```
function q_k_1 = NextState(q_k, q_dot_k, dt, max_joint_vel)
% *** KINEMATICS Simulator ***
% Takes q_k: The current state of the robot
             (12 variables: 3 for chassis, 5 for arm, 4 for wheel angles)
응
        q_dot_k: The joint and wheel velocities
             (9 variables: 5 for arm , 4 for wheels u)
        dt: The timestep size dt (1 parameter)
        max_joint_vel: The maximum joint and wheel velocity magnitude (1
parameter)
% Returns q_k_1: The next state (configuration) of the robot (12 variables)
% The function NextState is based on a simple first-order Euler step:
% - new arm joint angles = (old arm joint angles) + (joint speeds)*dt
% - new wheel angles = (old wheel angles) + (wheel speeds)*dt
% - new chassis configuration is obtained from odometry, as described in
Chapter 13.4
    [q_dot_k, in_bound] = bound(q_dot_k, -max_joint_vel, max_joint_vel);
    q_k_1 = zeros(12,1);
    % Joints Update & Wheels Update
    q_k_1(4:8) = q_k(4:8) + q_{dot_k(1:5)*dt};
    q_k_1(9:12) = q_k(9:12) + q_{dot_k(6:9)*dt};
    % Odometry Update [phi, x, y]
    load("youBotParams.mat", 'F')
    wheel_speeds = q_dot_k(6:9);
   phi_k = q_k(1);
    V = F * wheel_speeds;
    dV_{omg} = V(1) * dt;
    dV_x = V(2) * dt;
    dV_y = V(3) * dt;
    % 2D pose exponential
    if dV_omg == 0
        dq_{chassis_body} = [0, dV_x, dV_y]';
    else
        dq_chassis_body = [dV_omg;
                           dV_x * sin(dV_omg)/dV_omg + dV_y * (cos(dV_omg) -
1)/dV_omg;
                           dV_x * (1 - cos(dV_omg))/dV_omg + dV_y *
sin(dV_omg)/dV_omg];
    end
                                                0];
    rot\_odom\_body = [[1,
           [0, cos(phi_k), -sin(phi_k)];
           [0, sin(phi_k), cos(phi_k)]];
    dq_chassis_odom = rot_odom_body * dq_chassis_body;
    q_k_1(1:3) = q_k(1:3) + dq_{chassis_odom};
    [q_k_1, joints_checked] = checkJointLimits(q_k_1);
    % disp(joints_checked)
```

#### end

```
Not enough input arguments.

Error in NextState (line 17)

[q_dot_k, in_bound] = bound(q_dot_k, -max_joint_vel, max_joint_vel);
```

```
function [q_checked, joints_in_bound] = checkJointLimits(q)
% Takes q: The current state of the robot
           (12 variables: 3 for chassis, 5 for arm, 4 for wheel angles)
응
% Returns q_checked: The constrained state of the robot (12 variables)
          joints_in_bound: if arm joints are in bound (1 array)
    % Arm Joints
    q_{arm} = q(4:8);
    % Joint Lower Bounds and Upper Bounds
    q_lowerBounds = [-inf, -3*pi/4, -5*pi/6, -5*pi/6, -inf]';
    q_{upperBounds} = [inf, pi/2, 5*pi/6, 5*pi/6, inf]';
    [q_arm, joints_in_bound] = bound(q_arm, q_lowerBounds, q_upperBounds);
    q_{checked} = [q(1:3); q_{arm}; q(9:12)];
end
Not enough input arguments.
Error in checkJointLimits (line 9)
    q_{arm} = q(4:8);
            ^^^^
```

### **Parameters**

#### lengths saved in meters

```
x_0e = 0.033;
x_b0 = 0.1662;
% chassis frame \{b\} is at a height of z0
z0 = 0.0963;
% youBot dimensions
z1 = 0.0026;
z2 = 0.147;
z3 = 0.155;
z4 = 0.135;
z5 = 0.2176;
% front-back distance between the wheels: 2*1
1 = 0.47 / 2;
% side-to-side distance between the wheels: 2*w
w = 0.3 / 2;
% radius of the wheels: r
r = 0.0475;
```

### **Body Frame Screw Axes**

## **Zero E-E Config**

end-effector frame {e} to arm base frame {0}

# youBot Configs

arm base frame {0} to chassis frame {b} (static transform)

```
T_b0 = [[1, 0, 0, x_b0];
       [0, 1, 0, 0];
       [0, 0, 1,
                 z1];
       [0, 0, 0,
                   1]];
% Velocity Forward Kinematics of Chassis
F = (r/4) .* [[-1/(1 + w), 1/(1 + w), 1/(1 + w), -1/(1 + w)];
                                       1,
             [
                      1,
                                1,
                                                      1];
             [
                                1,
                                           -1,
                                                      1]];
                      -1,
save youBotParams.mat z0 1 w r B M_0e T_b0 F
```

```
clear; close all; clc;
q_{dot} = [pi/4 pi/4 pi/4 pi/4 pi/4 -1 1 1 -1]';
dt = 0.01;
max_joint_vel = 200;
t = [0:dt:1];
q = zeros(12, length(t));
for i = 2:length(t)
    q(:, i) = NextState(q(:, i-1), q_dot, dt, max_joint_vel);
end
disp(q')
writematrix(q','testData_NextState.csv')
  Columns 1 through 7
                    0
                               0
                                                     0
                                                0.0079
    0.0012
                    0
                               0
                                     0.0079
                                                           0.0079
                                                                     0.0079
    0.0025
                    0
                                     0.0157
                                                0.0157
                                                           0.0157
                               0
                                                                      0.0157
    0.0037
                    0
                                     0.0236
                                                0.0236
                                                           0.0236
                                                                     0.0236
                               0
    0.0049
                    0
                               0
                                     0.0314
                                                0.0314
                                                           0.0314
                                                                     0.0314
    0.0062
                    0
                               0
                                     0.0393
                                                0.0393
                                                           0.0393
                                                                     0.0393
    0.0074
                    0
                               0
                                     0.0471
                                                0.0471
                                                           0.0471
                                                                     0.0471
    0.0086
                    0
                               0
                                     0.0550
                                                0.0550
                                                           0.0550
                                                                      0.0550
    0.0099
                    0
                                     0.0628
                                                           0.0628
                                                                     0.0628
                               0
                                                0.0628
    0.0111
                    0
                               0
                                     0.0707
                                                0.0707
                                                           0.0707
                                                                      0.0707
    0.0123
                    0
                               0
                                     0.0785
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                                                           0.0785
                                                                     0.0785
    0.0136
                    0
                               0
                                     0.0864
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                    0
                                     0.0942
                                                0.0942
                                                           0.0942
                                                                     0.0942
    0.0148
                               0
    0.0160
                    0
                                     0.1021
                                                0.1021
                                                           0.1021
                               0
                                                                      0.1021
    0.0173
                    0
                                     0.1100
                                                0.1100
                                                           0.1100
                                                                     0.1100
                               0
    0.0185
                    0
                               0
                                     0.1178
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                                                                     0.1178
                                     0.1257
                                                                     0.1257
    0.0197
                    0
                               0
                                                0.1257
                                                           0.1257
    0.0210
                    0
                               0
                                     0.1335
                                                0.1335
                                                           0.1335
                                                                     0.1335
    0.0222
                    0
                               0
                                     0.1414
                                                0.1414
                                                           0.1414
                                                                     0.1414
                                                           0.1492
    0.0234
                    0
                                     0.1492
                                                0.1492
                                                                     0.1492
                               0
    0.0247
                    0
                               0
                                     0.1571
                                                0.1571
                                                           0.1571
                                                                      0.1571
    0.0259
                    0
                               0
                                     0.1649
                                                0.1649
                                                           0.1649
                                                                      0.1649
    0.0271
                    0
                               0
                                     0.1728
                                                0.1728
                                                           0.1728
                                                                      0.1728
                    0
    0.0284
                               0
                                     0.1806
                                                0.1806
                                                           0.1806
                                                                     0.1806
    0.0296
                    0
                                     0.1885
                                                0.1885
                               0
                                                           0.1885
                                                                      0.1885
    0.0308
                    0
                               0
                                     0.1963
                                                0.1963
                                                           0.1963
                                                                     0.1963
    0.0321
                    0
                               0
                                     0.2042
                                                0.2042
                                                           0.2042
                                                                     0.2042
                    0
    0.0333
                               0
                                     0.2121
                                                0.2121
                                                           0.2121
                                                                     0.2121
    0.0345
                    0
                               0
                                     0.2199
                                                0.2199
                                                           0.2199
                                                                      0.2199
    0.0358
                    0
                               0
                                     0.2278
                                                0.2278
                                                           0.2278
                                                                      0.2278
                                                           0.2356
    0.0370
                    0
                                     0.2356
                                                0.2356
                                                                     0.2356
                               0
    0.0382
                    0
                               0
                                     0.2435
                                                0.2435
                                                           0.2435
                                                                      0.2435
    0.0395
                    0
                               0
                                     0.2513
                                                0.2513
                                                           0.2513
                                                                      0.2513
    0.0407
                    0
                               0
                                     0.2592
                                                0.2592
                                                           0.2592
                                                                     0.2592
                                                0.2670
    0.0419
                                     0.2670
                                                                     0.2670
                               0
                                                           0.2670
```

0.0432	0	0	0.2749	0.2749	0.2749	0.2749
0.0444	0	0	0.2827	0.2827	0.2827	0.2827
0.0456	0	0	0.2906	0.2906	0.2906	0.2906
0.0469	0	0	0.2985	0.2985	0.2985	0.2985
0.0481	0	0	0.3063	0.3063	0.3063	0.3063
0.0494	0	0	0.3142	0.3142	0.3142	0.3142
0.0506	0	0	0.3220	0.3220	0.3220	0.3220
0.0518	0	0	0.3299	0.3299	0.3299	0.3299
0.0531	0	0	0.3377	0.3377	0.3377	0.3377
0.0543	0	0	0.3456	0.3456	0.3456	0.3456
0.0555	0	0	0.3534	0.3534	0.3534	0.3534
0.0568	0	0	0.3613	0.3613	0.3613	0.3613
0.0580	0	0	0.3691	0.3691	0.3691	0.3691
0.0592	0	0	0.3770	0.3770	0.3770	0.3770
0.0605	0	0	0.3848	0.3848	0.3848	0.3848
0.0617	0	0	0.3927	0.3927	0.3927	0.3927
0.0629	0	0	0.4006	0.4006	0.4006	0.4006
0.0642	0	0	0.4084	0.4084	0.4084	0.4084
0.0654	0	0	0.4163	0.4163	0.4163	0.4163
0.0666	0	0	0.4241	0.4241	0.4241	0.4241
0.0679	0	0	0.4320	0.4320	0.4320	0.4320
0.0691	0	0	0.4398	0.4398	0.4398	0.4398
0.0703	0	0	0.4477	0.4477	0.4477	0.4477
0.0716	0	0	0.4555	0.4555	0.4555	0.4555
0.0728	0	0	0.4634	0.4634	0.4634	0.4634
0.0740	0	0	0.4712	0.4712	0.4712	0.4712
0.0753	0	0	0.4791	0.4791	0.4791	0.4791
0.0765	0	0	0.4869	0.4869	0.4869	0.4869
0.0777	0	0	0.4948	0.4948	0.4948	0.4948
0.0790	0	0	0.5027	0.5027	0.5027	0.5027
0.0802	0	0	0.5105	0.5105	0.5105	0.5105
0.0814	0	0	0.5184	0.5184	0.5184	0.5184
0.0827	0	0	0.5262	0.5262	0.5262	0.5262
0.0839	0	0	0.5341	0.5341	0.5341	0.5341
0.0851	0	0	0.5419	0.5419	0.5419	0.5419
0.0864	0	0	0.5498	0.5498	0.5498	0.5498
0.0876	0	0	0.5576	0.5576	0.5576	0.5576
0.0888	0	0	0.5655	0.5655	0.5655	0.5655
0.0901	0	0	0.5733	0.5733	0.5733	0.5733
0.0913	0	0	0.5812	0.5812	0.5812	0.5812
0.0925	0	0	0.5890	0.5890	0.5890	0.5890
0.0938	0	0	0.5969	0.5969	0.5969	0.5969
0.0950	0	0	0.6048	0.6048	0.6048	0.6048
0.0962	0	0	0.6126	0.6126	0.6126	0.6126
0.0975	0	0	0.6205	0.6205	0.6205	0.6205
0.0987	0	0	0.6283	0.6283	0.6283	0.6283
0.0999	0	0	0.6362	0.6362	0.6362	0.6362
0.1012	0	0	0.6440	0.6440	0.6440	0.6440
0.1024	0	0	0.6519	0.6519	0.6519	0.6519
0.1036	0	0	0.6597	0.6597	0.6597	0.6597
0.1049	0	0	0.6676	0.6676	0.6676	0.6676
0.1061	0	0	0.6754	0.6754	0.6754	0.6754
0.1073	0	0	0.6833	0.6833	0.6833	0.6833
0.1086	0	0	0.6912	0.6912	0.6912	0.6912

0.1098	0	0	0.6990	0.6990	0.6990	0.6990
0.1110	0	0	0.7069	0.7069	0.7069	0.7069
0.1123	0	0	0.7147	0.7147	0.7147	0.7147
0.1135	0	0	0.7226	0.7226	0.7226	0.7226
0.1147	0	0	0.7304	0.7304	0.7304	0.7304
0.1160	0	0	0.7383	0.7383	0.7383	0.7383
0.1172	0	0	0.7461	0.7461	0.7461	0.7461
0.1184	0	0	0.7540	0.7540	0.7540	0.7540
0.1197	0	0	0.7618	0.7618	0.7618	0.7618
0.1209	0	0	0.7697	0.7697	0.7697	0.7697
0.1221	0	0	0.7775	0.7775	0.7775	0.7775
0.1234	0	0	0.7854	0.7854	0.7854	0.7854

#### Columns 8 through 12

0	0	0	0	0
0.0079	-0.0100	0.0100	0.0100	-0.0100
0.0157	-0.0200	0.0200	0.0200	-0.0200
0.0236	-0.0300	0.0300	0.0300	-0.0300
0.0314	-0.0400	0.0400	0.0400	-0.0400
0.0393	-0.0500	0.0500	0.0500	-0.0500
0.0471	-0.0600	0.0600	0.0600	-0.0600
0.0550	-0.0700	0.0700	0.0700	-0.0700
0.0628	-0.0800	0.0800	0.0800	-0.0800
0.0707	-0.0900	0.0900	0.0900	-0.0900
0.0785	-0.1000	0.1000	0.1000	-0.1000
0.0864	-0.1100	0.1100	0.1100	-0.1100
0.0942	-0.1200	0.1200	0.1200	-0.1200
0.1021	-0.1300	0.1300	0.1300	-0.1300
0.1100	-0.1400	0.1400	0.1400	-0.1400
0.1178	-0.1500	0.1500	0.1500	-0.1500
0.1257	-0.1600	0.1600	0.1600	-0.1600
0.1335	-0.1700	0.1700	0.1700	-0.1700
0.1414	-0.1800	0.1800	0.1800	-0.1800
0.1492	-0.1900	0.1900	0.1900	-0.1900
0.1571	-0.2000	0.2000	0.2000	-0.2000
0.1649	-0.2100	0.2100	0.2100	-0.2100
0.1728	-0.2200	0.2200	0.2200	-0.2200
0.1806	-0.2300	0.2300	0.2300	-0.2300
0.1885	-0.2400	0.2400	0.2400	-0.2400
0.1963	-0.2500	0.2500	0.2500	-0.2500
0.2042	-0.2600	0.2600	0.2600	-0.2600
0.2121	-0.2700	0.2700	0.2700	-0.2700
0.2199	-0.2800	0.2800	0.2800	-0.2800
0.2278	-0.2900	0.2900	0.2900	-0.2900
0.2356	-0.3000	0.3000	0.3000	-0.3000
0.2435	-0.3100	0.3100	0.3100	-0.3100
0.2513	-0.3200	0.3200	0.3200	-0.3200
0.2592	-0.3300	0.3300	0.3300	-0.3300
0.2670	-0.3400	0.3400	0.3400	-0.3400
0.2749	-0.3500	0.3500	0.3500	-0.3500
0.2827	-0.3600	0.3600	0.3600	-0.3600
0.2906	-0.3700	0.3700	0.3700	-0.3700
0.2985	-0.3800	0.3800	0.3800	-0.3800

0.3063	-0.3900	0.3900	0.3900	-0.3900
0.3142	-0.4000	0.4000	0.4000	-0.4000
0.3220	-0.4100	0.4100	0.4100	-0.4100
0.3299	-0.4200	0.4200	0.4200	-0.4200
0.3377	-0.4300	0.4300	0.4300	-0.4300
0.3456	-0.4400	0.4400	0.4400	-0.4400
0.3534	-0.4500	0.4500	0.4500	-0.4500
0.3613	-0.4600	0.4600	0.4600	-0.4600
0.3691	-0.4700	0.4700	0.4700	-0.4700
0.3770	-0.4800	0.4800	0.4800	-0.4800
0.3848	-0.4900	0.4900	0.4900	-0.4900
0.3927	-0.5000	0.5000	0.5000	-0.5000
0.4006	-0.5100	0.5100	0.5100	-0.5100
0.4084	-0.5200	0.5200	0.5200	-0.5200
0.4163	-0.5300	0.5300	0.5300	-0.5300
0.4241	-0.5400	0.5400	0.5400	-0.5400
0.4241	-0.5500	0.5500	0.5500	-0.5500
		0.5600		
0.4398	-0.5600		0.5600	-0.5600
0.4477	-0.5700	0.5700	0.5700	-0.5700
0.4555	-0.5800	0.5800	0.5800	-0.5800
0.4634	-0.5900	0.5900	0.5900	-0.5900
0.4712	-0.6000	0.6000	0.6000	-0.6000
0.4791	-0.6100	0.6100	0.6100	-0.6100
0.4869	-0.6200	0.6200	0.6200	-0.6200
0.4948	-0.6300	0.6300	0.6300	-0.6300
0.5027	-0.6400	0.6400	0.6400	-0.6400
0.5105	-0.6500	0.6500	0.6500	-0.6500
0.5184	-0.6600	0.6600	0.6600	-0.6600
0.5262	-0.6700	0.6700	0.6700	-0.6700
0.5341	-0.6800	0.6800	0.6800	-0.6800
0.5419	-0.6900	0.6900	0.6900	-0.6900
0.5498	-0.7000	0.7000	0.7000	-0.7000
0.5576	-0.7100	0.7100	0.7100	-0.7100
0.5655	-0.7200	0.7200	0.7200	-0.7200
0.5733	-0.7300	0.7300	0.7300	-0.7300
0.5812	-0.7400	0.7400	0.7400	-0.7400
0.5890	-0.7500	0.7500	0.7500	-0.7500
0.5969	-0.7600	0.7600	0.7600	-0.7600
0.6048	-0.7700	0.7700	0.7700	-0.7700
0.6126	-0.7800	0.7800	0.7800	-0.7800
0.6205	-0.7900	0.7900	0.7900	-0.7900
0.6283	-0.8000	0.8000	0.8000	-0.8000
0.6362	-0.8100	0.8100	0.8100	-0.8100
0.6440	-0.8200	0.8200	0.8200	-0.8200
0.6519	-0.8300	0.8300	0.8300	-0.8300
0.6597	-0.8400	0.8400	0.8400	-0.8400
0.6676	-0.8500	0.8500	0.8500	-0.8500
0.6754	-0.8600	0.8600	0.8600	-0.8600
0.6833	-0.8700	0.8700	0.8700	-0.8700
0.6912	-0.8800	0.8800	0.8800	-0.8800
0.6990	-0.8900	0.8900	0.8900	-0.8900
0.7069	-0.9000	0.9000	0.9000	-0.9000
0.7147	-0.9100	0.9100	0.9100	-0.9100
0.7226	-0.9200	0.9200	0.9200	-0.9200

0.7304	-0.9300	0.9300	0.9300	-0.9300
0.7383	-0.9400	0.9400	0.9400	-0.9400
0.7461	-0.9500	0.9500	0.9500	-0.9500
0.7540	-0.9600	0.9600	0.9600	-0.9600
0.7618	-0.9700	0.9700	0.9700	-0.9700
0.7697	-0.9800	0.9800	0.9800	-0.9800
0.7775	-0.9900	0.9900	0.9900	-0.9900
0.7854	-1.0000	1.0000	1.0000	-1.0000

### Milestone 2 Video Link:

https://youtu.be/zyl5\_ieC4NQ