Tree Coordinates

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We consider metric space to be a pair, (M, ρ), where M is a set and $\rho : M \times M \to \mathbb{R}$ such that the following conditions hold:

- $\rho(x, y) \geq 0$
- $\rho(x, y) = 0 \Leftrightarrow x = y$
- $\rho(x, y) = \rho(y, x)$
- $\rho(x, y) \leq \rho(x, z) + \rho(z, y)$

where $\rho(x, y)$ is the *distance* between points x and y.

Let's define the *product* of two metric spaces, $(M_1, \rho_1) \times (M_2, \rho_2)$, to be (M, ρ) such that:

- $M = M_1 \times M_2$
- $\rho(z_1, z_2) = \rho_1(x_1, x_2) + \rho_2(y_1, y_2)$, where $z_1 = (x_1, y_1)$, $z_2 = (x_2, y_2)$.

So, it follows logically that (M, ρ) is also a metric space. We then define *squared metric space*, $(M, \rho)^2$, to be the product of a metric space multiplied with itself: $(M, \rho) \times (M, \rho)$.

For example, $(\mathbb{R}, abs)$, where $abs(x, y) = |x - y|$ is a metric space. $(\mathbb{R}, abs)^2 = (\mathbb{R}^2, abs_2)$, where $abs_2((x_1, y_1), (x_2, y_2)) = |x_1 - x_2| + |y_1 - y_2|$.

In this challenge, we need a tree-space. You're given a tree, $T = (V, E)$, where V is the set of vertices and E is the set of edges. Let the function $\rho : V \times V \to \mathbb{Z}$ be the distance between two vertices in tree T (i.e., $\rho(x, y)$ is the number of edges on the path between vertices x and y). Note that (V, ρ) is a metric space.

You are given a tree, T, with n vertices, as well as m points in $(V, \rho)^2$. Find and print the distance between the two furthest points in this metric space!

Input Format

The first line contains two space-separated positive integers describing the respective values of n (the number of vertices in T) and m (the number of given points).
Each line i of the $n - 1$ subsequent lines contains two space-separated integers, u_i and v_i, describing edge i in T.
Each line j of the m subsequent lines contains two space-separated integers describing the respective values of x_j and y_j for point j.

Constraints

- $1 \leq n \leq 7.5 \cdot 10^4$
- $2 \leq m \leq 7.5 \cdot 10^4$
- $1 \leq u_i, v_i \leq n$
- $1 \leq x_j, y_j \leq n$

Scoring

This challenge uses **binary** scoring, so you *must* pass all test cases to earn a positive score.

Output Format

Print a single non-negative integer denoting the maximum distance between two of the given points in metric space $(T, \rho)^2$.

Sample Input 0

```
2 2
1 2
1 2
2 1
```

Sample Output 0

```
2
```

Explanation 0

The distance between points $(1, 2)$ and $(2, 1)$ is $\rho(1, 2) + \rho(2, 1) = 2$.

Sample Input 1

```
7 3
1 2
2 3
3 4
4 5
5 6
6 7
3 6
4 5
5 5
```

Sample Output 1

```
3
```

Explanation 1

The best points are $(3, 6)$ and $(5, 5)$, which gives us a distance of $\rho(3, 5) + \rho(6, 5) = 2 + 1 = 3$.

```
#include <vector>
#include <climits>
#include <cstring>
#include <cstdlib>
#include <fstream>
#include <numeric>
#include <sstream>
#include <iostream>
#include <algorithm>
#include <unordered_map>

using namespace std;


int main(){
    int n;
    int m;
    cin >> n >> m;
    vector< vector<int> > edges(n-1,vector<int>(2));
    for(int edges_i = 0;edges_i < n-1;edges_i++){
       for(int edges_j = 0;edges_j < 2;edges_j++){
          cin >> edges[edges_i][edges_j];
       }
    }
    vector< vector<int> > points(m,vector<int>(2));
    for(int points_i = 0;points_i < m;points_i++){
       for(int points_j = 0;points_j < 2;points_j++){
          cin >> points[points_i][points_j];
       }
    }
    // your code goes here
    return 0;
}

```

Line: 1 Col: 1

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