



The World of Languages
and Languages of the World

The Language of Mathematics

Get you thinking caps on...Is mathematics a language?

Objectives



ίπποπόταμος
WoLLoW the HiPPo

- Today we will
- Consider mathematics as a language
- Look at symbols within Maths – their origin and their meaning
- Crack some codes

Let's Go!

What makes a language? Think of 4 things:

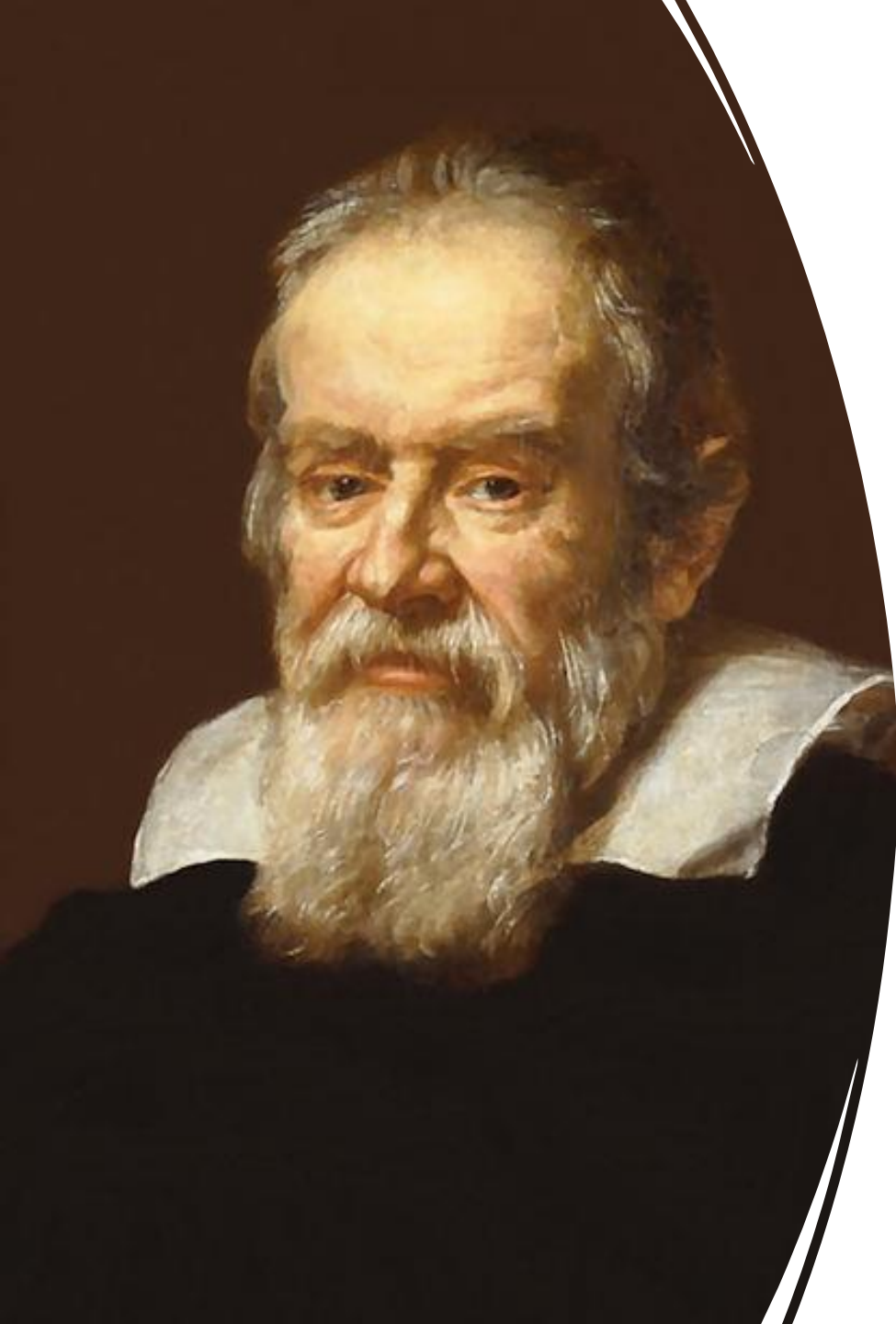
1

2

3

4

So, is mathematics a language?



Yes, it's a language!

"Mathematics is the language in which God has written the universe." (Galileo)

It has a:

- Vocabulary
- Meaning
- Grammar
- Syntax (arrangement of words and phrases)
- People use and understand they symbols



Are these
symbols
nouns or
verbs? (6
of each)

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x or *

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$y = g(x)$

Secant Lines

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$
$$f(x) = \lim_{h \rightarrow 0} \frac{x^2 + 2xh + h^2 - x^2}{h}$$
$$= \lim_{h \rightarrow 0} \frac{2xh + h^2}{h}$$
$$= \lim_{h \rightarrow 0} (2x + h)$$
$$= 2x$$

$g(x+h) - g(x)$

$$= \lim_{h \rightarrow 0} h(2x)$$

So, why do mathematicians use symbols instead of written words?

Think of three reasons:

- 1
- 2
- 3

What did you come up with?

Symbols are used as they can act as a universal language as they are the same all over the world.

Symbols are quicker to write than words – they take less space and less time to jot down.

Symbols are flexible and they reduce the cognitive load.

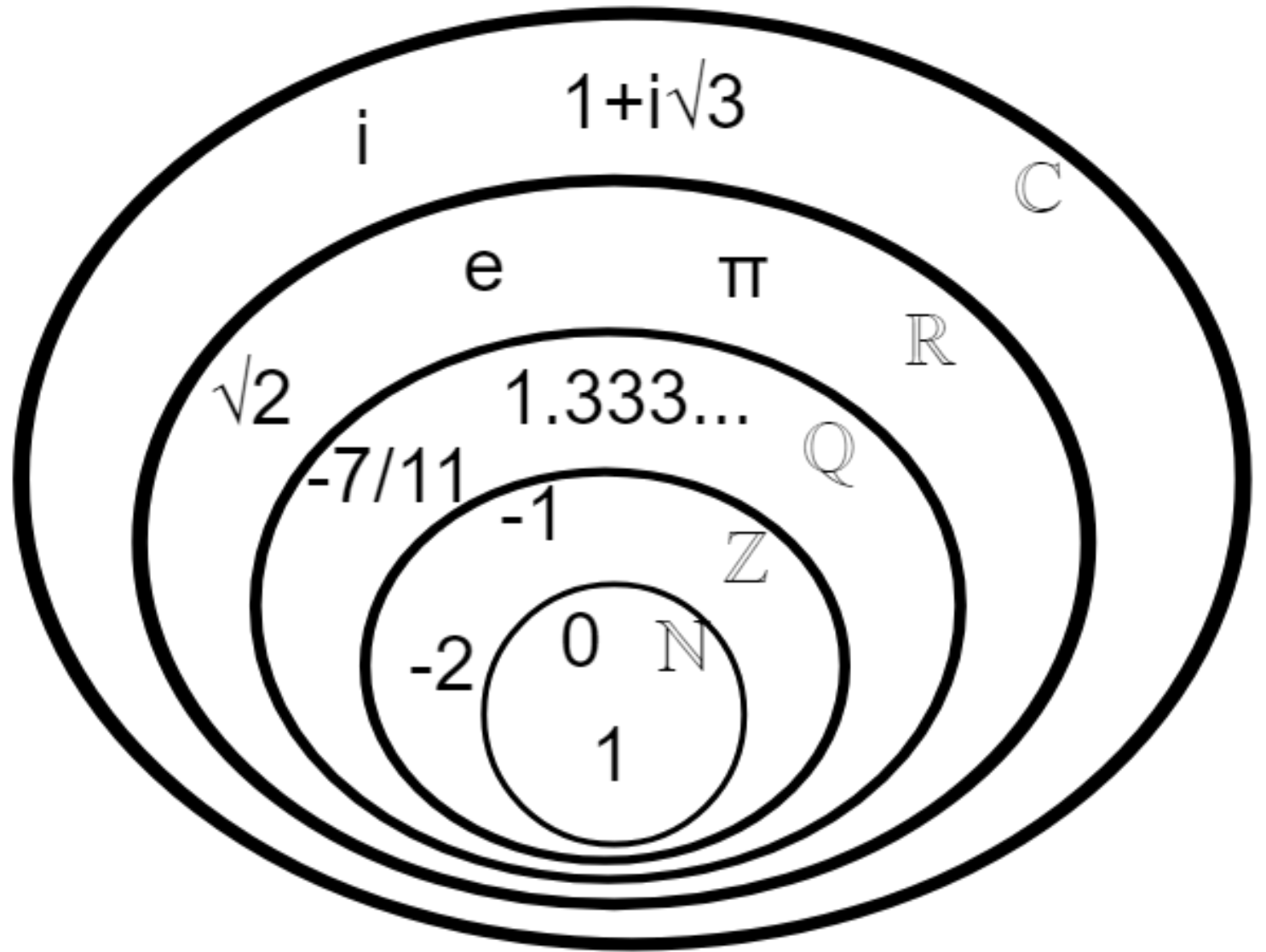
The Evolution of Numbers – do you know any of these terms?

- Natural Numbers N
- Whole Numbers W
- Integers Z
- Rational Numbers Q
- Real Numbers R
- Complex Numbers C

Language Detectives – crack this code!

$\mathbb{N} \subseteq \mathbb{Z} \subseteq \mathbb{Q} \subseteq \mathbb{R} \subseteq \mathbb{C}$

Does this
help?





Natural Numbers

- We use these numbers to count.
 - These numbers came about in around 4000 BC.
 - How many apples are in this basket?
 - So, natural numbers are 1,2,3,4 etc.
-
- What about zero?



ΙΠΠΟΤΟΤΑΜΟΣ
FOLLOW THE HIPPO

Zero is tricky. It is also a Natural Number. It came later, about 3000 years ago.

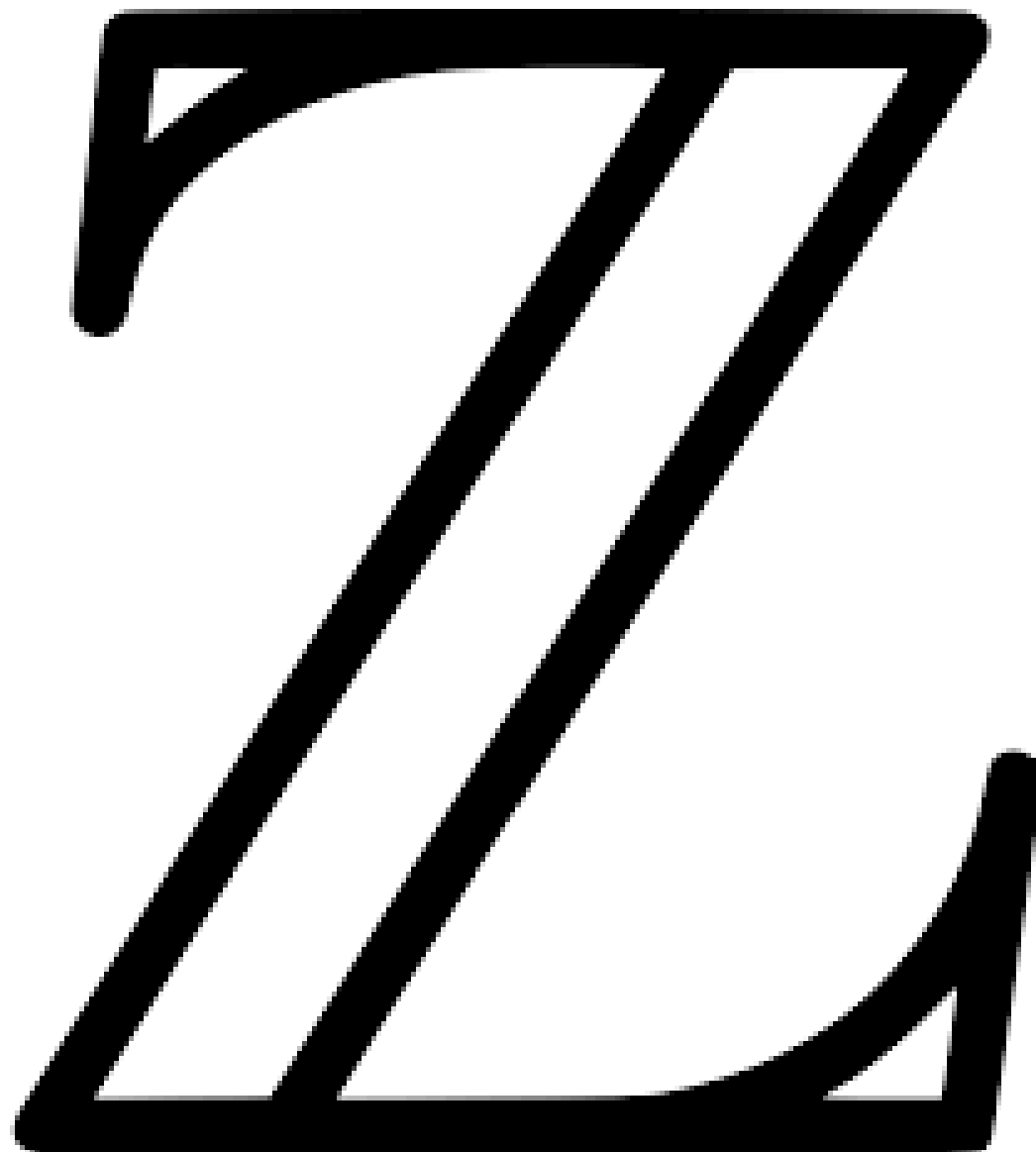
How can we count, if there is nothing to count? The second picture is just an empty basket!



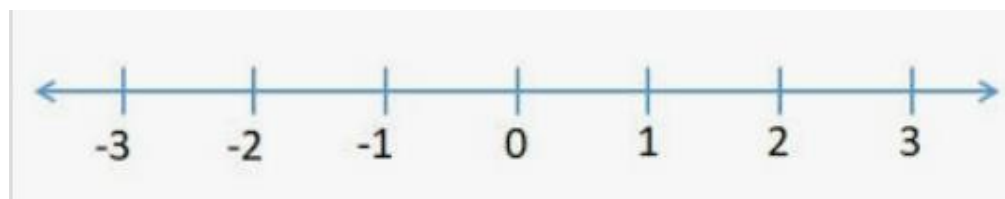
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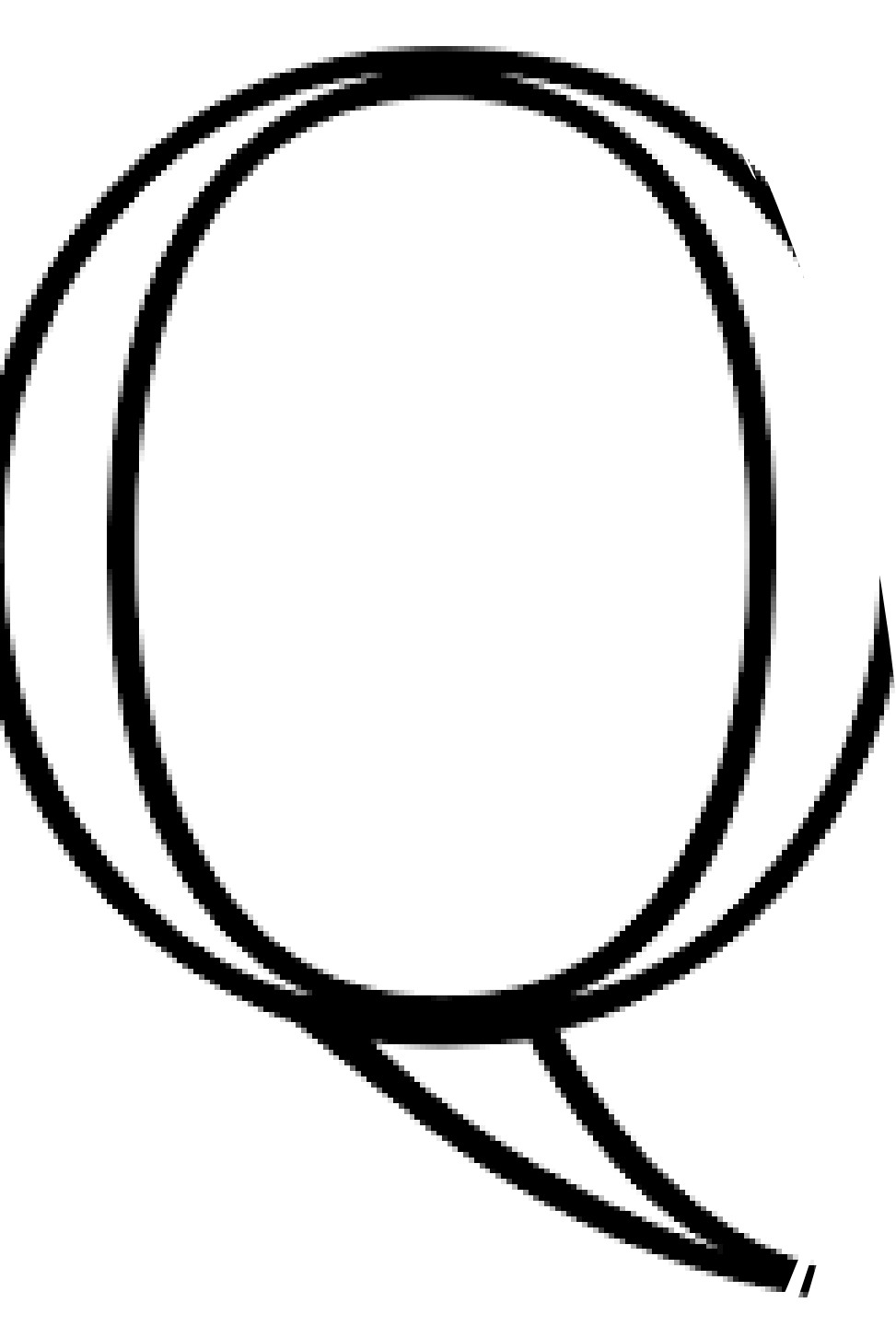


Integers – does this help?



Why Z and not I?

It's taken from the German word Zahlen meaning "numbers"!



Rational Numbers

A Rational Number can be made by dividing an integer by an integer.

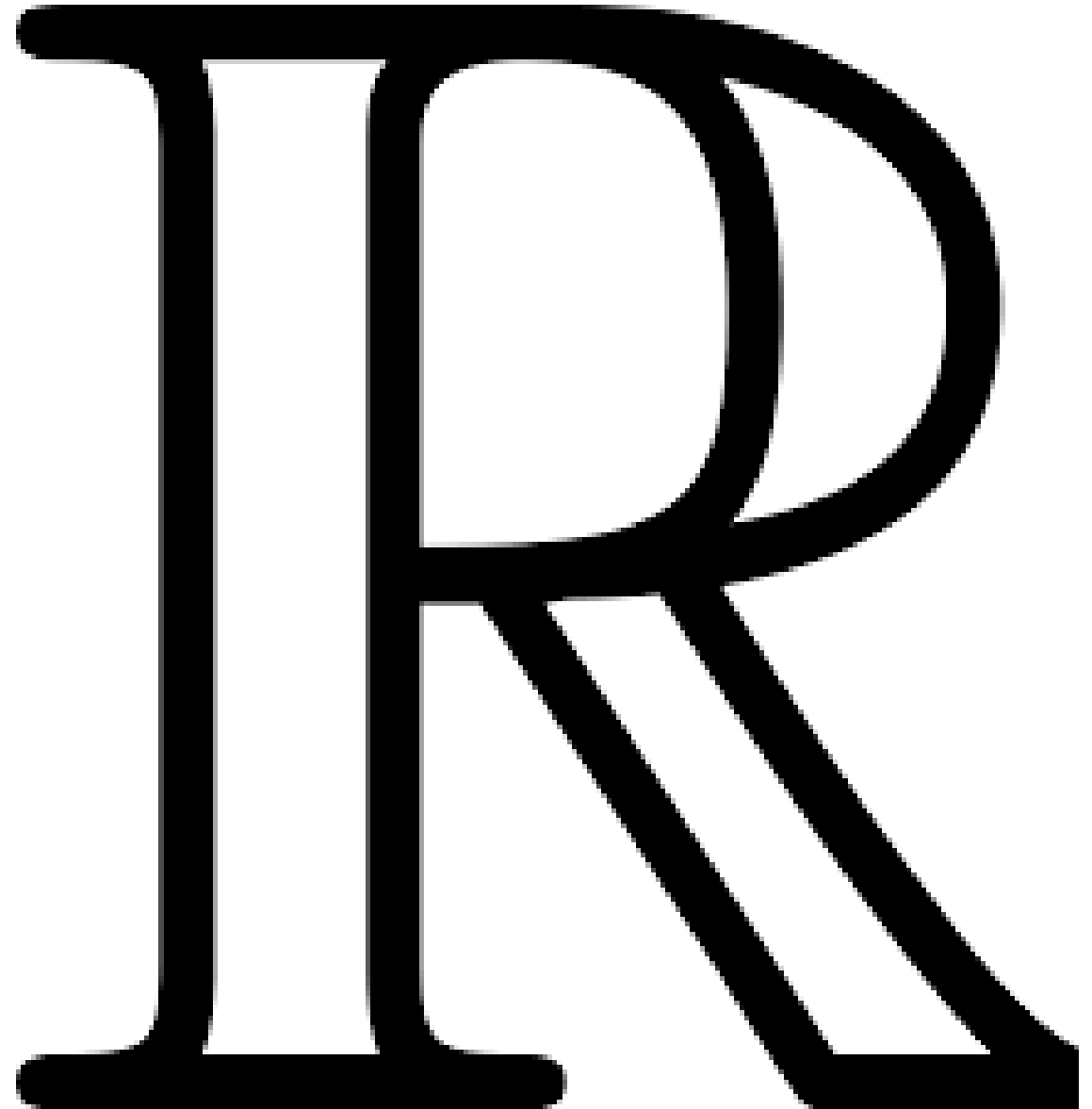
E.g. 1.5 is a rational number. $1.5 = 3/2$ (3 and 2 are both integers)

Why Q and not R?

Well, Q stands for "Quotient"

Real Numbers

- Real numbers can be thought of as points on an infinitely long line called the number line or real line: an infinite decimal expansion!
- They are positive, negative, large, small, fractions, decimals





Complex Numbers

- A complex number is part of a number system that extends the real numbers with a specific element "i". This is called the imaginary unit.

So, now to crack the code! You need to work out what \subseteq means!

$$\mathbb{N} \subseteq \mathbb{Z} \subseteq \mathbb{Q} \subseteq \mathbb{R} \subseteq \mathbb{C}$$

This is how we order numbers and
therefore how we bring order to the
universe!

WoLLoW would like to know...

N is a subset of Z.

Z is a subset of Q.

Q is a subset of R.

R is a subset of C.

So, now can you give an example of each of these subsets?

N

Z

Q

R

C



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