



Definite Random Walks

by [zemen](#)

Problem

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Alex has a board game consisting of:

- A *chip* for marking his current location on the board.
- n *fields* numbered from 1 to n . Each position i has a value, f_i , denoting the *next* position for the chip to jump to from that field.
- A *die* with m faces numbered from 0 to $m - 1$. Each face j has a probability, p_j , of being rolled.

Alex then performs the following actions:

- Begins the game by placing the chip at a position in a field randomly and with equiprobability.
- Takes k turns; during each turn he:
 - Rolls the die. We'll denote the number rolled during a turn as d .
 - Jumps the chip d times. Recall that each field contains a value denoting the *next* field number to jump to.
- After completing k turns, the game ends and he must calculate the respective probabilities for each field as to whether the game ended with the chip in that field.

Given n, m, k , the game board, and the probabilities for each *die* face, print n lines where each line i contains the probability that the chip is on field i at the end of the game.

Note: All the probabilities in this task are rational numbers modulo $M = 998244353$. That is, if the probability can be expressed as the irreducible fraction $\frac{p}{q}$ where $q \bmod M \neq 0$, then it corresponds to the number $(p \times q^{-1}) \bmod M$ (or, alternatively, $p \times q^{-1} \equiv x \pmod{M}$). [Click here](#) to learn about *Modular Multiplicative Inverse*.

Input Format

The first line contains three space-separated integers describing the respective values of n (the number of positions), m (the number of die faces), and k (the number of turns).

The second line contains n space-separated integers describing the respective values of each f_i (i.e., the index of the field that field i can transition to).

The third line contains m space-separated integers describing the respective values of each p_j (where $0 \leq p_j < M$) describing the probabilities of the faces of the m -sided die.

Constraints

- $1 \leq n \leq 6 \times 10^4$
- $4 \leq m \leq 10^5$
- $1 \leq k \leq 1000$
- $1 \leq i, f_i \leq n$
- $0 \leq p_j < M$
- The sum of $p_j \bmod M$ is 1

Note: The time limit for this challenge is doubled for *all* languages. Read more about standard time limits at our [environment](#) page.

Output Format

Print n lines of output in which each line i contains a single integer, x_i (where $0 \leq x_i < M$), denoting the probability that the chip will be on field i after k turns.

Sample Input 0

```
4 5 1
2 3 2 4
332748118 332748118 332748118 0 0
```

Sample Output 0

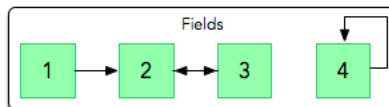
```
582309206
332748118
332748118
748683265
```

Explanation 0

The diagram below depicts the respective probabilities of each *die* face being rolled:

Game Die					
Face	0	1	2	3	4
P_j	332748118	332748118	332748118	0	0
Probability	$\frac{1}{3}$	$\frac{1}{3}$	$\frac{1}{3}$	0	0

The diagram below depicts each field with an arrow pointing to the *next* field:



There are four equiprobable initial fields, so each field has a $\frac{1}{4}$ probability of being the chip's initial location. Next, we calculate the probability that the chip will end up in each field after $k = 1$ turn:

1. The only way the chip ends up in this field is if it never jumps from the field, which only happens if Alex rolls a **0**. So, this field's probability is $\frac{1}{4} \cdot \frac{1}{3} = \frac{1}{12}$. We then calculate and print the result of $\frac{1}{12} \bmod 998244353 = 582309206$ on a new line.

2. The chip can end up in field **2** after one turn in the following scenarios:

- Start in field **1** and roll a **1**, the probability for which is $\frac{1}{4} \cdot \frac{1}{3} = \frac{1}{12}$.
- Start in field **2** and roll a **0** or a **2**, the probability for which is $\frac{1}{4} \cdot \frac{2}{3} = \frac{2}{12}$.
- Start in field **3** and roll a **1**, the probability for which is $\frac{1}{4} \cdot \frac{1}{3} = \frac{1}{12}$.

After summing these probabilities, we get a total probability of $\frac{1}{12} + \frac{2}{12} + \frac{1}{12} = \frac{1}{3}$ for the field. We then calculate and print the result of $\frac{1}{3} \bmod 998244353 = 332748118$ on a new line.

3. The chip can end up in field **3** after one turn in the following scenarios:

- Start in field **1** and roll a **2**, the probability for which is $\frac{1}{4} \cdot \frac{1}{3} = \frac{1}{12}$.
- Start in field **2** and roll a **1**, the probability for which is $\frac{1}{4} \cdot \frac{1}{3} = \frac{1}{12}$.
- Start in field **3** and roll a **0** or a **2**, the probability for which is $\frac{1}{4} \cdot \frac{2}{3} = \frac{2}{12}$.

After summing these probabilities, we get a total probability of $\frac{1}{12} + \frac{1}{12} + \frac{2}{12} = \frac{1}{3}$ for the field. We then calculate and print the result of $\frac{1}{3} \bmod 998244353 = 332748118$ on a new line.

4. If the chip is initially placed in field 4, it will always end up in field 4 regardless of how many turns are taken (because this field loops back onto itself). Thus, this field's probability is $\frac{1}{4}$. We then calculate and print the result of $\frac{1}{4} \bmod 998244353 = 748683265$ on a new line.

[f](#) [t](#) [in](#)


Submissions:39

Max Score:100

Difficulty: Expert

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Java 7



```
1 import java.io.*;
2 import java.util.*;
3 import java.text.*;
4 import java.math.*;
5 import java.util.regex.*;
6
7 public class Solution {
8
9     public static void main(String[] args) {
10         Scanner in = new Scanner(System.in);
11         int n = in.nextInt();
12         int m = in.nextInt();
13         int k = in.nextInt();
14         int[] f = new int[n];
15         for(int f_i=0; f_i < n; f_i++){
16             f[f_i] = in.nextInt();
17         }
18         int[] p = new int[m];
19         for(int p_i=0; p_i < m; p_i++){
20             p[p_i] = in.nextInt();
21         }
22         // your code goes here
23     }
24 }
25
```

Line: 1 Col: 1

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