

# **Data Structures and Algorithms**

## **Assignment 3**

**Jan 1 Semester**

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## Algorithms

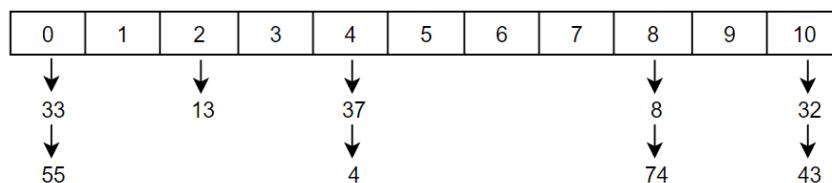
### 1 Question 1

**Hash Function:**  $h(x) = x \bmod 11$

**Value:** 33, 13, 32, 8, 55, 37, 43, 74, 103

The hash address:	K:	33	13	32	8	55	37	43	74	103
	$H(x)$	0	2	10	8	0	4	10	8	4

#### 1.1 a) When Separate Chaining is used to handle collisions



← Hash Table using  
Chaining Resolution

#### 1.2 b) When Collision are handled by linear probing

0	1	2	3	4	5	6	7	8	9	10
35	55	13	43	37	103			8	74	32

← Hash table using  
Linear Porbing Resolution

#### 1.3 C) When collison are handled by double hashing

**Second Hash Function:**  $h'(x) = (x \bmod 5) + 1$

**Overall Function:**  $H(x) = (h(x) + i \times h'(x)) \bmod 11, \text{ where } i = 0, 1, 2, 3, \dots$

The hash address:	K:	33	13	32	8	55	37	43	74	103
	$h(x)$	0	2	10	8	0	4	10	8	4
	$h'(x)$					1		4	5	4

Since  $h(55) = 0$ , which is already occupied, collision occurs.

To solve this problem, we use the second hash function is applied.

$h'(55) = (55 \bmod 5) + 1 = 1$ , 1 is the new location and its not occupied, the vaule will be place in location 1.

Similar for  $h(43)$ ,  $h(74)$ ,  $h(103)$ .

However as you can see there is is still collision between  $h(43)$ ,  $h(103)$ .

In order to solve this, we will then use the overall function.

**For  $h(43)$ ,**

Let  $i$  be 0,  $H(43) = (10 + 0 \times 4) \bmod 11 = 10$  (location 10 is occupied, collision)

Let  $i$  be 1,  $H(43) = (10 + 1 \times 4) \bmod 11 = 3$  (location 3 is empty, no collision)

(part c will be continued in the next page)

**For  $h(103)$ ,**

## Algorithms

Let  $i$  be 0,  $H(103) = (4 + 0 \times 4) \bmod 11 = 4$  (location 4 is occupied, collision)  
 Let  $i$  be 1,  $H(103) = (4 + 1 \times 4) \bmod 11 = 8$  (location 8 is occupied, collision)  
 Let  $i$  be 2,  $H(103) = (4 + 2 \times 4) \bmod 11 = 1$  (location 1 is occupied, collision)  
 Let  $i$  be 3,  $H(103) = (4 + 3 \times 4) \bmod 11 = 5$  (location 5 is empty, no collision)

### Hash table using Double-hashing Resolution

0	1	2	3	4	5	6	7	8	9	10
33	55	13	43	37	103		74	8		32

#### 1.4 d) When Collision are handled by quadratic probing

**Quadratic probing Function:**  $h'(x, i) = (h(x) + 0.5 i + 0.5 i^2) \bmod 11$ ,  
 where  $i = 1, 2, 3$

Collision had occur for  $h(55), h(43), h(74), h(103)$ . We have to use the Quadratic probing Function to handle the collision.

**For  $h(55)$ ,**

Let  $i$  be 1,  $h'(55, 1) = 55 + (0.5 \times 1) + (0.5 \times 1^2) \bmod 11 = 1$ ,  
 (location 1 is empty, no collision)

**For  $h(43)$ ,**

Let  $i$  be 1,  $h'(43, 1) = 43 + (0.5 \times 1) + (0.5 \times 1^2) \bmod 11 = 0$ ,  
 (location 0 is occupied, collision)

Let  $i$  be 2,  $h'(43, 2) = 43 + (0.5 \times 2) + (0.5 \times 2^2) \bmod 11 = 1$ ,  
 (location 1 is empty, no collision)

**For  $h(74)$ ,**

Let  $i$  be 1,  $h'(74, 1) = 74 + (0.5 \times 1) + (0.5 \times 1^2) \bmod 11 = 9$ ,  
 (location 9 is empty, no collision)

**For  $h(103)$ ,**

Let  $i$  be 1,  $h'(103, 1) = 103 + (0.5 \times 1) + (0.5 \times 1^2) \bmod 11 = 5$ ,  
 (location 5 is empty, no collision)

### Hash table using Quadratic Probing Resolution

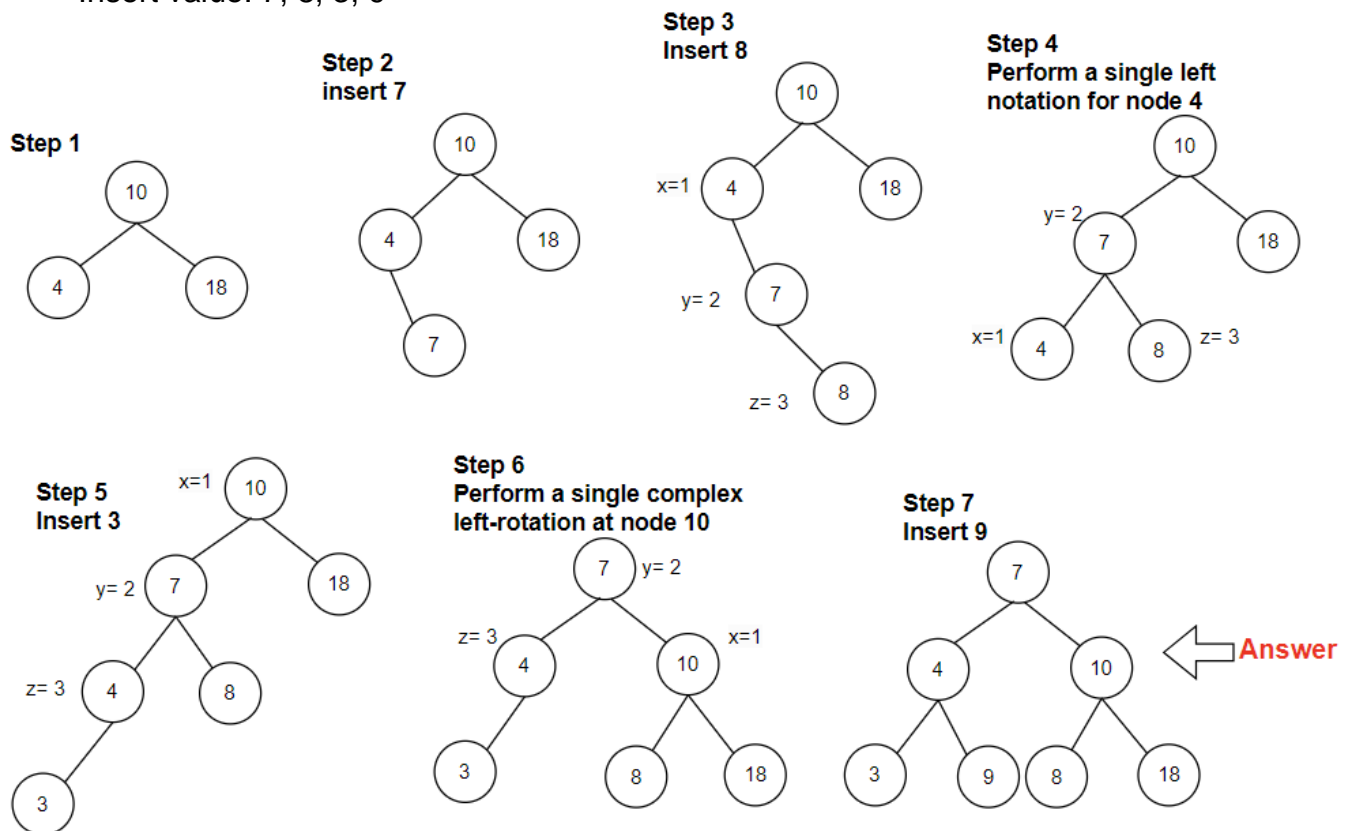
0	1	2	3	4	5	6	7	8	9	10
33	55	13	43	37	103			8	74	32

## Algorithms

### 2 Question 2

#### 2.1 a) Insert element into partially constructed AVL

Insert value: 7, 8, 3, 9



#### 2.2 b) Make the array into a Maximum Heap

Value: 65, 57, 85, 48, 47, 61, 75, 5, 25, 85, 20, 42

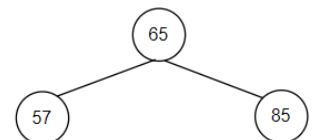
**Step 1:**  
Insert 65



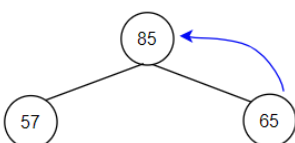
**Step 2:**  
Insert 57



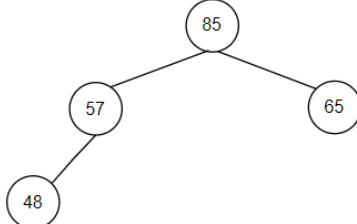
**Step 3:**  
Insert 85



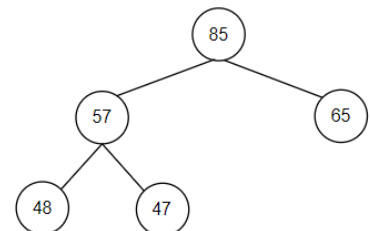
**Step 5:**  
Heapify



**Step 5:**  
Insert 48

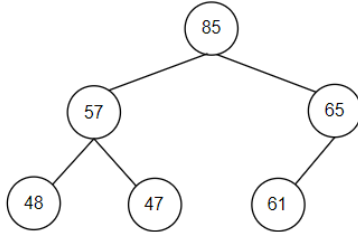


**Step 6:**  
Insert 47

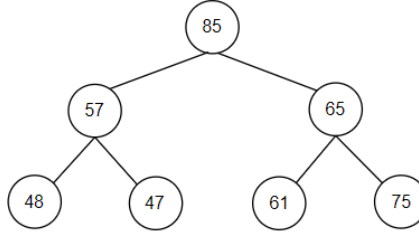


## Algorithms

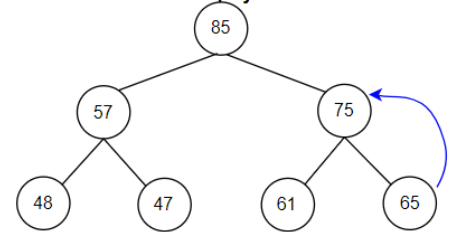
**Step 7:  
Insert 61**



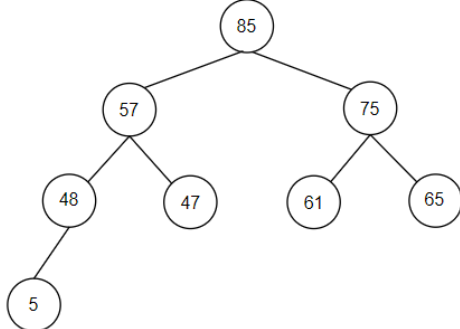
**Step 8:  
Insert 75**



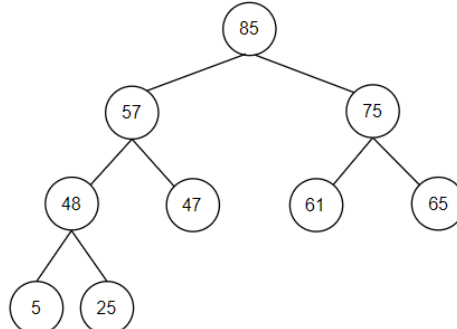
**Step 9:  
Heapify**



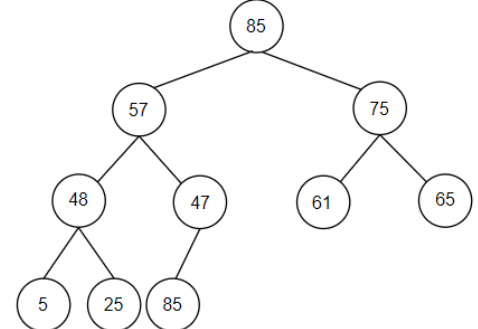
**Step 10:  
Insert 5**



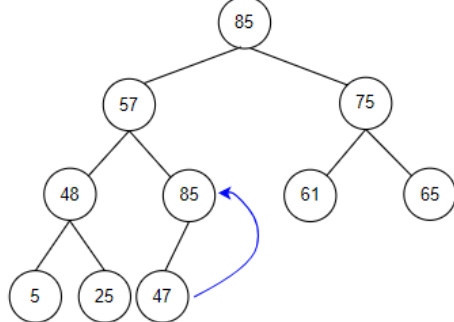
**Step 11:  
Insert 25**



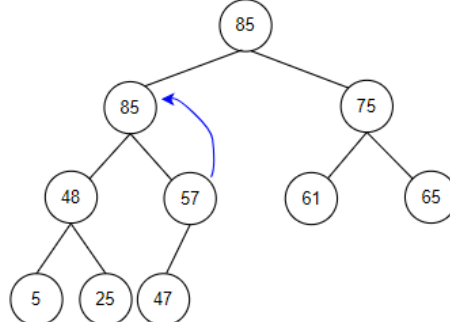
**Step 12:  
Insert 85**



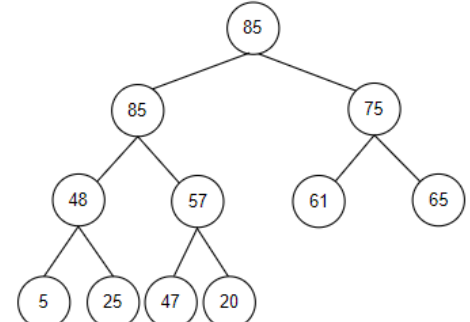
**Step 13:  
Heapify**



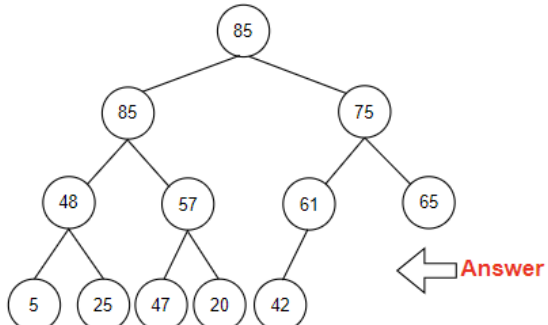
**Step 14:  
Heapify**



**Step 15:  
Insert 20**



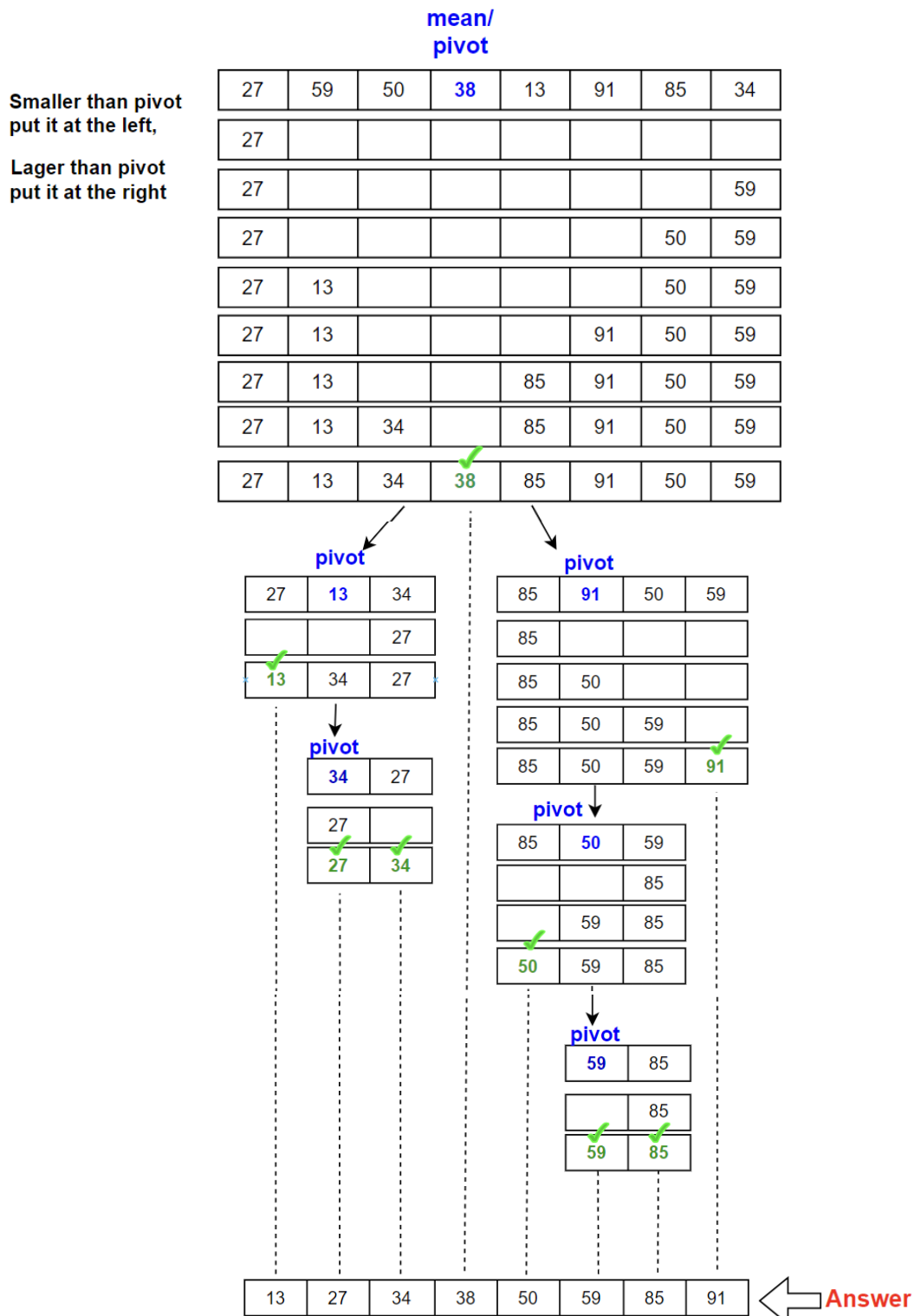
**Step 16:  
Insert 42**



## Algorithms

### 3 Question 3

- Quicksort with middle-of tree (mean) pivot
- Sorting the array in a accending order.



## Algorithms

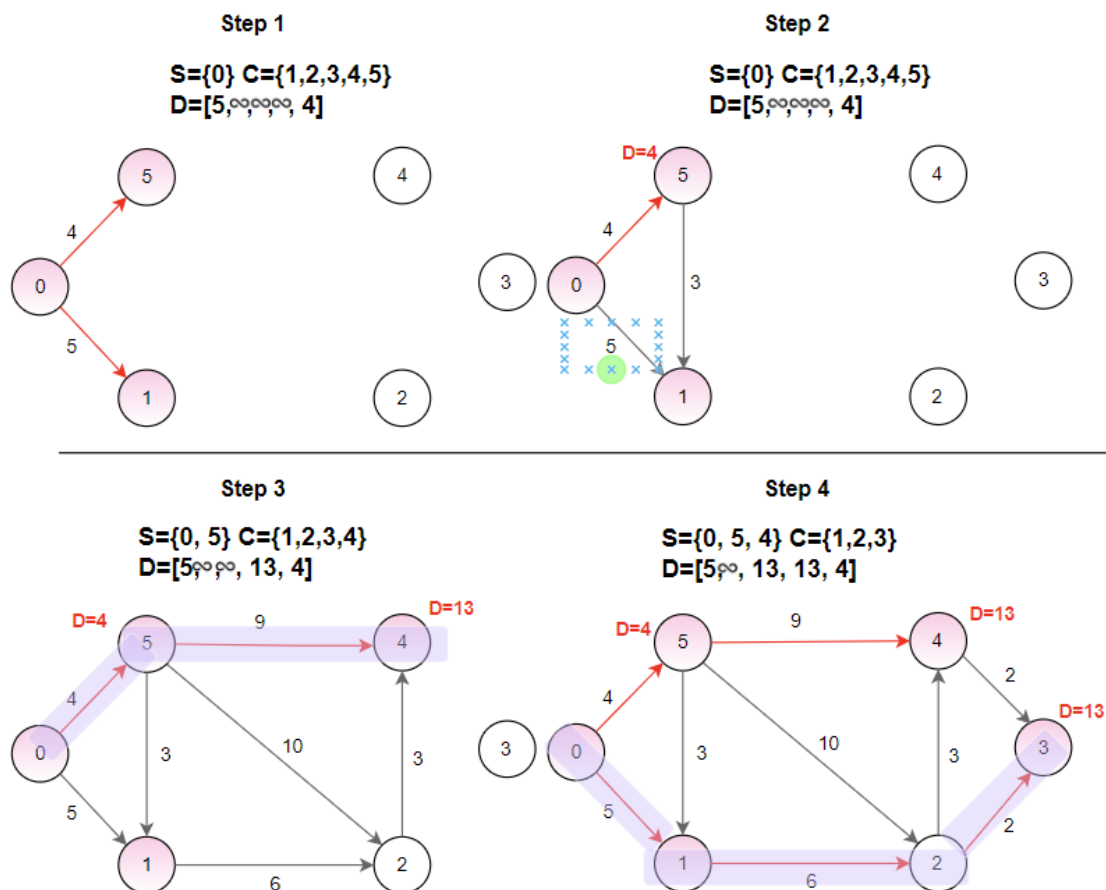
### 4 Question 4

#### 4.1 Adjacency Matrix

A	0	1	2	3	4	5
0	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$
1	5	$\infty$	$\infty$	$\infty$	$\infty$	3
2	$\infty$	6	$\infty$	$\infty$	$\infty$	10
3	$\infty$	$\infty$	2	$\infty$	2	$\infty$
4	$\infty$	$\infty$	3	$\infty$	$\infty$	9
5	4	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$

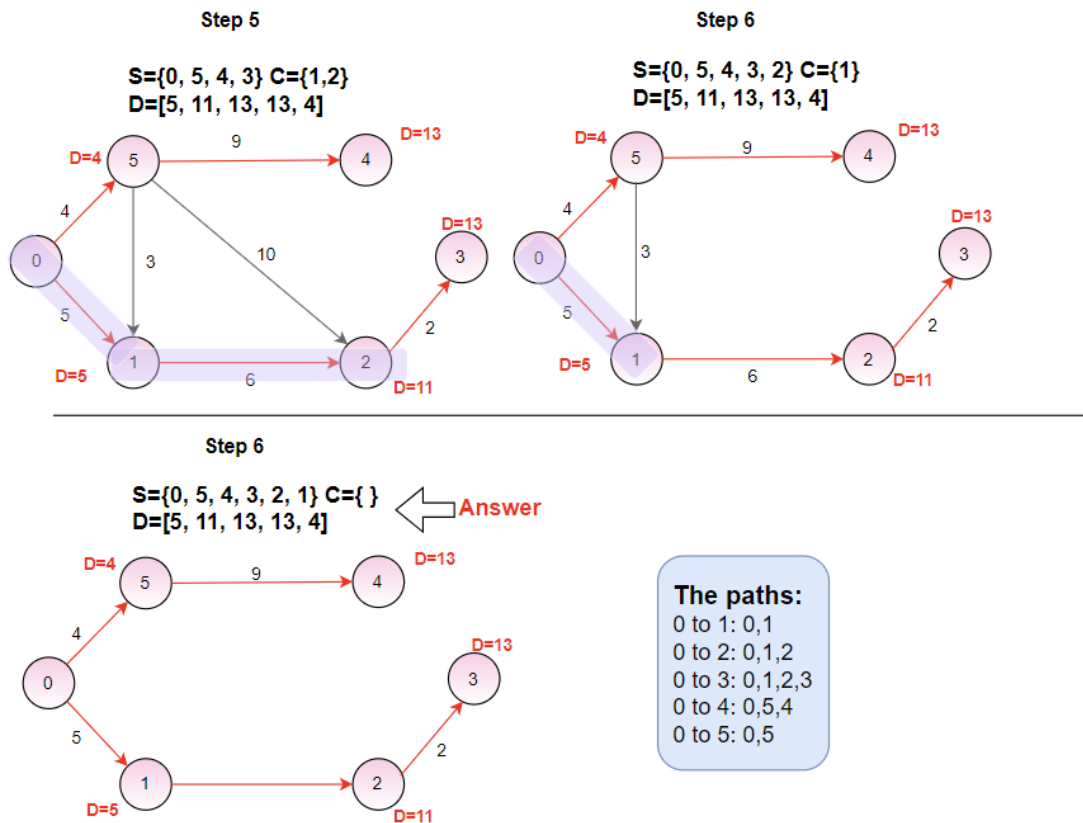
#### 4.2 Show all paths from 0 to all other network nodes.

Method 1(both answer are the same)





## Algorithms



### Method 2 (both answer are the same)

#### Step 1

A	0	1	2	3	4	5
0	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$
1	5	$\infty$	$\infty$	$\infty$	$\infty$	3
2	$\infty$	6	$\infty$	$\infty$	$\infty$	10
3	$\infty$	$\infty$	2	$\infty$	2	$\infty$
4	$\infty$	$\infty$	3	$\infty$	$\infty$	9
5	4	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$

P =	D =
0	5
0	$\infty$
0	$\infty$
0	$\infty$
0	4

$V=5$   
 $C=\{1,2,3,4\}$   
 $S=\{0\}$

#### Step 2

A	0	1	2	3	4	5
0	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$
1	5	$\infty$	$\infty$	$\infty$	$\infty$	3
2	$\infty$	6	$\infty$	$\infty$	$\infty$	10
3	$\infty$	$\infty$	2	$\infty$	2	$\infty$
4	$\infty$	$\infty$	3	$\infty$	$\infty$	9
5	4	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$

P =	D =
0	5
0	$\infty$
5	14
0	$\infty$
5	13
0	4

$V=5$   
 $C=\{1,2,3,4\}$   
 $S=\{0\}$

## Algorithms

### Step 3

A	0	1	2	3	4	5
0	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$
1	5	$\infty$	$\infty$	$\infty$	$\infty$	3
2	$\infty$	6	$\infty$	$\infty$	$\infty$	10
3	$\infty$	$\infty$	2	$\infty$	2	$\infty$
4	$\infty$	$\infty$	3	$\infty$	$\infty$	9
5	4	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$

P =	D =
0	5
1	11
0	$\infty$
5	13
0	4

V= 1  
C= {2,3,4}  
S={0,5}

### Step 4

A	0	1	2	3	4	5
0	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$
1	5	$\infty$	$\infty$	$\infty$	$\infty$	3
2	$\infty$	6	$\infty$	$\infty$	$\infty$	10
3	$\infty$	$\infty$	2	$\infty$	2	$\infty$
4	$\infty$	$\infty$	3	$\infty$	$\infty$	9
5	4	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$

P =	D =
0	5
1	11
2	13
5	13
0	4

V= 2  
C= {3,4}  
S={0,1,5}

### Step 5

A	0	1	2	3	4	5
0	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$
1	5	$\infty$	$\infty$	$\infty$	$\infty$	3
2	$\infty$	6	$\infty$	$\infty$	$\infty$	10
3	$\infty$	$\infty$	2	$\infty$	2	$\infty$
4	$\infty$	$\infty$	3	$\infty$	$\infty$	9
5	4	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$

P =	D =
0	5
1	11
2	13
5	13
0	4

V= 4  
C= {3}  
S={0,1,2,5}

### Step 6

A	0	1	2	3	4	5
0	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$
1	5	$\infty$	$\infty$	$\infty$	$\infty$	3
2	$\infty$	6	$\infty$	$\infty$	$\infty$	10
3	$\infty$	$\infty$	2	$\infty$	2	$\infty$
4	$\infty$	$\infty$	3	$\infty$	$\infty$	9
5	4	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$

P =	D =
0	5
1	11
2	13
5	13
0	4

V= 3  
C= { }  
S={0,1,2,4,5}

### Step 7

A	0	1	2	3	4	5
0	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$
1	5	$\infty$	$\infty$	$\infty$	$\infty$	3
2	$\infty$	6	$\infty$	$\infty$	$\infty$	10
3	$\infty$	$\infty$	2	$\infty$	2	$\infty$
4	$\infty$	$\infty$	3	$\infty$	$\infty$	9
5	4	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$

P =	D =
0	5
1	11
2	13
5	13
0	4

V= 5  
C= { }  
S={0,1,2,3,4,5}

#### The paths:

0 to 1: 0,1  
0 to 2: 0,1,2  
0 to 3: 0,1,2,3  
0 to 4: 0,5,4  
0 to 5: 0,5

## Algorithms

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### 5 Question 5

#### 5.1 Is the heuristic in the problem admissible?

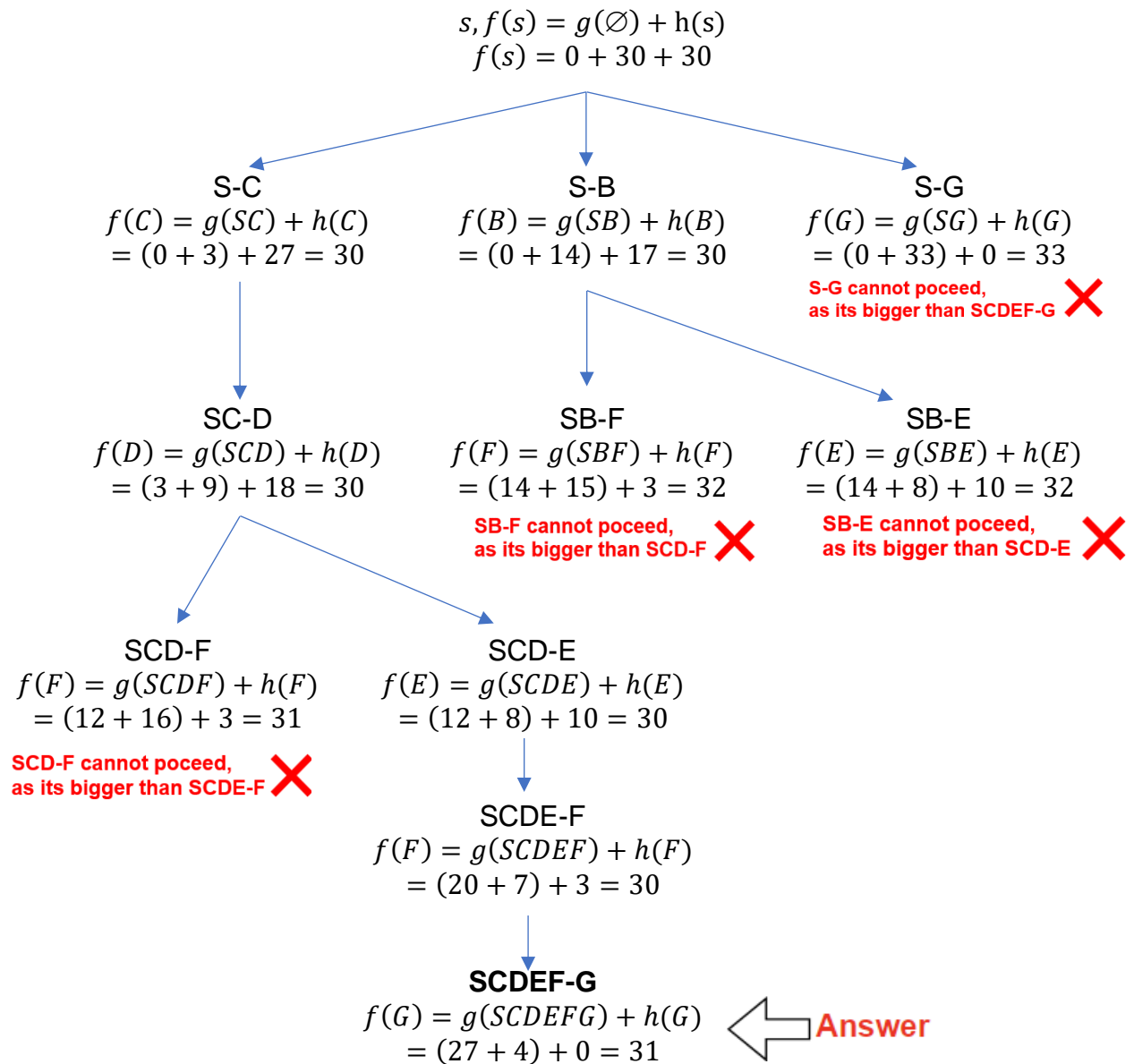
For every node  $n$ ,  $\forall(s,s') : h(s) - h(s') \leq c(s,s')$ .

States	$h(s) - h(s')$	$c(s,s')$	$h(s) - h(s') \leq c(s,s')$
<b>S-C</b>	$30 - 27 = 3$	$C(S,C) = 3$	True
<b>S-B</b>	$30 - 17 = 13$	$C(S,B) = 14$	True
<b>S-G</b>	$30 - 0 = 30$	$C(S,G) = 33$	True
<b>C-D</b>	$27 - 18 = 9$	$C(C,D) = 9$	True
<b>B-E</b>	$17 - 18 = 7$	$C(B,E) = 8$	True
<b>B-F</b>	$17 - 10 = 7$	$C(B,F) = 15$	True
<b>D-F</b>	$18 - 3 = 15$	$C(D,F) = 16$	True
<b>D-E</b>	$18 - 3 = 8$	$C(D,E) = 8$	True
<b>E-F</b>	$10 - 3 = 7$	$C(E,F) = 7$	True
<b>F-G</b>	$3 - 0 = 3$	$C(F,G) = 4$	True

Answer: Yes, the heuristic specified in the problem is admissible.

## Algorithms

### 5.2 Find the shortest path using A\*Search



Answer: There is no need to continue as the goal is G. The shortest route is SCDEFG at cost 31.