```
In [258... from sklearn.model_selection import train_test_split
          from sklearn.preprocessing import StandardScaler, OneHotEncoder
          from sklearn.decomposition import PCA
          import numpy as np
          from sklearn.metrics import precision_score, recall_score, f1_score
          from RevGEN_MLP import RevGEN_MLP
          import pandas as pd
          import matplotlib.pyplot as plt
          import seaborn as sns
          \textbf{from} \ \texttt{scipy.stats} \ \textbf{import} \ \texttt{gaussian\_kde}
          from matplotlib.colors import ListedColormap
          from sklearn.ensemble import IsolationForest,RandomForestClassifier
          from sklearn.metrics import accuracy_score
          from sklearn.model selection import StratifiedKFold
          from sklearn.model_selection import cross_val_score
          import torch
          import torch.nn as nn
           import torch.optim as optim
          from sklearn.metrics import accuracy_score, classification_report
```

RevGEN-MLP

Loading and Preparing Data for Training

```
In [259... df = pd.read_csv("wine+quality\\winequality-white.csv", sep=";") # Insert path to dataset here
          df['good'] = (df['quality'] >= 7).astype(int)
          X = df.drop(['quality', 'good'], axis=1)
          y = df['good']
          column names = X.columns
          X = X.values
         y = y.values
In [260... # Split into train/test
         X_train, X_test, y_train, y_test= train_test_split(
             X, y, test_size=0.2, random_state=42, stratify=y
         # One-hot encode labels
          encoder = OneHotEncoder(sparse_output=False)
          y_train_encoded = encoder.fit_transform(y_train.reshape(-1, 1))
         y_test_encoded =encoder.transform(y_test.reshape(-1, 1))
          # Scale features
          ANN_scaler = StandardScaler()
          X_train_scaled = ANN_scaler.fit_transform(X_train)
          X_test_scaled = ANN_scaler.transform(X_test)
```

Training RevGEN-MLP

```
In [261... num_layer = 3
         num_epochs = 101
In [262... # Set seed for reproducibility
          np.random.seed(42)
          # Initialize model
          model = RevGEN MLP(
             n_layers=num_layer,
              x=X_train_scaled[0].reshape(-1, 1),
              y_actual=y_train_encoded[0].reshape(-1, 1),
              epochs=num_epochs,
             loss_function="cross_entropy"
          # Training Loop
          for epoch in range(num_epochs):
             loss epoch = 0
              correct_train = 0
              # Shuffle training indices
              indices = np.random.permutation(X_train_scaled.shape[0])
              for i in indices:
                  x_sample = X_train_scaled[i].reshape(-1, 1)
                  y_sample = y_train_encoded[i].reshape(-1, 1)
                  # Train and accumulate loss
```

```
model.train(input=x_sample, target=y_sample)
                  loss_epoch += model.loss_fn(input=x_sample, target=y_sample)
                  # Predict and count correct predictions
                  pred = model.forward(x_sample)
                  if np.argmax(pred[:2]) == np.argmax(y_sample):
                      correct_train += 1
              # Compute average training metrics
              avg_train_loss = loss_epoch / X_train_scaled.shape[0]
              train_accuracy = correct_train / X_train_scaled.shape[0]
              # Evaluate on test set every 10 epochs
              if epoch % 10 == 0 or epoch == num_epochs - 1:
                  correct_test = 0
                  test_loss_epoch = 0
                  for i in range(X_test_scaled.shape[0]):
                      x_sample = X_test_scaled[i].reshape(-1, 1)
                      y_sample = y_test_encoded[i].reshape(-1, 1)
                      pred = model.forward(x sample)
                      if np.argmax(pred[:2]) == np.argmax(y_sample):
                          correct_test += 1
                      test_loss_epoch += model.loss_fn(input=x_sample, target=y_sample)
                  avg_test_loss = test_loss_epoch / X_test_scaled.shape[0]
test_accuracy = correct_test / X_test_scaled.shape[0]
                  print(f"Epoch {epoch:3d} | "
                         f"Train Loss: {avg_train_loss:.4f} | Train Acc: {train_accuracy * 100:.2f}% | "
                        f"Test Loss: {avg_test_loss:.4f} | Test Acc: {test_accuracy * 100:.2f}%")
         Epoch 0 | Train Loss: 0.5016 | Train Acc: 77.44% | Test Loss: 0.4701 | Test Acc: 78.16%
         Epoch 10 | Train Loss: 0.3573 | Train Acc: 81.60% | Test Loss: 0.4194 | Test Acc: 78.16%
         Epoch 20 | Train Loss: 0.3402 | Train Acc: 83.51% | Test Loss: 0.4025 | Test Acc: 80.82%
         Epoch 30 | Train Loss: 0.3296 | Train Acc: 83.97% | Test Loss: 0.3938 | Test Acc: 82.24%
         Epoch 40 | Train Loss: 0.3293 | Train Acc: 83.92% | Test Loss: 0.3862 | Test Acc: 81.94%
         Epoch 50 | Train Loss: 0.3202 | Train Acc: 84.64% | Test Loss: 0.3898 | Test Acc: 81.63%
         Epoch 60 | Train Loss: 0.3135 | Train Acc: 85.17% | Test Loss: 0.3814 | Test Acc: 82.35%
         Epoch 70 | Train Loss: 0.3057 | Train Acc: 85.40% | Test Loss: 0.3785 | Test Acc: 82.35%
         Epoch 80 | Train Loss: 0.2987 | Train Acc: 85.71% | Test Loss: 0.3795 | Test Acc: 82.55%
         Epoch 90 | Train Loss: 0.2936 | Train Acc: 86.29% | Test Loss: 0.3792 | Test Acc: 82.55%
         Epoch 100 | Train Loss: 0.2876 | Train Acc: 86.65% | Test Loss: 0.3653 | Test Acc: 83.37%
In [263... correct = 0
          y_preds = []
          y_true = []
          for i in range(X_test_scaled.shape[0]):
              x sample = X test scaled[i].reshape(-1, 1)
              y_sample = y_test_encoded[i].reshape(-1, 1)
              pred = model.forward(x_sample)
              pred_class = np.argmax(pred[0:2])
              true_class = np.argmax(y_sample)
              y_preds.append(pred_class)
              y_true.append(true_class)
              if pred_class == true_class:
                  correct += 1
          x_sample = X_test_scaled[0].reshape(-1, 1)
          pred = model.forward(x_sample)
          test_accuracy = correct / X_test_scaled.shape[0]
          precision = precision_score(y_true, y_preds, average='macro', zero_division=0)
          recall = recall_score(y_true, y_preds, average='macro', zero_division=0)
          f1 = f1_score(y_true, y_preds, average='macro', zero_division=0)
          print(f"Test Accuracy: {test_accuracy * 100:.2f}%")
          print(f"Precision:
                                  {precision * 100:.2f}%")
                                  {recall * 100:.2f}%")
          print(f"Recall:
         Test Accuracy: 83.37%
         Precision:
                        75.82%
         Recall:
                        72.14%
```

Invertibility Check

Small reconstruction errors close to zero are expected due to floating-point precision limits

```
In [264... x_sample = X_test_scaled[0].reshape(-1, 1)
          x_sample_unscaled = ANN_scaler.inverse_transform(x_sample.reshape(1, -1))
          print("Original Sample:", x_sample_unscaled)
          # Forward pass
          pred = model.forward(x_sample)
          print("\nOutput (Classes):", pred[0:2].ravel())
          print("Output (Latent Variable):", pred[2:].ravel())
          # Reconstruct
          reconstructed_sample = model.reverse(pred)
          # Unscale reconstruction
          reconstructed_sample_unscaled = ANN_scaler.inverse_transform(
              reconstructed_sample.reshape(1, -1)
          print("\nReconstructed Sample:", reconstructed_sample_unscaled.ravel())
          mse_scaled = np.mean((x_sample - reconstructed_sample)**2)
          mse_unscaled = np.mean((x_sample_unscaled - reconstructed_sample_unscaled)**2)
          print("\nMSE Error (Scaled Data): ", mse_scaled)
print("MSE Error (Unscaled Data): ", mse_unscaled)
         Original Sample: [[6.0000e+00 1.7000e-01 3.6000e-01 1.7000e+00 4.2000e-02 1.4000e+01
           6.1000e+01 9.9144e-01 3.2200e+00 5.4000e-01 1.0800e+01]]
         Output (Classes): [0.98050259 0.01949741]
         Output (Latent Variable): [ 3.92619796e+00 -4.75037097e-02 -3.29723407e-02 -1.94034664e-02
          -3.49284453e-02 -1.56047654e-03 -4.75244660e-02 9.84343548e-01
          -6.25475829e-02]
         Reconstructed Sample: [6.00000000e+00 1.70000000e-01 3.60000000e-01 1.70000002e+00
          4.20000001e-02 1.39999999e+01 6.10000002e+01 9.91440000e-01
          3.22000000e+00 5.3999999e-01 1.08000000e+01]
         MSE Error (Scaled Data): 2.2025489842542087e-17
         MSE Error (Unscaled Data): 3.1172022567704e-15
```

Generation

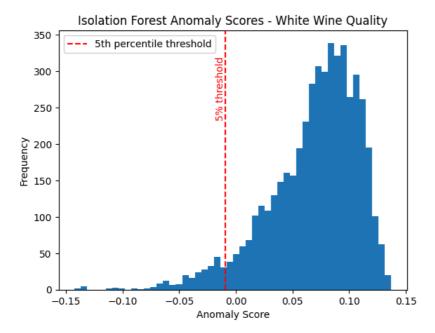
```
In [265... detector = IsolationForest(random_state=42).fit(X)

scores = detector.decision_function(X)

# Plot histogram
plt.hist(scores, bins=50)
threshold = np.percentile(scores, 5)
plt.axvline(threshold, color='red', linestyle='--', label='5th percentile threshold')

# Add Label
plt.text(threshold, plt.ylim()[1]*0.9, '5% threshold', color='red', rotation=90, va='top', ha='right')

plt.title("Isolation Forest Anomaly Scores - White Wine Quality")
plt.xlabel("Anomaly Score")
plt.ylabel("Frequency")
plt.legend()
plt.show()
```

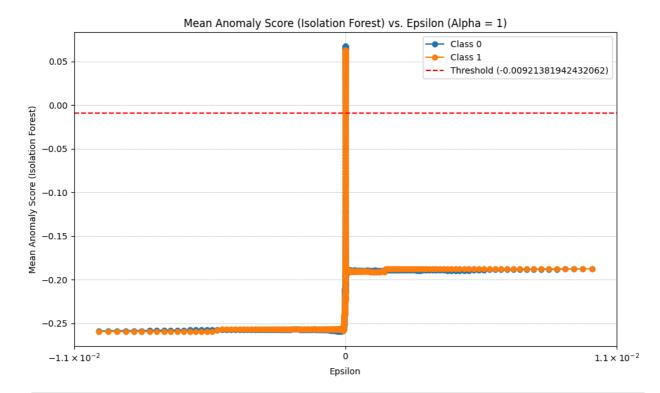


```
In [266...
         def generate_data_with_epsilon(model,epsilon):
              pred_classes = []
              inputs = []
              original_inputs = []
              original_classes = []
              original_prob = []
              pred_probability = []
              for test,truth in zip(X_test_scaled,y_test_encoded):
                  x_sample = test.reshape(-1, 1)
                  pred = model.forward(x sample)
                  class_probs = pred[0:2].ravel()
                  max_prob = np.max(class_probs)
                  if np.argmax(pred[:2]) == np.argmax(truth):
                      if max_prob >= 0.8:
                          original_prob.append(max_prob)
                          pred_class = np.argmax(class_probs)
                          original\_inputs.append (ANN\_scaler.inverse\_transform (x\_sample.reshape(1, -1))[0])
                          original_classes.append(pred_class)
                          vector = pred.copy()
                          vector[2:] = vector[2:] + epsilon
                          new_input = model.reverse(input=vector)
                          new_pred = model.forward(new_input)
                          max_prob = np.max(new_pred[0:2])
                          pred_probability.append(max_prob)
                          new_pred_class = np.argmax(new_pred[0:2])
                          new_input_unscaled = ANN_scaler.inverse_transform(new_input.reshape(1, -1))[0]
                          pred_classes.append(new_pred_class)
                          inputs.append(new_input_unscaled)
              # Build DataFrame
              data = {col: [] for col in column_names}
              data["Class"] = []
              data["Probability"] = []
              for sample in inputs:
                  for i, col in enumerate(column_names):
                      data[col].append(sample[i])
              for cls in pred_classes:
                  data["Class"].append(cls)
              for prob in pred_probability:
                  data["Probability"].append(prob * 100)
              generated_df = pd.DataFrame(data=data)
              return generated_df
```

Anomaly Score Threshold

The following code decides the anomaly score threshold used to guide generation. The first threshold represents moderately anomalous data whereas the second threshold represents extremely anomalous data.

```
In [267...
           threshold_1 = np.percentile(scores,5)
           threshold_2 = -0.15
In [268... exponents = np.linspace(-12, -2, 600)
          positive_epsilons = 10 ** exponents
negative_epsilons = -positive_epsilons
           epsilons = np.sort(np.concatenate([negative_epsilons, positive_epsilons]))
           threshold = threshold_1 # Change threshold as needed
           results = []
           \begin{tabular}{ll} \textbf{for} & \textbf{epsilon in epsilons:} \\ \end{tabular}
               generate_df = generate_data_with_epsilon(model, epsilon)
               anomaly_score_results = []
               for cls in generated df["Class"].unique():
                   subset = generated_df[generated_df["Class"] == cls]
                   features = subset.drop(columns=["Class", "Probability"]).to_numpy()
                   score = detector.decision_function(features)
                   anomaly_score_results.append({
                        "Class": cls,
                        "Score": score.mean()
                   })
               scored_df = pd.DataFrame(anomaly_score_results)
               mean score by class = scored df.set index("Class")["Score"]
               below_threshold = mean_score_by_class[mean_score_by_class < threshold].to_dict()</pre>
               results.append({
                    "epsilon": epsilon,
                    "mean_score": mean_score_by_class.to_dict(),
               })
In [269...
          class_names = []
           for r in results:
               for cls in r["mean_score"]:
                   if cls not in class_names:
                       class names.append(cls)
           class_names.sort()
           # PLot
           plt.figure(figsize=(10, 6))
           for cls in class_names:
               eps = []
               overlaps = []
               for r in results:
                   eps.append(r["epsilon"])
                   overlaps.append(r["mean_score"].get(cls))
               plt.plot(eps, overlaps, marker='o', label=f'Class {cls}')
           # Threshold line
           plt.axhline(y=threshold, color='red', linestyle='--', label=f'Threshold ({threshold})')
           # Log scale on x-axis
           plt.xlabel("Epsilon")
           plt.ylabel("Mean Anomaly Score (Isolation Forest)")
           plt.title("Mean Anomaly Score (Isolation Forest) vs. Epsilon (Alpha = 1)")
           plt.legend()
           plt.xscale("symlog")
           plt.grid(True, which="both", ls="--", linewidth=0.5)
           plt.tight_layout()
           plt.show()
```



```
In [270... best_epsilons = {}
          best_eps_overall = None
max_abs_eps = 0 # Track Largest absolute epsilon
           for cls in class_names:
               best_pos_eps = None
               best_neg_eps = None
               best pos diff = float('inf')
               best_neg_diff = float('inf')
               for r in results:
                   score = r["mean_score"].get(cls)
                   eps = r["epsilon"]
                   if score is not None and score < threshold:</pre>
                       diff = threshold - score
                       if eps > 0 and diff < best pos diff:</pre>
                           best pos diff = diff
                           best_pos_eps = eps
                       elif eps < 0 and diff < best_neg_diff:</pre>
                           best_neg_diff = diff
                           best_neg_eps = eps
               best_epsilons[cls] = {
    "best_positive": best_pos_eps,
                   "best_negative": best_neg_eps
               }
               for eps in [best_pos_eps, best_neg_eps]:
                   if eps is not None and abs(eps) > max_abs_eps:
                       max_abs_eps = abs(eps)
                       best_eps_overall = eps
           for cls, eps_dict in best_epsilons.items():
               print(f"Class {cls}:")
               print(f" Best positive epsilon: {eps_dict['best_positive']}")
               print(f" Best negative epsilon: {eps_dict['best_negative']}")
          print(f"\nBest overall epsilon across all classes: {best_eps_overall}")
         Class 0:
           Best positive epsilon: 3.7522389225313985e-08
           Best negative epsilon: -3.474573495735988e-08
         Class 1:
           Best positive epsilon: 2.8670089481484573e-08
           Best negative epsilon: -2.554733341531624e-08
         Best overall epsilon across all classes: 3.7522389225313985e-08
```

Generated Confidently Classified Anomalies

```
In [271... epsilon = max_abs_eps
          pred_classes = []
          inputs = []
          original_inputs = []
          original_classes = []
          original_prob = []
          pred_probability = []
          for test,truth in zip(X_test_scaled,y_test_encoded):
              x_sample = test.reshape(-1, 1)
              pred = model.forward(x_sample)
              class_probs = pred[0:2].ravel()
              max_prob = np.max(class_probs)
              if np.argmax(pred[:2]) == np.argmax(truth):
                  if max prob >= 0.8:
                      original_prob.append(max_prob)
                      pred_class = np.argmax(class_probs)
                      original_inputs.append(ANN_scaler.inverse_transform(x_sample.reshape(1, -1))[0])
                      original_classes.append(pred_class)
                      vector_neg_epsilon = pred.copy()
                      vector_neg_epsilon[2:] = vector_neg_epsilon[2:] - epsilon
                      # Revese pass for when epsilon is substracted to latent variables
                      new_input_neg = model.reverse(input=vector_neg_epsilon)
                      new_pred = model.forward(new_input_neg)
                      max_prob = np.max(new_pred[0:2])
                      pred_probability.append(max_prob)
                      new_pred_class_neg = np.argmax(new_pred[0:2])
                      vector_pos_epsilon = pred.copy()
                      vector_pos_epsilon[2:] = vector_pos_epsilon[2:] + epsilon
                      # Revese pass for when epsilon is added to latent variables
                      new_input_pos = model.reverse(input=vector_pos_epsilon)
                      new pred = model.forward(new input pos)
                      max_prob_pos = np.max(new_pred[0:2])
                      pred_probability.append(max_prob_pos)
                      new_pred_class_pos = np.argmax(new_pred[0:2])
                      new_input_unscaled_pos = ANN_scaler.inverse_transform(new_input_pos.reshape(1, -1))[0]
                      new\_input\_unscaled\_neg = ANN\_scaler.inverse\_transform(new\_input\_neg.reshape(1, -1))[0]
                      pred_classes.append(new_pred_class_pos)
                      inputs.append(new_input_unscaled_pos)
                      pred_classes.append(new_pred_class_neg)
                      inputs.append(new_input_unscaled_neg)
          data = {col: [] for col in column_names}
          data["Class"] = []
          data["Probability"] = []
          for sample in inputs:
              for i, col in enumerate(column_names):
                  data[col].append(sample[i])
          for cls in pred_classes:
              data["Class"].append(cls)
          for prob in pred_probability:
              data["Probability"].append(prob * 100)
          generated_df = pd.DataFrame(data=data)
In [272... generated_df = generated_df.drop_duplicates()
In [273... prediction_list = detector.predict(inputs).tolist()
          anomalies = prediction_list.count(-1) / len(inputs)
          print(f"Anomaly rate: {anomalies:.2%}")
          inputs = np.array(inputs)
          predictions = np.array(prediction_list)
          anomalous_inputs = inputs[predictions == -1]
```

```
generated_anomalies = pd.DataFrame(anomalous_inputs, columns=column_names)
          Anomaly rate: 53.18%
          generated_anomalies=generated_anomalies.drop_duplicates().reset_index(drop=True)
In [275... prediction list = detector.predict(X).tolist()
           anomalies = prediction_list.count(-1)/len(X)
           print(anomalies)
          0.06288280930992242
In [276...
          generated_anomalies
Out[276...
                    fixed
                              volatile
                                           citric
                                                                         free sulfur
                                                                                      total sulfur
                                                   residual
                                                                                                                 pH sulphates
                                                            chlorides
                                                                                                   density
                                                                                                                                  alcohol
                   acidity
                              acidity
                                           acid
                                                                           dioxide
                                                                                         dioxide
                                                     sugar
             0 6.086446
                             0.112474
                                       0.583002
                                                   9.735420 0.078754
                                                                          -8.140419
                                                                                      132.255094 0.997706 3.211788
                                                                                                                      0.235942 14.910125
                 9.597688
                             0.307134
                                       0.515876
                                                   2.180455 0.049811
                                                                          11.198634
                                                                                       15.950341 0.995507 2.859222
                                                                                                                      0.440415 10.810118
                 9.729108
                             0.101217
                                                                         -16.999349
                                                                                        2.872941 0.990959 2.941063
                                                                                                                      0.582996
                                                                                                                                 9.033697
                                       0.347579
                                                   3.575136 0.004413
                 5.555354
                             0.016548
                                       0.083258
                                                   1.278796 0.136015
                                                                          -6.542715
                                                                                      145.541693 0.998059 3.432095
                                                                                                                     -0.316792 14.705821
                 6 106977
                             0.398598
                                       0.658312
                                                   6 125418 0 092710
                                                                          40 878054
                                                                                      192 868882 0 996068 3 264201
                                                                                                                      0.365540
                                                                                                                                 9 252220
           575
                 7.254596
                             0.160508 -0.071140
                                                  -6.603866 0.060905
                                                                         118.752057
                                                                                      244.464510 0.993339 3.474930
                                                                                                                      0.406945 10.869855
                 7.745404
           576
                             0.379492
                                       0.691140
                                                  18.203867 0.053095
                                                                         143.247943
                                                                                      381.535492 0.995861 2.885070
                                                                                                                      0.773055 10.130145
                 6.570582
                             0.345718
                                       0.578047
                                                  35.604521
                                                             0.082153
                                                                          33.619794
                                                                                      269.186573 1.008135 2.927249
                                                                                                                      0.262278 13.835876
           578
                 5.932483
                            -0.012909 -0.368617
                                                  -3.227965 0.002782
                                                                         -43.001946
                                                                                        0.231800 0.986019 3.603846
                                                                                                                      0.540398
                                                                                                                                7.963634
                                                                                                                      0.747697 10.223431
           579
                 6.667309
                             0.126884
                                       0.114089
                                                  -4.393753 0.012747
                                                                         -15.603043
                                                                                       60.836853 0.986529 3.447220
```

580 rows × 11 columns

Transferability Of Confidently Clasified Anomalies

Testing Settings

```
In [277... confidence_threshold = 0.8
```

Randomn Forest

```
RF model = RandomForestClassifier(n estimators=200, random state=42)
In Γ278...
          RF_model.fit(X_train,y_train)
          y_pred = RF_model.predict(X_test)
           test_acc = accuracy_score(y_test, y_pred)
          test_precision = precision_score(y_test, y_pred,average="macro")
          test_recall = recall_score(y_test, y_pred,average="macro")
          print("Test Accuracy:", test_acc)
print("Test Precision:", test_precision)
          print("Test Recall:", test_recall)
         Test Accuracy: 0.8908163265306123
         Test Precision: 0.8663732677590605
         Test Recall: 0.7937426297169812
In [279... probs_all = RF_model.predict_proba(generated_anomalies.values)
          max_probs = np.max(probs_all, axis=1)
          pred_classes = np.argmax(probs_all, axis=1)
          mask = max_probs >= confidence_threshold
          RF_anomalies_list = generated_anomalies.values[mask]
          max_prob_rf = pred_classes[mask]
          high_confidence_count = np.sum(mask)
```

```
In [280... robustness = high_confidence_count/len(generated_anomalies.values)
    print(robustness)

0.3120689655172414

In [281... RF_df = pd.DataFrame(RF_anomalies_list, columns = column_names)

In [282... len(RF_anomalies_list)

Out[282... 181
```

Testing On Neural Networks

```
np.random.seed(42)
 torch.manual_seed(42)
 torch.cuda.manual seed all(42)
 torch.backends.cudnn.deterministic = True
 torch.backends.cudnn.benchmark = False
 # Model architecture
 class SimpleNet(nn.Module):
     def __init__(self, input_dim):
        super(SimpleNet, self).__init__()
         self.net = nn.Sequential(
            nn.Linear(input_dim, 64),
            nn.ReLU(),
            nn.Linear(64, 32),
             nn.ReLU(),
             nn.Linear(32, 16),
             nn.ReLU(),
             nn.Linear(16, 8),
            nn.ReLU(),
            nn.Linear(8, 2)
     def forward(self, x):
         return self.net(x)
X_train_tensor = torch.tensor(X_train_scaled, dtype=torch.float32)
 y_train_tensor = torch.tensor(y_train, dtype=torch.long)
 X_test_tensor = torch.tensor(X_test_scaled, dtype=torch.float32)
 y_test_tensor = torch.tensor(y_test, dtype=torch.long)
 # Initialize model, loss, optimizer
 test_model = SimpleNet(input_dim=X_train_tensor.shape[1])
 criterion = nn.CrossEntropyLoss()
 optimizer = optim.Adam(test_model.parameters(), lr=0.001)
 # Training Loop
 num\_epochs = 440
 for epoch in range(num_epochs):
     test_model.train()
     optimizer.zero_grad()
     outputs = test_model(X_train_tensor)
    loss = criterion(outputs, y_train_tensor)
     loss.backward()
     optimizer.step()
     if epoch % 10 == 0 or epoch == num epochs - 1:
         test model.eval()
         with torch.no_grad():
             test_outputs = test_model(X_test_tensor)
             preds = torch.argmax(test_outputs, dim=1)
             acc = accuracy_score(y_test_tensor, preds)
             print(f"Epoch {epoch:3d} | Loss: {loss.item():.4f} | Test Accuracy: {acc * 100:.2f}%")
```

```
Epoch 0 | Loss: 0.6743 | Test Accuracy: 78.37%
Epoch 10 | Loss: 0.6495 | Test Accuracy: 78.37%
         Epoch 20 | Loss: 0.6229 | Test Accuracy: 78.37%
         Epoch 30 | Loss: 0.5871 | Test Accuracy: 78.37%
         Epoch 40 | Loss: 0.5369 | Test Accuracy: 78.37%Epoch 40 | Loss: 0.5369 | Test Accuracy: 78.37%
         Epoch 50 | Loss: 0.4868 | Test Accuracy: 78.37%
         Epoch 60 | Loss: 0.4642 | Test Accuracy: 78.37%
         Epoch 70 | Loss: 0.4469 | Test Accuracy: 78.37%
         Epoch 80 | Loss: 0.4328 | Test Accuracy: 78.37%
         Epoch 90 | Loss: 0.4198 | Test Accuracy: 78.37%
         Epoch 100 | Loss: 0.4093 | Test Accuracy: 78.37%
         Epoch 110 | Loss: 0.4013 | Test Accuracy: 78.98%
         Epoch 120 | Loss: 0.3944 | Test Accuracy: 81.12%
         Epoch 130 | Loss: 0.3881 | Test Accuracy: 82.35%
         Epoch 140 | Loss: 0.3824 | Test Accuracy: 81.12%
         Epoch 150 | Loss: 0.3769 | Test Accuracy: 80.82%
         Epoch 160 | Loss: 0.3718 | Test Accuracy: 80.82%
         Epoch 170 | Loss: 0.3668 | Test Accuracy: 80.31%
         Epoch 180 | Loss: 0.3615 | Test Accuracy: 80.82%
         Epoch 190 | Loss: 0.3560 | Test Accuracy: 81.12%
         Epoch 200 | Loss: 0.3502 | Test Accuracy: 80.61%
         Epoch 210 | Loss: 0.3440 | Test Accuracy: 80.51%
         Epoch 220 | Loss: 0.3369 | Test Accuracy: 80.82%
        Epoch 230 | Loss: 0.3293 | Test Accuracy: 81.33%
         Epoch 240 | Loss: 0.3213 | Test Accuracy: 82.04%
         Epoch 250 | Loss: 0.3126 | Test Accuracy: 82.04%
         Epoch 260 | Loss: 0.3029 | Test Accuracy: 82.65%
         Epoch 270 | Loss: 0.2918 | Test Accuracy: 82.86%
         Epoch 280 | Loss: 0.2804 | Test Accuracy: 83.37%
         Epoch 290 | Loss: 0.2694 | Test Accuracy: 82.76%
         Epoch 300 | Loss: 0.2586 | Test Accuracy: 83.16%
         Epoch 310 | Loss: 0.2473 | Test Accuracy: 83.27%
         Epoch 320 | Loss: 0.2370 | Test Accuracy: 83.98%
         Epoch 330 | Loss: 0.2280 | Test Accuracy: 83.67%
         Epoch 340 | Loss: 0.2193 | Test Accuracy: 83.67%
         Epoch 350 | Loss: 0.2121 | Test Accuracy: 84.18%
         Epoch 360 | Loss: 0.2049 | Test Accuracy: 84.49%
         Epoch 370 | Loss: 0.1982 | Test Accuracy: 84.08%
         Epoch 380 | Loss: 0.1916 | Test Accuracy: 84.39%
         Epoch 390 | Loss: 0.1856 | Test Accuracy: 84.08%
         Epoch 400 | Loss: 0.1800 | Test Accuracy: 84.80%
         Epoch 410 | Loss: 0.1743 | Test Accuracy: 84.90%
         Epoch 420 | Loss: 0.1691 | Test Accuracy: 84.29%
         Epoch 430 | Loss: 0.1651 | Test Accuracy: 85.20%
         Epoch 439 | Loss: 0.1630 | Test Accuracy: 85.41%
In [284... test_model.eval()
          correct = 0
          y_preds = []
          y true = []
          for i in range(X test scaled.shape[0]):
              x_sample = torch.tensor(X_test_scaled[i].reshape(1, -1), dtype=torch.float32)
              y_sample = y_test_encoded[i].reshape(-1) # Assuming one-hot encoded
              with torch.no_grad():
                  logits = test model(x sample)
                  probs = torch.softmax(logits, dim=1).numpy().flatten()
                  pred_class = np.argmax(probs)
                  true_class = np.argmax(y_sample)
              y preds.append(pred class)
              y_true.append(true_class)
              if pred_class == true_class:
          x_sample = torch.tensor(X_test_scaled[0].reshape(1, -1), dtype=torch.float32)
          with torch.no_grad():
              pred = test_model(x_sample)
          test_accuracy = correct / len(X_test_scaled)
          precision = precision\_score(y\_true, \ y\_preds, \ average='macro', \ zero\_division=0)
          recall = recall_score(y_true, y_preds, average='macro', zero_division=0)
          f1 = f1_score(y_true, y_preds, average='macro', zero_division=0)
          print(f"Test Accuracy: {test_accuracy * 100:.2f}%")
          print(f"Precision: {precision * 100:.2f}%")
          print(f"Recall:
                                 {recall * 100:.2f}%")
          print(f"F1 Score:
                                 {f1 * 100:.2f}%")
```

```
Test Accuracy: 85.41%
         Precision: 78.71%
         Recall:
                       77.20%
         F1 Score:
                       77.91%
In [285... MLP anomalies list = []
          high_confidence_count = 0
          test = []
          scaled_anomalous_inputs = ANN_scaler.transform(generated_anomalies.values)
          test model.eval()
          for x in scaled_anomalous_inputs:
              x_{tensor} = torch.tensor(x.reshape(1, -1), dtype=torch.float32) # shape: [1, input_dim]
              with torch.no_grad():
                  logits = test model(x tensor) # shape: [1, 2]
                  probs = torch.softmax(logits, dim=1).numpy().flatten() # convert to numpy array
                  max_prob = np.max(probs)
              if max_prob >= confidence_threshold:
                  high_confidence_count += 1
                  MLP anomalies list.append(x)
                  if np.argmax(probs) ==1:
                      test.append(x)
          MLP anomalies list = ANN scaler.inverse transform(MLP anomalies list)
          robustness = high_confidence_count / len(generated_anomalies.values)
          print(f"Robustness: {robustness}")
         Robustness: 0.9620689655172414
In [286... len(MLP anomalies list)
Out[286... 558
In [287... MLP_df = pd.DataFrame(MLP_anomalies_list, columns = column_names)
```

KNN Classifier

```
In [288... from sklearn.neighbors import KNeighborsClassifier
          n = 5
          neigh = KNeighborsClassifier(n_neighbors=n)
           neigh.fit(X_train_scaled, y_train)
          y_pred = neigh.predict(X_test_scaled)
          test_acc = accuracy_score(y_test, y_pred)
           test_precision = precision_score(y_test, y_pred,average="macro")
           test_recall = recall_score(y_test, y_pred,average="macro")
          print("Test Accuracy:", test_acc)
print("Test Precision:", test_precision)
          print("Test Recall:", test_recall)
         Test Accuracy: 0.8418367346938775
         Test Precision: 0.7709322843652139
         Test Recall: 0.7385883451257862
In [289... KNN_anomalies_list = []
          high_confidence_count = 0
           scaled_anomalous_inputs = ANN_scaler.transform(generated_anomalies.values)
           for x in scaled_anomalous_inputs:
               probs = neigh.predict_proba(x.reshape(1, -1))
               max_prob = np.max(probs)
               if max_prob >= confidence_threshold:
                   high_confidence_count += 1
                   KNN_anomalies_list.append(x)
           robustness = high_confidence_count / len(scaled_anomalous_inputs)
           KNN_anomalies_list = ANN_scaler.inverse_transform(KNN_anomalies_list)
           print(robustness)
         0.8689655172413793
In [290... len(KNN_anomalies_list)
Out[290... 504
```

```
In [291... knn_df = pd.DataFrame(KNN_anomalies_list, columns = column_names)
```

Checking Shared Vulnerabilities

```
In [292... feature_names = column_names.tolist()
 In [ ]: # Drop duplicates in each DataFrame
          df_rf = RF_df.drop_duplicates()
          df knn = knn df.drop duplicates()
          df_nn = MLP_df.drop_duplicates()
          # Merge on all columns to find common rows
          common_rows = df_rf.merge(df_knn, how='inner').merge(df_nn, how='inner')
          print("Number of common rows:", len(common_rows))
         Number of common rows: 175
In [294...
         # Convert to NumPy array if needed
          inputs = common_rows.values
          # Predict with both models
          rf_preds = RF_model.predict(inputs)
          knn_preds = neigh.predict(inputs)
          # Find indices where class == 1
           rf class1 indices = np.where(rf preds == 1)[0]
          knn_class1_indices = np.where(knn_preds == 1)[0]
          # Extract corresponding samples
          rf_class1_samples = inputs[rf_class1_indices]
          knn_class1_samples = inputs[knn_class1_indices]
In [295...
         common_rows
Out[295...
                   fixed
                             volatile
                                        citric
                                                 residual
                                                                      free sulfur
                                                                                    total sulfur
                                                          chlorides
                                                                                                density
                                                                                                                  sulphates
                                                                                                                               alcohol
                  acidity
                             acidity
                                                                         dioxide
                                         acid
                                                   sugar
                                                                                      dioxide
                9.597688
                            0.307134 0.515876
                                                2.180455 0.049811
                                                                       11.198634
                                                                                     15.950341 0.995507 2.859222
                                                                                                                   0.440415 10.810118
                 6.106977
                            0.398598 0.658312
                                                 6.125418
                                                          0.092710
                                                                       40.878054
                                                                                    192.868882 0.996068 3.264201
                                                                                                                   0.365540
                                                                                                                             9.252220
                6.293023
                            8.274583 0.105290
                                                                       53.121951
                                                                                    211.131122 0.995572 3.155799
                                                                                                                   0.494460
                                                                                                                             9.147780
             2
                 6.539539
                            0.566692 0.706849
                                                19.732222
                                                          0.060097
                                                                       84.150819
                                                                                    196.144227 0.995985 2.988620
                                                                                                                   0.885661
                                                                                                                             8.632607
                7 026955
                                                17.000645 0.073933
                                                                                    160.166482 0.994863 2.931235
             4
                            0.476785 0.615207
                                                                       82.178961
                                                                                                                  0.671063
                                                                                                                             9.772395
           170
                 6.969716
                            0.447190 0.659189
                                                23.975092 0.068123
                                                                       85.590345
                                                                                    246.353353 0.998559 2.874866
                                                                                                                  0.746867
                                                                                                                             8.715935
                 8 171122
                           0.415752 0.536599
                                                15 638762 0 067464
                                                                       47 425637
                                                                                    105 926753 0 993054 3 074616
                                                                                                                  0.582376
                                                                                                                             9 450628
           171
           172
                7.634846
                            0.513103  0.251729
                                                12.723552 0.077459
                                                                       36.546933
                                                                                    155.910549 1.001677 3.232583
                                                                                                                   0.356781 10.144241
                            0.249777 0.352794
           173
                7.610545
                                                13.843082 0.077915
                                                                       10.505264
                                                                                    140.725924 1.000278 3.273470
                                                                                                                  0.134926 10.917273
                7.745404
                           0.379492 0.691140
                                                18.203867 0.053095
                                                                      143.247943
                                                                                    381.535492 0.995861 2.885070
                                                                                                                  0.773055 10.130145
         175 rows × 11 columns
In [296...
          # Filter rows where any feature column has a negative value
          negative_rows = common_rows[feature_names][(common_rows[feature_names] < 0).any(axis=1)]</pre>
         negative rows
```

Out[297...

	fixed acidity	volatile acidity	citric acid	residual sugar	chlorides	free sulfur dioxide	total sulfur dioxide	density	рН	sulphates	alcohol
11	5.535680	0.121270	0.018666	-3.184112	0.014720	46.376041	150.461355	0.993912	3.288320	0.295626	9.143875
14	6.290587	0.427309	-0.260097	-6.052626	0.021421	-10.483904	61.032187	0.986866	3.355864	0.445388	8.996359
26	6.206194	0.321373	0.044749	-2.184957	0.020074	5.662817	65.865415	0.989398	3.250668	0.476161	8.963407
30	8.118618	0.469542	0.691650	-0.108228	0.215253	25.046513	177.544802	0.996380	3.158287	0.385128	10.530506
46	9.593996	1.025138	0.384150	-1.597036	0.042891	44.602843	165.630049	0.998769	3.043500	0.408887	10.511838
49	7.069956	0.393858	0.167114	1.684714	0.062314	-20.075436	68.344077	0.985221	3.362987	0.466079	9.898336
58	6.244912	0.108512	-0.043215	1.632855	0.140079	27.763642	109.620568	0.992356	3.055638	0.514244	7.385408
74	6.109634	0.162299	0.042065	-0.850620	0.023369	-7.223909	55.094690	0.989732	3.390418	0.491652	8.932659
77	6.251114	0.214155	0.063757	-3.328095	0.020184	4.624540	99.552407	0.993348	3.213874	0.216625	9.268605
78	5.853652	0.028557	0.020012	-7.146336	0.027531	31.015026	107.122188	0.992802	3.219658	0.245165	9.294121
90	6.052540	0.498555	-0.060431	0.373474	0.037512	11.448171	154.141503	0.992103	3.325719	0.509858	8.227442
94	7.491870	0.373341	0.033311	-0.821683	0.017792	-15.884827	66.500531	0.988002	3.177260	0.333239	9.706036
100	6.853973	0.136171	0.008831	-0.048106	0.023302	-18.018820	56.979251	0.987176	3.337411	0.478306	9.724123
101	5.768085	0.030900	0.395587	-0.658790	0.015249	8.006535	110.431788	0.995521	3.346019	0.140844	9.353341
104	6.768259	0.216597	-0.048608	-0.111871	0.021329	7.097973	96.136291	0.989506	3.369727	0.454715	8.828130
107	7.430412	0.093461	-0.012158	-3.292199	0.028621	-4.684588	27.376304	0.985707	3.170362	0.534332	9.528912
117	6.205999	0.203580	0.152772	-0.179144	0.030020	-7.401202	78.042455	0.989682	3.175592	0.631116	8.508034
118	6.140264	0.044401	-0.111963	-8.194881	0.006293	26.813371	81.549597	0.992393	3.304863	0.096834	10.005137
134	5.985239	0.334834	0.297655	-0.254301	0.107361	5.326056	36.137575	0.989774	3.255648	0.520277	8.079908
144	6.218968	0.309468	0.029699	-0.162545	0.118048	54.520779	181.148742	0.996321	3.302286	0.254045	10.811922
159	6.696087	0.407913	-0.048879	-2.098421	0.056640	17.236542	67.682094	0.996294	3.469830	0.196641	10.246661
160	6.855161	0.230980	0.092447	-0.532175	0.186738	21.496664	42.991580	0.992230	3.306240	0.539875	7.094077

In [298... negative_rows.reset_index(drop=True)

Out[298...

		fixed acidity	volatile acidity	citric acid	residual sugar	chlorides	free sulfur dioxide	total sulfur dioxide	density	рН	sulphates	alcohol
	0	5.535680	0.121270	0.018666	-3.184112	0.014720	46.376041	150.461355	0.993912	3.288320	0.295626	9.143875
	1	6.290587	0.427309	-0.260097	-6.052626	0.021421	-10.483904	61.032187	0.986866	3.355864	0.445388	8.996359
	2	6.206194	0.321373	0.044749	-2.184957	0.020074	5.662817	65.865415	0.989398	3.250668	0.476161	8.963407
	3	8.118618	0.469542	0.691650	-0.108228	0.215253	25.046513	177.544802	0.996380	3.158287	0.385128	10.530506
	4	9.593996	1.025138	0.384150	-1.597036	0.042891	44.602843	165.630049	0.998769	3.043500	0.408887	10.511838
	5	7.069956	0.393858	0.167114	1.684714	0.062314	-20.075436	68.344077	0.985221	3.362987	0.466079	9.898336
	6	6.244912	0.108512	-0.043215	1.632855	0.140079	27.763642	109.620568	0.992356	3.055638	0.514244	7.385408
	7	6.109634	0.162299	0.042065	-0.850620	0.023369	-7.223909	55.094690	0.989732	3.390418	0.491652	8.932659
	8	6.251114	0.214155	0.063757	-3.328095	0.020184	4.624540	99.552407	0.993348	3.213874	0.216625	9.268605
	9	5.853652	0.028557	0.020012	-7.146336	0.027531	31.015026	107.122188	0.992802	3.219658	0.245165	9.294121
1	0	6.052540	0.498555	-0.060431	0.373474	0.037512	11.448171	154.141503	0.992103	3.325719	0.509858	8.227442
1	1	7.491870	0.373341	0.033311	-0.821683	0.017792	-15.884827	66.500531	0.988002	3.177260	0.333239	9.706036
1	2	6.853973	0.136171	0.008831	-0.048106	0.023302	-18.018820	56.979251	0.987176	3.337411	0.478306	9.724123
1	3	5.768085	0.030900	0.395587	-0.658790	0.015249	8.006535	110.431788	0.995521	3.346019	0.140844	9.353341
1	4	6.768259	0.216597	-0.048608	-0.111871	0.021329	7.097973	96.136291	0.989506	3.369727	0.454715	8.828130
1	5	7.430412	0.093461	-0.012158	-3.292199	0.028621	-4.684588	27.376304	0.985707	3.170362	0.534332	9.528912
1	6	6.205999	0.203580	0.152772	-0.179144	0.030020	-7.401202	78.042455	0.989682	3.175592	0.631116	8.508034
1	7	6.140264	0.044401	-0.111963	-8.194881	0.006293	26.813371	81.549597	0.992393	3.304863	0.096834	10.005137
1	8	5.985239	0.334834	0.297655	-0.254301	0.107361	5.326056	36.137575	0.989774	3.255648	0.520277	8.079908
1	9	6.218968	0.309468	0.029699	-0.162545	0.118048	54.520779	181.148742	0.996321	3.302286	0.254045	10.811922
2	0	6.696087	0.407913	-0.048879	-2.098421	0.056640	17.236542	67.682094	0.996294	3.469830	0.196641	10.246661
2	1	6.855161	0.230980	0.092447	-0.532175	0.186738	21.496664	42.991580	0.992230	3.306240	0.539875	7.094077

```
In [299... common_rows[feature_names].iloc[14]
```

volatile acidity 6.290587
volatile acidity 0.427309
citric acid -0.260097
residual sugar -6.052626
chlorides Out[299... fixed acidity free sulfur dioxide -10.483904 total sulfur dioxide 61.032187 density 0.986866 рΗ 3.355864 sulphates 0.445388 8.996359 alcohol Name: 14, dtype: float64

Example of Anomalous Sample

```
In [300... sample_row = negative_rows.iloc[1]
         print("Input row (original scale):")
         print(sample_row)
        Input row (original scale):
                       6.290587
cy 0.427309
        fixed acidity
        volatile acidity
        citric acid
                               -0.260097
        residual sugar
                              -6.052626
        chlorides
                               0.021421
        free sulfur dioxide -10.483904
        total sulfur dioxide 61.032187
        density
                                0.986866
        sulphates
                                0.445388
        alcohol
                                8.996359
        Name: 14, dtype: float64
In [301... sample_row = common_rows.iloc[14] # You can change the index if needed
         scaled_sample = ANN_scaler.transform(sample_row.values.reshape(1, -1))
          x_tensor = torch.tensor(scaled_sample, dtype=torch.float32)
```

test_model.eval()

```
with torch.no_grad():
             logits = test_model(x_tensor)
              probs = torch.softmax(logits, dim=1).numpy().flatten()
              max_prob = np.max(probs)
          predicted_class = np.argmax(probs)
print("Neural Network Model")
          print("Probability of Low Quality:", probs[0]*100,"%")
          print("Probability of Hih Quality Quality:", probs[1]*100,"%")
         Neural Network Model
         Probability of Low Quality: 99.99154 %
         Probability of Hih Quality Quality: 0.008464073 %
In [302... probs = neigh.predict_proba(sample_row.values.reshape(1,-1))
          print("K-NN Model (K = 5)")
          print("Probability of Low Quality:", probs[0][0]*100,"%")
          print("Probability of Hih Quality Quality:", probs[0][1]*100,"%")
         K-NN Model (K = 5)
         Probability of Low Quality: 100.0 %
         Probability of Hih Quality Quality: 0.0 \%
In [303... probs = RF_model.predict_proba(sample_row.values.reshape(1,-1))
          print("Random Forest Model")
          print("Probability of Low Quality:", probs[0][0]*100,"%")
          print("Probability of Hih Quality Quality:", probs[0][1]*100,"%")
         Random Forest Model
         Probability of Low Quality: 83.0 %
         Probability of Hih Quality Quality: 17.0 %
```