

HW 1

1) I would prefer live classes over Zoom at scheduled times.

2)

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selection_sort(int s = V.size(), s > 1; s--) {
    int mi(0);
    for(int i = 1; i < s; i++) {
        if (V[mi] > V[i])
            mi = i;
    }
    swap(V[mi], V[s-1]);
}

```

$$\frac{n^2 - n}{2} = \frac{2n}{2} + \frac{2}{2}$$

The outer loop goes  $n$  times

The inner loop goes  $s$  times each iteration

$$[n + (n-1) + \dots + 3 + 2] + [1 + 2 + \dots + (n-1)]$$

$$2s = (n+1) + (n+1) + \dots + (n+1)$$

$$= \frac{(n+1)(n+1)}{2} = \frac{(n+1)^2}{2} \quad \text{for worst case } V[mi] > V[i]$$

$$\sum_{s=2}^n C_1 = \sum_{s=1}^{n-1} C_1 = (n-1) \quad \text{for number of swaps}$$



$$3) \quad n \lg n, n, 4^{\lg n}, \sqrt{n}, \lg(n^2), (\lg n)^2$$

$$\lim_{n \rightarrow \infty} \frac{4^{\lg n}}{n \lg n} = \frac{2x}{\log_2 x + \lg 2} = \frac{2 \ln(2)x}{\ln(x) + 1} = \frac{2 \ln(2)}{\frac{1}{x}} = \infty \quad 4^{\lg n} \text{ faster than } n \lg n$$

$$\lim_{n \rightarrow \infty} \frac{n \lg n}{n} = \lg n = \infty \quad n \lg n \text{ faster than } n$$

$$\lim_{n \rightarrow \infty} \frac{n}{(\lg n)^2} = \frac{1}{\frac{2 \lg n}{\ln(n)^2}} = \frac{\lg(n)}{2 \lg(2)} = \frac{\ln(2)}{\frac{2}{\ln(2)x}} = \frac{\ln^2(2)x}{2} = \infty$$

$$\lim_{n \rightarrow \infty} n \text{ is faster than } (\lg n)^2$$

$$\lim_{n \rightarrow \infty} \frac{(\lg n)^2}{\lg(n^2)} = \frac{\frac{2 \lg(n)}{\ln(n)^2}}{\frac{2}{\ln(2)x}} = \lg(n) = \infty$$

$$(\lg n)^2 \text{ is faster than } \lg(n^2)$$

$$\lim_{n \rightarrow \infty} \frac{\lg(n^2)}{\sqrt{n}} = \frac{\frac{2}{\ln(2)x}}{\frac{1}{2\sqrt{x}}} = \frac{4}{\ln(2)\sqrt{n}} = 0$$

$$\lg(n^2) \text{ is slower than } \sqrt{n}$$

$$\lim_{n \rightarrow \infty} \frac{\sqrt{n}}{(\lg n)^2} = \frac{\frac{1}{2\sqrt{x}}}{\frac{2 \lg(x)}{\ln(2)x}} = \frac{\ln(2)\sqrt{x}}{4 \lg x} = \frac{\ln^2(2)}{8} \sqrt{x} = \infty$$

$$\sqrt{n} \text{ faster than } (\lg n)^2$$

$$\lim_{n \rightarrow \infty} \frac{n}{\sqrt{n}} = \infty \quad n \text{ is faster than } \sqrt{n}$$



Slowest to fastest:

$\lg(n^2)$ ,  $(\lg n)^2$ ,  $\sqrt{n}$ ,  $n$ ,  $n \lg n$ ,  $4^{\lg n}$