

# Desafios de Programação Estrutura de Dados

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# STL Vector

| Função                  | Descrição   |
|-------------------------|---|
| <i>resize(n, val)</i>   | redimensiona o vetor para ter n elementos inicializados com o valor val |
| <i>push_back(val)</i>   | adiciona o elemento no final do vetor                                   |
| <i>pop_back()</i>       | remove o último elemento do vetor                                       |
| <i>insert(it, val)</i>  | insere o elemento val antes da posição especificada por it              |
| <i>sort(first,last)</i> | ordena os elementos no intervalo [first,last) em ordem crescente        |

## Exemplo: vector

```
#include <vector>
#include <algorithm>
#include <iostream>
#define all(v) v.begin(),v.end()
using namespace std;
typedef vector<int> vi;
int main(){
    vi v1;
    v1.resize(3, 0); // Aloca três posições e inicializa com zero
    v1[0] = 5; v1[1] = 4; v1[2]=6;
    v1.push_back(9);
    vi::iterator it = v1.begin();
    v1.insert(it,7); // insere no começo
    for(int i = 0; i < v1.size(); i++) cout << v1[i] << endl;
    int maior = *max_element(all(v1));
    cout << "maior:_" << maior << endl;
    vi v2(v1.begin(), v1.begin()+3);
    for(int i = 0; i < v2.size(); i++) cout << v2[i] << endl;
    vi v3(v1); // copy v1
    cout << "sort_vector" << endl;
    sort(all(v3));
    reverse(all(v3));
    for(int i = 0; i < v3.size(); i++) cout << v3[i] << endl;
}
```

# STL queue

| Função           | Descrição  |
|------------------|--|
| <i>push(val)</i> | insere o elemento val na fila                              |
| <i>back()</i>    | retorna uma referência para o elemento mais novo na fila   |
| <i>pop()</i>     | remove o elemento mais antigo na fila                      |
| <i>front()</i>   | retorna uma referência para o elemento mais antigo na fila |

## Exemplo: queue

```
#include <iostream>
#include <algorithm>
#include <queue>
using namespace std;

int main()
{
    queue<int> fila;
    fila.push(2); fila.push(3);
    fila = queue<int> ();
    fila.push(2); fila.push(3); fila.push(4);
    cout << fila.size() << endl;
    cout << fila.back() << endl;
    while( !fila.empty() ){
        cout << fila.front() << " ";
        fila.pop();
    }
}
```

# STL stack

| Função           | Descrição   |
|------------------|---|
| <i>push(val)</i> | insere o elemento val no topo da pilha                  |
| <i>top()</i>     | retorna uma referência para o elemento no topo da pilha |
| <i>pop()</i>     | remove o elemento do topo da pilha                      |

## Exemplo: stack

```
#include <iostream>
#include <algorithm>
#include <vector>
#include <queue>
#include <stack>
using namespace std;
int main()
{
    stack <int> p;
    p.push(4);
    p.push(5);
    p.push(6);
    while( !p.empty() )
    {
        cout << p.top() << "␣";
        p.pop();
    }

}
```

# STL bitset

```
#include <bits/stdc++.h>
using namespace std;
#define M 32
int main()
{
    // default constructor initializes with all bits 0
    bitset<M> bset1;
    // bset2 is initialized with bits of 20
    bitset<M> bset2(20);
    // bset3 is initialized with bits of specified binary string
    bitset<M> bset3(string("1100"));
    // cout prints exact bits representation of bitset
    cout << bset1 << endl; // 00000000000000000000000000000000
    cout << bset2 << endl; // 0000000000000000000000000000010100
    cout << bset3 << endl; // 000000000000000000000000000001100
    cout << endl;
    // declaring set8 with capacity of 8 bits
    bitset<8> set8; // 00000000
    // setting first bit (or 6th index)
    set8[1] = 1; set8[4] = 1;
    cout << set8 << endl; // 00010010
    // count function returns number of set bits in bitset
    int numberof1 = set8.count();
```



## STL bitset

```
// size function returns total number of bits in bitset
// so there difference will give us number of unset(0)
// bits in bitset
int numberof0 = set8.size() - numberof1;
cout << set8 << "_has_" << numberof1 << "_ones_and_"
    << numberof0 << "_zeros\n";
// test function return 1 if bit is set else returns 0
cout << "bool_representation_of_" << set8 << ":\n";
for (int i = 0; i < set8.size(); i++)
    cout << set8.test(i) << "_";
cout << endl;
// any function returns true, if atleast 1 bit
// is set
if (!set8.any())
    cout << "set8_has_no_bit_set.\n";
if (!bset1.any())
    cout << "bset1_has_no_bit_set.\n";
// none function returns true, if none of the bit
// is set
if (!bset1.none())
    cout << "bset1_has_all_bit_set\n";
// bset.set() sets all bits
cout << set8.set() << endl;
// bset.set(pos, b) makes bset[pos] = b
```

# STL bitset

```
// bset.set(pos) makes bset[pos] = 1 i.e. default
// is 1
cout << set8.set(4) << endl;

// reset function makes all bits 0
cout << set8.reset(2) << endl;
cout << set8.reset() << endl;

// flip function flips all bits i.e. 1 <=> 0
// and 0 <=> 1
cout << set8.flip(2) << endl;
cout << set8.flip() << endl;

// Converting decimal number to binary by using bitset
int num = 100;
cout << "\nDecimal_number:_" << num
    << "_Binary_equivalent:_" << bitset<8>(num);

return 0;
}
```

# BitMask

```
#include <vector>
#include <stdio.h>
#include <iostream>
#define INT_SIZE (8*sizeof(int))
#define high(x) ((x)/INT_SIZE)
#define low(x) ((x)%INT_SIZE)
using namespace std;
class BitMask{
public:
    vector<int> bit;
    vector<unsigned> mask;
    BitMask(int N){
        bit.assign(N/INT_SIZE+1, 0);
        mask.assign(INT_SIZE, 0);
        mask[0] = 1;
        for(int i=1; i<INT_SIZE; i++){
            mask[i] = (1<<i);
        }
    }
    void set(int x){ bit[high(x)] |= mask[low(x)];}
    void reset(int x){ bit[high(x)] &= ~(mask[low(x)]);}
    bool test(int x){ return (bit[high(x)] & mask[low(x)]) != 0 ;}
};
```

# STL set

| Função                         | Descrição  |
|--------------------------------|--|
| <code>insert(val)</code>       | adiciona o elemento <code>val</code> , mas não permite elementos duplicados                                    |
| <code>erase(val)</code>        | remove o elemento <code>val</code>   |
| <code>erase(position)</code>   | remove o elemento apontado pelo iterator <code>position</code>   |
| <code>erase(first,last)</code> | remove todos os elementos entre <code>first</code> e <code>last</code>   |
| <code>count(val)</code>        | o número de vezes que <code>val</code> aparece no set  |
| <code>find(val)</code>         | se existe o elemento <code>val</code> a função devolve seu iterator; caso contrário devolve <code>end()</code> |

# Exemplo Set

```
#include <iostream>
#include <set>
using namespace std;
int main(){
    set<int> myset;
    set<int>::iterator itlow, itup, it;
    for(int i = 1; i <= 10; i++) myset.insert(i);
    myset.insert(8); // nao insere
    itlow=myset.lower_bound (3);
    itup=myset.upper_bound (6);
    myset.erase(itlow, itup); // 1 2 7 8 9 10
    it = myset.find(7); // Complexidade logaritmica
    myset.erase(it); // 1 2 8 9 10
    cout << "size_of_set:" << myset.size() << endl;
    if( myset.count(7) == 0) cout << "7_is_not_a_element_of_myset"
    for (it=myset.begin(); it!=myset.end(); ++it) //Percorre em ord
        cout << ' ' << *it;
}
```

# STL map

| Função                         | Descrição   |
|--------------------------------|---|
| <code>insert(val)</code>       | adiciona o elemento <code>val</code>  |
| <code>erase(val)</code>        | remove o elemento <code>val</code>  |
| <code>erase(position)</code>   | remove o elemento apontado pelo iterator <code>position</code>  |
| <code>erase(first,last)</code> | remove todos os elementos entre <code>first</code> e <code>last</code>  |
| <code>find(val)</code>         | se existe o elemento <code>val</code> então a função devolve seu <code>it</code> ; caso contrário devolve <code>map::end()</code> |

## Exemplo map

```
#include <iostream>
#include <algorithm>
#include <vector>
#include <map>
using namespace std;
int main()
{
    char poema [] = "Sou_chama_sem_luz_jardim_\
sem_luar_luar_sem_amor";
    map<char, int> mapa;
    map<char, int>::iterator it;
    for(int i = 0; poema[i] != '\0'; i++)
    {
        char c = poema[i];
        mapa[c]++;
    }

    for(it = mapa.begin(); it != mapa.end(); it++)
    {
        if( it->second > 0 )
            printf("mapa[%c] = %d\n", it->first, it->second );
    }
}
```

## Exemplo unordered\_map

```
#include <iostream>
#include <stdio.h>
#include <algorithm>
#include <vector>
#include <unordered_map>
#include <time.h>
using namespace std;

int main()
{
    char poema [] = "Sou_chama_sem_luz_jardim_\
sem_luar_luar_sem_amor";
    unordered_map <char, int> mapa;
    unordered_map <char, int>::iterator it;
    for(int i = 0; poema[i] != '\0'; i++){
        char c = poema[i];
        mapa[c]++;
    }
    for(it = mapa.begin(); it != mapa.end(); it++){
        if( it->second > 0 )
            printf("mapa[%c] = %d\n", it->first, it->second );
    }
}
```



## Exercício 3

Determine se existe dois elementos distintos  $x, y$  em  $L$  tal que  $x+y=\text{sum}$ . Seja  $n$  ( $1 \leq n \leq 10^6$ ) o tamanho do vetor. Qual é o método mais viável para esse problema.

- Para cada elemento  $x$ , faça uma busca binária pelo elemento  $\text{sum}-x$ .
- Insira cada elemento em uma tabela de dispersão. Antes de inserir, verifique se  $\text{sum}-x$  está presente na tabela de dispersão.

Leia:

http:

[//marathoncode.blogspot.com.br/2012/10/sum-problem.html](http://marathoncode.blogspot.com.br/2012/10/sum-problem.html)

# Sum problem

```
bool twosum(vector<int> &v, int sum)
{
    int i, j;
    sort(v.begin(), v.end());
    i = 0;
    j = v.size() - 1;

    while( i < j)
    {
        if( v[i] + v[j] == sum) return true;
        else if( v[i] + v[j] > sum){
            j--;
        } else {
            i++;
        }
    }
    return false;
}
```

# Sum problem

```
bool twosum_with_map(vector<int> &v, int sum)
{
    map<int, int> mapa;
    map<int, int>::iterator it;
    for(int i = 0; i < (int) v.size(); i++)
    {
        it = mapa.find(sum-v[i]);
        if( it != mapa.end() ) return true;
        mapa[v[i]] = i;
    }
}
```

# Sum problem

```
bool twosum_with_unordered_map(vector<int> &v, int sum)
{
    unordered_map<int, int> mapa;
    unordered_map<int, int>::iterator it;
    for(int i = 0; i < (int) v.size(); i++)
    {
        it = mapa.find(sum-v[i]);
        if( it != mapa.end() ) return true;
        mapa[v[i]] = i;
    }
}
```

# Testes computacionais

```
twosum
Found
time                =      5.18100
twosum\_with\_map
Found
time                =      0.00200
twosum\_with\_unordered\_map
Found
time                =      0.00300
```

## STL priority\_queue

| Função  | Descrição  | Complexidade |
|---------|--|--------------|
| empty() | verifica se a fila de prioridade está vazia      | $O(1)$       |
| size()  | devolve o número de elementos na estrutura       | $O(1)$       |
| push()  | insere um novo elemento na fila de prioridade    | $O(\lg n)$   |
| pop()   | remove o elemento do topo da fila de prioridade  | $O(\lg n)$   |
| top()   | devolve o elemento do topo da fila de prioridade | $O(1)$       |

## Exemplo 1: priority\_queue

```
#include <iostream>
#include <algorithm>
#include <queue>
using namespace std;
int main()
{
    //fila de prioridade mínima
    priority_queue<int, vector<int>, greater<int>> > pq;
    pq.push(30); pq.push(20);
    pq.push(25); pq.push(40);
    while( !pq.empty() )
    {
        cout << pq.top() << " ";
        pq.pop();
    }
    cout << endl;
    //20 25 30 40
}
```

## Exemplo 2: priority\_queue

```
#include <iostream>
#include <algorithm>
#include <queue>
using namespace std;
int main()
{
    //fila de prioridade mínima
    priority_queue<int, vector<int>, greater<int>> > pq;
    pq.push(30); pq.push(20);
    pq.push(25); pq.push(40);
    while( !pq.empty() )
    {
        cout << pq.top() << " ";
        pq.pop();
    }
    cout << endl;
    //20 25 30 40
}
```



## Exemplo 3: priority\_queue

```
#include <iostream>
#include <algorithm>
#include <queue>
using namespace std;
int main()
{
    //fila de prioridade máxima
    priority_queue<int, vector<int>, less<int>> > pq;
    pq.push(30); pq.push(20);
    pq.push(25); pq.push(40);
    while( !pq.empty() )
    {
        cout << pq.top() << " ";
        pq.pop();
    }
    cout << endl;
    //40 30 25 20
}
```

## Exemplo 4: priority\_queue

```
#include <iostream>
#include <algorithm>
#include <queue>
using namespace std;
typedef bool (*comp)(int, int);
bool compare(int a, int b)
{
    return (a<b);
}
int main()
{
    int v[] = {10,60,50,20};
    priority_queue<int> pq1(v,v+4); //default less<int>
    priority_queue<int, vector<int>, comp> pq2(compare);
    pq2.push(10); pq2.push(60);
    pq2.push(50); pq2.push(20);
    while( !pq2.empty() )
    {
        cout << pq2.top() << " ";
        pq2.pop();
    }
    cout << endl;
}
```

## Exemplo 5 priority\_queue

```
#include <iostream>
#include <queue>
using namespace std;

class Human {
public:
    string name;
    int age;
    Human(string name, int age);
};

Human::Human(string name, int age) : name(name), age(age) {}
bool operator<(Human a, Human b) {return (a.age < b.age);}

int main() {

    Human p1("Child",5);
    Human p2("Grandfather",70);
    priority_queue<Human> Q;
    Q.push(p1);
    Q.push(p2);

}
```

## Exemplo 6 priority\_queue

```
#include <iostream>
#include <algorithm>
#include <vector>
#include <queue>
#include <time.h>
#include <stdio.h>
using namespace std;
typedef vector<int> vi;
int main(){
    clock_t clk;
    double elapsed;
    default_random_engine generator;
    uniform_int_distribution<int> distribution(1, 1000000000);
    vi v1, v2;
    for(int i = 0; i < 10000000; i++){
        int x = distribution(generator);
        v1.push_back ( x );v2.push_back ( x );
    }
    clk = clock();
    sort(v1.begin(), v1.end(), greater<int>());
    for(int i = 0; i < 10; i++) cout << v1[i] << " ";
    cout << endl;
    elapsed = ((double) (clock() - clk)) / CLOCKS_PER_SEC;
    printf("time %10.5f\n", elapsed);
```

## Exemplo 6 priority\_queue

```
clk = clock();
make_heap(v2.begin(), v2.end());
for(int i = 0; i < 10; i++){
    cout << v2.front() << " ";
    std::pop_heap(v2.begin(), v2.end());
    v2.pop_back();
}
cout << endl;
elapsed = ((double) (clock() - clk)) / CLOCKS_PER_SEC;
printf("time_#####=%10.5f\n", elapsed);
clk = clock();
priority_queue<int> pq(v1.begin(), v1.end());
for(int i = 0; i < 10; i++){
    cout << pq.top() << " "; pq.pop();
}
cout << endl;
elapsed = ((double) (clock() - clk)) / CLOCKS_PER_SEC;
printf("time_#####=%10.5f\n", elapsed);
}
```

## Exemplo 6 priority\_queue

```
999999945 999999761 999999642 999999323 999999321 999999264
999999229 999999227 999999125 999999055
time = 6.89800
999999945 999999761 999999642 999999323 999999321 999999264
999999229 999999227 999999125 999999055
time = 1.16000
999999945 999999761 999999642 999999323 999999321 999999264
999999229 999999227 999999125 999999055
time = 1.66500
```

# Exemplo UnionFind

```
#include <iostream>
#include <vector>
#include <stdio.h>
using namespace std;
class UnionFind {
private:
    vector<int> p, rank, setSize;
    int numSets;
public:
    UnionFind(int N): numSets(N){
        rank.resize(N,0); p.resize(N,0); setSize.resize(N,1);
        for(int i=0; i<N; i++) p[i]=i;
    }
    int findSet(int i) {
        return (p[i]==i)? i : (p[i] = findSet(p[i]));
    }
    bool isSameSet(int i, int j){
        return findSet(i) == findSet(j);
    }
}
```

# Exemplo UnionFind

```
void unionSet(int i, int j){
    if( !isSameSet(i,j)){
        numSets--;
        int x = findSet(i), y = findSet(j);
        if(rank[x]>rank[y]){ p[y]=x; setSize[x] += setSize[y]; }
        else{
            p[x]=y; setSize[y] += setSize[x];
            if(rank[x]==rank[y]) rank[y]++; }
    }
}

int numDisjointSets(){ return numSets; }
int sizeOfSet(int i){ return setSize[findSet(i)]; }
};
```



# Exemplo UnionFind

```
int main(){
    UnionFind Set(10);
    Set.unionSet(5,6);
    Set.unionSet(6,7);
    cout << Set.numDisjointSets() << endl;
    Set.unionSet(0,1);
    cout << Set.numDisjointSets() << endl;
    Set.unionSet(5,8);
    cout << Set.numDisjointSets() << endl;
    cout << Set.sizeOfSet(5) << endl;
}
```

# Table

| i | 1 | 2     | 3     | 4     | 5     |
|---|---|-------|-------|-------|-------|
| f | 1 | 1     | 2     | 2     | 3     |
|   | 1 | 1...2 | 1...3 | 1...4 | 1...5 |
| c | 1 | 3     | 6     | 10    | 15    |

# Table

```
#include <stdio.h>
#include <vector>

using namespace std;
class Table{
private:
    vector<int> t;
public:
    Table(int n){t.assign(n+1,0);}
    read(int b){ return t[b];}
    void update(int k, int v){
        for( ; k < (int)t.size(); k++) t[k] += v;
    }
    int range(int a, int b){return read(b)-read(a-1);}
};

int main(){
    int f[] = {2,4,5,5,6,6,6,7,7,8,9};
    Table t(10);
    for(int i = 0; i < 10; i++) t.update(i+1,f[i]); //11
    printf("fst(1,3) = %d\n", t.range(1,3) );
}
```

# Sparse Table

```
#include <stdio.h>
#include <vector>
#include <math.h>

using namespace std;
class SparseTable{
private:
    int n;
    vector <int> A;
    vector < vector <int> > lookup;
    void process();
public:
    SparseTable(const vector <int> &A);
    int query(int L, int R);
};
```

# Sparse Table

```
SparseTable::SparseTable(const vector<int> &A){
    A = _A;
    n = _A.size();
    lookup.resize( n );
    for(int i =0; i < n; i++){
        lookup[i].resize( (int)(ceil(log2(n))), 0 );
        process();
    }

void SparseTable::process(){
    //inicialize lookup para intervalo com tamanho 1
    for(int i = 0; i < n; i++){
        lookup[i][0] = A[i];
    }
    //compute o valor de intervalos maiores
    //a partir de intervalos menores
    for(int j = 1; 1 << j <= n; j++){
        for(int i = 0; i+(1<<j)-1<n; i++){
            lookup[i][j] = lookup[i][j-1] + lookup[i+(1<<(j-1))][j-1];
        }
    }
}
```

# Sparse Table

```
int SparseTable::query(int L, int R){
    if(L==R){
        return lookup[L][0];
    }else{
        int j = (int) log2(R-L+1);
        return lookup[L][j] + query(L+(1<<j),R);
    }
}

int main(){
    int f[] = {1,2,3,4,5,6,7};
    vector<int> A(f,f+7);
    SparseTable st(A);
    printf("query(%d,%d) = %d\n", 2,4, st.query(2,6) );
}
```

# Binary Indexed Tree

|    |   |       |   |       |   |       |   |       |   |
|----|---|-------|---|-------|---|-------|---|-------|---|
| i  | 1 | 2     | 3 | 4     | 5 | 6     | 7 | 8     | 9 |
| f  | 1 | 2     | 3 | 4     | 5 | 6     | 7 | 8     | 9 |
|    | 1 | 1...2 | 3 | 1...4 | 5 | 5...6 | 7 | 1...8 | 9 |
| st | 1 | 3     | 3 | 10    | 5 | 11    | 7 | 36    | 9 |

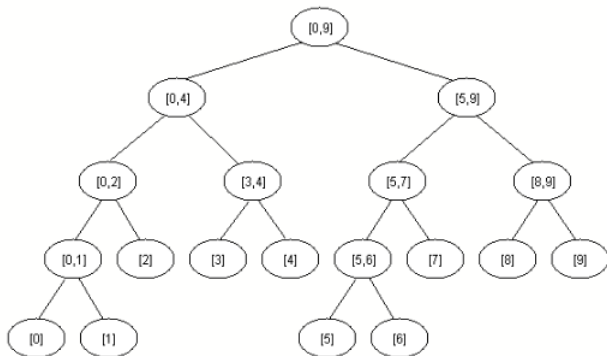
- Para alterar o valor de  $f[3]$  precisamos atualizar  $st[3], st[4], st[8]$ .
- Precisamos somar ( $1 \ll$  posição do bit menos significativo).
  - ▶  $3 = (11)_2 + (01)_2 = (100)_2 = 4$
  - ▶  $4 = (100)_2 + (100)_2 = (1000)_2 = 8$
  - ▶  $8 = (1000)_2 + (1000)_2 = (10000)_2 = 16$
- Para calcular  $f[1] + \dots + f[6]$  precisamos somar  $st[6] + st[4]$
- Precisamos decrementar ( $1 \ll$  posição do bit menos significativo).
  - ▶  $6 = (110)_2 - (10)_2 = (100)_2 = 4$
  - ▶  $4 = (100)_2 - (100)_2 = (000)_2 = 0$

# Segment Tree

```
#include <stdio.h>
#include <vector>
using namespace std;
class FenwickTree{
private:
vector <int> ft;
public:
FenwickTree(int n){ ft.assign(n+1,0);}
int read(int b){
int sum = 0;
for(; b; b -= (b & -b)) sum+= ft[b];
return sum;
}
void update(int k ,int v){
for( ; k < (int) ft.size(); k += (k & -k) ) ft[k] += v;
}
int range(int a, int b){
if(a==0) return read(b);
else return read(b) - read(a-1);
}
};
```



# Segment Tree



# Segment Tree

```
class SegmentTree {
private:
    vector<int> st,A;
    int n;
    int left(int p) { return p << 1;}
    int right(int p){ return (p << 1) + 1; }

    void build(int p, int L, int R);
    int rmq(int p, int L, int R, int i, int j);

public:
    SegmentTree(const vector<int> &A){
        A = _A;
        n = (int)A.size();
        //  $2 * 2^{(\text{floor}(\lg n) + 1)} = O(4n)$ 
        st.assign(4*n,0);
        build(1, 0, n-1);
    }

    int rmq(int i, int j){ return rmq(1,0,n-1,i,j); }
}
```

# Segment Tree

```
void build(int p, int L, int R){
    if(L==R){
        st[p]=L;
    }else{
        build(left(p), L, (L+R)/2);
        build(right(p), (L+R)/2+1, R);
        int p1 = st[left(p)];
        int p2 = st[right(p)];
        st[p] = (A[p1]<=A[p2])? p1 : p2;
    }
}
```

# Segment Tree

```
int rmq(int p, int L, int R, int i, int j) {  
    if (i > R || j < L) return -1;  
    if (L >= i && R <= j) return st[p];  
    int p1 = rmq(left(p), L, (L + R) / 2, i, j);  
    int p2 = rmq(right(p), (L + R) / 2 + 1, R, i, j);  
  
    if (p1 == -1) return p2;  
    if (p2 == -1) return p1;  
    return (A[p1] <= A[p2]) ? p1 : p2;  
}
```

# Segment Tree

```
void update(int p, int L, int R, int i)
{
    if( L == R) return ;
    if( i >= L && i <= R)
    {
        int mid = L+R/2;
        if( i <= mid ) update(left(p) , L, (L+R)/2, i);
        else update(right(p), (L+R)/2 + 1, R, i);
        int p1 = st[left(p)];
        int p2 = st[right(p)];
        st[p] = (A[p1]<=A[p2])? p1:p2;
    }
}
```

# Segment Tree

```
class SegmentTree {
private:
    //
public:
    SegmentTree(const vector<int> &A){
        A = _A; n = (int)A.size(); st.assign(4*n,0);
        build(1, 0, n-1);
    }
    int update(int k, int val){A[k] = val; update(1,0,n-1,k)};
    int rmq(int i, int j){ return A[rmq(1,0,n-1,i,j)]};
};

int main(){
    int arr[] = {18,17,13,19,15,11,20};
    vector<int> A(arr, arr+7);
    SegmentTree st(A);
    printf("RMQ(4,6) = %d\n", st.rmq(4,6));
    printf("RMQ(1,3) = %d\n", st.rmq(1,3));
    st.update(2,10);
    printf("RMQ(1,3) = %d\n", st.rmq(1,3));
}
```

# Grafo : Matriz Adjacência

```
#include <vector>
#include <iostream>
using namespace std;

class Graph{
private:
    vector<vector<bool>> M;
public:
    int N;
    Graph(int N): N(N){
        M.resize(N);
        for(int j=0;j<N;j++){
            M[j].resize(N, false);
        }
    }
    vector<bool>& operator [](int i) { return M[i]; }
    edge(int a, int b, bool directed = false){
        M[a][b]=1;
        if(!directed)M[b][a]=1;
    }
};
```

# Grafo : Matriz Adjacência

```
void dfs(Graph & G, vector<int> &visited , int i){  
    if (!visited[i]){  
        cout << "visitando_" << i << endl;  
        visited[i] = true;  
        for(int j = 0; j < G.N; j++){  
            if(G[i][j]){  
                dfs(G, visited , j);  
            }  
        }  
    }  
}
```

```
bool conexo(Graph & G){  
    vector<int> visited;  
    visited.assign(G.N, false);  
    dfs(G, visited , 0);  
    for(int i = 0; i < (int)visited.size(); i++){  
        if (!visited[i]) return false;  
    }  
    return true;  
}
```



# Grafo : Matriz Adjacência

```
int main(){
    Graph G(5);
    G.edge(0,1);
    G.edge(1,2);
    G.edge(3,4);
    cout << (conexo(G) ? "conexo" : "desconexo") << endl;
    G.edge(2,3);
    cout << (conexo(G) ? "conexo" : "desconexo") << endl;
}
```

# Grafo : Matriz Lista de Adjacência

```
#include <vector>
#include <iostream>
using namespace std;

class Graph{
public:
    int N;
    vector<vector<int>> > adj;
    Graph(int N): N(N){
        adj.resize(N);
    }
    edge(int a, int b, bool directed = false){
        adj[a].push_back(b);
        if(!directed) adj[b].push_back(a);
    }
};
```

# Grafo : Matriz Lista de Adjacência

```
void dfs(Graph & G, vector<int> &visited , int i){
    if(!visited[i]){
        cout << "visitando_" << i << endl;
        visited[i] = true;
        for(int j = 0; j < G.adj[i].size(); j++){
            int u = G.adj[i][j];
            dfs(G, visited , u);
        }
    }
}

bool conexo(Graph & G){
    vector<int> visited;
    visited.assign(G.N, false);
    dfs(G, visited , 0);
    for(int i = 0; i < (int)visited.size(); i++){
        if(!visited[i]) return false;
    }
    return true;
}
```