

$$1) \Delta C_1 = \frac{\partial C}{\partial S} \Big|_{S_0,0} (S - S_0)$$

$$\Delta C_2 = \frac{\partial C}{\partial S} \Big|_{S_0,0} (S - S_0) + \frac{1}{2} \frac{\partial^2 C}{\partial S^2} \Big|_{S_0,0} (S - S_0)^2$$

$$\sigma = 0.3 \quad S_0 = 60 \quad r = 0.04 \quad K = 79 \quad T = \frac{3}{4} \quad S = 64$$

$$d_1 = \frac{\ln(60/79) + (0.04 + \frac{1}{2}(0.3)^2)(\frac{3}{4})}{0.3\sqrt{\frac{3}{4}}} = -0.8135$$

$$d_2 = d_1 - 0.3\sqrt{\frac{3}{4}} = -1.0733$$

$$\Delta C_1 = \Phi(-0.8135)(64 - 60) = \$0.83$$

$$\Delta C_2 = 0.83 + \frac{1}{2} \frac{e^{-\frac{(-0.8135)^2}{2}}}{60\sqrt{2\pi(0.3)^2(\frac{3}{4})}} (4)^2 = \$0.98$$

$$\Delta C = 64 \Phi\left(\frac{\ln(64/79) + (0.04 + \frac{1}{2}(0.3)^2)(\frac{3}{4})}{0.3\sqrt{\frac{3}{4}}}\right)$$

$$- 79 e^{-0.04(\frac{3}{4})} \Phi\left(\frac{\ln(64/79) + (0.04 - \frac{1}{2}(0.3)^2)(\frac{3}{4})}{0.3\sqrt{\frac{3}{4}}}\right)$$

$$- 60 \Phi(d_1) + 79 e^{-0.04(\frac{3}{4})} \Phi(d_2) \\ = \$0.99$$

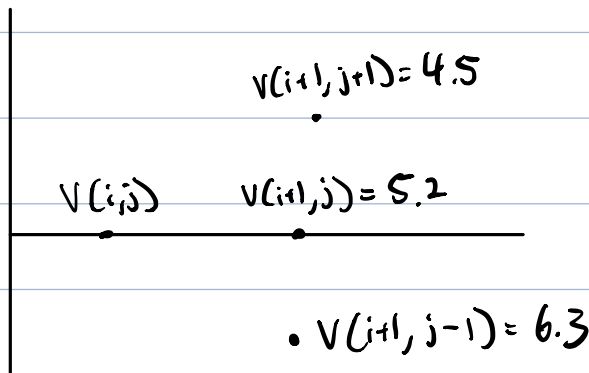
The estimate using both delta and gamma is closer to the actual.

$$2) \text{ Delta} = 1(\Delta) + n\left(\frac{dS}{S}\right) = 0$$

$$n = -0.21$$

Sell 0.21 of ABW stock

3) a)



Put option. As S increases, V decreases

$$b) \quad h = \frac{1}{12} \quad K = 0.1 \quad r = 0.1 \quad \sigma = 0.3$$

$$P_1 = \frac{(0.3)^2/12}{2(0.1)^2} + \left(0.1 - \frac{(0.3)^2}{2}\right)\left(\frac{1/12}{2(0.1)}\right) = 0.3979$$

$$P_2 = 1 - \frac{(0.3)^2/12}{(0.1)^2} = 0.25$$

$$P_3 = \frac{(0.3)^2/12}{2(0.1)^2} - \left(0.1 - \frac{(0.3)^2}{2}\right)\left(\frac{1/12}{2(0.1)}\right) = 0.3521$$

$$V(i, j) = \frac{1}{1 + (0.1/12)} (0.3979(4.5) + 0.25(5.2) + 0.3521(6.3)) \\ = \$5.26$$