

HW3

Given $f(n) = 2n^2 + 7n + 3$, answer the following questions by “yes” or “no”. [10 points]

1a.) Yes $f(n) = O(n^2)$

B. Yes

C. Yes

D. No .

E. No

2. Given $f(n) = 7n^2 + 2n + 1$, prove that $f(n) = O(n^2)$. [10 points]

PROVE:

$f(n) = O(n^2)$.

Need to find a constant **c** and **n(0)** such that

$7n^2 + 2n + 1 \leq c(n^2)$ for all $n > n(0)$

Let $c = 10$ and $k = 1$

$7n^2 + 2n + 1 \leq 10n^2$ for all $n > 1$

$7n^2 \leq 10n^2 - 2n - 1$ for all $n > 1$

$7n^2 / n^2 \leq (10n^2 / n^2) - (2n / n^2) - (1/n^2)$

$7 \leq 10 - (2/n) - (1/n^2)$ for all $n > 1$

$7 \leq 10$ **TRUE**

Check

Let $n = 2$ and $k = 1$ for all $n > 1$

$7 \leq 10 - (2/2) - (1/4)$

$7 \leq 8.75$ **TRUE**

Therefore $7n^2 + 2n + 1 = O(n^2)$

