	Combinatorics a	and Probability	y	a	acb	3 x	2	
		cab			abc		h	_
Problem 1		_			bac	clo	j a	Ψ.
		ab可多模位	No.		bca		7	Ì
(a) In how many ways can the least other?	tters (a, b), c) d, e, f be	e arranged so that			and b	are nex	t to ead	ch
(b) In how many ways can the leach other?	etters <i>a, b, c, a, e, f</i> b \(\times \(\times \)			etters	a and b	are no	t next	to
(c) In how many ways can the lead the other but a and c are not?	tters a, b, c, d, e, f be						t to ead	:h
Problem 2			ab	Fil				
A 1 1. 1 . 1 .	dom from Σ^4 , where	$\Sigma = \{a, b, c, d, e\}.$		tv	W v2 v) 2	סעו	
(a) What is the probability that to the probability that the probability the probability that the probability that the probability the probability that the probab	he letters in the wor	d are distinct?	P(A)=	345	φ · · · · · · · · · · · · · · · · · · ·		9	
(b) What is the probability that t	here are no vowels i	n the word? $\mathcal{P}\mathcal{U}$	7)=-	40	$\frac{1}{2} = \frac{0}{6}$	<u> </u>		
(c) What is the probability that t	he word begins with	n a vowel? 🕇			3	•		
(d) What is the expected number			3 + Xp)=	ELX)+ H)	(s)		
(e) Let <i>x</i> be the answer to the pro-	evious question. Wh	at is the probabil	ity of t	he wo	ord havi	ng [x]	or mo	re
vowels? $\binom{8}{J} = 2$.	Vol: 2.4) 33		L	oct.		•	
Problem 3		3		1	2	3 '	ф <u>7</u>	- {
A black die and a red die are toss		bability that	1	2	3	4	5 6	
(a) the sum of the values is even	? $\frac{18}{36} = \frac{1}{2}$		3	3 U	Q J 6 7 2	<i>b</i>) 8	÷ 8
(b) the number on the red die is $\frac{1}{2}$	bigger than the num	nber on the black	die?+	5	<i>b</i>	1	9	[[
(c) the number on the red die is	twice the number or	n the black die?	6	ס ל	€ -	9	bo	c(
12 (P) 15 Ta			- 1					_

Problem 4 文本化为信息。

Team α faces team β in a 5-match series. Matches are either won or lost, i.e., there are no draws. It takes 3 wins to win the series. Team α has probability p (0 < p < 1) of winning a match. Consider each of the following situations and calculate the probability that they will lose the whole series.

(a) They have lost the first match of the series already.

 $(4) p^{2} (1-p)^{2} + (4) p (1-p)^{3}$

(b) They have lost one of the first two matches of the series already.

- (c) They have lost the first two matches of the series already.
- (d) They have lost one of the first three matches of the series already.
- (e) They have lost two of the first three matches of the series already.

Problem 5

Let E_1, E_2 be two events. Prove that $P(E_1 \setminus E_2) = P(E_1) - P(E_2)$ implies $P(E_2 \setminus E_1) = 0$.