Two pointer and Binary Search Professor Wladimir

Two pointer

```
Solução Trivial: \mathcal{O}(n^2)
Solução two pointer com vetor ordenado: \mathcal{O}(n)
Solução two pointer com vetor não ordenado: \mathcal{O}(n \log n)
```

Two Integer Sum II

Given an array of integers numbers that is sorted in non-decreasing order.

Return the indices (1-indexed) of two numbers, [index1, index2], such that they add up to a given target number target and index1 i index2. Note that index1 and index2 cannot be equal, therefore you may not use the same element twice.

There will always be exactly one valid solution.

Your solution must use $\mathcal{O}(1)$ additional space.

```
vector<int> twoSum(vector<int>& numbers, int target) {
           vector <int> res;
           int i = 0;
3
           int j = numbers.size() - 1;
           while(i < j){
               int A = numbers[i];
                int B = numbers[j];
                if(A+B == target){
10
                    res.push_back(i+1);
11
12
                    res.push_back(j+1);
13
                    return res;
                }else if(A+B < target){</pre>
14
                    i++;
15
                }else {
16
                    j--;
17
18
           }
19
       }
20
```

```
Solução Trivial: \mathcal{O}(n^3)
Solução two pointer : \mathcal{O}(n^2)
```

Given an integer array nums, return all the triplets [nums[i], nums[j], nums[k]] where nums[i] + nums[j] + nums[k] == 0, and the indices i, j and k are all distinct.

The output should not contain any duplicate triplets. You may return the output and the triplets in any order.

```
Example 1:

Input: nums = [-1,0,1,2,-1,-4]

Output: [[-1,-1,2],[-1,0,1]]

Explanation:

nums[0] + nums[1] + nums[2] = (-1) + 0 + 1 = 0.

nums[1] + nums[2] + nums[4] = 0 + 1 + (-1) = 0.

nums[0] + nums[3] + nums[4] = (-1) + 2 + (-1) = 0.

The distinct triplets are [-1,0,1] and [-1,-1,2].
```

```
vector<vector<int>>> threeSum(vector<int>& nums) {
1
2
       vector< vector<int> > triplet;
3
4
5
       set < vector<int> > s;
6
       sort(nums.begin(), nums.end() );
       for(int i = 0; i < nums.size()-2; i++){</pre>
10
           if(i > 0 && nums[i] == nums[i-1]) continue;
11
           if( nums[i] > 0) break;
12
           int j = i+1;
13
           int k = nums.size() - 1;
14
           int target = -nums[i];
15
           cout << "target " << target << endl;</pre>
16
           while(j < k){
17
                int soma = nums[j] + nums[k];
18
19
                if(soma == target){
                    //triplet.push_back({nums[i], nums[j], nums[k]});
20
                    s.insert({nums[i], nums[j], nums[k]});
21
                    j++;
22
23
                    k--;
                }else if(soma > target){
24
                    k--;
25
                }else{
                    j++;
                }
28
29
30
           }
31
32
       for(auto triple : s){
33
           triplet.push_back(triple);
35
       return triplet;
36
37 }
```

```
vector<vector<int>> threeSum(vector<int>& nums) {
       vector<vector<int>>> res;
       sort(nums.begin(), nums.end());
3
4
       for(int i = 0; i < nums.size() - 2; i++){</pre>
           //pula os elementos repetidos já processados
6
           if(i > 0 && nums[i] == nums[i-1]) continue;
8
           int target = -nums[i];
           int start = i + 1;
10
           int end = nums.size() - 1;
11
12
           while(start < end){</pre>
13
                int sum = nums[start] + nums[end];
14
                if(sum == target){
15
                    res.push_back({nums[i], nums[start], nums[end]});
16
                    //pula elementos repetidos
17
                    while(start < end && nums[start] == nums[start + 1]) start++;</pre>
18
                    //pula elementos repetidos
19
                    while(start < end && nums[end] == nums[end - 1]) end--;</pre>
20
21
                    start++;
                    end--;
22
                } else if(sum < target){</pre>
23
                    start++;
                } else {
25
                    end--;
26
                }
27
           }
29
30
31
       return res;
32 }
```

Binary Search

Search a 2D Matrix

You are given an m x n 2-D integer array matrix and an integer target.

- Each row in matrix is sorted in non-decreasing order.
- The first integer of every row is greater than the last integer of the previous row.

Return true if target exists within matrix or false otherwise. Can you write a solution that runs in $O(\log(m * n))$ time?

```
bool searchMatrix(vector<vector<int>>& matrix, int target) {
2
3
           int start = 0;
4
           int end = matrix.size() - 1;
5
           int sol = -1;
6
           //Encontrando o maior indice da linha em que o primeiro elemento é menor ou
7
            \rightarrow igual ao target
           while( start <= end ){</pre>
8
                int mid = (start +end)/2;
10
                if( matrix[mid][0] <= target ){</pre>
11
                    sol = mid;
12
                    start = mid+1;
13
                }else{
14
                    end = mid-1;
15
                }
16
17
18
           if(sol == -1) return false;
19
            //cout << "linha " << sol << endl;
21
22
           start = 0;
23
            end = matrix[sol].size() - 1;
25
           while( start <= end ){</pre>
26
                int mid = (start + end)/2;
28
                if( matrix[sol][mid] == target ){
29
                    return true;
30
                }else if( matrix[sol][mid] > target ){
31
                    end = mid-1;
32
                }else {
33
                    start = mid+1;
34
           }
36
37
           return false;
38
39
       }
40
```

```
1 bool searchMatrix(vector<vector<int>>% matrix, int target) {
       int n = matrix.size(); // rows
3
       int m = matrix[0].size(); //cols
4
       int start = 0;
6
       int end = n*m - 1;
8
       while( start <= end){</pre>
9
          int r, c, mid;
10
          mid = (start + end)/2;
11
12
          r = mid/m;
13
          c = mid\%m;
14
15
          if( matrix[r][c] == target )
16
17
               return true;
           else if( matrix[r][c] > target){
18
               end = mid - 1;
19
           }else{
20
               start = mid + 1;
21
22
23
       }
24
       return false;
25
26 }
```