

# Asymmetric Key Encryption





# Symmetric Vs. Asymmetric

## Symmetric

- Single shared key
  - Encrypts and decrypts
- Faster than Asymmetric Encryption
- Problem: How do you share the key Securely?

## Asymmetric

- 2 keys
  - 1 public
  - 1 private
- Asymmetric
  - Encrypt using public key then decrypt using private key
  - Encrypt using private key then decrypt using public key
- Does not require a shared secret



## 2 Keys (Public and Private)

- The generated keys are related to each other
- But one cannot be guessed from the other
- A message encrypted with the public key can ONLY be decrypted with the private key and vice versa
- What do I do with my keys?
  - Share your public key with the world
  - Hide your private key from everyone



# Principles of Asymmetric Key Encryption

- Alice picks 2 prime numbers,  $p$  and  $q$  as the private key.
- She multiplies them together for the public key.
- Bob encrypts his message to Alice with the her public key.
- Alice Decrypts Bob's message with her private key.
- Eve would need to know  $p$  and  $q$  to decrypt the message.
- Prime generation and multiplication is easy
- Prime factorization is hard (for now...)



# Digital Signing (Basic)

- Not only do people wish to hide what they are sending, but they want to make sure the message really came from the stated sender
  - Did this really come from Alice?
- Asymmetric Key encryption allows “signing” of messages
- Signing -
  - Alice encrypts message with her **private** key
  - Everyone with the Alice’s **public** key can decrypt, not very secure
  - Assumed only Alice has access to her private key
  - Therefore, only Alice could have encrypted/signed the message



# Certificate Authorities

- How do you get someone's public key??
  - Could post it to a keybase
- Problem - Eve can give Alice a fake public key and claim it is Bob's public key
- How does Alice know she really has Bob's public key?
- Need a trusted 3rd party to distribute public keys - Certificate Authority
  - 3 Biggest: Comodo, Symantec, GoDaddy
- New Problem: How does Alice know a key really came from her trusted CA?



## Certificate Authorities (2)

- Signing
  - The CA can sign the key before they send it to you
  - This makes it so you know that the key came from the CA
- Same problem as before
  - How do you get the CA's public key?
- Hard coded into web browsers
  - Set of trusted keys directly coded into your web browser (potential attack vector?).
  - CA's can be forced to create a "valid" key for someone (the government?)



# Use in Conjunction with Symmetric Key Encryption

- Why??
  - Asymmetric is pretty great, why bother with symmetric?
- Speed
- Asymmetric is extremely slow compared to symmetric
  - This is important for large files
- Don't want to encrypt an entire message using asymmetric key encryption
- Ideally, users exchange a symmetric key using asymmetric encryption then use the shared key from then on





# Sending a message (more advanced)

Alice wants to send a message to Bob:

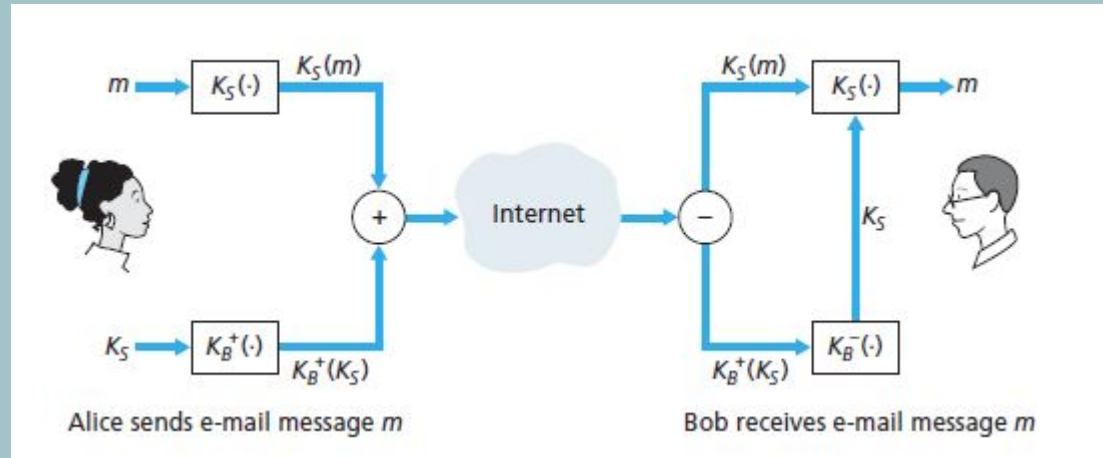
1. Alice generates a symmetric key (session key)  $K_s$
2. Alice encrypts message with  $K_s$
3. Alice encrypts  $K_s$  with Bob's public key  $K_B^+$
4. Concatenate encrypted key onto encrypted message

Bob receives the package:

1. de-concatenates message
2. decrypts  $K_s$  with his private key  $K_B^-$
3. decrypts entire message with  $K_s$

This allows Alice to implement higher security measures while still getting the message to Bob quickly

## Sending a message (more advanced)





# Use in Conjunction with Hashing

- Why?
- Speed, same as before
- Don't want to encrypt an entire message using asymmetric key encryption
- Hash the message, then sign the hash



# Signing a message (More Advanced)

Alice wants to sign her message to Bob:

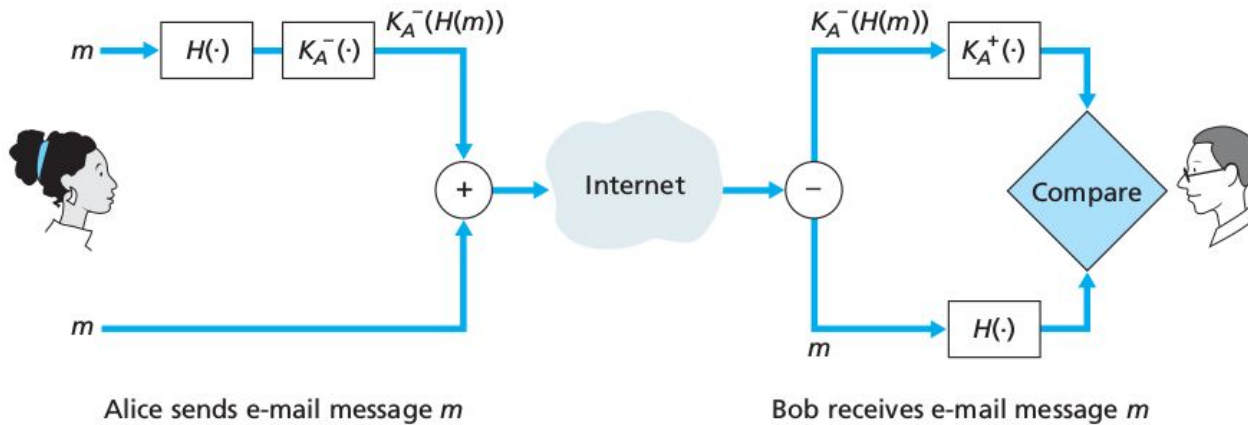
1. Alice hashes the message
2. Alice signs the hash  $H$ , with her private key  $K_A^-$
3. Concatenate message and signed hash, send package

Bob receives the package:

1. Bob decrypts the hash  $H_a$ , with  $K_A^+$ . This proves it was signed by the real Alice.
2. Bob generates a hash of the message  $H_b$
3. Bob compares  $H_b$  with  $H_a$

This allows Bob to be sure the message was unchanged and definitely came from Alice

# Signing a message (More Advanced)



**Figure 8.20** ♦ Using hash functions and digital signatures to provide sender authentication and message integrity

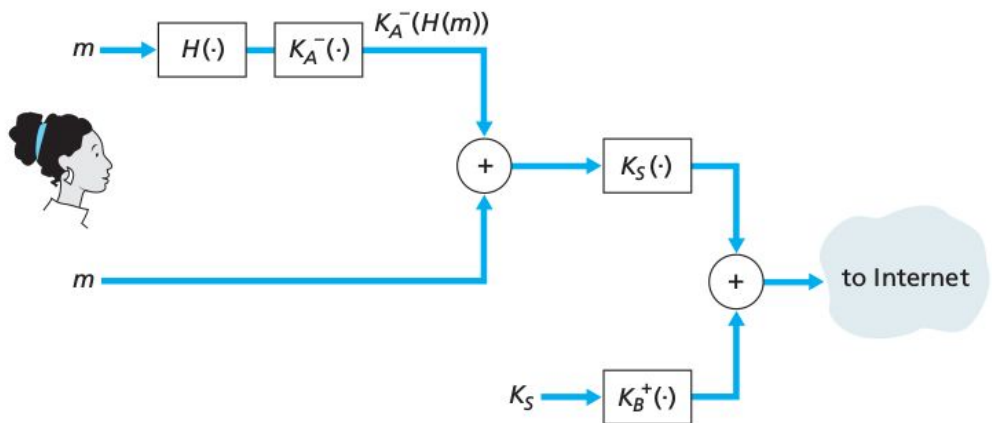


# Super Secure Communication

Alice wants to send a message to Bob:

1. Alice hashes the message,  $H_a$
2. Alice signs the message, ie encrypts  $H_a$  with  $K_A^-$
3. Concatenates the message and signature together
4. Alice generates a session key  $K_s$
5. Alice encrypts the concatenation with  $K_s$
6. Alice encrypts  $K_s$  with Bob's public key  $K_B^+$
7. Concatenates encrypted key and encrypted package together sends

# Super Secure Communication



**Figure 8.21** ♦ Alice uses symmetric key cryptography, public key cryptography, a hash function, and a digital signature to provide secrecy, sender authentication, and message integrity



## Super Secure Communication (2)

Bob receives the package:

1. Bob de-concatenates the encrypted  $K_s$  from the encrypted package
2. Bob uses  $K_B^-$  to decrypt  $K_s$
3. Bob uses  $K_s$  to decrypt the package
4. Bob de-concatenates the encrypted hash  $H_a$  from the message
5. Bob decrypts  $H_a$  using  $K_A^+$
6. Bob generates a hash of the message  $H_b$
7. Compare  $H_a$  and  $H_b$

All together this provides a communication form that hides data, ensures the data has not been altered, and verifies the sender.





# A Ton of Work Though...

- A lot of steps to just send a message. What if you forget a step or do something out of order?
- A program that uses this is PGP, pretty good privacy, which implements the steps listed above to make sending an encrypted email easier
- Most secure communication over the internet utilizes asymmetric key encryption
- For Example:
  - SSL
  - HTTPS
  - SSH