoex.com/>

17



<https://www.maicoin.com/zh-TW>

18

國內首家可接受虛擬貨幣付款的蛋糕餐飲店 Coin Cake開幕!

Coin Cake為虛擬貨幣概念店，可接受民眾以比特幣、以太幣等虛擬貨幣付款，民眾結帳時可掃描店家QRCode取得付款錢包資訊，線上支付虛擬貨幣完成付款。

文/ 蘇文彬 | 2017-10-16 發表

讚 4.5 萬 按讚加入iThome粉絲團 讚 477 分享



<https://www.ithome.com.tw/news/117488>

19

Birth of Bitcoin

20

Birth of Bitcoin

- Described by Satoshi Nakamoto (中本聰) in 2008
- Introduced as open-source software on the evening of January 3, 2009

Bitcoin: A Peer-to-Peer Electronic Cash System

Satoshi Nakamoto
satoshin@gmx.com
www.bitcoin.org

Abstract. A purely peer-to-peer version of electronic cash would allow online payments to be sent directly from one party to another without going through a financial institution. Digital signatures provide part of the solution, but the main benefits are lost if a trusted third party is still required to prevent double-spending. We propose a solution to the double-spending problem using a peer-to-peer network.

<http://bitcoin.org/bitcoin.pdf> 中本聰

21

Author	Topic: Pizza for bitcoins? (Read 602235 times)	
laszlo Full Member 👤👤👤	Pizza for bitcoins? May 18, 2010, 12:35:20 AM	#1
Activity: 199	I'll pay 10,000 bitcoins for a couple of pizzas.. like maybe 2 large ones so I have some left over for the next day. I like having left over pizza to nibble on later. You can make the pizza yourself and bring it to my house or order it for me from a delivery place, but what I'm aiming for is getting food delivered in exchange for bitcoins where I don't have to order or prepare it myself, kind of like ordering a 'breakfast platter' at a hotel or something, they just bring you something to eat and you're happy!	
	I like things like onions, peppers, sausage, mushrooms, tomatoes, pepperoni, etc.. just standard stuff no weird fish topping or anything like that. I also like regular cheese pizzas which may be cheaper to prepare or otherwise acquire.	
	If you're interested please let me know and we can work out a deal.	
	Thanks, Laszlo	
	BC: 157fRqAKrDyGHR1Bx3yDxeMv8Rh45aUet	
bitcoin2paysafe Newbie 👤	Re: Pizza for bitcoins? May 18, 2010, 06:42:11 PM	#2
Activity: 12	In which country do you live?	
laszlo Full Member 👤👤👤	Re: Pizza for bitcoins? May 18, 2010, 06:46:48 PM	#3
Activity: 199	Jacksonville, Florida zip code 32224 United States	

<https://bitcointalk.org/index.php?topic=137.0>

22



Today, bitcoiners the world over will celebrate the anniversary of the most expensive pizzas in history.

Bought on 22nd May 2010 by Laszlo Hanyecz, the programmer paid a fellow Bitcoin Talk forum user 10,000 BTC for two Papa John's pizzas. Back then – when the technology was just over a year old – that equated to roughly \$25, but is **\$5.12m** by today's exchange rate.

<http://www.coindesk.com/bitcoin-pizza-day-celebrating-pizza-bought-10000-btc>

23

Missing: hard drive containing Bitcoins worth £4m in Newport landfill site

A digital 'wallet' containing 7,500 Bitcoins that James Howells generated on his laptop is buried under four feet of rubbish

Buried somewhere under four feet of mud and rubbish, in the Docksway landfill site near Newport, Wales, in a space about the size of a football pitch is a computer hard drive worth more than £4m.

It belonged to James Howells, who threw it out when he was clearing up his desk in mid-summer and discovered the part, rescued from a defunct Dell laptop. He found it in a drawer and put it in a bin.

And then last Friday he realised that it held a digital wallet with 7,500 Bitcoins created for almost nothing in 2009 - and then worth about the same.

<https://www.theguardian.com/technology/2013/nov/27/hard-drive-bitcoin-landfill-site>

24



<https://blockchain.info/charts/market-price?timespan=2years>

25

UCLA Prof Wants to Nominate Satoshi Nakamoto for Nobel Prize in Economics

"He can write his speech, digitally sign it and send it to me securely."

Leon Pick | Innovation (CryptoCurrency) | Monday, 09/11/2015|16:29 GMT

A professor of finance at the University of California- Los Angeles (UCLA), Bhagwan Chowdhry, wants to nominate Bitcoin's unknown creator(s), Satoshi Nakamoto, for the Nobel Prize in Economics.

<http://www.financemagnates.com/cryptocurrency/innovation/ucla-prof-wants-to-nominate-satoshi-nakamoto-for-nobel-prize-in-economics>

26

Satoshi Nakamoto Not Eligible For Nobel Prize

Although UCLA Professor Bhagwan Chowdhry chose to nominate the pseudonymous creator of Bitcoin, Satoshi Nakamoto, for the Nobel Prize for Economic Sciences, it appears the The Royal Swedish Academy of Sciences will not consider the nomination unless the legendary Nakamoto were to reveal his identity.

The organization's press officer, Hans Reuterskiöld, [told Inverse.com](#) that the prize is never awarded anonymously nor after someone has died.



The prize, as in this instance, the Sveriges Riksbank Prize in Economic Science in Memory of Alfred Nobel, is never awarded anonymously nor posthumously.

<https://www.cryptocoinsnews.com/satoshi-nakamoto-not-eligible-nobel-prize>

27

FinTech

28

區塊鏈 Blockchain

- 區塊鏈技術是 Bitcoin 的基礎，受全世界重視的程度已經超越 Bitcoin 本身
- “A blockchain is a decentralized network with memory” (Vitalik Buterin)
- 關鍵：以 hash function 串接資料
 - Hash function – 雜湊函數、赫序函數、哈希函數

29

「區塊鏈」技術進軍華爾街，十年內 200 萬個銀行工作將蒸發

作者 黃 威 | 發布日期 2016 年 04 月 10 日 9:00 | 分類 人力資源, 自動化 | G+ | 1 讚 | 分享 | 1,298



摩根大通與花旗等銀行成功將比特幣跨後的區塊鏈技術 (blockchain) 應用在信用違約交換 (credit default swap, CDS) 市場上，此進展將能讓區塊鏈技術在主流金融領域站穩腳步，幫銀行省下人事成本，花旗報告甚至稱銀行引進自動化未來十年會少 200 萬個銀行工作。

<http://technews.tw/2016/04/10/blockchain-applied-on-wall-street>

30

區塊鏈將讓銀行 10 年內消失？比特幣大老：言之過早

作者 MoneyDJ | 發布日期 2016 年 04 月 12 日 16:40 | 分類 支付方案, 財經 | G+ | 1 讚 | 分享 | 133



金融科技 (Fintech) 來勢洶洶，「區塊鏈」(Blockchain) 技術更成為顯學，雖然許多業界大老警告銀行的生存恐受威脅，俄羅斯聯邦儲備銀行 (Sberbank) 副總裁 Andrey Sharov 上週更警告銀行可能 2026 年就會因為區塊鏈而全面消失，但比特幣非營利組織「比特幣基金會」(Bitcoin Foundation) 董事長 Brock Pierce 卻認為，討論這些都還言之過早。

<http://finance.technews.tw/2016/04/12/blockchain-bank-fintech>

31

未來，核武器可能也用區塊鏈進行控制？

Posted on 2016-10-11 in 科技



核武器、區塊鏈，兩種風馬牛不相及的事物，卻可能在未來擦出不一樣的火花。

外媒透露，美國國防部旗下高級研究計劃局 DARPA 正在以資金的方式支持部分區塊鏈的研究，主要目的是：研究區塊鏈能否在保護高度敏感數據上提供幫助，並且確定其在軍用衛星、核武器等數個場景中的應用潛力。

今年 9 月，DARPA 將一份價值 180 萬美元的合作共同授予 Galois 和 Guardtime，目的是驗證 Guardtime 基於區塊鏈技術研製的 KSI (Keyless Signature Infrastructure, 無秘鑰簽名基礎架構) 系統可靠性。

其中，Galois 被公認為「形式驗證 (Formal Verification,)」領域的領軍企業。至於「形式驗證」則可以概括為：通過形式化驗證過程，證明一個系統不存在某個缺陷，同時匹配某個或某些屬性。

而 KSI 系統主要目標是網際網路中的 APT (Advanced Persistent Threat, 高級持續性威脅) 攻擊，因為前者能夠將網絡中的證據保存下來。即便黑客能夠突破漏洞、修改系統日誌文件、甚至是調整安全軟體的白名單，但是只要留有蹤跡，從能將其繩之於法。

<https://kknews.cc/tech/m4kmbp.html>

32

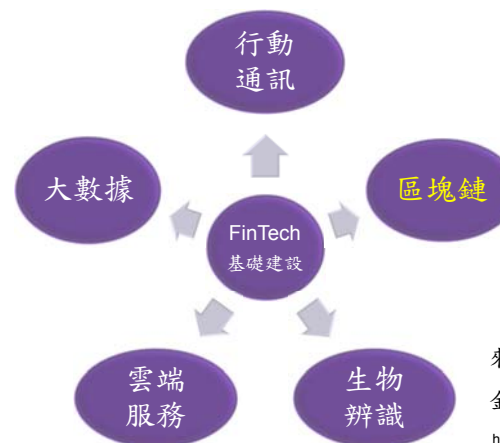
金融科技 FinTech

- **FinTech** (Financial Technology) is a buzzword today
- **FinTech** is an economic industry composed of companies that use technology to make **financial services** more **efficient**
- **FinTech** companies are generally startups founded with the purpose of disrupting incumbent financial systems and corporations that rely less on **software**

https://en.wikipedia.org/wiki/Financial_technology

33

FinTech 基礎建設



來源：金管會（金融監督管理委員會）
金融科技發展策略白皮書 2016.5.12
<http://www.fsc.gov.tw/ch/home.jsp?id=478&parentpath=0,7>

34

政策四大面向 十一項重點



35

Cryptography

36

Cryptography 密碼學



37

Bitcoin Tutorial

• How the Bitcoin protocol actually works

- Published by Michael Nielsen on December 6, 2013
- <http://www.michaelnielsen.org/ddi/how-the-bitcoin-protocol-actually-works>
- “This is the best explanation of the Bitcoin protocol that I have read” by Bruce Schneier https://www.schneier.com/blog/archives/2013/12/bitcoin_explana.html
- “To understand the post, you need to be comfortable with **public key cryptography**, and with the closely related idea of **digital signatures**. I’ll also assume you’re familiar with **cryptographic hashing**.”
- “In the world of atoms we achieve security with devices such as locks, safes, signatures, and bank vaults. In the world of bits we achieve security with cryptography. That is why **Bitcoin is at heart a cryptographic protocol**.”

38

The Book “Mastering Bitcoin”



39

Public Key Cryptography (PKC)

40

Caesar Cipher

- Gāius Jūlius Caesar (100 BC – 44 BC)

- A Roman military and political leader and one of the most influential men in world history
- He played a critical role in the transformation of the Roman Republic into the Roman Empire



- Caesar Cipher

- Encode: $A \leftrightarrow 0, B \leftrightarrow 1, C \leftrightarrow 2, \dots, Y \leftrightarrow 24, Z \leftrightarrow 25$
 - Plaintext: SPY (18 15 24)
 - Ciphertext: VSB (21 18 1)
- Encryption: $c = p + 3 \pmod{26}$
- Decryption: $p = c - 3 \pmod{26}$

41

Symmetric Cryptography

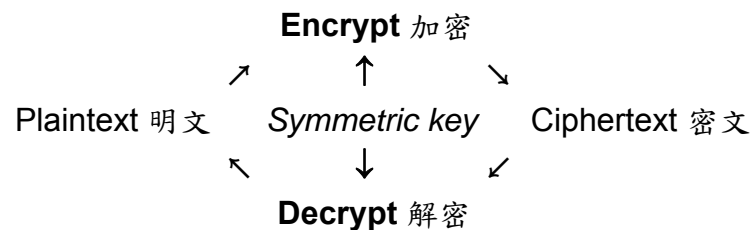


- Analogy: Safe with a strong lock, only Alice and Bob have a copy of the key

- Alice encrypts
 - locks message in the safe with her key
- Bob decrypts
 - uses his copy of the key to open the safe

42

Symmetric Cryptography



DES (Data Encryption Standard)

AES (Advanced Encryption Standard)

43

Asymmetric Cryptography

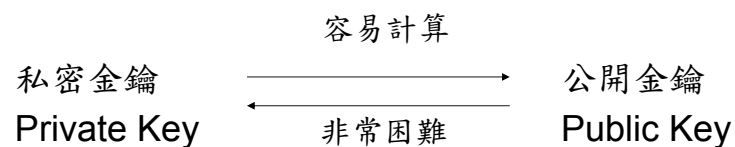
- New Idea: Use the “mailbox” principle

- Everyone can drop a letter
- But only the owner has the correct key to open the box



44

私密金鑰 與 公開金鑰

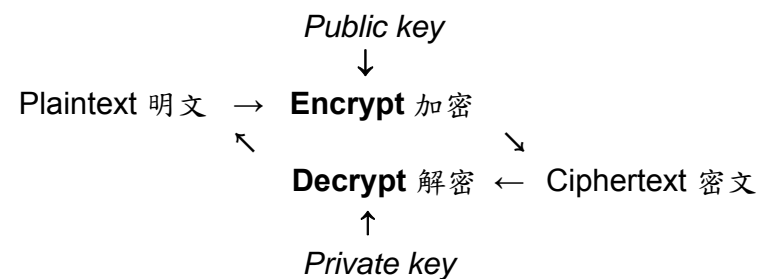


藉由數學工具達成此目的

Whit Diffie 和 Martin Hellman 於 1976 年提出此觀念

45

Public Key Cryptosystem 公鑰密碼系統

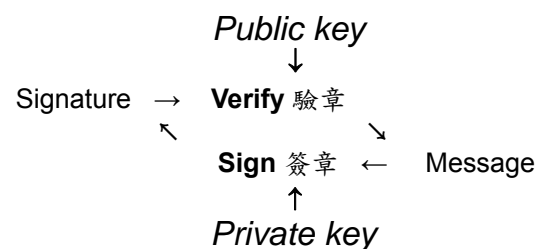


RSA (Rivest – Shamir – Adleman 1977)

ECC (Elliptic Curve Cryptosystem 橢圓曲線密碼系統)

46

Digital Signature 數位簽章



- * 資料完整性 (Integrity)
- * 身份鑑別性 (Authentication)
- * 不可否認性 (Non-Repudiation)

47

Electronic Signatures Act

全國法規資料庫
Laws & Regulations Database of The Republic of China

最新訊息 | 法規類別 | 法規檢索 | 司法判解 | 條約協定 | 兩岸協議 | 綜合查詢 | 跨機關檢索

現在位置: 首頁 > 法規

法規	
名稱	電子簽章法
公布日期	民國 90 年 11 月 14 日

法令規章

名稱: 臺灣證券交易所股份有限公司證券商採用數位簽章注意要點

Taiwan Stock Exchange Corporation Directions for the Use of Digital Signatures by Securities Firms

公發布日: 民國 91 年 10 月 24 日

修正日期: 民國 103 年 12 月 19 日

臺灣證券交易所
TAIWAN STOCK EXCHANGE

48

Certificate

49

Certificate

- Certificates bind the identity of user to public key
- The trusted authority that issues the certificate is referred to as certification authority (CA)
- The party who receives a certificate, e.g., Bob, verifies Alice's public key using the public key of the CA

• Cert(Alice) =

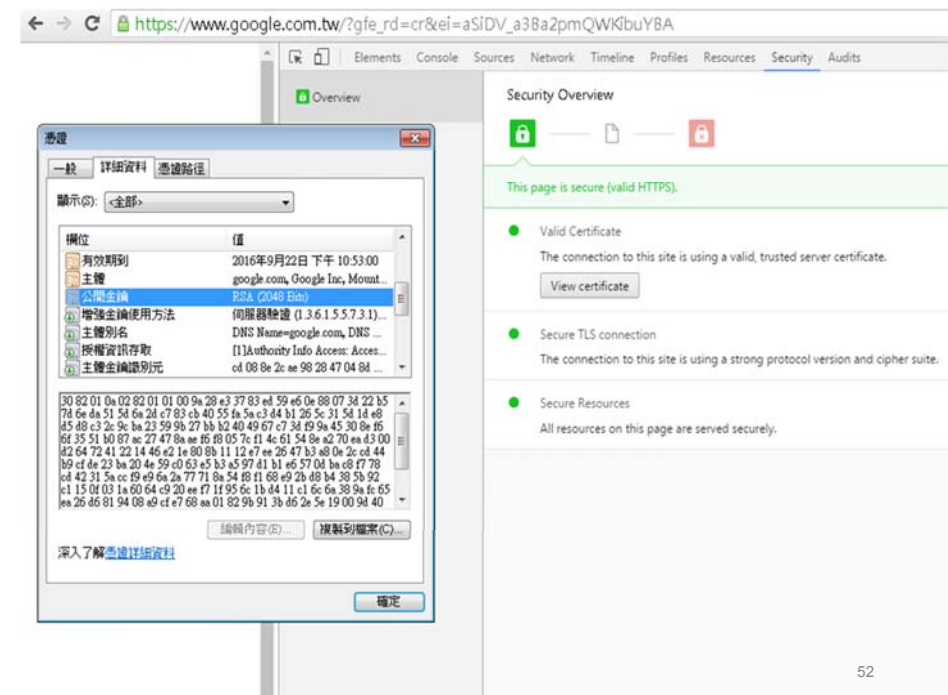
$$(k_{pub_A}, ID(Alice), sig_{k_{pr_{CA}}}(k_{pub_A}, ID(Alice)))$$

50



HTTPS (also called HTTP over TLS, HTTP over SSL, and HTTP Secure) is a protocol for secure communication over a computer network which is widely used on the Internet.

51



52

PKI – Public Key Infrastructure

- The entire system that is formed by CAs together with the necessary support mechanisms is called a Public-Key Infrastructure (PKI)



<http://moica.nat.gov.tw/moica.html>

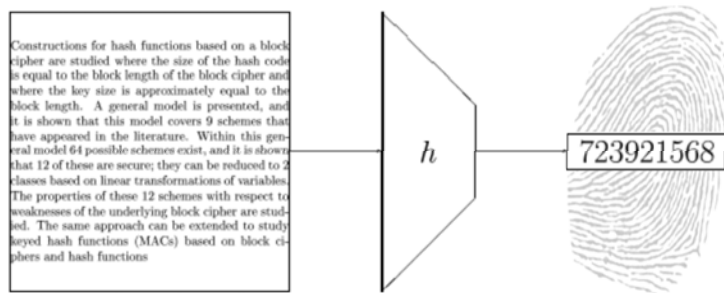
53

Hash Function

54

Hash Function 雜湊函數

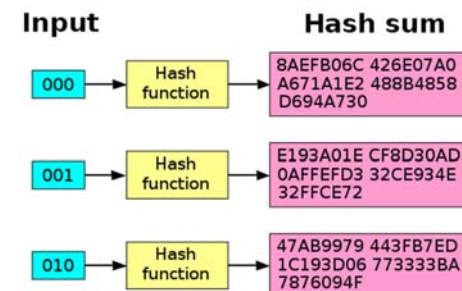
- An efficient function mapping binary strings of **arbitrary length** to binary strings of **fixed length**, called the **hash-value** or **hash-code** (fingerprint, checksum)



55

Avalanche Effect 雪崩效應

- A desirable property of cryptographic algorithms, typically block ciphers and cryptographic hash functions
- When an input is changed slightly (e.g., flipping a single bit) the output changes significantly (e.g., half the output bits flip)

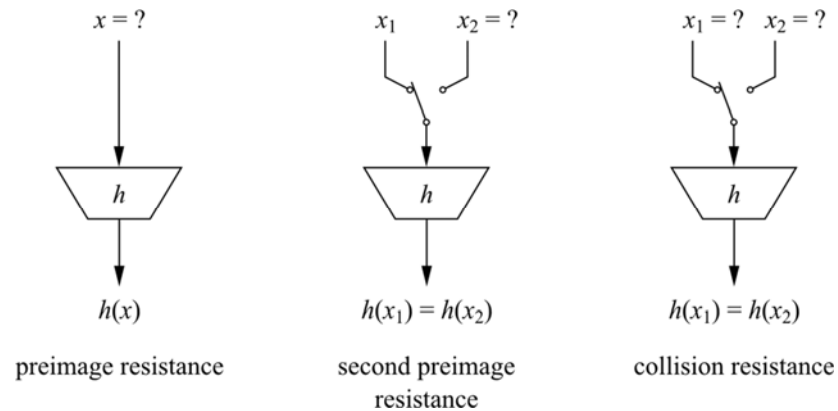


The **SHA-1** hash function exhibits good avalanche effect. When a single bit is changed the hash sum becomes completely different.

https://en.wikipedia.org/wiki/Avalanche_effect

56

Security Properties



57

Cryptographic Hash Functions

- H is a function with **one-way property (pre-image resistance)** if given any y , it is *computationally infeasible* to find any value x in the domain of H such that $H(x) = y$
- H is **collision free (resistant)** if it is *computationally infeasible* to find $x' \neq x$ such that $H(x') = H(x)$
- H is a **cryptographic hash function** if
 - Input: bit strings of arbitrary length
 - Output: bit strings of fixed length
 - H has one-way property
 - H is collision free

58

SHA: Secure Hash Algorithm

- The Secure Hash Algorithm is a family of cryptographic hash functions published by the National Institute of Standards and Technology (NIST) as a U.S. Federal Information Processing Standard (FIPS)

Algorithm and variant	Output size (bits)	Internal state size (bits)	Block size (bits)	Rounds	Bitwise operations	Security (bits)
SHA-1 FIPS 180	160	160	512	80	and, or, add, xor, rot	Theoretical attack (2^{61})
SHA-224	224	256	512	64	and, or, xor, shr, rot, add	112
SHA-256 Bitcoin	256	(8 × 32)	512	64	and, or, xor, shr, rot, add	128
SHA-2 FIPS 180	384	512	1024	80	and, or, xor, shr, rot, add	192
SHA-384	512	(8 × 64)	1024	80	and, or, xor, shr, rot, add	256
SHA-512	224					112
SHA-512/224	256					128
SHA-512/256	224	1152	1088	24	and, xor, rot, not	112
SHA-3 FIPS 202	256	1600	1088	24	and, xor, rot, not	128
SHA3-224 Ethereum (Keccak 256)	384	(5 × 5 × 64)	832	24	and, xor, rot, not	192
SHA3-384	512		576			256
SHA3-512						

https://en.wikipedia.org/wiki/Secure_Hash_Algorithm

59

Merkle-Damgård Construction for SHA-1 / SHA-2

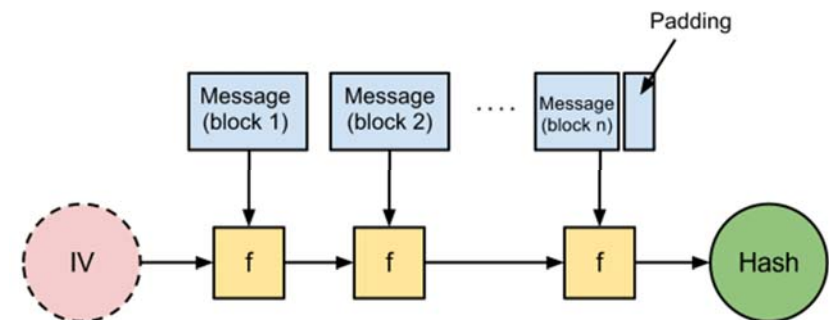


Image Courtesy <http://joncave.co.uk/2012/08/i-captured-the-flag>

60

SHA-256

- One iteration in a SHA-2 family compression function


- The blue components perform the following operations

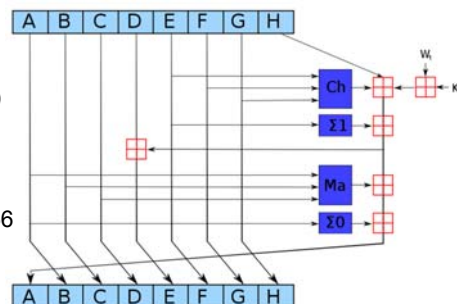
$$\text{Ma}(A, B, C) = (A \wedge B) \oplus (A \wedge C) \oplus (B \wedge C)$$

$$\text{Ch}(E, F, G) = (E \wedge F) \oplus (\neg E \wedge G)$$

$$\Sigma_0(A) = (A \ggg 2) \oplus (A \ggg 13) \oplus (A \ggg 22)$$

$$\Sigma_1(E) = (E \ggg 6) \oplus (E \ggg 11) \oplus (E \ggg 25)$$

- The bitwise rotation uses different constants for SHA-512
- The given numbers are for SHA-256
 -  is addition modulo 2^{32}



<http://en.wikipedia.org/wiki/SHA-2>

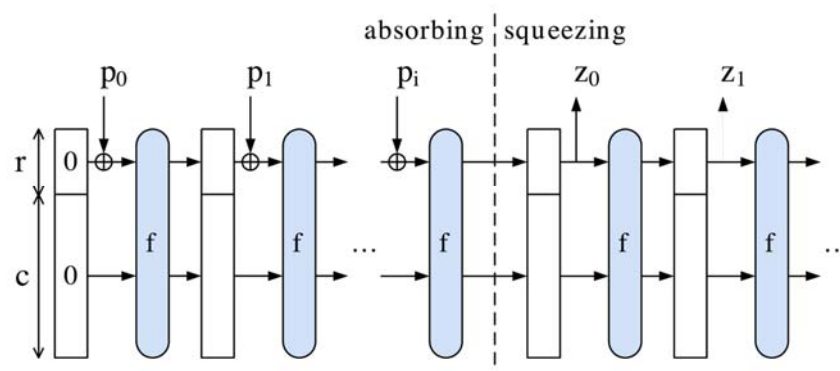
61

SHA-3 Competition Winner: Keccak

- Designers:
 - Guido Bertoni (Italy) of STMicroelectronics
 - Joan Daemen (Belgium) of STMicroelectronics
 - Gilles Van Assche (Belgium) of STMicroelectronics
 - Michaël Peeters (Belgium) of NXP Semiconductors
- Not very fast in software implementation, but in hardware implementations it is notably faster than all other finalists
- In its largest instance, the state consists of a 5×5 array of 64-bit words, 1600 bits total
 - Reduced versions are defined for smaller power-of-2 word sizes w down to 1 bit (25 bits total state)
 - Smaller state sizes can be used to test cryptanalytic attacks
 - Intermediate state sizes (e.g., from $w=4$, 100 bits, to $w=32$, 800 bits) also provide practical, lightweight, alternatives

62

SHA-3 / Keccak: Sponge Construction



63

Applications

- Verifying the Integrity of Files or Messages
- Password Verification
- File or Data Identifier
- Pseudorandom Generation & Key Derivation
- Proof-of-Work (POW)

https://en.wikipedia.org/wiki/Cryptographic_hash_function

64

Abstract Algebra

65

Floor and Ceiling

- **Definition**

- 1) The **floor** $\lfloor x \rfloor$ of $x \in \mathbf{R}$ is the largest integer $\leq x$
- 2) The **ceiling** $\lceil x \rceil$ of $x \in \mathbf{R}$ is the smallest integer $\geq x$

- **Example**

- $\lfloor e \rfloor = 2$, $\lceil e \rceil = 3$, $\lfloor -3.1416 \rfloor = -4$, $\lceil -3.1416 \rceil = -3$

- **Example**

- 1) $25 = 3 \times 7 + 4$ [7: divisor, 3: quotient, 4: remainder]
- 2) $25 \bmod 7 = 25 - \lfloor 25/7 \rfloor \times 7 = 25 - 3 \times 7 = 25 - 21$

66

Modular Function

- **Definition**

$m, n \in \mathbf{Z}$, $m > 0$, define

$$n \bmod m = n - \lfloor n/m \rfloor \times m$$

- i.e., the remainder after dividing n by m , which is ≥ 0 and $< m$

- **Example** 58 in the base 3 representation

$$a_0 = 58 \bmod 3 = 1 \quad 19 = \lfloor 58/3 \rfloor$$

$$a_1 = 19 \bmod 3 = 1 \quad 6 = \lfloor 19/3 \rfloor$$

$$a_2 = 6 \bmod 3 = 0 \quad 2 = \lfloor 6/3 \rfloor$$

$$a_3 = 2 \bmod 3 = 2 \quad 0 = \lfloor 2/3 \rfloor$$

$$(2011)_3 = 2 \times 3^3 + 0 \times 3^2 + 1 \times 3^1 + 1 \times 3^0 = 58$$

67

Group 群

- **Definition** A **group** $(G, *)$ is a set G with an operation $*$, such that the following conditions are satisfied :

- 1) **Closure** $a * b \in G$ for all $a, b \in G$
- 2) **Associativity** $a * (b * c) = (a * b) * c$ for all $a, b, c \in G$
- 3) **Identity** There is an element $e \in G$ such that $a = a * e = e * a$ for each $a \in G$
- 4) **Inverse** For each $a \in G$, there is an element $b \in G$ such that $a * b = b * a = e$

68

Group

- **Example** Each of the following sets with the specified operation is a group
 - $\mathbf{Z}, \mathbf{Q}, \mathbf{R}, \mathbf{C}$ with + (addition)
 - $\mathbf{Q}^*, \mathbf{R}^*, \mathbf{C}^*$ with \times (multiplication)
 - $5\mathbf{Z} = \{5a \mid a \in \mathbf{Z}\}$ with +
 - $\{1, -1\}$ with \times
 - $\mathbf{Z}_6 = \{0, 1, 2, 3, 4, 5\}$ with + modulo 6
 - $\mathbf{Z}_7^* = \{1, 2, 3, 4, 5, 6\}$ with \times modulo 7
 - $\{(x, y) \in \mathbf{R}^2 \mid y^2 = x^3 + ax + b\} \cup \{\infty\}$ with point addition and point doubling laws on elliptic curves

69

Abelian Group 交換群

- **Definition** A group $(G, *)$ is **commutative** or **abelian** if $a * b = b * a$ for all $a, b \in G$
- **Example**
 - $\mathbf{Z}, \mathbf{Q}, \mathbf{R}, \mathbf{C}$ with + are commutative
 - $\mathbf{Z}_9^* = \{1, 2, 4, 5, 7, 8\}$ with $[\times \text{ modulo } 9]$ is commutative
 - $\mathbf{Z}_p^* = \{1, 2, \dots, p-1\}$ with $[\times \text{ modulo } p]$ is commutative for every prime p

\times	1	2	4	5	7	8
1	1	2	4	5	7	8
2	2	4	8	1	5	7
4	4	8	7	2	1	5
5	5	1	2	7	8	4
7	7	5	1	8	4	2
8	8	7	5	4	2	1

70

Cyclic Group 循環群

- **Definition** A group $(G, *)$ is **cyclic** if there exists a **generator** $g \in G$ such that every $a \in G$ is of the form $a = g * \dots * g$ (n copies) for some $n \in \mathbf{Z}$
- **Example**
 - $(\mathbf{Z}, +)$ is cyclic with generators 1 and -1
 - (\mathbf{Z}_7^*, \times) is cyclic: $\{1 = 3^0 = 3^6, 2 = 3^2, 3 = 3^1, 4 = 3^4, 5 = 3^5, 6 = 3^3\}$
 - (\mathbf{Z}_9^*, \times) is cyclic with generators 2 and 5
- **Example**
 - $(\mathbf{Q}, +)$ is not cyclic
 - (\mathbf{Z}_8^*, \times) is not cyclic (Klein 4)

\times	1	3	5	7
1	1	3	5	7
3	3	1	7	5
5	5	7	1	3
7	7	5	3	1

71

Group Order

- **Definition** The **order** (denoted as $|G|$) of a group $(G, *)$ is the number of the elements in G
- **Example**
 - $|\mathbf{Z}_p| = p, |\mathbf{Z}_p^*| = p - 1$ for any prime p
 - $|\mathbf{Z}_9^*| = 6$
 - $|\mathbf{Z}_n^*| = |\{a \in \mathbf{Z}_n \mid \gcd(a, n) = 1\}| = \phi(n)$
 - Euler ϕ -function [ϕ : phi]

72