```
append
```

The built-in

```
predicate append(?List1, ?List2, ?List1_then_List2) succeeds
if List1 followed by List2 = List1 then List2. Examples:
```

```
?- append([a, b], [c, d, e], Result).
Result = [a, b, c, d, e].
true.
?- append([a, b], SecondBit, [a, b, c, d, e]).
SecondBit = [c, d, e]
true.
?- append(FirstBit, [c, d, e], [a, b, c, d, e]).
FirstBit = [a, b]
true.
```

A not uncommon beginner's mistake is to use append ([Head], Tail,

List) to build a <u>list</u> instead of something like List = [Head | Tail].

This will work, but is like using a bulldozer to dig a hole to plant out a seedling.

Note: there is also an unrelated version of append that takes a single parameter. This is described under <u>files</u>, and is referred to as append/1 - i.e. <u>largument</u>, while the append in this article is referred to as append/3 - 3 arguments.

arg

Not a cry of frustration at yet another error message, but rather, an abbreviation for <u>argument</u>, and also the name of a built-in metalogical predicate, that extracts arguments from a <u>structure</u>. Example: ?- arg(2, buys(john, beer), Arg).

Arg = beer

It is also possible to put arguments into terms using arg, should this prove useful:

```
?- X = likes(mary, Y), arg(2, X, pizza).
X = likes(mary, pizza)
Y = pizza
```

argument

See arg, term.

arithmetic

Many of the usual arithmetic operators are available in Prolog:

Operator Meaning Example 2 is 1 + 1.addition subtraction 1 is 2 - 1. unary minus Try the query X is 1, Y is - X. 4 is 2 * 2. multiplication 2 is 6 / 3. division integer division 1 is 7 // 4. // integer remainder 3 is 7 mod 4. mod ** exponentiation 1.21 is 1.1 ** 2.

Except in the context of an arithmetic comparison operator, arithmetic expressions need to be explicitly *evaluated* in Prolog, using the <u>is</u> built-in predicate.

Mostly one uses these operators in a goal more like this:

```
X \underline{is} Y + 2
```

where Y is a variable already bound to a numeric value, or perhaps a arithmetic comparison goal like this:

```
X > Y * Z
```

Here's another example: a rule to tell if a (whole) number is *odd*: odd (Num) :- 1 is Num mod 2.

Another way to do this one is to use =:=:

```
odd(Num) := Num \mod 2 = := 1.
```

If you wanted to be more cautious, you could first check that Num is in fact a whole number:

```
odd (Num) :- integer (Num), 1 is Num mod 2.
```

As usual in digital computations, with fractional numbers, it is necessary to be careful with approximation issues. Thus the final example in the table above, 1. 21 is 1. 1 ** 2. actually fails when

typed into Prolog as a query. This is because 1.1 ** 2, as represented in computers, actually comes out to be something like 1.21000000001. See the section on <u>comparison operators</u> for a solution to this issue.

Note that SWI Prolog does some apparently strange stuff in the domain of arithmetic:

```
?- X is [a].
X = 97.
?- X is [a] + [b].
X = 195.
?- X is sqrt(23456).
X = 153.154.
?- X is sqrt([23456]).
X = 153.154.
?- X is sqrt(123456789).
X = 11111.1.
?- X is sqrt([123456789]).
X = 13.3791.
```

The ASCII code for a is 97, which sort of explains the first two query outcomes. The last pair of queries are particularly strange. It is best to avoid relying on this sort of thing, and stick to standard arithmetical notation. Avoid strange tricks: code should be comprehensible.

See also comparison operators, built-in functions.

arity

The arity of a functor is the number of arguments it takes. For example, the arity of likes, as in likes (jane, pizza), is 2, as it takes

two arguments, jane and pizza.

```
Arity Example Could Mean ...

0 linux. a bit like #define LINUX in* C
1 happy(fido). Fido is happy.
2 likes(jane, pizza).
3 gave(mary, john, book). Mary gave John a book.
```

* hard to use in practice in Prolog: if the code contains linux. then you could test for this, but if it doesn't, then testing linux in your code will trigger an "Undefined procedure: linux/0" error. You can work around this by declaring linux to be dynamic - i.e. putting the line

```
:- dynamic linux/0. in your code (usually at the start).
```

Every fact and rule in a Prolog program, and every <u>built-in</u> <u>predicate</u> has an arity. Often this is referred to in descriptions of these facts and rules, by appending / and the arity to the name of the rule or fact. For example, the built-in predicate <u>member/2</u> has arity 2.

A fact or rule can have more than one arity. For example, you might want to have two versions of make terms:

```
% make(X, Y, Z): X makes Y for Z
make(fred, chest_of_drawers, paul).
make(ken, folding_bicycle, graham).
% make(X, Y): X makes Y
make(steve, fortune).
make(kevin, mistake).
```

What we have here are make/3 and make/2.

assert, asserta, assertz

assert is a meta-predicate that adds its single argument, which may be a fact or a rule, to the Prolog database. The idea is that you construct or learn a new fact or rule in the course of executing your Prolog program, and you want to add it to the database. asserta ensures that the added fact/rule is added before any other facts or rules with the same functor), while assertz adds the fact after any other rules or facts with the same functor. When more than one rule/fact with the same functor is present in the database, they are tried in the order that they appear in the database, hence the need for asserta and assertz.

You would use asserta in the common case where the new fact is supposed to save the effort involved in checking the fact using rules and other facts. You might use assertz, for example, if you were trying to construct a queue data structure (where items are added to the *end* of the queue. Examples:

```
?- assert(rich(mary)).
true.
?- rich(mary).
true.
?- assert((happy(X) :- rich(X), healthy(X))).
X = _G180
?- assert(healthy(mary)).
true.
?- happy(X).
X = mary
```

Facts/rules that are loaded from a file cannot be mixed with facts/rules that are created using <code>assert/asserta/assertz</code> without take the special step of declaring the procedure in question to be $\underline{dynamic}$. For example, if you have a rule to say, compute N!, with

header factorial (+N, -Result), i.e

with functor factorial and arity 2, and you also want to

use asserta to add pre-computed values of some factorials to the Prolog database (see also<u>memoisation</u>), then you need to declare factorial to be dynamic, by including the following with your loaded rules for factorial:

```
:- dynamic factorial/2.
```

Programs with asserted facts and rules can be extra hard to debug.

See also retract, retractall, dynamic.

atom

An atom, in Prolog, means a single data item. It may be of one of four types:

- a string atom, like 'This is a string' or
- a symbol, like likes, john, and pizza, in likes (john, pizza). Atoms of this type must start with a lower case letter.
 They can include digits (after the initial lower-case letter) and the underscore character (_).
- the empty list []. This is a strange one: other lists are not atoms. If you think of an atom as something that is not divisible into parts (the original meaning of the word *atom*, though subverted by subatomic physics) then [] being an atom is less surprising, since it is certainly not divisible into parts.
- strings of special characters, like <--->, ..., ===>. When using atoms of this type, some care is needed to avoid using strings of special characters with a predefined meaning, like the <u>neck</u> symbol :-, the <u>cut</u> symbol !, and various <u>arithmetic</u> and <u>comparison</u> operators.

 The available special characters for constructing this class of atom are: +, -, *, /, <, >, =, :, ., &, _, and ~.

Numbers, in Prolog, are not considered to be atoms.

atom is also the name of a built-in predicate that tests whether its single argument is an atom.

```
?- atom(pizza).
true.
?- atom(likes(mary, pizza)).
false.
```

```
?- atom(<-->).
true.
?- atom(235).
false.
?- X = some_atom, atom(X).
X = some atom.
```

The final example means that atom(X) has succeeded, with X bound

to some_atom.

atom_chars

The built-in Prolog predicate atom_chars can convert an atom into the

list of its constituent letters, or vice-versa. A fairly broad concept of atom is used: this predicate will glue together (or split up) any reasonable characters you give it. A possible list would be to put together a list of letters read, one character at a time, to make a word - that is, an atom whose name is the word. Examples:

```
?- atom_chars(pizza, List).
List = [p, i, z, z, a]
?- atom_chars(Atom, [b, e, e, r]).
Atom = beer
?- atom_chars(2007, List).
List = ['2', '0', '0', '7']
?- atom_chars(Atom, ['[', '3', '', ', ', '4', ']']).
Atom = '[3, 4]'
```

See also atom codes.

atom codes

The built-in Prolog predicate atom_codes can convert an atom into the

list of the numeric codes used internally to represent the characters in the atom, or vice-versa. Examples:

```
?- atom_codes(pizza, List).
List = [112, 105, 122, 122, 97]
?- atom_codes(Atom, [98, 101, 101, 114]).
```

See also atom chars.

backtracking

Backtracking is basically a form of searching. In the context of Prolog, suppose that the Prolog interpreter is trying to satisfy a sequence of goalsgoal_1, goal_2. When the Prolog interpreter finds a set of variable bindings which allow goal_1 to be satisfied, it commits itself to those bindings, and then seeks to satisfy goal 2. Eventually one of two things happens: (a) goal_2 is satisfied and finished with; or (b) goal_2 cannot be satisfied. In either case, Prolog backtracks. That is, it "un-commits" itself to the variable bindings it made in satisfying *goal_1* and goes looking for a different set of variable bindings that allow *goal_1* to be satisfied. If it finds a second set of such bindings, it commits to them, and proceeds to try to satisfy goal_2 again, with the new bindings. In case (a), the Prolog interpreter is looking for extra solutions, while in case (b) it is still looking for the first solution. So backtracking may serve to find extra solutions to a problem, or to continue the search for a first solution, when a first set of assumptions (i.e. variable bindings) turns out not to lead to a solution.

Example: here is the definition of the built-in Prolog predicate member:

```
member(X, [X | Rest]). % X is a member if its the first element
member(X, [Y | Rest]) :-
    member(X, Rest). % otherwise, check if X is in the Rest
```

You may not think of member as a backtracking predicate, but

backtracking is built into Prolog, so in suitable

circumstances, member will backtrack:

```
?- member(X, [a, b, c]).

X = a ;

X = b ;

X = c ;

false.
```

Here member backtracks to find every possible solution to the query given to it. Consider also:

```
?- member(X, [a, a, a]).
```

```
X = a ;
X = a ;
X = a ;
false.
```

Here member backtracks even though it keeps on finding the same

answer. What about

```
?- member(a, [a, a, a]).
true;
true;
true;
false.
```

This is because prolog has three ways of proving that a is a member

```
of [a, a, a].
```

The term backtracking also applies to seeking several sets of variable bindings to satisfy a single goal.

In some circumstances, it may be desirable to inhibit backtracking, as when only a single solution is required. The Prolog <u>cut</u> goal allows this.

Tracing the execution of a piece of Prolog code that backtracks can be a good way to figure out what happens during backtracking. If you wanted to experiment with backtracking by tracing member, you could achieve this by copying the code for member, given above, changing the name from member to saymem in the three places where it appears, and then tracing your mem procedure.

bagof

The built-in predicate bagof (+Template, +Goal, -Bag) is used to collect a list Bag of all the items Template that satisfy some goal Goal.

Example: assume

```
likes(mary, pizza).
likes(marco, pizza).
likes(Human, pizza) :- italian(Human).
italian(marco).
```

Then

```
?- bagof(Person, likes(Person, pizza), Bag).
Person = _G180
Bag = [mary, marco, marco]
```

Notice that Bag contains the item marco twice, because there are two ways to prove that marco likes pizza - the fact and via the rule. bagof fails ifGoal has no solutions.

```
See also <u>setof</u>, and, for differences between bagof and findall, see findall.
```

binding

Binding is a word used to describe giving a value to a <u>variable</u>. It normally occurs during application of a Prolog rule, or an attempt to satisfy the<u>goals</u> in a Prolog <u>query</u>.

Suppose that the Prolog database contains just the single fact likes (mary, pizza). and that there is a query:

```
?- likes(mary, What).
```

Prolog will search the (tiny) database, find that the query can be satisfies if What = pizza, do it will bind What to pizza and report success:

```
?- likes(mary, What).
What = pizza;
false.
```

Now suppose that there is a rule and facts in Prolog's database:

```
teaches (Teacher, Student):-
   lectures (Teacher, Subject), studies (Student, Subject).
lectures (codd, databases).
studies (fiona, databases).
studies (fred, databases).
```

and that the user issues the query:

```
?- teaches (codd, Who).
```

The Prolog interpreter first matches the head of the rule with the query, and so binds Teacher to codd. It then finds a fact that indicates a subject that Codd lectures - namely lectures (codd, databases). At this point, the variable Subject is bound to databases (Subject = databases). In other words, Subject, perhaps temporarily, has the value databases. Then Prolog tries to satisfy the second goal studies (Student, Subject) with Subject = databases, i.e. it tries to satisfy studies (Student, databases). When it finds the solution, studies (fiona, databases) it will bind Subject to fiona, and report the solution:

```
?- teaches(codd, Who).
Who = fiona
```

Notice that the binding Subject = databases was made in solving the query, but it is not reported, as it is not explicitly part of the query.

Then, if the user types ";", Prolog will <u>backtrack</u> and undo the binding Student = fiona and look for another value for Subject that satisfiesstudies (Student, databases), and find as Student = fred. However, while binding (and unbinding) is involved in this step, it is properly treated under <u>backtracking</u>.

body

the last part of a Prolog <u>rule</u>. It is separated from the <u>head</u> by the <u>neck</u> symbol, written as :-. It has the form of a comma-separated list of <u>goals</u>, each of which is a functor, possibly followed by a comma-separated list of arguments, in parentheses. E.g. in the rule

```
sister_of(X, Y) := female(Y), X = Y, same_parents(X, Y).
```

the three goals female(Y), X = Y, same_parents(X, Y) form the body.

built-in predicate

To make Prolog programming more practical, a number of <u>predicates</u> or are built into Prolog. These include some utility procedures, which *could* have been programmed by the Prolog user, and some which do non-logic programming things, like the input and output routines, debugging routines, and a range of others.

Bratko

This refers to the text used in COMP9414/9814 at the University of New South Wales, Australia:

Bratko, I., *Programming in Prolog for Artificial Intelligence*, 4th Edition, Addison-Wesley, 2011

built-in

functions, abs, atan, ceiling, cos, exp, float, floor, log, round, sign, sin, s

qrt, tan, truncate

A small number of mathematical functions are built into Prolog, including:

```
Function
              Meaning
              absolute value of Exp : i.e. Exp if Exp \geq 0, -Exp
abs (Exp)
              if Exp < 0
              arctangent (inverse tangent) of Exp: result is in
atan (Exp)
              radians
cos (Exp)
              cosine of the Exp : Exp is in radians
              e^{\text{Exp}}: e is 2.71828182845...
exp(Exp)
              natural logarithm of Exp: i.e. logarithm to the
log(Exp)
              base* e
sin(Exp)
              sine of the Exp: Exp is in radians
sart (Exp)
              square root of the Exp
tan(Exp)
              tangent of the Exp: Exp is in radians
              sign (+1 or -1) of the Exp: <math>sign(-3) = -1 =
sign(Exp)
              sign(-3.7)
              float of the Exp: float(22) = 22.0 - see
float (Exp)
              also float the predicate
floor (Exp)
              largest integer \leq Exp: floor (1.66) = 1
truncate(Exp) remove fractional part of Exp: truncate(-1.5) =
```

```
round (Exp) -1, truncate (1.5) = 1

round (Exp) \text{round Exp to nearest integer: round (1.6)} = 2, round (1.3) = 1

ceiling (Exp) \text{smallest integer} \ge \text{Exp: ceiling (1.3)} = 2
```

These functions should be used in a context where they will actually be evaluated, such as following <u>is</u> or as part of an

arithmetic comparison operatorlike =:= or >.

Example:

```
?- X is sqrt(2).
X = 1.41421
```

Compare this with the following, where sqrt(2) is not evaluated, because = does not evaluate its arguments.

```
?- X = sqrt(2).
X = sqrt(2)
Another example:
?- X is log(3+2).
X = 1.60944.
```

These mathematical functions may correspond to arity 2 built-in predicates: for example, one can do this:

```
?- sqrt(2, X).
X = 1.41421
```

Some versions of SWI Prolog (e.g. 5.6.47) implement many of these arity 2 predicates, but not e.g. exp/2.

* High School Maths Reminder Service: if you want the logarithm to base a, divide $\log(\text{Exp})$ by $\log(a)$. E.g. $\log_{10}(X) = \log(X)/\log(10)$, and $\log_2(X) = \log(X)/\log(2)$.

cal1

call is a built-in meta-predicate that allows its single argument to be called/invoked as a goal. For example, a program might create a goal (perhaps using <u>=</u>..) on the fly, and then, presumably later in the program, need to test the goal. Here are queries that perform these

roles - in a real program, both the assert and the call would be built in to Prolog procedures written by the programmer.

```
?- assert(likes(mary, pizza)).
?- call(likes(Person, pizza)).
Person = mary
?- Goal =.. [likes, mary, What], call(Goal).
Goal = likes(mary, pizza)
What = pizza
```

clause

A clause in Prolog is a unit of information in a Prolog program ending with a full stop (". "). A clause may be a fact, like:

```
likes(mary, pizza).
food(pizza).
```

or a rule, like:

```
eats (Person, Thing) :- likes (Person, Thing), food (Thing).
```

A clause may also be a query to the Prolog interpreter, as in:

```
?- eats (mary, pizza).
```

A group of clauses about the same relation is termed a procedure.

commenting your code

In Prolog, a the start of a comment is signalled by the character %.

Comments are ignored by the Prolog interpreter; their purpose is to help a human reader understand the Prolog code. Examples:

```
% This is a full line comment.
```

% The next line contains a part-line comment. member(Item, [Item|Rest]). % member succeeds if Item is 1st object in list.

Commenting Guidelines

As in other programming languages, comments should be used freely to explain the high-level significance of sections of code, to explain tricky sections of code, etc. Comments should *not* echo what the code already clearly says. Comments like that actually get in the way of understanding, for example because they are likely to make the reader

ignore the comments. Where it is possible to make code understandable by using a meaningful <u>functor</u>name or <u>variable</u> name, this is preferable to a comment.

It is good practice to begin each Prolog procedure with a comment describing what it does, e.g.

```
% member (Item, List) - succeeds if the item is a member of the list
```

If the list needs to have some special properties, e.g. if it must be a list of numbers, or must be instantiated (that is, have a value) at the time the procedure is called, then this *header* comment should say so:

```
% member(Item, List) - succeeds if the item is a member of the list;
% List must be instantiated at the time member is called. Item
need not
% be instantiated.
```

It can be a good idea for the header comments to indicate examples of the kind of data on which the procedure is intended to operate, and what the result should be, if this can be done reasonably briefly. E.g.

```
% Examples of use:
% ?- member(b, [a, b, c]).
% true.
%
% ?- member(X, [a, b, c]).
% X = a ;
% X = b ;
% X = c ;
% false.
```

Each file of Prolog code should begin with a (file) header comment, indicating who wrote the code, when, and what it is (overall) intended to do. This would be enough in a short Prolog assignment. In a "industrial strength" Prolog system, there would be details on the origins of algorithms used, and a revision history.

A good source of examples of Prolog commenting is example code made available in class, such as <u>this one</u>. Note however that this one is rather more heavily commented than usual, for instructional purposes. Note also that code examples presented on screen may be *under*-commented, because of the difficulty of fitting the comments and the code on the screen, and because the oral

presentation accompanying the on-screen material replaces the comments to some extent.

Don't make your lines of comments (or code) too long - long lines can be hard to read, and really long lines may be folded, turning your neat formatting into a dog's breakfast. Stick to a maximum line length of 70 or 80 characters. Cute lines and/or boxes constructed of comment characters have the side effect of preventing the reader from seeing as much of your code at one time. The reader may then have to page up and down to figure out what your code does. They will not like you for this.

The use of <u>cuts</u> should normally be commented to explain why the cut is necessary.

It is a bad idea to comment (almost) every line, partly because of the clutter, and the distraction that this causes, and partly because most such comments are pointless duplications of the code (and/or comment things obvious except to a novice Prolog programmer):

Example of bad commenting (every line commented):

```
factorial (0, 1).
                                         % Factorial of 0 is 1.
factorial(N, FactN) :-
    N > 0,
                                         % N is positive
    Nminus1 is N-1,
                                         % Calculate N minus 1
    factorial (Nminus1, FactNminus1), % recursion
                                         % N! = N * (N - 1)!
    FactN is N * FactNminus1.
Of these comments, only the first and last are even faintly justifiable,
and even these are probably too obvious, as, particularly for the last
comment, the variable names tell you everything you need to know. It
looks pretty, with all the %-signs neatly lined up, but it forces the
reader to check through all the unnecessary comments in case there is
anything important there. This code needs a procedure header
comment, and probably nothing else, though a beginning Prolog
programmer might be justified in pointing out that the line \mathbb{N} > 0, is
there to make sure that the rule is only used in the case where N is
positive. (If you're not sure why this is so important, try leaving out N >
```

0, and test the function on say N = 2.) So the comment would be "% only use rule if N > 0."

How to write even worse comments!

It's easy - just write comments that are actually wrong. ②
Review your comments in a cool moment, and make sure that what they say is true.

The + - ? convention for arguments to procedures

A convention often used to make the role of arguments to a procedure clearer is to tag them with +, -, and ?, as follows:

Tag Meaning

- argument is expected to be *instantiated* (i.e. have a value + rather than be a variable) when the procedure is called as a <u>goal</u>.
- argument is expected to be a *variable to be bound* when the procedure is called as a <u>goal</u>.
- ? argument may be either instantiated, or be an unbound variable, when the procedure is called as a <u>goal</u>.

Example:

```
% factorial(+N, -FactorialN).
%% supply a value for N, and FactorialN will be computed.

% member(?Item, ?List).

%% Item and List may either be instantiated, or a variable
%% (but in fact at least one of them must be instantiated!)
It's worth checking out, by the way, what happens if List is not instantiated ...
?- member(a, List).

List = [a|_G231];
List = [_G230, a|_G234];
List = [_G230, _G233, a|_G237]
```

Spelling, grammar, etc.

It's no bad thing if all of these comments are spelled correctly and are grammatically phrased. (Sometimes it is appropriate to abbreviate, so perhaps your comments don't all need to be full sentences.) It makes life harder for folks trying to read your code, if they have to wade through poor spelling and grammar. Remember that the people reading your code will include people you will *want* to understand your comments easily - helpers, markers, colleagues, your boss, even yourself in a year's time when you've forgotten how you got the code to work ... So get into good commenting habits from the start.

See also <u>indentation</u> and <u>white space</u>.

comparison operators

E1 >= E2

(Only some of the operators below are relevant to COMP9414 at University of New South Wales - see green colouring below.) Prolog has two main classes of comparison operators - arithmetic comparison operators (and similar alphabetic comparison operators) and unification-style operators:

Comparison Definition ? X = Y succeeds if X and Y unify (match) in the Prolog sense No

succeeds if X and Y do not unify; i.e. X \= Y No if not (X = Y)succeeds if terms T1 and T2 are identical; T1 == T2No e.g. names of variables have to be the same T1 \== T2 succeeds if terms T1 and T2 are not identical No succeeds if values of expressions E1 and E2 E1 = := E2Yes are equal succeeds if values of expressions E1 and E2 E1 = E2Yes are not equal succeeds if numeric value of expression El E1 < E2 Yes is < numeric value of E2 succeeds if numeric value of expression E1 $E1 = \langle E2 \rangle$ Yes is ≤ numeric value of E2 succeeds if numeric value of expression E1 E1 > E2Yes is > numeric value of E2

succeeds if numeric value of expression E1

Yes

	is ≤ numeric value of E2	
T1 @< T2	succeeds if T1 is alphabetically $<$ T2	No
T1 @=< T2	succeeds if T1 is alphabetically \leqslant T2	No
T1 @> T2	succeeds if T1 is alphabetically $>$ T2	No
T1 @>= T2	succeeds if T1 is alphabetically \geqslant T2	No

See also <u>is</u> is not a comparison operator, but is frequently confused with = by novice Prolog programmers. Briefly, you use X is Exp to *evaluate* an arithmetic expression, like Y + 2, that contains an arithmetic operator, like +, and bind the resulting value to the variable X to the left of the the operator is.

As an example of @< and its relatives,

```
?- likes(mary, pizza) @< likes(mary, plums). true.
```

This succeeds because likes and mary are the same in both terms, and pizza alphabetically precedes plums.

Comparison of fractional numbers: When comparing two fractional numbers, problems can arise from the approximate nature of representations of fractional numbers in computers. Sometimes it will work as expected, and sometimes not. For example, the query 1. 21

=:= 1.1 * 1.1. fails with SWI Prolog on the computer where this article was written. You can and should work around this problem by, instead of testing fractional numbers for equality, doing something like the following:

```
?- abs(1.21 - 1.1 * 1.1) < 0.000001.
```

```
<u>abs</u> signifies "absolute value": abs (X) = X if X \ge 0 and abs (X) = -X if X = < 0.
```

More generally, test for abs(X - Y) < Tiny, where Tiny is bound to small number (or is a small number, as in the example). How small to make Tiny above depends on the particular case - you might need to

use a smaller number if X and Y need to be *very* close together to make your algorithm work correctly.

consult

These pre-defined pseudo-predicates allow one to load Prolog code into a running Prolog interpreter. Example:

```
?- consult ('myprogram. pl').
```

This loads the contents of the Prolog program in the

file myprogram. pl into the running Prolog's database. **Note** that in SWI Prolog, at least, before loading the new facts and rules into the database, Prolog first removes all facts and rules that relate to procedures in myprogram. pl. So if myprogram. plcontains, for example,

the fact likes (jane, pizza) then all facts and rules about likes that have two arguments will be removed from the Prolog database before the new facts in myprogram. pl are loaded up. This is convenient when

you are using consult to re-load a program after editing it (e.g. in another window, with the Prolog interpreter left running), but could be a little surprising if you were trying to load extra facts from a file.

It is possible to consult more than one file at a time, by replacing the single file name with a list of files:

```
?- consult(['file1.pl', 'file2.pl', 'file3.pl']).
% file1.pl compiled 0.00 sec, 524 bytes
% file2.pl compiled 0.01 sec, 528 bytes
% file3.pl compiled 0.00 sec, 524 bytes
true.
```

It is also possible to abbreviate a consult call, simply typing the list of (one or more) files as a goal for Prolog:

```
?- ['file1.pl', 'file2.pl', 'file3.pl'].
```

In some Prolog implementations, consulting user causes the Prolog interpreter to read facts and rules from the user's terminal:

```
?- [user].
|: likes(jane, pizza).
|: bad_dog(Dog) :-
|: bites(Dog, Person),
|: is_human(Person),
|: is_dog(Dog).
|: <control-D>
% user://1 compiled 0.00 sec, 1,156 bytes true.
?-
```

current input stream

At any given time, input to Prolog comes from the "current input stream". When Prolog starts up, the current input stream is the keyboard of the computer/workstation from which Prolog was started.

However, you might wish to get input/read from somewhere else during the execution of your Prolog program - for example, you might want to read from a file held on the computer on which the program is running, or on some local file server. To change the current input stream, you use the Prolog built-in extra-logical

predicate see. If Prolog executes the goal see ('input. dat'), then

input will subsequently come from the file input. dat, in the current working directory of the workstation* that is running Prolog. If the specified file cannot be found in the current working directory, an error may be reported, as in this interaction with SWI Prolog:

```
?- see('nosuchfile.dat').
ERROR: see/1: source_sink `nosuchfile.dat' does not exist (No such
file or directory)
```

Other errors are possible - you may not have the right to read the file in question, for example. If the file does exist and is readable, then subsequent read operations get their data from the file. The parameter to see can be just the file name, as illustrated above, or it could be a path to the file that is wanted:

```
e.g. see ('/Users/billw/prologstuff/input. dat') Prolog will continue to issue prompts for more queries while you are "seeing" a file, but any explicit read operations access the file. The built-in
```

extra-logical predicate seen (with no argument) allows you to revert to reading data from the keyboard. Example (assuming info. dat starts with the line hungry (jack).):

```
?- see('info.dat'), read(X).
X = hungry(jack)
?- seen, read(Y).
|: full(jack).
Y = full(jack)
```

See also current output stream, input, output, files.

*Strictly speaking, input. dat will be expected to be in the current working directory of the command interpreter that started Prolog. The command interpreter will be running on the workstation/computer, and sending output to a window on that workstation or computer.

current output stream

At any given time, input to Prolog goes to the "current output stream". When Prolog starts up, the current output stream is the window or console of the computer/workstation from which Prolog was started. In other words, when your program writes things using the predicates described in the article on writing, they appear on your screen.

However, you might wish to write to somewhere else during the execution of your Prolog program - for example, you might want to write to a file held on the computer on which the program is running, or on some local file server.

To change the current output stream, you use one of the Prolog built-in extra-logical predicates tell and append/1*. If Prolog executes the goaltell ('output. dat'), then output will subsequently go to the file output. dat, in the current working directory of the workstation* that is running Prolog.

If the specified file cannot be found in the current working directory, it will be created. If the file does exist, it will be overwritten. If you useappend/1, subsequent write operations will add material to the end of the file, instead of overwriting the file. If you do not have

permission to write files in the current directory, you will see an error message:

```
?- tell('/usr/bin/ztrash').
ERROR: tell/1: No permission to open source_sink `/usr/bin/ztrash'
(Permission denied)
```

This means that either you do not have permission to write files in the directory /usr/bin, or if the file ztrash already exists in this directory, that you do not have permission to write to that file.

If the file is able to be written, then subsequent write operations send their data to the file. The parameter to tell can be a path to the file that is wanted, as in the example above, or it could be just the file name, e.g. tell('output.dat'). Prolog will continue to issue prompts for more queries and print bindings while you are "telling" or "appending" a file, but any explicit write operations access the file.

The built-in extra-logical predicate told (with no argument) allows you to revert to writing data to the original window. Example:

```
?- tell('info.dat'), write(thirsty(jack)), nl.
true.
?- told, write(drunk(jack)).
drunk(jack)
true.
?- halt.
% cat info.dat # - # is Unix comment char, cat lists info.dat
thirsty(jack)
%
```

See also current input stream, input, output, files.

Strictly speaking, output. dat will be expected to be in the current working directory of the command interpreter that started Prolog. The command interpreter will be running on the workstation/computer, and sending output to a window on that workstation or computer.

^{*} append/1 is not related to <u>append/3</u>, which in turn has nothing to do with output streams.

The cut, in Prolog, is a <u>goal</u>, written as !, which always succeeds, but cannot be <u>backtracked</u> past. It is used to prevent unwanted backtracking, for example, to prevent extra solutions being found by Prolog.

The cut should be used sparingly. There is a temptation to insert cuts experimentally into code that is not working correctly. If you do this, bear in mind that when debugging is complete, you should understand the effect of, and be able to explain the need for, every cut you use. The use of a cut should thus be commented.

Example: Suppose we have the following facts:

```
teaches (dr_fred, studies (alice, history). english).
teaches (dr_fred, studies (angus, english).
teaches (dr_fred, drama). studies (amelia, teaches (dr_fiona, drama).
physics). studies (alex, physics).
```

Then consider the following queries and their outputs:

```
?- teaches(dr_fred, Course), studies(Student, Course).
Course = english
Student = alice;
Course = english
Student = angus;
Course = drama
Student = amelia;
false.
```

Backtracking is not inhibited here. Course is initially bound to history, but there are no students of history, so the second goals fails, backtracking occurs, Course is re-bound to english, the second goal is tried and two solutions found (alice and angus), then

backtracking occurs again, and Course is bound to drama, and a final Student, amelia, is found.

```
?- teaches(dr_fred, Course), !, studies(Student, Course). false.
```

This time Course is initially bound to history, then the cut goal is executed, and then studies goal is tried and fails (because nobody studies history). Because of the cut, we cannot backtrack to the teaches goal to find another binding for Course, so the whole query fails.

```
?- teaches(dr_fred, Course), studies(Student, Course), !.
Course = english
Student = alice ;
false.
```

Here the teaches goal is tried as usual, and Course is bound to history, again as usual. Next the studies goal is tried and fails, so we don't get to the cut at the end of the query at this point, and backtracking can occur. Thus the teaches goal is re-tried, and Course is bound to english. Then the studiesgoal is tried again, and succeeds, with Student = alice. After that, the cut goal is tried and of course succeeds, so no further backtracking is possible and only one solution is thus found.

```
?-!, teaches(dr_fred, Course), studies(Student, Course).
Course = english
Student = alice;
```

```
Course = english
Student = angus ;

Course = drama
Student = amelia ;

false.
?-
```

In this final example, the same solutions are found as if no cut was present, because it is never necessary to backtrack past the cut to find the next solution, so backtracking is never inhibited.

Cuts in Rules

In practice, the cut is used in rules rather than in multi-goal queries, and some particular idioms apply in such cases. For example, consider the following code for max(X, Y, Max), which is supposed to bind Max to the larger of X and Y (which are assumed to be numbers).

```
\max(X, Y, X) := X > Y, !.
\max(X, Y, Y).
```

This is a way of saying: "if the first rule succeeds, use it and don't try the second rule. (Otherwise, use the second rule.) We could instead have written:

```
\max(X, Y, X) := X > Y.
\max(X, Y, Y) := X = < Y.
```

in which case both rules will normally be tried (unless backtracking is prevented by a cut in some other part of the code). This is slightly less

efficient if X is in fact greater than Y (unnecessary backtracking occurs)

but easier for people to understand, though regular Prolog programmers rapidly get to recognise this type of idiom. The extra computation in the case of max is trivial, but in cases where the second rule involves a long computation, there might be a strong argument for using the cut on efficiency grounds.

debugging

means removing errors from program code. This is done by (1) observing the errors (i.e. <u>testing</u>); (2) locating the cause in the code; (3) correcting the errors.

(1) and (2) are often the hard part. Once you have observed or detected an error, <u>tracing</u> the code in question can help find the problem. Sometimes inserting calls to <u>write</u> into parts of the code where you think that the problem might be can help to localise the error.

Ultimately, reading your code carefully will be part of the task. So it would be a good idea to write the code carefully in the first place, in order to make it easy to understand. See also <u>error and warning</u> messages and commenting and white space.

declarative

A declarative programming language is one in which the relationships between the data are stated (or *declared* in a (usually logic-based) language, and then some automatic mechanism, e.g. a theorem-prover, is used to answer <u>queries</u> about the data. Prolog is a declarative programming language. Haskell, Miranda, Lisp, and Scheme are *functional* programming languages, in which all constructs are expressed using functions, function arguments, and function results, and C, C++, Java, Perl, Pascal, Modula-2, and Fortran are examples of (high-level) *procedural* programming languages, in which the program code expresses procedures to follow in manipulating the data.

dynamic

In Prolog, a procedure is either <u>static</u> or dynamic. A static procedure is one whose facts/rules are predefined at the start of execution, and do not change during execution. Normally, the facts/rules will be in a file of Prolog code which will be loaded during the Prolog session. Sometimes, you might want to add extra facts (or maybe even extra rules) to the procedure, during execution of a Prolog query,

using <u>asserta/assertz"</u>, or maybe remove facts/rules

using <u>retract/retractall</u>. To do this, you must declare the procedure to be dynamic.

You can declare a procedure to be dynamic by including in your code (normally adjacent to the facts/rules for that procedure) a suitable dynamic directive. Example - suppose you have a procedure called likes, with arity 2, and you have a "starter set" of facts/rules in your Prolog program, but you want to infer extra facts

about likes during execution, and add them to the data base so that they don't need to be recomputed each time they are used. [You would normally only do this - add the new facts to the database - if the extra facts were slow to compute.] You need to

declare likes (with arity 2) to be dynamic. You do this as follows:

```
:- dynamic likes/2.
```

[By the way, notice that this leaves open the possibility that a different version of likes (with arity 3, say) might not be dynamic.]

See also <u>memoisation</u>.

efficiency

```
There are many ways for code to be inefficient. This article
concentrates on the issue of avoiding unnecessary recursive calls.
Consider the following exercise: write a Prolog
predicate printOrAdd (IntegerList, Sum) which binds the even
numbers from its input list IntegerList to a list EvensList, and at the
same time adds up the odd numbers in IntegerList and binds them
to Sum. Here are two versions of the
code, print0rAdd and print0rAdd1:
% printOrAdd is an inefficient solution to the task posed above:
printOrAdd([], [], 0).
% even numbers
printOrAdd([First | Rest], [First | RestOfEvens], Sum) :-
  printOrAdd(Rest, RestOfEvens, Sum),
  0 is First mod 2.
% odd numbers
printOrAdd([First | Rest], RestOfEvens, Sum) :-
  printOrAdd(Rest, RestOfEvens, SumOfRest),
  1 is First mod 2,
  Sum is SumOfRest + First.
```

```
% printOrAdd1 is a corrected version of printOrAdd which
% avoids the unnecessary recursive calls.

printOrAdd1([], [], 0).

printOrAdd1([First | Rest], [First | RestOfEvens], Sum) :-
    0 is First mod 2,
    printOrAdd1([First | RestOfEvens, Sum).

printOrAdd1([First | Rest], RestOfEvens, Sum) :-
    1 is First mod 2,
    printOrAdd1([Rest, RestOfEvens, SumOfRest),
    Sum is SumOfRest + First.
?- printOrAdd([1, 2, 3, 4, 5, 6], Evens, SumOfOdds).
Evens = [2, 4, 6],
SumOfOdds = 9;
false.
```

The first version makes the recursive call in the two recursive rules before it tests to see if First is even or odd. If half the numbers are even and half odd, then clearly half of the recursive calls will be wasted. However, the situation is actually *much* worse than that, because of Prolog's automatic backtracking. The backtracking means that Prolog will eventually try all three rules for printOrAdd, and two of them will cause recursive calls, each of which will in turn generate two recursive calls, each of which ... Thus for a list of length 100, say, there will be more than 2^{100} recursive calls. If Prolog could manage a billion recursive calls per second, 2^{100} recursive calls would take about 2^{70} seconds, or about 30 trillion years.

The solution, of course, is to test before you make a recursive call, as is done in printOrAdd1. Always test <u>before</u> you make a recursive call; never call before you test.

error and warning messages

The messages from the Prolog interpreter when your program goes wrong can be difficult for a beginner to interpret. Little can be said in general, as the messages vary from system to system. You can find a guide for some of the messages produced by SWI Prolog here. See also underscore variables, debugging.

fact

A fact is a Prolog <u>clause</u> with a head with no variables in it, and no body, like

```
happy (fred).
likes (mary, pizza).

as opposed to this rule:
happy (Person) :-
    healthy (Person),
    enough_money (Person),
```

has friends (Person).

Bodiless clauses with variables, like ...

```
member(Item, [Item | RestOfList]).
```

... behave like rules in that they provide a general way of knowing that, for any Item, that item is a member of a list of which it is the first item (see also <u>member</u>). The clause above is likely to generate a SWI Prolog warning message like this:

```
Singleton variables: [RestOfList]
```

to tell you that the variable RestOfList is only mentioned once in the code (so may be a spelling mistake, for example). You can suppress the warning by writing, instead:

```
member(Item, [Item | ]).
```

using a <u>don't-care variable</u>, although this may be more difficult for a human to follow, particularly a beginnner at Prolog.

fail

Built-in Prolog predicate with no arguments, which, as the name suggests, always fails. Useful for forcing backtracking and in various other contexts.

See also true, repeat, input schema.

findal1

The built-in predicate findall (+Template, +Goal, -List) is used to collect a list List of all the items Template that satisfy some goal Goal.

Example: assume

```
likes(mary, pizza).
likes(marco, pizza).
likes(Human, pizza) :- italian(Human).
```

```
italian(marco).
Then
?- findall(Person, likes(Person, pizza), Bag).
Person = _G180
List = [mary, marco, marco]
```

findall succeeds and binds List to the empty list, if Goal has no solutions. This can be convenient if you don't want your goal to fail just because the collection of solutions is empty. (In other cases, you *would* want the goal to fail if there are no solutions.)

Another difference between <u>bagof</u> and findall is the extent of backtracking done before binding the third parameter (List). For example, assume:

```
believes (john, likes (mary, pizza)).
believes (frank, likes (mary, fish)).
believes (john, likes (mary, apples)).
```

Then bagof and findall exhibit the following behaviour:

```
?- bagof(likes(mary, X), believes(_, likes(mary, X)), Bag).
X = _G188
Bag = [likes(mary, fish)];

X = _G188
Bag = [likes(mary, pizza), likes(mary, apples)];
false.
?- findall(likes(mary, X), believes(_, likes(mary, X)), Bag).
X = _G181
Bag = [likes(mary, pizza), likes(mary, fish), likes(mary, apples)];
false.
```

You can see that bagof is collecting frank's beliefs about
what mary likes, binding Bag, then backtracking and collecting john's

beliefs and rebinding Bag, while findall all finds everybody's beliefs and binds them all to Bag, just once.

See also setof.

files, tell, telling, told, see, seeing, seen, append/1

When one writes a Prolog program, usually the facts and rules of the program are stored in a (text) file, and then loaded into the Prolog interpreter. Files have other uses in Prolog, too.

For example, we may wish to write out a table of results that have been computed for us by our Prolog program. One can use built-in predicates likewrite, nl, putc, tab and others to write out the table, but by default it will appear on the computer screen. To direct this output to a file, we use the tell built-in predicate. Suppose that we wish to write the table to a file called "mytable.data". By executing the (pseudo-)goaltell("mytable.data"), we tell Prolog that the new *current output stream* is to be the file "mytable.data". Subsequent writes will go to this file. When one wishes to stop writing to the file and resume writing on the screen, one uses the built-in predicate told (with no arguments). Also, the

query ?- telling (X). binds X to the name of the current output file. If the current output stream is not a file, then X will be bound to something that indicates that the current output stream is the screen for example, in Unix, X may be bound to the atom stdout (standard output, which is normally the screen). Example:

^{?-} tell('mytable.data'), write('***** Table of results *****'), nl, told.

[%] the file mytable.data should now contain a single line of text as above

The built-in Prolog predicate append/1 is like tell, except that it arranges for subsequent write operations to add data to the end of the specified file, rather than overwriting the file with the first subsequent write operation. If myothertable, data initially contains, say, a single

line, This is the first line, then append/1 works as follows:

```
?- append('myotherfile.dat'), write('Here is another line'), nl.
true.
?- halt.
% cat myotherfile.dat # - # is Unix comment char, cat lists file
contents
This is the first line
Here is another line
%
```

The situation for reading from a file is analogous to writing (except that there is no analogue for append/1). One can use built-in predicates like read, getc and others to read, by default from the keyboard. By executing the (pseudo-)goal see ('mydata. text'), we tell Prolog that the new *current input stream* is to be the file mydata. text. Subsequent reads will come from this file. When one wishes to stop reading from the file and resume reading from the keyboard, one uses the built-in predicate seen (with no arguments).

Also, the query ?— seeing(X). binds X to the name of the current input file. If the current input stream is not a file, then X will be bound to something that indicates that the current output stream is the screen - for example, in Unix, X may be bound to the atom stdin (standard input, which is normally the keyboard). Example:

```
?- see('mydata.text'), read(X), seen, write(X), n1.
% the first Prolog term in the file mydata.text should now appear
% on the screen, having been read from the file with read(X), and
then
% written to the screen with write(X) and n1.
```

What happens if you try to read from a file and there is nothing (left) to read, either because the file is empty, or you have previously read everything there was to read in this file? In this case, Prolog binds the variable that was the argument to read to the special

atom end_of_file. Knowing this means that you can test after a read to make sure that you did not hit end of file. Example:

```
?- see('empty.dat'), read(Term).
Term = end of file
```

See also <u>current input stream</u>, <u>current output</u>
stream, <u>input</u>, <u>output</u>. <u>append/3</u> is unrelated to append/1.

functor, functor

In Prolog, the word functor is used to refer to the atom at the start of a <u>structure</u>. For example, in likes (mary, pizza), likes is the functor. In a more complex structure, like

```
persondata (name (smith, john), date (28, feb, 1963))
```

the top-level functor is termed the *principal functor* - in this case persondata - There is also a built-in predicate called functor, used to extract the functor and <u>arity</u> of a structure.

There is also a built-in predicate functor with three

arguments: functor (Term, Functor, Arity), which succeeds if Term is a <u>term</u> with functor Functor and <u>arity</u> Arity. Examples:

```
?- functor(likes(mary, pizza), Functor, Arity).
Functor = likes
Arity = 2
?- functor(likes(X, Y), Functor, Arity).
X = _G180
Y = _G181
```

```
Functor = likes
Arity = 2
?- functor(likes, Functor, Arity).
Functor = likes
Arity = 0
?- functor(X, likes, 2).
X = likes(_G232, _G233)
```

Sometimes there are reasons to want to have the functor somewhere other than at the start of the structure. For example, in the

expression X < Y, "<" is a functor:

```
?- functor(2 < 4, Functor, Arity).
Functor = (<),
Arity = 2.
?- 2 < 4.
true.
?- <(2, 4).
true.
See op to find out how this works.</pre>
```

The term functor is used in a different sense in mathematics and in functional programming, and a different way again in philosophy.

goal

A query to the Prolog interpreter consists of one or more goals. For example, in

```
?- lectures (john, Subject), studies (Student, Subject).
```

there are two goals, lectures (john, Subject) and studies (Student,

Subject). A goal is something that Prolog tries to satisfy by finding

values of the variables (in this case Student and Subject) that make

the goal <u>succeed</u>. These value(s) are then said to be <u>bound</u> to the variable(s). If Prolog is unable to do this, the goal *fails* (and Prolog will print "false" in response to the query). If all the goals in a query succeed, Prolog prints the bindings necessary to make the query

succeed. (If you then, in SWI Prolog, type a semicolon (;) Prolog will <u>backtrack</u> and look for another set of bindings that will satisfy the goals in the query.

Sometimes it is not necessary to bind variables in order to satisfy a goal. For example, there is no variable to bind, when the goal is likes (mary, pizza) and the Prolog database already

contains likes (mary, pizza). In this case, Prolog will print "true" in response to the query, rather than printing bindings.

Goals occur in rules as well as in queries. In

```
happy(Dog) :-
  is_dog(Dog),
  go for walk(Dog).
```

 $is_dog(Dog)$ and $go_for_walk(Dog)$ are the two goals that form the body of the rule.

halt

This "goal", with no arguments, allows you to exit from Prolog in an operating-system-independent way. Typing the "end-of-file" character (control-D in Unix/Linux systems) will also get you out. Different operating systems may use different end-of-file characters.

Example of halt:

```
% prolog
--- Welcome message from Prolog interpreter ---
?- halt.
%
```

The "%" signs in this example represent the operating system command interpreter (aka "shell") prompt, *not* a Prolog <u>comment</u>.

head

The first part of a Prolog <u>rule</u>. It is separated from the <u>body</u> by the <u>neck</u> symbol :-. It normally has the form of a <u>functor</u> (i.e. a <u>relation</u> symbol, followed by a comma-separated list of parameters, in parentheses. E.g. in the rule $sister_of(X, Y) := female(Y)$, X = Y, $Same_parents(X, Y)$.

sister_of(X, Y) is the head.

if-then-else, ->

```
The built-in <u>infix</u> predicate \cdots \rightarrow \cdots; \cdots functions as an if ... then ... else ... facility. Example: \min (A, B, \min) := A < B \rightarrow \min = A; \min = B.
```

This version of min (which, like the one below, assumes that A and B are numbers) says "if A < B then unify Min with A otherwise unify Min with B". Possibly it is easier to understand a two-rule version of min:

```
min(A, B, A) :- A \le B.

min(A, B, B) :- B \le A.
```

That is, the minimum of A and B is A if A \leq B; the minimum is B if B \leq A. However, the \rightarrow definition of min does illustrate the operation of \rightarrow .

The code illustration has a rather procedural-programming feel to it that may comfort beginning users of Prolog. Possibly it should be avoided by them just for this reason! At least, they should avoid using it when the only reason for using it is the procedural feel. If use of -> massively reduced the length of the code, thereby simplifying it, that might be an argument for using it.

The detailed semantics of $\cdots \rightarrow \cdots$; \cdots is relatively complex. The following description is quoted from the SWI Prolog help text on \rightarrow :

The ->/2 construct commits to the choices made at its left-hand side, destroying choice-points created inside the clause

(by ;/2), or by goals called by this clause. Unlike !/0, the choice-point of the predicate as a whole (due to multiple clauses) is not destroyed. The combination ;/2 and ->/2 acts as if defined by:

```
If \rightarrow Then ; _Else :- If, !, Then. If \rightarrow _Then ; Else :- !, Else. If \rightarrow Then :- If, !, Then.
```

Please note that (If -> Then) acts as (If -> Then; fail), making the construct fail if the condition fails. This unusual semantics is part of the ISO and all de-facto Prolog standards.

Because of the cuts in this definition, the effect of \rightarrow and \cdots

-> ··· ; ··· can be unanticipated. Beginning Prolog programmers should use it with as much care as a cut. Programmers who already know a programming language with an if-then-else construct (like C, C++, Java, ...) are likely to react to discovering ··· -> ··· ; ··· with little cries of joy and relief, and use it at every opportunity. A safer reaction is "if you don't fully understand the semantics, don't use it."

COMP9414 and COMP9814 students at UNSW are forbidden to use it in any situation in which cuts are forbidden, primarily because we want you to learn how to manage without it (and cuts) where possible.

indentation

Indenting your Prolog code in a standard way is a technique, along with <u>commenting</u> it, to make your code more easily understood (by humans). The standard way to lay out a Prolog procedure is exemplified below, using a procedure to compute the length of a list. Comments have been omitted, to allow you to focus just on the indentation.

```
listlength([], 0).
listlength([Head | Tail], Length) :-
    listlength(Tail, TailLength),
    Length is TailLength + 1.
```

The rule is to align heads of rules against the left margin, and to indent body clauses, normally all by the same amount. Sometimes further indentation is needed, for example if the code involves a

complex <u>term</u> that won't fit on one line. In this case, you would indent the term to exhibit its structure.

```
book(
    title('The Strange Case of Dr Jekyll and Mr Hyde and Other
Tales of Terror'),
    author(given_names(['Robert', 'Louis']),
        surname('Stevenson')
    ),
    publisher('Penguin Books')
), ...
```

Sometimes the indentation rules can be bent: for example, it is not unusual to put on a single line, a rule with a body that contains just a single (short) clause.

```
happy (Person) :- rich (Person).
```

<u>Comments</u> on indented code should also be indented, if they can't be fitted on the same line as the code.

```
% sum_even_elements(+ListOfNumbers, -Sum): compute Sum of even
items in ListOfNumbers
sum_even_elements([], 0). % base case
sum_even_elements([FirstNum | Rest], Sum) :-
    % check whether FirstNum is even
    0 is FirstNum mod 2,
    % if we get here it was even, so process rest of list and add
FirstNum to result
    sum_even_elements(Rest, SumForRest),
    Sum is FirstNum + SumForRest.
sum_even_elements([FirstNum | Rest], Sum) :-
    % this rule handles the case where FirstNum is /not/ even
    0 =\= FirstNum mod 2,
    sum_even_elements(Rest, Sum).
```

This example is more heavily commented than necessary, in order to demonstrate the commenting convention.

See also <u>comments</u> and <u>white space</u>.

infix and prefix predicates/procedures

Most built-in constructs in Prolog, and, by default, the procedures and terms that you write yourself, use *prefix* syntax - that is, the name of the term/procedure (the <u>functor</u>) precedes the arguments (which are

surrounded by parentheses and separated by commas). For example, when we use the built-in predicate member, we write something like member (Item, [a, b, c]) - first the predicate name, member, then "(", then the first argument, Item, then a comma, then the second argument, [a, b, c], then ")".

However, with built-in predicates like =, < and > that are usually written between their arguments, as in First < Max, we write, in Prolog as in mathematics, in *infix* notation. Another infix built-in "predicate" is <u>is</u>, which is used in evaluating arithmetic expressions.

It is possible in Prolog to define your own infix (and postfix) operators, and modify the syntactic handling of prefix operators - see op.

input in

Prolog, read, end_of_file, get, get_byte, getc, flush_output

Input in Prolog is not always needed, as often the <u>query</u> process provides all the input that is needed. If explicit input is required, a set of extra-logical built-in predicates is available. These include:

- read(X) which reads the next term in the current input stream,
 which means the window on your workstation unless you have done something slightly fancy with files, and unifies it with the variable X.
- end_of_file: if there is nothing to read in the current input
 stream, read(X) causes X to be bound to the special
 symbol end_of_file. Unless you are absolutely sure you have
 some other way of knowing when there will be no more input data to read, you should check to make sure that the term that

- you have read is not end_of_file. Ways that you might be (almost) absolutely sure: the first term read might be a number indicating how many further terms are to be read.
- get_byte (C) which reads a single character from the current input stream, and binds the equivalent integer code, in the range 0 to 255. If there is no further character to read, C is bound to -1.
- get (C) is like get_byte(C), except that it reads the
 first non-blank character, if any, from the current input stream.
- flush_output is actually an output goal, which ensures that any output which has been requested but not yet performed, is performed right now. Output might not be completed until there is enough to make it worthwhile, or until an operation like flush output forces it.

Example 1: Assume that input is coming from the user's workstation window and that procedure read_a_char is defined as:

```
read_a_char(C) :-
  write('Type: '), flush_output,
  get_byte(C).
```

Then you can do the following - note that 43 is the character code for the character +.

```
?- read_a_char(Ch).
Type: +
Ch = 43
```

See also <u>atom_codes</u>, for conversion of a string of numeric character codes to an atom composed of the characters represented by those character codes. For example, 102, 105, 100, and 111 are the numeric codes for the letters f, i, d, and o. atom_codes can be used as follows:

```
?- atom_codes(A, [102, 105, 100, 111]).
```

Example 2: Assume that there is a file called inputdata, which contains on its first line the term likes (mary, pizza).

with a full stop at the end of the term.

```
?- see('inputdata'), read(Term), seen.
Term = likes(mary, pizza)
```

NB: *No* full stop at the end of Term's binding.

input schema

In any programming language, it is possible to specify schemata that how to code common programming tasks. The following is a schema for reading material from a file and processing it

```
dountilstop :-
  repeat,
  read(X),
  (X = stop, !
  ;
  process(X),
  fail
).
```

In this case, the code reads data, a <u>term</u> at a time, from the current input stream. To make that input stream a file called, say, inputdata, you would invoke the code as follows:

```
?- see ('inputdata'), dountilstop, seen.
```

The call to fail is there to force backtracking. The call to repeat is there to force the code to endlessly repeat - that is, until something terminates the backtracking. This "something" is the <u>cut</u> after X =

stop - if the term read is the <u>atom</u> stop, the goal X = stop succeeds, the cut is executed, and the rule terminates.

To use the schema, replace the read operation with the one you want (might be getc or ratom or ...), replace the call to process with a call to a procedure that does whatever *you* want to do to the data, and

you're in business. Actually - you'll probably find a few other adjustments are needed, but at least you're on the right track.

See also read, repeat, see, seen, ; (or), and fail.

is, evaluation

The is built-in predicate is used in Prolog to force the **evaluation** of arithmetic expressions. If you just write something like X = 2 + 4, the result is to bind X to the unevaluated term 2 + 4, not to 6. Example:

$$?- X = 2 + 4.$$

 $X = 2+4$

If instead you write X is 2 + 4, Prolog arranges for the second argument, the arithmetic expression 2 + 4, to be evaluated (giving the result 6) before binding the result to X.

$$?- X is 2 + 4.$$
 $X = 6$

It is only and always the second argument that is evaluated. This can lead to some strange-looking bits of code, by mathematical standards. For example, mod is the remainder-after-division operator, so in

Prolog, to test whether a number N is even, we write 0 is N mod 2, rather than the usual mathematical ordering: $N \mod 2 = 0$.

What is the difference between N = 1 and N is 1? In final effect, nothing. However, with N is 1, Prolog is being asked to do an extra step to work out the value of 1 (which, not surprisingly, is 1). Arguably, it is better to use N = 1, since this does not call for an unnecessary evaluation.

The message is: use is only when you need to evaluate an arithmetic expression.

Actually, you don't need to use is to **evaluate** arithmetic expressions that are arguments to the arithmetic <u>comparison operators</u> >, >=, < =<, =:= (equal), and =\= (not equal), all of which automatically evaluate their arguments.

```
Note the syntax of is: either
```

```
<variable> is <expression>
```

or

<numeric constant> is <expression>

Thus things like X*Y is Z*W do not work, as X/Y is an expression, not a variable - use either

```
0 is X*Y - Z*W or X*Y =:= Z*W instead.
```

A common mistake, for people used to procedural programming languages like C and Java, is to try to change the binding of a variable by using an goal like N is N + 1. This goal will never succeed, as it requires N to have the same value as N + 1, which is impossible. If you find yourself wanting to do something like this, you could look at the code for factorial in the article on tracing for inspiration.

Another common mistake is to try a goal involving is before the variable(s) on the right-hand side of the is has/have been instantiated. Prolog cannot evaluate an arithmetic expression if it doesn't know the values of variables in the expression. This is why the following example fails:

```
?- X is Y + 1, Y = 3.
```

ERROR: is/2: Arguments are not sufficiently instantiated Compare this with:

$$?- Y = 3$$
, X is Y + 1.
Y = 3,
X = 4.

lists

A list in Prolog is written as a comma-separated sequence of items, between square brackets. For example, [1, 2, 3] is a list.

The empty list is written [].

A list with just a single item, say the number 7, is written [7].

Frequently it is convenient to refer to a list by giving the first item, and a list consisting of the rest of the items. In this case, one writes the list as [First | Rest].

We have expressed this here using variables, but this need not be so, for example, we could write [1, 2, 3] as:

- [1 | [2, 3]]
- [1 | Rest], where Rest is bound to [2, 3]
- [First | [2, 3]], where First is bound to 1
- [First | Rest], where First is bound to 1, and Rest is bound to [2, 3]
- [1, 2 | [3]]
- [1, 2, 3 | []]

and many more possibilities.

You should always write your Prolog list in the most compact reasonable format. So for example, while $[X \mid []]$ is the same list as [X], the second version is much easier to read, so you should use it.

Lists can also be expressed using a normal term syntax, using the built-in predicate name . - that is, a full stop or period. In this case, the empty list atom ([]) must be used to terminate the list. However, this approach is more cumbersome, and in practice people use the [1,

2, 3]- style syntax. Example:

```
?- X = .(1, .(2, .(3, []))).
X = [1, 2, 3]
listing
```

The built-in meta-predicate listing can be used to check what is actually in the Prolog database during a Prolog session. It comes in two flavours: with no argument (listing/0) and with one argument

(listing/1). With no arguments, it causes the contents of the Prolog database to be printed out. With one argument - the name of a procedure - it prints out just the rules and/or facts relating to that procedure. Examples, assuming you have started Prolog with a program file that contains the facts and rules

In the case of listing/0, Prolog may also print out some internal house-keeping information.

member built-in predicate

This predicate takes a item and a list as arguments, and succeeds if the item is a member of the list:

```
?- member(a, [b, a, c]).
true.
?- member(X, [b, a, c]).
X = b:
X = a;
X = c:
false.
?- member(happy(fido), [angry(rex), happy(fido)]).
true.
?- member(a, [b, [a], c]).
false.
?- member([a], [b, [a], c]).
true.
?- member(a, Y).
Y = [a|_{G310}];
Y = [G309, a G313];
Y = [_{G309}, _{G312}, a|_{G316}];
Y = [G309, G312, G315, a | G319];
```

... and so on for as long as you press ";". The response to this last

query says that a is a member of an (uninstantiated) list Y if a is the first member or the second member or the third member or the fourth member or ...

The variables _G309, _G310, _G313, etc. represent bits of the list Y that we have no information about.

See also backtracking.

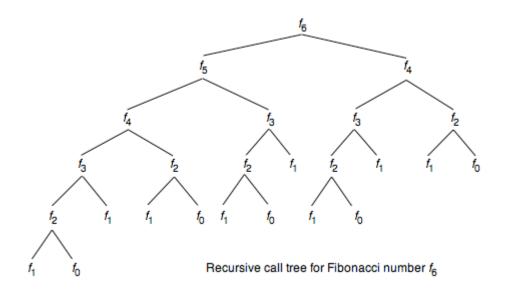
memoisation

Memoisation means storing a fact (e.g. using <u>asserta</u>), that has been inferred during the execution of your program, in the Prolog database, to avoid possibly having to infer the same fact again, later in the execution of the program.

Whether this is worth doing depends on the nature of the problem. If facts are regularly re-inferred (possibly as a consequence of a recursive solution), then memoisation could be a very good idea. Some algorithms perform double or multiple recursion (that is, they "recurse" on more than one variable), and both recursive branches can end up re-calculating the same thing, leading in some cases to exponential growth in the number of sub-cases as the size of the problem grows. The classic example is the recursive computation of the *n*-th Fibonacci number, which is (recursively) defined* by:

$$f_0 = f_1 = 1$$
, and,
for $n > 1$, $f_n = f_{n-2} + f_{n-1}$.

* Note that a non-recursive expression for f_n is also known - something we ignore here since this example is about recursion.



As can be seen (or rather, extrapolated) from the diagram, the number of calls grows exponentially, and the Fibonacci numbers rapidly become infeasible to calculate by the naive recursive program:

```
fib_naive(N, Result) :-
   N > 1,
   Nminus2 is N - 2,
   Nminus1 is N - 1,
   fib_naive(Nminus1, FibNminus2),
   fib_naive(Nminus1, FibNminus1),
   Result is FibNminus1 + FibNminus2.
```

However, by memoising, the computation becomes perfectly feasible for much larger values of n:

```
fib_{memo}(0, 1).
```

```
fib_memo(1, 1).
fib_memo(N, Result) :-
    N > 1,
    Nminus2 is N - 2,
    Nminus1 is N - 1,
    fib_memo(Nminus2, Fib2Nminus2),
    fib_memo(Nminus1, Fib2Nminus1),
    Result is Fib2Nminus1 + Fib2Nminus2,
    asserta((fib_memo(N, Result) :- !)).
```

Note the use of <u>asserta</u> to store the memoised value at the *start* of the collection of facts for fib_memo, so that it will be checked *before* trying the rule. Note also the <u>cut</u> (!) at the end of the assserta-ed rule, which stops the algorithm from backtracking and trying the rule after it has found a solution using the memoised value(s). This cut is *necessary*, as otherwise, while the first solution would be found fast, the code would repeatedly find the same solution a huge number of times, taking a huge amount of computing time.

See also assert, dynamic.

More?

The usual response to a Prolog query that does not have variables in it, or which only has underscores in it is true. or false. However, in some versions of Prolog, including recent versions of SWI-Prolog (e.g. version 5.6.47) another possible response can occur: More? This means (1) true. and (2) that there are other alternatives for Prolog to explore, that *might* allow it to conclude true. in a different way. I.e. Prolog may be able to prove that your query is true in more than one way. For example, suppose that <code>likes(jane, pizza)</code> is in your Prolog program as a fact, but can also be inferred using a rule and some other facts.

```
?- likes(jane, pizza).
More?
```

The More? is a prompt to allow you to find out if this is so - i.e. that the query can be proven in more than one way. Type a semicolon if you want Prolog to go ahead and look for a different proof. Type return if you are happy with a single proof.

If you want to suppress this behaviour, you can insert <u>cuts</u> to prevent the backtracking that is finding the extra (possible) proofs, or you can, in SWI-Prolog, use this query:

```
set_prolog_flag(prompt_alternatives_on, groundness). or alternatively, put the following directive in your Prolog source code:
```

```
:- set_prolog_flag(prompt_alternatives_on, groundness).
```

You may also be able to avoid responses of More? in some cases by re-ordering relevant <u>clauses</u> in your program.

Here's some example code to demonstrate More? :

```
happy(fido).
happy(rex).
happy(Dog) :- is_dog(Dog), walkies(Dog).
happy(Dog) :- is_dog(Dog), chase_car(Dog).
is_dog(fido).
is_dog(rex).
walkies(fido).
walkies(rex).
chase_car(fido).
```

There are three ways to prove fido is happy: from the fact, and from each of the two rules. So:

Prolog Dialogue

Commentary

```
?- happy(fido).
More?; happy(fido) proven using fact
More?; happy(fido) proven using "walkies" rule
true. happy(fido) proven using "chase_car" rule
?- happy(rex).
More; happy(rex) proven using fact
More; happy(rex) proven using "walkies" rule
false. happy(rex) not provable using "chase_car" rule
```

mutual recursion

Sometimes a <u>procedure</u> does not explicitly refer to itself (this would be (simple) <u>recursion</u>), but rather refers to a second procedure which in turn refers to the first. This sets up a two-step *mutual recursion*. Three- or more- step mutual recursion situations can also occur. The usual conditions applicable to recursion must occur - there must be a "trivial branch" somewhere in the cycle of mutually recursive procedures, and somewhere in the cycle something must happen to ensure that, each time around the cycle, a simpler version of the problem is being solved.

neck

the symbol :-, used in a Prolog <u>rule</u> to separate the <u>head</u> from the <u>body</u>. Usually read as *if*. Thus

a :- b, c.

is read as

a (is true) if b and c (are true).

negation, not, \+

The concept of logical negation in Prolog is problematical, in the sense that the only method that Prolog can use to tell if a proposition is false is to try to prove it (from the facts and rules that it has been told about), and then if this attempt fails, it concludes that the proposition is false. This is referred to as *negation as failure*. An obvious problem is that Prolog may not have been told some critical fact or rule, so that it will not be able to prove the proposition. In such a case, the falsity of the proposition is only relative to the "mini-world-model" defined by the facts and rules known to the Prolog interpreter. This is sometimes referred to as the *closed-world assumption*.

A less obvious problem is that, depending again on the rules and facts known to the Prolog interpreter, it may take a very long time to determine that the proposition cannot be proven. In certain cases, it might "take" infinite time.

Because of the problems of negation-as-failure, negation in Prolog is represented in modern Prolog interpreters using the symbol \+, which is supposed to be a mnemonic for *not provable* with the \ standing

for *not* and the + for *provable*. In practice, current Prolog interpreters tend to support the older operator not as well, as it is present in lots of older Prolog code, which would break if not were not available.

Examples:

true.

```
?- \+ (2 = 4).

true.

?- not(2 = 4).
```

Arithmetic comparison operators in Prolog each come equipped with a negation which does not have a "negation as failure" problem, because it is always possible to determine, for example, if two numbers are equal, though there may be approximation issues if the comparison is between fractional (floating-point) numbers. So it is probably best to use the arithmetic <u>comparison operators</u> if numeric quantities are being compared. Thus, a better way to do the comparisons shown above would be:

```
?- 2 =\= 4.
```

true.

number, number(-)

Numbers in Prolog can be whole numbers, like:

1 1313 0 -97 9311

or fractional numbers, like:

3.14 -0.0035 100.2

The range of numbers that can be used is likely to be dependent on the number of bits (amount of computer memory) used to represent the number. The treatment of real numbers in Prolog is likely to vary from implementation to implementation - real numbers are not all that heavily used in Prolog programs, as the emphasis in Prolog is on symbol manipulation. number is also the name of a built-in predicate which tests its single argument and succeeds if that argument is a number. *Examples*:

```
?- number(2.1).
true.
?- number(-8).
true.
?- X = 7, number(X).
X = 7.
?- number(1+1).
false.
```

The last query fails because 1+1 is an unevaluated expression, not a number. See <u>is</u>, for more on evaluation.

The built-in Prolog extra-logical predicate once takes a single argument, which must be a "callable term" - one that makes sense as a goal - e.g.happy (X) makes sense as a goal, but 23 does not - and calls the term in such a way as to produces just one solution. It is defined as:

```
once (P) := P, !.
```

See also !, call, backtracking.

op, infix, prefix, and postfix operators, precedence in Prolog Syntax:

```
:- op(+Precedence, +Type, :Name).
```

The Prolog built-in predicate op serves to define the Type and Precedence of infix and postfix, and prefix operators in Prolog terms. Prolog terms normally begin with the <u>functor</u> (e.g. likes,

in likes (mary, pizza)) but exceptions exist - for example, arithmetic expressions are written in the usual infix way (i.e. as X + 1, rather

than +(X, 1), and negation can be written without parentheses, as a prefix operator: not P.

The table below lists the predefined infix operators in SWI-Prolog. You may wish to add infix operators of your own. For example, you might wish to define an infix and. This can be done as follows:

```
:- op (700, xfy, and).
```

This declares and to be an operator with precedence 700 and type xfy.

Note two things: (1) the fact that these things are referred two as operators does *not* mean that an operation is performed when they are encountered. This is not usually the case; and (2) the declaration of an operator only affects the external appearance of the operator in your program - internally, the standard representation is used - for example X + 1 really is internally represented by Prolog as +(X, 1).

Precedence is an integer between 0 and 1200. Precedence 0 removes the declaration. Type is one of: xf, yf, xfx, xfy, yfx, yfy, fy or fx.

The findicates the position of the functor, while x and y indicate the position of the arguments. Thus xfx, xfy, and yfx all indicate an infix operator.y should be interpreted as "in this position a term with precedence equal to or less than the precedence of the functor should occur". For x the precedence of the argument must be strictly less than that of the functor. The precedence of a term is 0, unless its principal functor is an operator, in which case the precedence is the precedence of this operator. A term enclosed in brackets (...) has precedence 0.

To see how this works, consider the arithmetic expression a-b-c. In normal maths, this is interpreted as (a-b)-c, rather than a-(b-c).

To achieve this, the binary infix operator – must be declared as type yfx so that the first argument has precedence over the second.

Then, internally, a - b - c will be represented as -(-(a, b), c) rather than -(a, -(b, c)).

Built-in Operators (SWI-Prolog)

```
Prec. Type Operator
```

```
1200
      xfx \longrightarrow : -
      fx :-, ?-
1200
            dynamic, discontiguous, initialization,
1150
      fx
            module_transparent, multifile, thread_local, volatile
1100
      xfy
            ;,
      xfy \rightarrow, op*\rightarrow
1050
      xfy ,
1000
954
      xfy
900
      fy
            \+
900
      fx
            <, =, =.., =@=, =:=, =<, ==, =\=, >, >=, @<, @=<, @>,
700
            @>=, \=, \==, is
600
      xfy
      yfx +, -, /\, \/, xor
500
500
      fx +, -, ?, \setminus
400
      yfx *, /, //, rdiv, \langle \langle , \rangle \rangle, mod, rem
200
      xfx **
200
      xfy
```

Note that all operators can be redefined by the user, most commonly accidentally and with disastrous results.

or, logical disjunction, ;

The logical <u>conjunction</u> (logical-and, \wedge) of <u>goals</u> is achieved in Prolog by separating the goals by commas:

```
happy(X) := rich(X), famous(X).
```

says that X is happy if X is rich and X is famous. What about logical-or,

 \vee , also called <u>disjunction</u>? If we want to say

that X is happy if X isrich **or** if X is famous, we have two possibilities:

- 1. use two alternative rules
- 2. use the ; operator (pronounced "or").

Option 1:

```
happy1(X) :- rich(X).
happy1(X) :- famous(X).
```

Option 2:

```
happy2(X) := rich(X) ; famous(X).
```

Sometimes it is necessary, or at least advisable, to wrap parentheses () around a disjunction in order to make clear what how the conjunctions and disjunctions interact. If you leave out the parentheses, Prolog has its own rules about the <u>precedence</u> of logical-and and logical-or, which might or might not correspond to what you intend. If you use parentheses, the things inside the parentheses are done first, so everything is crystal clear.

Option 3:

```
happy3(X) :- attractive(X), ( rich(X) ; famous(X) ).
```

This says X is happy3 if X is attractive, and X is either rich or famous:

```
happy3(X) \Leftarrow attractive(X) \land (rich(X) \lor famous(X)).*
```

* The Prolog Dictionary wishes to acknowledge that a range of world religions and philosophies would not agree that the criteria specified for happy1, happy2, and happy3 are either necessary nor sufficient for happiness. The definitions given in this article, are, therefore, purely intended as Prolog programming examples, and should not be taken as a practical guide to life. Thank you.

output in Prolog

Output in Prolog is not always needed, as often the <u>variable bindings</u> return all the information that is required. If explicit output is required, a set of extra-logical built-in predicates is available.

These include:

- write(X) which writes the <u>term</u> X to the current output stream (which means the window on your workstation unless you have done something<u>fancy</u>).
- print (X, ···) which writes a variable number of arguments to the current output stream. If an argument is a string (like 'Hello world!\n') then the string is printed without quotes, and any '\n' and '\t' are interpreted as newline and tab, respectively. A newline is printed at the end of the printing operation.
- prin(X, ···) is like print except that it does not append a
 newline to the end of the output.
- tab (N) prints N spaces to output N should be a number.
- nl starts a new line.
- put (C) prints a single character to the current output stream. C might be bound to a number in the range 0 to 255, in which case the number is treated as a character code, and the equivalent character is printed, or it might be bound to a character, e.g. C = 'a', in which case obviously the character is printed.

predicate

Used to refer to the functionality afforded by a Prolog <u>procedure</u>. In this dictionary, we tend to talk about procedures when the code is

written by the programmer, but predicates when the functionality is built-in, as with member.

procedure

A procedure in Prolog is a group of <u>clauses</u> about the same <u>relation</u>, for example:

```
is_a_parent(Parent) :- father_of(Parent, _Child).
is_a_parent(Parent) :- mother_of(Parent, _Child).
```

Here, two clauses together define the condition for someone to be a parent - together they form a procedure.

See also <u>underscore</u> for the reason for putting an underscore (_) character at the front of the <u>variable_Child.</u>

query

A query is a list of one or more <u>goals</u> typed to the Prolog interpreter's ?- prompt, separated by commas, and terminated with a full stop (.). For example,

?- *lectures* (*john*, *Subject*), *studies* (*Student*, *Subject*). is a query comprising two goals. Prolog tries to satisfy the goals, and if it manages to do this, the query is said to <u>succeed</u>. If not, the query fails.

If the query fails, Prolog types "false.". If it succeeds, Prolog either types the list of <u>variable bindings</u> it had to assume in order to make the query succeed, or, if no variable bindings were necessary, it types "true.".

If several variable bindings allow the query to succeed, then normally (i.e. in the absence of <u>cuts</u>) all the bindings will be typed out, one after the other, with the Prolog user typing a; to let the Prolog system know that they are ready to see the next set of bindings.

recursion

A recursive <u>rule</u> is one which refers to itself. That is, its <u>body</u> includes a <u>goal</u> which is an instance of the relation that appears in the <u>head</u>of the rule. A well-known example is the <u>member procedure</u>:

```
member(Item, [Item|Rest]).
member(Item, [ |Rest]) :- member(Item, Rest).
```

The second <u>clause</u> is clearly recursive - member occurs both in the head and the body. A recursive procedure can work because of two things:

- 1. the instance of the relation (like member) in the body is in some way simpler than that in the head, so that Prolog is being asked to solve a simpler problem. (In member, the list that is the argument to member in the body is shorter by one than that in the head.)
- 2. there must be a "trivial branch" "base case" or "boundary case" to the recursion that is, a clause that does *not* involve recursion. (In the case of member, the first clause is the trivial branch it says that member succeeds if I tem is the first member of the list that is the second argument.)

A recursive **data structure** is one where the <u>structures</u> include substructures whose principle <u>functor</u> is the same as that of the whole structure. For example, the tree structure: tree(tree(empty, fred, empty), john, tree(empty, mary, empty)) is recursive. Recursive data structures require recursive procedures to process them.

It can help, in understanding recursion, to separate the different depths of recursive invocation of Prolog rules by drawing boxes around the parts that correspond to a particular invocation, and giving separate (but systematic) names to the variables in each invocation. So if the rule involves a variable X, then in the first invocation, we refer to X as X1, while in the second (recursive) invocation, we refer to the new X as X2, and so on.

Let's try this out with the recursive procedure sumlist. In each recursive call of sumlist, there is a separate instance of the

variables First, Rest, Sum, and SumOfRest, and these are distinguished by subscripts - so First₁ is the instance of First in the top-level call of sumlist, and First₂ is the instance of First in the first recursive call to sumlist.

% sumlist(NumList, SumOfList) - binds SumOfList to the sum

```
% of the list NumList of numbers.
% Rule 1:
sumlist([], 0).
% Rule 2:
sumlist([First | Rest], Sum) :-
   sumlist (Rest, SumOfRest), % Goal 2.1
   Sum is First + SumOfRest. % Goal 2.2
and the query
?- sumlist([5, 2, 1], Answer).
sumlist[5, 2, 1], Answer).
Choose Rule: only rule 2 matches, with
First_1 = 5; Rest_1 = [2, 1]; Sum_1 = Answer
Goal 2.1: sumlist(Rest<sub>1</sub>, SumOfRest<sub>1</sub>),
         sumlist([2, 1], SumOfRest1),
         Choose Rule: only rule 2 matches, with
         First_2 = 2; Rest_2 = [1]; Sum_2 = SumOfRest_1
         Goal 2.1: sumlist(Rest<sub>2</sub>, SumOfRest<sub>2</sub>),
                  sumlist([1], SumOfRest<sub>2</sub>),
                  Choose Rule: only rule 2 matches, with
                  First_3 = 1; Rest_3 = []; Sum_3 = SumOfRest_2
                  Goal 2.1: sumlist(Rest<sub>3</sub>, SumOfRest<sub>3</sub>),
                           sumlist([], SumOfRest<sub>3</sub>),
                           Choose Rule: only rule 1 matches, with
                           0 = SumOfRest<sub>3</sub>
                           \therefore SumOfRest<sub>3</sub> = 0
                  Goal 2.2: Sum<sub>3</sub> is First<sub>3</sub> + SumOfRest<sub>3</sub>.
                  = 1 + 0
                  = 1
                  \therefore SumOfRest<sub>2</sub> = Sum<sub>3</sub> = 1
         Goal 2.2: Sum<sub>2</sub> is First<sub>2</sub> + SumOfRest<sub>2</sub>.
         = 2 + 1
         = 3
```

```
Goal 2.2: Sum₁ is First₁ + SumOfRest₁.

= 5 + 3

= 8

∴ Answer = Sum₁ = 8
```

Try doing a Prolog $\underline{\text{trace}}$ of the same query and procedure, and compare the results.

Here are some tips on <u>writing recursive procedures in Prolog</u>..

See also mutual recursion.

relation

The word *relation*, in Prolog, has its usual mathematical meaning. See <u>relations</u> and <u>functions</u> if you are not sure about what this is. A *unary*relation is a set of objects all sharing some property. Example:

```
is_dog(fido).
is_dog(rex).
is_dog(rover).
```

A *binary* relation is a set of pairs all of which are related in the same way. Example:

```
eats(fido, biscuits).
eats(rex, chocolate).
eats(rover, cheese).
eats(lassie, bone).
```

Similarly for *ternary* relations (triples) and so on. In the examples above, is_dog and eats are the <u>functors</u> for the relations. Prolog stores information in the form of relations, or more specifically relational instances, like those above, and also in the form of rules.

It is also possible in Prolog to have *nullary* relations (a relation with no arguments), though they are perhaps not often used. Example:

```
program_untested.
```

This could be used as a goal in a query:

```
?- program_untested.
```

Possibly a better way to do this would be to use a unary relation:

```
program status (untested).
```

However, the point is that nullary relations are there in Prolog, should you find a use for them.

See also the the next entry for more detail.

relations and functions in mathematics and in Prolog (If you are looking for the Prolog implementation of mathematical functions like sin, cos, sqrt, log, exp, etc., look under <u>built-in</u> <u>functions</u>.)

A *binary* relation, in mathematics, is a set of ordered pairs. For example, if we are thinking about the 3 animals: *mouse*, *rabbit*, and *sheep*, and the "smaller" relation, then the set of pairs would be {(*mouse*, *rabbit*), (*mouse*, *sheep*), (*rabbit*, *sheep*)}. In mathematical

notation, you would write, e.g., (mouse, rabbit) \subseteq smaller, or mouse smaller rabbit. Or you might use a symbol instead of smaller, perhaps "<" - mouse < rabbit, or σ - mouse σ rabbit. This is referred to as an *infix* notation, because the name of the relation is written in-between the two objects (mouse and rabbit).

In Prolog, instead, by default we use prefix notation: smaller (mouse,

rabbit). See op if you want to define an infix operator in a Prolog program.

This view of a relation is sometimes called the *extensional* view - you can lay out the full "extent" of the relation, at least in the case of a relation over a finite number of items, like our "smaller" example. The alternative view is called *intensional*, where we focus on the meaning of the relation. In Prolog, this corresponds to a rule expressing the relation, such as:

```
smaller(X, Y) :-
   volume(X, XVolume),
   volume(Y, YVolume),
   XVolume < YVolume.</pre>
```

This, of course, only defines a meaning or intension for smaller relative to the unspecified meaning of the

relation volume (_, _), and the meaning of<, which is defined by the Prolog implementation.

When we come to non-binary relations, such as unary ones (like is_a_dog(fido)) or ternary ones (like gives(john, mary, book) or between(rock, john, hard_place)) the infix relation doesn't make any sense, so prefix notation is normal. (Postfix notation - fido is_a_dog can work for unary relations.)

While we often don't think of it this way, a *function* is a kind of relation. If you are thinking about the function $f(x) = x^2$, then the essential thing is that for each value of x, there is a value of f(x) (namely x^2). In fact, there is a *unique* value of f(x). So a function (of a single variable) can be viewed as a binary relation such that for every relevant first component x, there is exactly one pair in the relation that has that first component*: the pair is (x, f(x)). In the case of $f(x) = x^2$, the pairs are (x, x^2) for every applicable value of x. We need to specify what the applicable values of x are - the *domain* of the function. If the domain is $\{1, 2, 3\}$, then the pairs are $\{(1,1), (2,4), (3,9)\}$. If the domain is all natural numbers, then we can't write out the extension of the function in full, but we can use a set expression such as $\{(n, n \times n) \mid n \in N\}$ where N signifies the set of all natural numbers.

In Prolog, despite the fact that it uses a relational notation (except for arithmetic expressions), functions are common, but expressed using the relational notation that depends on the definition/convention in the previous paragraph. In our Prolog code defining smaller (X, Y), above, the relation called volume is in fact a function written relationally. We are saying that for every relevant object X there is a value XVolume that is the volume of X. This is a function-type relationship.

The notion of domain applies to relations as well as functions: a more detailed definition of a binary relation *on a set A* says that such a

relation is a subset of the set $A \times A$ of all pairs of elements of A. A is the *domain* of the relation. A binary relation between sets A and B is a subset of $A \times B$. And so on for ternary relations and beyond. A unary relation on A is just a subset of A. Thus is_a_dog is a subset of the set of all Animals. Or a subset of the set of all Things, depending on just how broadly you want to consider the concept of being a dog.

However, in Prolog, domains of relations are not explicitly addressed.* The notion of domain corresponds exactly to that of *type* in typed programming languages like, C, C++, Java, Haskell, etc. Prolog has no built-in way of confining the definition of a relation (whether extensionally or by a rule) to a particular domain. If you want to, you can build type-checking into your rules, e.g. by giving an definition of a type as a unary relation. For example, if you wanted to define the type of all popes, you could enumerate them all, though the list would be long:

```
pope(peter).
...
pope(john_paul_ii).
pope(benedict xvi).
```

Then the goal pope (X) would check if X was/is a pope.

Another example: when defining the relation sister in Prolog, you would usually write something like:

```
sister(Person1, Person2) :-
  female(Person1), female(Person2),
  mother(Person1, Mother), mother(Person2, Mother),
  father(Person1, Father), father(Person2, Father),
  Person1 \== Person2.
```

female (Person1) and female (Person2) are type-checks - without them,

you are defining sibling, not sister. In practice, you can't enumerate all females, unlike all popes, but in many cases you would be able to enumerate all the relevant ones.

In some cases, you might be able to write rules to do type-checking. Prolog includes some built-in predicates for

type-checking: number (X) succeeds if X is a number,

while integer (X) succeeds only if X is a an integral (whole) number. Here is a rule to check if a number is divisible by 3.

```
div_by_3(X) :-
X mod 3 =:= 0.
```

beats (rock, scissors).

There is no special syntax for creating functions in Prolog (though there are special arrangements for <u>built-in mathematical functions</u>). To create a function in Prolog, you have to use the relation syntax and create a "relation that happens to be a function". You can do this extensionally, as in

```
beats(paper, rock).
beats(scissors, paper).
or intensionally, with a rule, as with the function f(x) = x², which
could be coded in Prolog like this (using the name square_of):
square_of(X, XSquared) :-
   number(X),
   XSquared is X * X.
used as in the next examples:
?- square_of(3.2, Y).
Y = 10.24
```

The number (X) test implicitly limits the domain of the function to numbers.

Note that while we defined square_of with a functional usage in mind, it can still be used in a relational sense if desired:

```
?- square_of(3, 9). true.
```

Footnotes:

* if there is, not *exactly*, but *at most* one pair in the relation that has x as its first member, we say that the relation is a *partial function*. A partial function is like a function that has "holes" in it - f(x) never has more than one value, but for some x in the domain of the function, f(x) might not have any value. A real-life example is the partial function *eldest_child_of*, defined on the domain of all adult humans.

there are a couple of areas of Prolog where there is some built-in type-checking - for example, the built-in predicate < will generate an error message if you try to use it compare a string like 'mouse' with a number like 9.

repeat

The built-in predicate repeat behaves as if defined by:

```
repeat.
repeat :- repeat.
```

Thus repeat succeeds when first called, thanks to the first clause. If the Prolog interpreter subsequently backtracks, the second clause (repeat :- repeat.) is tried. This initiates a new call to repeat, which succeeds via the first clause, and so on.

For a practical example of a use of repeat, see here.

retract, retractall

retract is a built-in meta-predicate used to remove facts or rules from the Prolog database while a program is executing. It is most often used in partnership with <u>assert</u> (or one of its relatives). For example, your program might have hypothesised that some fact or rule is correct, added it to the Prolog database using <u>assert</u> (or one of its relatives), then your program explores the consequences of that assumption, and concludes that the fact or rule was wrong. So then the program retracts the fact or rule.

More prosaically, you might simply have a query that runs repeatedly during a single prolog session, discovers some new facts in each run, but needs to get rid of them at the start of the next query. So again, retract can be used to clean the discovered facts out of the database.

```
?- assert(likes(mary, pizza)).
true.
?- likes(mary, pizza).
true.
?- retract(likes(mary, pizza)).
true.
?- likes(mary, pizza).
false.
?- assert((happy(X) :- rich(X), famous(X))).
X = _G180
true.
?- retract((happy(X) :- rich(X), famous(X))).
X = _G180
true.
```

Don't worry about the X = _G180, that's just SWI Prolog renaming the variable X with a unique name so it doesn't get confused with the (different) variable X that you might have used in some other rule.

Note also the extra pair of parentheses () around the rule, as opposed to the fact.

What a call to retract actually does is to remove the *first* fact or rule that matches the argument to retract. If you want to remove, say, all the facts relating to likes with two arguments, it looks as though you might have to call retract repeatedly. Never fear, retractall is here! This meta-predicate, as its name suggests, retracts *all* facts or rules that match its single argument. For example:

```
?- assert(likes(mary, pizza)), assert(likes(john, beer)).
true.
?- listing(likes).
:- dynamic likes/2.
likes(mary, pizza).
likes(john, beer).
```

The ":- dynamic/2" tells us that likes/2 is a built-in predicate that can be modified during program execution (see $\underline{dynamic}$). This is to stop the program modifying unauthorised parts of itself, and becoming totally un-debuggable. Example continues:

```
?- retractall(likes(X, Y)).
X = _G180
Y = _G181
?- listing(likes).
:- dynamic likes/2.
true.
```

See also <u>assert</u>. Programs that use retract and retractall may be particularly difficult to debug.

Tip: In some versions of Prolog, retractall may fail if there is nothing to retract. This may seem reasonable (though it is probably a bug in the particular implementation) but can get in the way of a "prophylactic" retractall call to make sure there are no left-over facts/rules lying around from earlier computations. To get around this, assert a dummy fact of the right type

(something assert(likes(dummy, dummy)), assuming likes/2 is what you are trying to get rid of), before you call retractall. SWI Prolog does in fact succeed on a retractall call with no matching facts/rules.

rule

A rule in Prolog is a <u>clause</u>, normally with one or more <u>variables</u> in it. Normally, rules have a <u>head</u>, <u>neck</u> and <u>body</u>, as in: eats (Person, Thing) :- likes (Person, Thing), food (Thing).

This says that a Person eats a Thing if the Person likes the Thing, and the Thing is food. Note that Prolog has no notion of the meanings of eats, Person, Thing, likes, and food, so for Prolog the rule is simply abstract symbol manipulation. However, presumably the author of the rule intended to have the meaning stated above. It would be possible

```
to write the rule as e(P, T) := 1(P, T), f(T). or even xx(X1, X2) :=
```

xxx (X1, X2), xxxx (X2). Obviously the rule is much more readable if meaningful procedure names and variable names are used.

Sometimes, in a "rule", the body may be empty:

```
member(Item, [Item|Rest]).
```

This says that the Item is a member of any list (the second argument) of which it is the *first* member. Here, no special condition needs to be satisfied to make the head true - it is always true.

Such rules can be re-expressed so that they have a body - e.g.

```
member(Item, [Head | Rest]) :- Head = Item.
```

This forces Prolog to perform another step (checking that Head = Item) so it is deprecated.

Sometimes in a rule, there might be no variables, or none in the head of the rule:

```
start_system :-
   initialise,
   invoke_system,
   finalise.
```

Such rules tend to have a very procedural style, effectively specifying a sequence of steps that need to be done in sequence. It's a look that is best avoided, or at least minimised.

See also <u>fact</u>.

setof

The built-in Prolog predicate setof (+Template, +Goal,

-Set) binds Set to the list of all instances of Template satisfying the goal Goal.

For example, given the facts and rule:

```
happy(fido).
happy(harry).
happy(X) :- rich(X).
rich(harry).

it follows that

?- setof(Y, happy(Y), Set).
Y = _G180
Set = [fido, harry];
false.
```

Notice that:

- there are two ways to prove that harry is happy
 - o from the fact happy (harry).
 - o from the rule and the fact rich (harry).

However, harry only appears once in the binding for Set;

• the binding for Set is in sorted order.

Compare:

```
?- bagof(Y, happy(Y), Bag).
Y = _G180
Bag = [fido, harry, harry];
false.
and
?- findall(Y, happy(Y), Bag).
Y = _G180
Bag = [fido, harry, harry];
false.
```

The differences between bagof and findall on the one hand, and setof on the other hand, include the fact that with setof, you get sorted order and no repetitions. (For differences between bagof and findall, see findall.)

set of will fail (and so not bind Set) if the there are no instances of Template for which Goal succeeds - i.e. effectively it fails

if Set would be empty. bagof also fails in these circumstances,

while findall does not (it binds the variable that is its third argument to the empty list, or, if the third argument is instantiated, it succeeds if the third argument is the empty list).

side-effects

Prolog is supposedly a <u>declarative</u> language - that is, one which specifies relationships between concepts using <u>facts</u> and <u>rules</u> and then uses a logic engine to answer queries that relate to those facts and rules, typically by finding <u>bindings</u> for variables that allow queries to succeed.

However, in "real" Prolog, there are <u>built-in predicates</u> that do no comform to this pattern. These include input-output "predicates"

like see, seeing, seen, tell, telling, told, write, nl, prin, print, put,

and <u>read</u>, <u>get</u>, <u>get</u> <u>byte</u>, <u>flush</u> <u>output</u>. All of these predicates succeed or fail independent of any logical aspect of the problem being solved - normally, in fact, they will succeed unless there is an error relating to the external input/output system - e.g. it may not be possible to read from a file because the user does not have permission to access the file, or because the file does not exist.

Even more extra-logical

are <u>assert</u>, <u>assertz</u> and <u>retract</u>, <u>retractall</u>, which even change the program that is running.

Side-effects take Prolog programs out of the world of strict logic (as does the <u>cut</u>, which changes the way the inference engine operates in solving a query). Programs with side-effects are harder to analyse that programs without side-effects. The practical impact of side-effects on the understandabilty of Prolog programs depends on how they are used. For example, using <u>memoisation</u> to record facts inferred in order to save re-calculation is probably harmless, but using <u>assert</u> to create new rules might in some cases make <u>debugging</u> a program next to impossible. Use side-effects with care.

singleton variables

SWI Prolog sometimes produces an warning message like this:

```
% cat example.pl
happy(Pet) :-
   dog(Pet),
   walkies(Oet).
% prolog -s example.pl
Warning: example.pl:1:
   Singleton variables: [Oet]
```

This is alerting you to the fact that the variable 0et has only been used once in the rule it appears in. Such variables are often (but not always) spelling mistakes. In this case, 0et should have been Pet.

Sometimes singleton variable reports are caused by the programmer trying to write helpful, readable code, like this version of member:

```
member(Item, [Item | Rest]).
member(Item, [NotItem | Rest]) :-
    \[ \+ Item = NotItem,
    member(Item, Rest).

Prolog would report
    Singleton variables: [Rest]
for such code, because the helpfully-named variable Rest is only used
once in member(Item, [Item | Rest]). The solution is to put an
underscore(_) at the start of this instance of Rest, thus
replacing member(Item, [Item | Rest]). with member(Item, [Item |
    _Rest]). SWI Prolog will treat _Rest as adon't-care variable and not
report it.
spy
```

The built-in pseudo-predicate spy allows one to trace the execution of a query in a selective manner. If you want to find out about each time that a particular predicate is called, you spy that predicate: see example below.

```
?- listing (happy).
```

As you can see, the call to rich is traced, but not much else. See also <u>trace</u>, which traces the execution of everything.

Turn spying off with nospy:

```
[debug] ?- nospy(rich).
% Spy point removed from rich/1
```

true. **static**

A Prolog procedure is static if its facts/rules do not change during the execution of the program of which they are part. This is the default: most Prolog procedures are static. The opposite of static is <u>dynamic</u>. **structures**

Structures in Prolog are simply objects that have several components, but are treated as a single object. Suppose that we wish to represent a date in Prolog - dates are usually expressed using a day, a month, and a year, but viewed as a single object. To combine the components

into a single structure, we choose a functor, say date, and use it to

group the components together - for the date usually expressed as 21 March 2004, we would probably write

```
date(21, mar, 2004)
```

Note that the order of the components is our choice - we might have instead written date (2004, mar, 21) The choice of functor is arbitrary, too.

The components between the parentheses are referred to as **arguments**. Thus in the date example, the arguments are 21, mar, and 2004.

Structures may be nested, too - the following example groups a name and a date, perhaps the person's date of birth:

```
persondata (name (smith, john), date (28, feb, 1963))

This term has two arguments, the first being name (smith, john) and the second being date (28, feb, 1963)
```

See also Bratko, section 2.1.3.

succeed

A Prolog goal succeeds if it is possible to either check it directly against the facts known to Prolog, or find bindings for variables in the goal that makes the goal true.

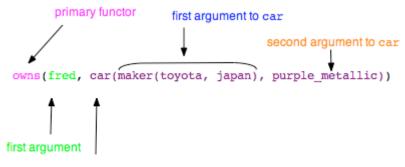
A <u>query</u> succeeds if each of its goals succeeds.

term

Syntactically, all data objects in Prolog are terms. For example, the <u>atom</u> mar and date and the <u>structure</u> date (2004, mar, 21) are terms.

So are the numbers 2004 and 21, for that matter. So in date (2004, mar, 21), the primary functor is date, the arity is 3, and the arguments are 2004, mar, and 21.

In general, a term of <u>arity</u> n can be an <u>atom</u> (the <u>functor</u>) followed by n **arguments**, which will be enclosed in parentheses () and separated by commas. Note that the arity might be 0, in which case there are no parentheses, commas, or arguments. A term can also be a number. Sometimes the term can use an <u>infix</u> operator like \langle , in which case the functor appears between the arguments (if the arity is 2) or before the argument but without parentheses (if the arity is 1).



second argument is itself a term of arity 2

For + and - (and occasionally ?) signs in front of arguments, in procedure header comments, see <u>comments</u>.

term type

testing, atom, atomic, compound, float, integer, nonvar, number, var

It may be useful to be able to test if a term is an number or a variable or something else. Prolog provides several such tests:

Goal	succeeds if X is …	
var(X)	an uninstantiated variable	
nonvar(X)	not a variable, or is an instantiated variable	
compound(X)	a compound term - not an unbound variable, and not atomic (see below)	
atom(X)	an atom, or bound to an atom	
integer(X)	an integer, or bound to an integer	
float(X)	a floating point (fractional) number such as 3.5 or 1.0, or bound to one - but, if float(X) is evaluated using \underline{is} , then you get $this\underline{float}$	
number(X)	a number, or bound to a number (integer or float)	
atomic(X)	a number, string, or atom, or bound to one	

testing your code

Here are some tips on testing your Prolog code.

And here are some tips on <u>writing recursive procedures in Prolog</u> that include some tips on debugging (in example 3).

tracing

Tracing the execution of a Prolog query allows you to see all of the goals that are executed as part of the query, in sequence, along with

whether or not they succeed. Tracing also allows you to see what steps occur as Prolog backtracks.

To turn on tracing in Prolog, execute the "goal"

?- trace.

true.

When you are finished with tracing, turn it off using the "goal"

?- notrace.

Here is an example of trace in action. First some code, which computes factorial N - the product of the numbers from 1 to N. By convention, factorial 0 is 1. Factorial N is often written N!, where the exclamation mark signifies the "factorial operator". Here is the code:

```
rule 1
                                  rule 2
factorial (0, 1).
                                           factorial(0) = 1
                                  rule 2,
factorial(N, NFact) :-
                                  goal 1
        N > 0,
                                           if N > 0, then
                                  rule 2,
                                           compute N - 1,
        Nminus1 is N-1,
                                  goal 2
        factorial (Nminus1,
                                           recursively work out
                                  rule 2,
                                           factorial (N-1),
Nminus1Fact),
                                  goal 3
        NFact is Nminus1Fact * N.
                                           then multiply that by N
                                  rule 2,
                                  goal 4
```

The tables above and below may not display correctly if viewed in a narrow window. If the commentary doesn't seem to line up correctly with the text to the left of it, try making your browser window wider.

Prolog dialog/trace output	Commentary
prolog -s factorial.pl	Invoke prolog, loading code for
blah blah blah …	factorial
?- trace.	Greeting from Prolog
true.	Turn on tracing
[trace] ?- factorial(3,	
X).	Call factorial
Call: (7) factorial(3,	Trace echoes query, replacing X with a
_G284) ? creep*	unique variable
^ Call: (8) 3>0 ? creep	Rule 2, Goal 1 (N $>$ 0) is invoked
Exit: (8) 3>0 ? creep	Goal 1 succeeds immediately

```
Call: (8) L205 is 3-1? Rule 2, Goal 2 invoked to compute 3 -
creep
  Exit: (8) 2 is 3-1?
                           and succeeds
                           Rule 2, Goal 3 is invoked: level 2 call
  Call: (8) factorial (2,
                           to factorial(2, ···)
L206) ? creep
                           Goal 1 again for new call to factorial
  Call: (9) 2>0 ? creep
                           Goal 1 succeeds
  Exit: (9) 2>0 ? creep
                           New version of goal 2
  Call: (9) L224 is 2-1? succeeds
                           Rule 2, Goal 3 is invoked: level 3 call
  Exit: (9) 1 is 2-1?
                           to factorial(1, ···)
                           Goal 1 again
  Call: (9) factorial(1,
                           succeeds
L225) ? creep
                           Goal 2 again
  Call: (10) 1>0 ? creep successfully
  Exit: (10) 1>0 ? creep
                           Rule 2, Goal 3 is invoked: recursive
  Call: (10) _L243 is 1-1? |call to factorial(0, ...)
                           This time, Rule 1 succeeds at once.
creep
  Exit: (10) 0 is 1-1?
                           This is Goal 4 of level 3
                           Compute 1 * 1 without trouble
creep
  Call: (10) factorial (0, so the level 3 factorial call succeeds
L244) ? creep
                           This is goal 4 of level 2
  Exit: (10) factorial (0, Compute 1 * 2 without trouble
1) ? creep
                           so the level 2 factorial call succeeds
  Call: (10) _L225 is 1*1? This is goal 4 of level 1
                           Compute 2 * 3 without trouble
  Exit: (10) 1 is 1*1?
                           so the level 1 factorial call succeeds
                          ••• with this binding of X - type ";" to
  Exit: (9) factorial(1,
1) ? creep
                           find more solutions
  Call: (9) L206 is 1*2 ? Prolog backtracks looking for another
                           solution
creep
  Exit: (9) 2 is 1*2?
  Exit: (8) factorial(2,
2) ? creep
  Call: (8) _G284 is 2*3?
creep
  Exit: (8) 6 is 2*3?
                           without success
                           Turn off tracing.
  Exit: (7) factorial (3,
6) ? creep
|X = 6|;
```

```
Redo: (10) factorial (0,
L244) ? creep
   Call: (11) 0>0 ? creep
   Fail: (11) 0>0 ? creep
   Fail: (9) factorial(1,
L225) ? creep
   Fail: (8) factorial(2,
L206) ? creep
   Fail: (7) factorial(3,
G284) ? creep
false.
[debug]
        ?- notrace. % turn
off tracing
true.
[debug]
        ?-
```

* What is this "creep" business? In SWI Prolog, the implementation of Prolog which this dictionary uses for the syntax of its examples, when you press return at the end of a line of tracing, Prolog prints "creep" on the *same* line, and then prints the next line of trace output on the next line. Pressing return again produces "creep" again and another line of tracing, and so on.

There are further tracing facilities in SWI Prolog. Do

```
?- help(trace).
to start to find out about them.
```

Built-in Prolog functions are not traced - that is, the internals of calls to things like member are not further explained by tracing them.

true

Built-in Prolog predicate with no arguments, which, as the name suggests, always succeeds.

See also fail, repeat.

See the article on <u>don't care</u> variables. **underscore**, **don't-care variable**

The Prolog variable _ (underscore) is a "don't-care" variable, which will match anything (atom, number, structure, ...). For example, the rule

```
bad(Dog) :- bites(Dog, _).
```

says that something (Dog) is bad if Dog bites anything. The "anything" is represented by _. Unlike other variables in Prolog, a bare _ can match different things in the same rule. So, for example, if gives (From, To, Gift) is a three-place procedure that is true if From gives Gift to To, then

```
giver(X) := gives(X, _, _).
```

signifies that someone (X) is a "giver" if X gives something to anybody

- the two _ s don't have to match the same thing. So if gives (fred,
john, black_eye). is stored in the Prolog database, then the rule
above allows us to infer that fred is a giver.

To be more explicit about the meaning of your rule, you could instead write:

```
bad (Dog) :- bites (Dog, Anybody).
```

This indicates what the variable is actually representing, but has the

feature that the binding of _Anybody typically doesn't get reported when Prolog finds a solution. In Prolog interpreters that report <u>singleton variables</u> (variables that are only used once in a rule often these are caused by typographical errors in the code, which is why Prolog warns you about them) do not report singleton variables that begin with _. This is useful is you are trying to get rid of warning messages in your Prolog code.

The rule

```
bad (Dog) :- bites (Dog, _Anybody).
in fact has a bug, in the sense that the _Anybody will match things
```

in fact has a bug, in the sense that the _Anybody will match things (like dogfood) that a dog might bite without being "bad". Maybe the rule should say instead:

```
bad(Dog) :-
   bites(Dog, Something),
   is_person(Something).
% add your own list of prohibitions - shoes, cats, ...
```

Prolog systems make internal use of variable names beginning with an underscore, e.g. _G157. These are not "don't-care" variables, but are chosen to not clash with any variable name a Prolog programmer is likely to use.

Underscores may also be used in the middle of variable or atom names, as in Intermediate_solution, likes_person - again, these are not "don't-care" variables. The idea is to make the variable or atom name more readable.

unification, =, \=

When we write a <u>goal</u> like X = Y in Prolog, we are testing for more than simple equality in the mathematical sense. We are testing whether X (which might be a <u>variable</u>, an atom, or an arbitrarily

complex term) *unifies* with Y (which might also be an atom, a variable, or a term). Two atoms, including numeric atoms, unify if they are the same. Two more complex terms unify if they have the same <u>functor</u> and their corresponding <u>arguments</u>unify. A variable always unifies with a term (provided that it is not previously unified with something different) by <u>binding</u> to that term. *Examples*:

?- fred = fred. true.	fred unifies with fred - they are the same atom.
?- X = fred. X = fred	X unifies with fred by binding X to fred.
?- X = likes(mary, pizza). X = likes(mary, pizza).	X unifies with likes(mary, pizza) by binding X to likes(mary, pizza).

```
?- likes(
         mary,
         book (
title (Title),
                         Note that the | characters at the start
              author (
                         of each line are continuation prompts
                         from Prolog because this query has been
given ('Herman'),
                         spread over more than one line.
                                 SurnameTerm, and Who are
                         Title,
SurnameTerm)))
                         bound in order to achieve unification.
                         The primary functors of the terms on
   likes(
                         either side of the = match, and
         Who,
                         unification proceeds by matching pairs of
         book (
                         corresponding arguments, for example, by
                         matching and unifying the first argument
title ('Moby Dick'),
                         on the left, mary, with the first
              author (
                         argument on the right,
                                                 Who. Unification
                         succeeds if all of the arguments
given ('Herman'),
                         match. This will include recursively
                         matching the arguments of substructures
surname('Melville')))).
                         such as the author/2 substructures.
Title = 'Moby Dick',
SurnameTerm =
surname('Melville'),
Who = mary.
```

The goal X = Y succeeds if X = Y would fail; it is the negated form of =.

Unnecessary Use of "=" to Force Unification

This is basically a style issue. Consider the two following alternative pieces of Prolog code for computing the maximum of two numbers.

The first version is to be preferred, particularly for a novice Prolog programmer, because it reinforces how Prolog works. It also does not involve the unnecessary Max = X or Max = Y.

Whenever you write "=" in a Prolog procedure, review the code to see whether you can get rid of the "=" clause by replacing the item on the left of "=" by the item to the right of it, elsewhere in the procedure. If you do this with max2, you get max1. Sometimes you may have written the "=" with the variable on the right, in which case you need to instead replace the item on the right of the "=" with the item to the left of it.

It should be possible to do this whenever there is a <u>variable</u> (rather than a more complex <u>term</u>) on at least one side of the "=".

```
univ, =...
```

The =.. meta-predicate, pronounced "univ", can be used to convert a list whose first item is a *non-numeric atom*, into a term, and vice-versa. For example,

```
?- Term =.. [likes, mary, pizza].
Term = likes(mary, pizza).
or
?- likes(mary, pizza) =.. List.
List = [likes, mary, pizza].
```

univ works with <u>infix operators</u>, too, though perhaps in a slightly unexpected way. Two examples:

```
?- op(700, xfy, and).
true.
?- Term =.. [and, p, q].
Term = p and q
```

```
?- Expression =.. [+, 2, 3], Value is Expression.

Expression = 2+3

Value = 5
```

variable

A variable in Prolog is a string of letters, digits, and underscores (_) beginning either with a capital letter or with an underscore. Examples:

```
X, Sister, _, _thing, _y47, First_name, Z2
```

The variable _ is used as a "don't-care" variable, when we don't mind

what value the variable has. For example:

```
is_a_parent(X) :- father_of(X, _).
is_a_parent(X) :- mother_of(X, _).
```

That is, X is a parent if they are a father or a mother, but we don't need to know who they are the father or mother of, to establish that they are a parent.

Variables are used in more than one way:

• to express constraints in parts of a rule: likes(A, B) :- dog(B), feeds(A, B).

Note that both A and B appear on both sides of the neck symbol

- the appearance of the same variable in two (or more places) in effect says that when the variable is <u>bound</u> to a value, it must be bound to the same value in all the places that it appears in a given rule.

Note that if the same variable appears in two or more different rules, it might be bound to different values in the different rules. This is achieved by Prolog renaming the variables internally, when it comes to use the rule - usually the names

are things like _1, _2, _3, etc. This is why variables with names

like these sometimes turn up in error messages when your Prolog program goes wrong.

- to formulate queries, as in the following example:
 - ?- studies (X, 9311). Prolog responds by finding all the

values for X for which studies (X, 9311) is true, and successively listing them, e.g.

```
X = fred;
X = jane;
X = abdul;
X = maria;
```

white space

In writing code in Prolog or any other programming language, white space (blank lines, indentation, perhaps alignment of related data items) can be used to make the code easier to follow. Here are some suggestions:

- Put a blank line before the start of any prolog procedure.
- Group collections of facts using blank lines.
- Sometimes it helps to line up comments, but not at the expense of making lines longer than about 75-80 characters.
- Don't put helper procedures in the middle of other procedures: separate them out before or after the procedure they help. If your helper procedure is used in several other procedures, you might want to put it right at the end of all your code.

Example. In moderate size browser windows, the bad example will have long lines that are folded by the browser, and the good example will not. In practice, you could make the lines in the good example rather longer - up to 75-80 characters.

Good	Bad
% smallest(+ListOfNumbers, -Min)	% smallest(ListOfNumbers, Min) binds
% binds Min to the smallest item	Min to the smallest item in the
% in the non-empty ListOfNumbers.	non-empty ListOfNumbers. ListOfNumbers
% ListOfNumbers should be	should be instantiated at time of call.
instantiated	smaller(A, B, A) :- A <= B.
% at time of call.	smaller(A, B, B) :- B < A.
smallest([FirstNum], FirstNum).	% This is a helper procedure for
smallest([FirstNum Rest], Min) :-	smallest.
smallest(Rest, MinRest),	smallest([FirstNum], FirstNum).
smaller(FirstNum,	smallest([FirstNum Rest], Min) :-
MinRest, Min).	smallest(Rest, MinRest),
	smaller(FirstNum, MinRest, Min).
% smaller(+First, +Second, -Smaller)	
% helper procedure for smallest.	
smaller(A, B, A) :-	
A <= B.	

```
smaller(A, B, B) :-
B < A.
```

See also $\underline{indentation}$ and $\underline{comments}$.