Climate Data Visualization -

Atmospheric CO_2 Concentration / Temperature / Precipitation

Wolfgang Vollmer

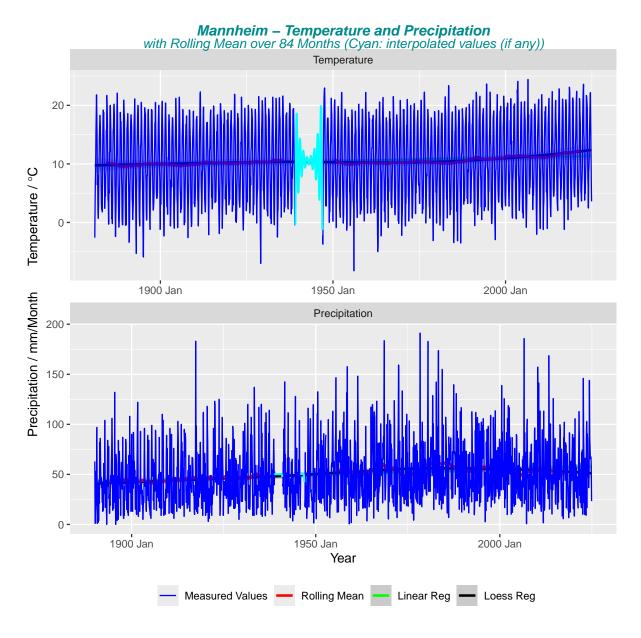
2025-01-03

Contents

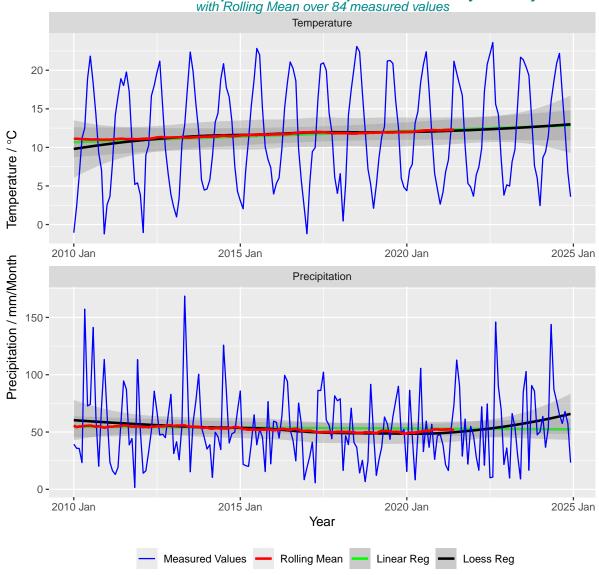
| 1 | Mannheim - Visualization of Temperature and Precipitation Data 1881 - 20 | | | | | |
|---|--|--------|--|----|--|--|
| | 1.1 | Month | lly Time Plots with Rolling Mean | 2 | | |
| | 1.2 | Yearly | plots with monthly breakdown | 4 | | |
| | | 1.2.1 | $30\mbox{-}\mbox{year}$ period plots with monthly breakdown - Cartesian and Polar Coordinates $% \left(1\right) =100$. | 4 | | |
| | | 1.2.2 | Plot Monthly Delta to Reference Period - Cartesian and Polar Coordinates $\ \ldots \ \ldots$ | 7 | | |
| | 1.3 | Yearly | Mannheim - Temperature and Precipitation | 11 | | |
| | | 1.3.1 | Plot Yearly Temperature and Precipitation | 11 | | |
| | | 1.3.2 | Plot Seasonal Yearly Temperature and Precipitation | 12 | | |
| 2 | Tre | nd and | Seasonal Analysis | 12 | | |
| | 2.1 | Time | Series Decomposition - Trend and Seasonal Components | 12 | | |
| | 2.2 | Period | licities - Season Frequency | 14 | | |
| | | 2.2.1 | Lag Plot - Differences | 14 | | |
| | | 2.2.2 | ACF / PACF Correlogram | 14 | | |
| | | 2.2.3 | Periodogram - Spectral Density Estimation of a Time Series | 14 | | |
| | | 2.2.4 | Seasonal vs non Seasonal ACF / Strength (Seasonal/Trend) | 16 | | |
| | | 2.2.5 | Spectral Entropy Test | 17 | | |
| | 2.3 | Statio | nary Process Test | 18 | | |
| 3 | Bac | kup | | 18 | | |
| | 3.1 | Mannl | neim - Average Yearly and Seasonal Data | 18 | | |
| | 3.2 | Data S | Sources | 19 | | |
| | | 3.2.1 | Temperatures and Precipitation | 19 | | |
| | | 3.2.2 | CO2 Concentrations | 20 | | |
| | 3.3 | R code | e | 20 | | |

1 Mannheim - Visualization of Temperature and Precipitation Data 1881 - 2024

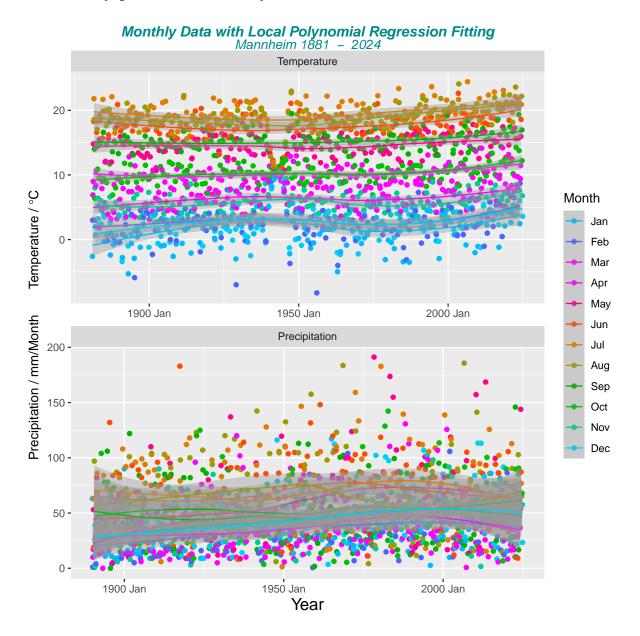
1.1 Monthly Time Plots with Rolling Mean







1.2 Yearly plots with monthly breakdown



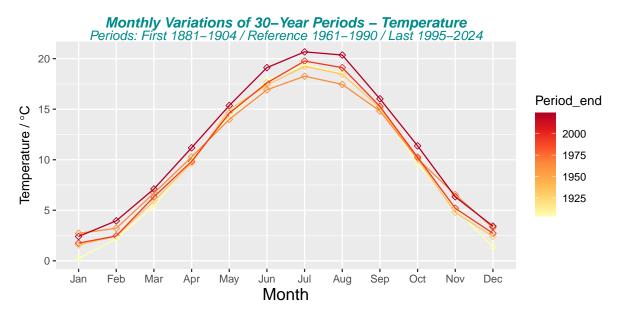
1.2.1 30-year period plots with monthly breakdown - Cartesian and Polar Coordinates

Table 1: 30-years Periods - Average Data (Temperature / degree C and Monthly Precipitation / mm)

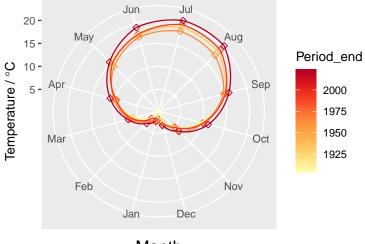
| City | Period | Temperature | Monthly Precipitation | Annual Precipitation |
|----------|-----------|-------------|-----------------------|----------------------|
| Mannheim | 1881-1904 | 9.9 | 41.7 | 500.1 |
| Mannheim | 1905-1934 | 10.2 | 45.2 | 542.9 |
| Mannheim | 1935-1964 | 10.4 | 49.4 | 593.2 |
| Mannheim | 1965-1994 | 10.4 | 56.4 | 677.1 |
| Mannheim | 1995-2024 | 11.4 | 54.1 | 649.2 |

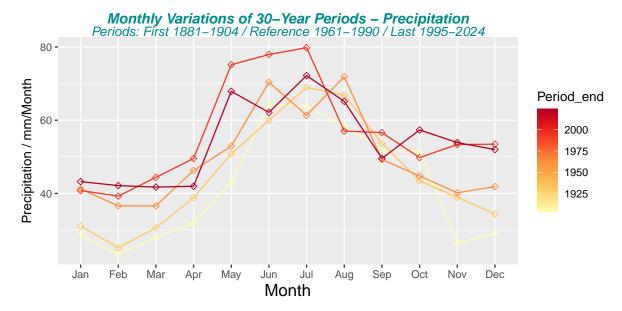
| City | Ref_Period | Temperature | Monthly Precipitation | Annual Precipitation |
|----------|------------|-------------|-----------------------|----------------------|
| Mannheim | 1961-1990 | 10.3 | 55.6 | 667.5 |

Note: First Period shorter in general (starts with first data year = 1881)

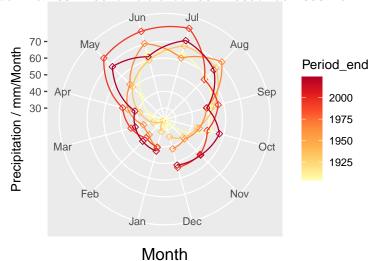


Monthly Variations of 30–Year Periods – Temperature Periods: First 1881–1904 / Reference 1961–1990 / Last 1995–2024

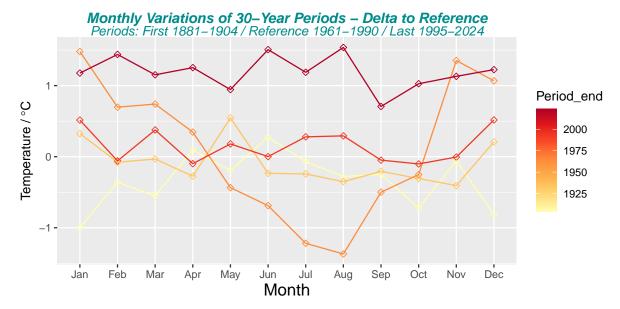




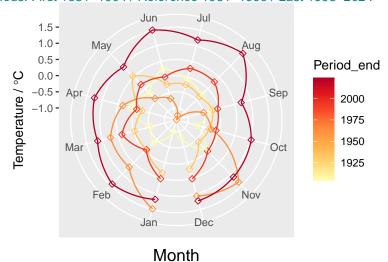
Monthly Variations of 30–Year Periods – Precipitation Periods: First 1881–1904 / Reference 1961–1990 / Last 1995–2024

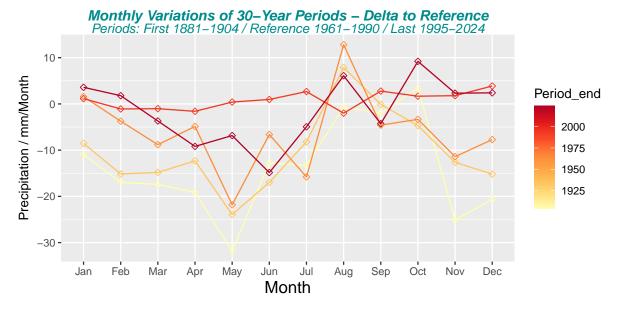


1.2.2 Plot Monthly Delta to Reference Period - Cartesian and Polar Coordinates

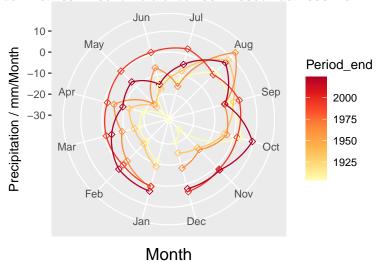


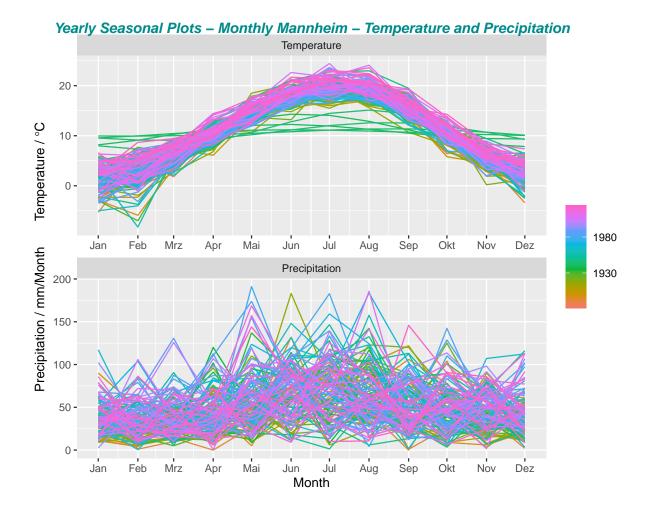
Monthly Variations of 30–Year Periods – Delta to Reference Periods: First 1881–1904 / Reference 1961–1990 / Last 1995–2024

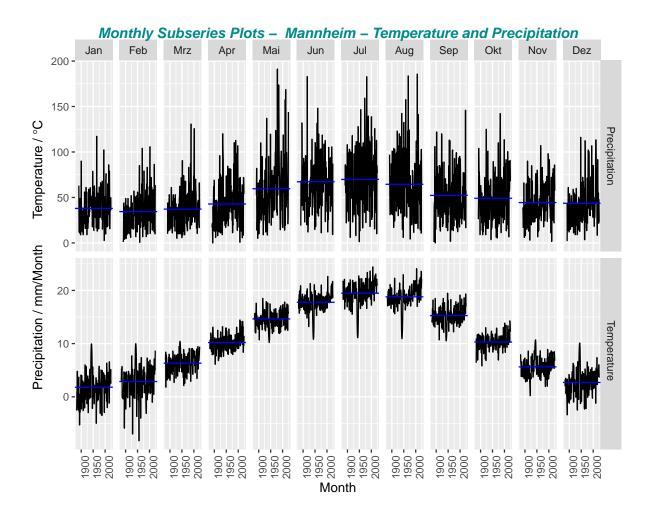




Monthly Variations of 30–Year Periods – Delta to Reference Periods: First 1881–1904 / Reference 1961–1990 / Last 1995–2024

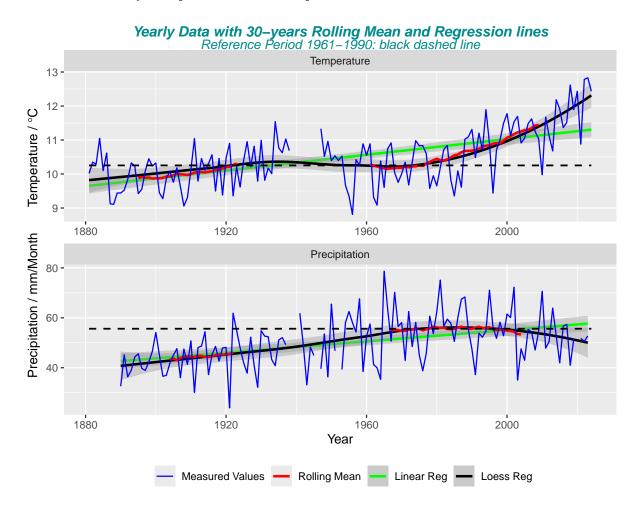




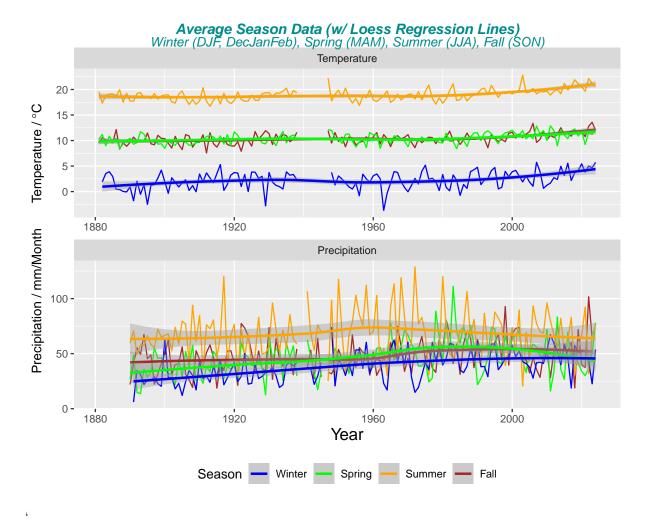


1.3 Yearly Mannheim - Temperature and Precipitation

1.3.1 Plot Yearly Temperature and Precipitation



1.3.2 Plot Seasonal Yearly Temperature and Precipitation



2 Trend and Seasonal Analysis

2.1 Time Series Decomposition - Trend and Seasonal Components

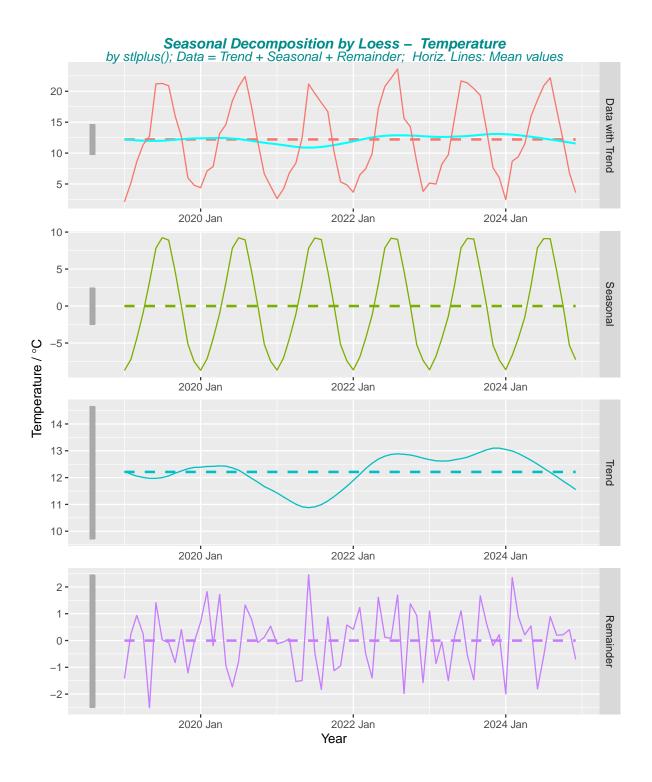
An additive model would be used when the variations around the trend do not vary with the level of the time series whereas a multiplicative model would be appropriate if the trend is proportional to the level of the time series.

Time series using an

- additive model: $y_t = T_t + C_t + S_t + \epsilon_t$
- multiplicative model: $y_t = T_t * C_t * S_t * \epsilon_t$

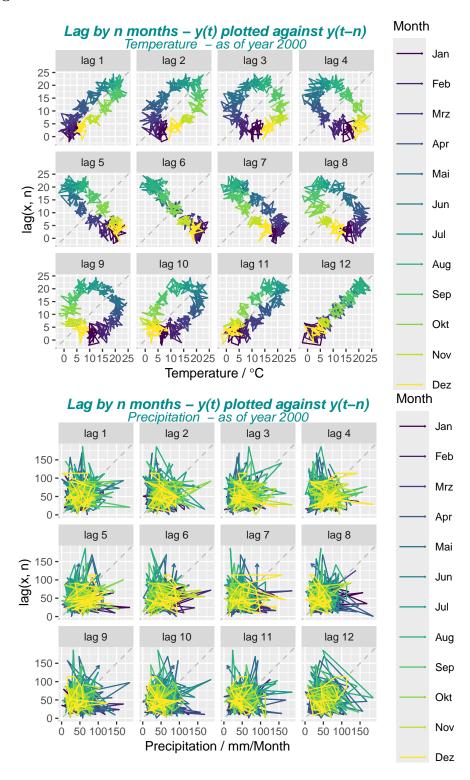
Trend / Cycle / Seasonal / Noise component Cyclical components is often grouped into the Trend component

For Seasonal decomposition of time series by Loess (stlplus) uses in general an additive error model, it only provides facilities for additive decompositions. It is possible to obtain a multiplicative decomposition by first taking logs of the data.



2.2 Periodicities - Season Frequency

2.2.1 Lag Plot - Differences



2.2.2 ACF / PACF Correlogram

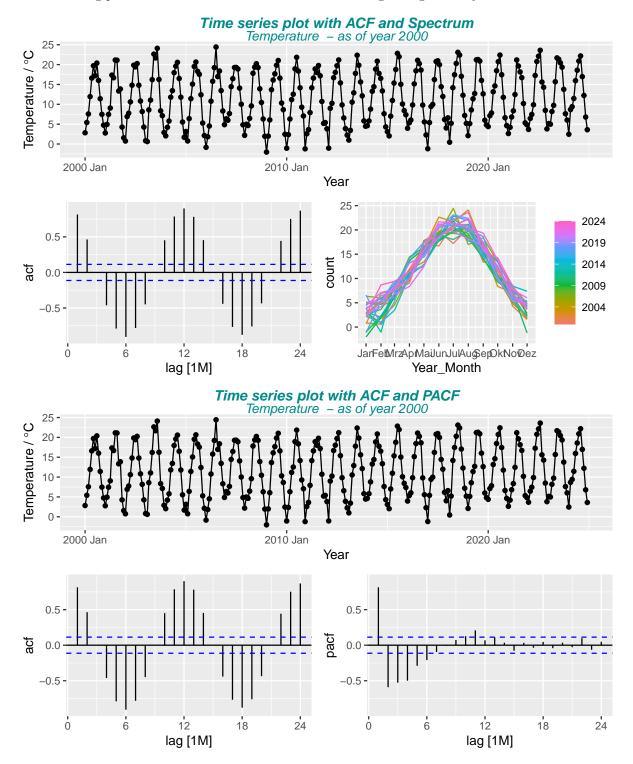
2.2.3 Periodogram - Spectral Density Estimation of a Time Series

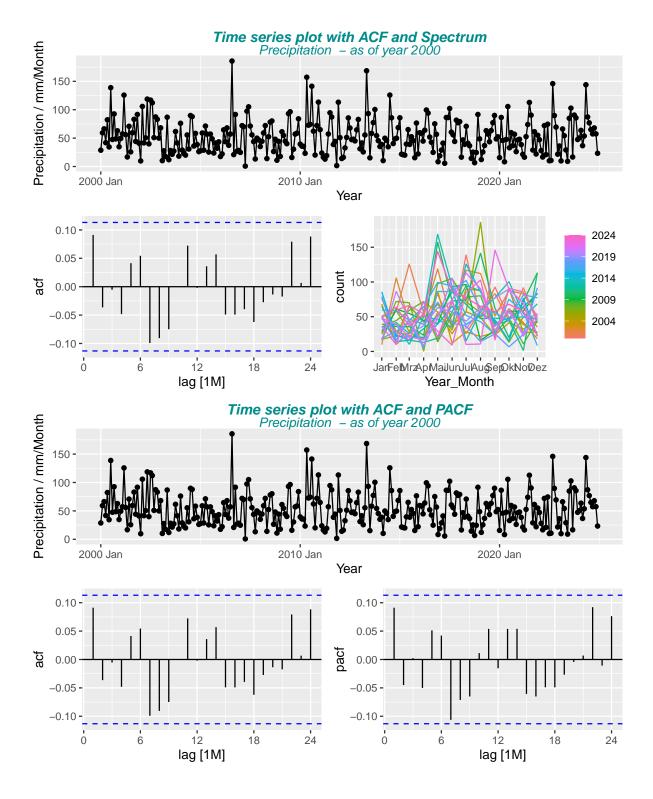
The spectral density characterizes the frequency content of the signal. One purpose of estimating the spectral density is to detect any periodicities in the data, by observing peaks at the frequencies corre-

sponding to these periodicities.

At frequency $\lambda=1/12$ there is a significant peak => This pattern repeats every full frequency = every 12 months / every year

The remaining peaks are random and therefore cannot be assigned significantly.



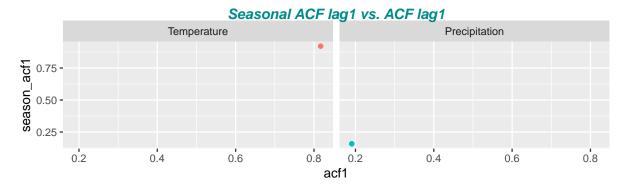


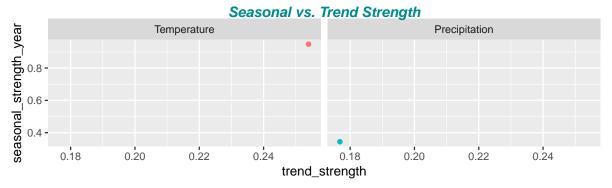
2.2.4 Seasonal vs non Seasonal ACF / Strength (Seasonal/Trend)

- Check acf1 and season_acf1 and compare with ACF Correlogram Plot
- acf1: first autocorrelation coefficient from the original data
- acf10: sum of square of the first ten autocorrelation coefficients from the original data
- diff1_acf1: first autocorrelation coefficient from the differenced data
- season_acf1: autocorrelation coefficient at the first seasonal lag

- Check Trend & Seasonal Strength close to 0/1: weak / strong and compare them
- stl e acfl: first autocorrelation coefficient of the remainder series
- stl_e_acf10: sum of squares of the first ten autocorrelation coefficients of the remainder series
- linearity: linearity of the trend component of the STL decomposition. It is based on the coefficient of a linear regression applied to the trend component
- curvature: curvature of the trend component of the STL decomposition. It is based on the coefficient from an orthogonal quadratic regression applied to the trend component.

```
#> [1] "Check acf1 and season_acf1 and compare with ACF Correlogram Plot"
#> # A tibble: 2 x 8
                    acf10 diff1_acf1 diff1_acf10 diff2_acf1 diff2_acf10 season_acf1
#>
     Measure acf1
             <dbl>
                                <dbl>
                                             <dbl>
                                                        <dbl>
                                                                     <dbl>
                                                                                 <dbl>
#> 1 Temper~ 0.817 3.57
                                0.456
                                             1.80
                                                       -0.384
                                                                     0.272
                                                                                 0.921
                                                       -0.648
#> 2 Precip~ 0.191 0.0752
                               -0.436
                                             0.196
                                                                     0.448
                                                                                 0.158
#> [1] "Check Trend & Seasonal Strength close to 0 / 1 : weak / strong and compare them"
  # A tibble: 2 x 10
     Measure
#>
                   trend_strength seasonal_strength_year seasonal_peak_year
     <fct>
#>
                             <dbl>
                                                     <dbl>
                                                                         <dbl>
                             0.254
                                                     0.948
#> 1 Temperature
                                                                             7
#> 2 Precipitation
                             0.177
                                                                             5
#> # i 6 more variables: seasonal_trough_year <dbl>, spikiness <dbl>,
       linearity <dbl>, curvature <dbl>, stl_e_acf1 <dbl>, stl_e_acf10 <dbl>
```





2.2.5 Spectral Entropy Test

- Entropy close to 0 => series has strong trend and seasonality (=> easy to forecast)
- Entropy close to 1 => series is very noisy (and so is difficult to forecast)
- #> [1] "Check entropy close to 0 or 1"
 #> # A tibble: 2 x 2

| #> | Measure | spectral_entropy |
|----|-----------------|------------------|
| #> | <fct></fct> | <dbl></dbl> |
| #> | 1 Temperature | 0.270 |
| #> | 2 Precipitation | 0.974 |

2.3 Stationary Process Test

Strict-sense stationarity / Weak (wide-sense) stationarity

Augmented Dickey-Fuller test => type3, a linear model with both drift and linear trend

Trend Stationary - underlying trend (function solely of time) can be removed, leaving a stationary process

3 Backup

3.1 Mannheim - Average Yearly and Seasonal Data

Table 3: Annual paste ("Temperature /", degree * C) (first and last 10 years)

| City | Measure | Year | Winter_avg | Spring_avg | Summer_avg | Fall_avg | Year_avg |
|----------|-------------|------|------------|------------|------------|----------|----------|
| Mannheim | Temperature | 1881 | NA | 10.2 | 19.6 | 9.5 | 10.0 |
| Mannheim | Temperature | 1882 | 1.9 | 11.2 | 17.3 | 10.6 | 10.3 |
| Mannheim | Temperature | 1883 | 3.5 | 9.0 | 18.8 | 10.1 | 10.3 |
| Mannheim | Temperature | 1884 | 3.9 | 10.9 | 19.1 | 10.0 | 11.1 |
| Mannheim | Temperature | 1885 | 3.0 | 9.7 | 19.2 | 9.5 | 10.1 |
| Mannheim | Temperature | 1886 | 0.4 | 10.5 | 18.7 | 12.2 | 10.6 |
| Mannheim | Temperature | 1887 | 0.4 | 8.5 | 20.0 | 8.3 | 9.1 |
| Mannheim | Temperature | 1888 | 0.0 | 9.3 | 17.5 | 9.6 | 9.1 |
| Mannheim | Temperature | 1889 | -0.1 | 10.1 | 19.3 | 8.9 | 9.4 |
| Mannheim | Temperature | 1890 | 0.9 | 10.4 | 17.7 | 9.6 | 9.4 |
| Mannheim | Temperature | 2015 | 3.1 | 11.1 | 21.2 | 11.2 | 11.9 |
| Mannheim | Temperature | 2016 | 5.6 | 10.3 | 19.9 | 11.3 | 11.4 |
| Mannheim | Temperature | 2017 | 2.2 | 11.9 | 20.6 | 10.9 | 11.5 |
| Mannheim | Temperature | 2018 | 3.7 | 12.3 | 21.9 | 12.2 | 12.6 |
| Mannheim | Temperature | 2019 | 4.1 | 10.9 | 21.1 | 11.5 | 11.9 |
| Mannheim | Temperature | 2020 | 5.4 | 11.9 | 20.5 | 11.9 | 12.4 |
| Mannheim | Temperature | 2021 | 3.8 | 9.2 | 19.7 | 10.7 | 10.9 |
| Mannheim | Temperature | 2022 | 5.0 | 11.5 | 22.2 | 12.8 | 12.8 |
| Mannheim | Temperature | 2023 | 4.7 | 11.2 | 21.2 | 13.6 | 12.8 |
| Mannheim | Temperature | 2024 | 5.7 | 12.3 | 20.6 | 12.0 | 12.4 |

Table 4: Annual Precipitation / mm/Month (first and last 10 years)

| City | Measure | Year | Winter_avg | Spring_avg | Summer_avg | Fall_avg | Year_avg |
|----------|---------------|------|------------|------------|------------|----------|----------|
| Mannheim | Precipitation | 1881 | NA | NA | NA | NA | NA |
| | Precipitation | 1882 | NA | NA | NA | NA | NA |
| Mannheim | Precipitation | 1883 | NA | NA | NA | NA | NA |
| Mannheim | Precipitation | 1884 | NA | NA | NA | NA | NA |
| Mannheim | Precipitation | 1885 | NA | NA | NA | NA | NA |
| Mannheim | Precipitation | 1886 | NA | NA | NA | NA | NA |
| Mannheim | Precipitation | 1887 | NA | NA | NA | NA | NA |
| Mannheim | Precipitation | 1888 | NA | NA | NA | NA | NA |
| Mannheim | Precipitation | 1889 | NA | NA | NA | NA | NA |

| City | Measure | Year | Winter_avg | Spring_avg | Summer_avg | Fall_avg | Year_avg |
|------------------|---------------|------|------------|------------|------------|----------|----------|
| Mannheim | Precipitation | 1890 | NA | 26.7 | 59.7 | 22.0 | 32.6 |
| Mannheim | Precipitation | 2015 | 58.7 | 26.7 | 52.1 | 45.8 | 42.0 |
| Mannheim | Precipitation | 2016 | 46.7 | 69.4 | 62.9 | 52.3 | 56.7 |
| Mannheim | Precipitation | 2017 | 18.7 | 44.4 | 83.0 | 60.5 | 57.4 |
| Mannheim | Precipitation | 2018 | 57.6 | 52.2 | 30.6 | 18.9 | 41.0 |
| Mannheim | Precipitation | 2019 | 50.8 | 41.8 | 54.7 | 71.9 | 51.5 |
| Mannheim | Precipitation | 2020 | 51.4 | 34.0 | 66.1 | 39.9 | NA |
| Mannheim | Precipitation | 2021 | NA | 30.1 | 92.4 | 37.4 | 51.8 |
| Mannheim | Precipitation | 2022 | 43.4 | 36.6 | 31.8 | 101.7 | 50.6 |
| Mannheim | Precipitation | 2023 | 22.6 | 49.8 | 65.6 | 64.3 | 52.7 |
| ${\bf Mannheim}$ | Precipitation | 2024 | 53.8 | 78.1 | 76.4 | NA | NA |

Table 5: Monthly Means over all Years (Temperature / degree C and Monthly Precipitation / mm)

| City | Month | Temperature | Precipitation |
|----------|----------------------|-------------|---------------|
| Mannheim | Jan | 1.8 | 37.9 |
| Mannheim | Feb | 2.9 | 34.4 |
| Mannheim | Mar | 6.3 | 37.2 |
| Mannheim | Apr | 10.2 | 42.8 |
| Mannheim | May | 14.6 | 59.6 |
| Mannheim | Jun | 17.8 | 67.2 |
| Mannheim | Jul | 19.5 | 69.8 |
| Mannheim | Aug | 18.8 | 64.5 |
| Mannheim | Sep | 15.3 | 52.2 |
| Mannheim | Oct | 10.3 | 49.1 |
| Mannheim | Nov | 5.6 | 44.4 |
| Mannheim | Dec | 2.7 | 43.6 |

3.2 Data Sources

3.2.1 Temperatures and Precipitation

• Basel / Davos: Federal Office of Meteorology and Climatology MeteoSwiss

https://www.meteoswiss.admin.ch/home/climate/swiss-climate-in-detail/homogeneous-data-series-since-1864.html

https://www.dwd.de/DE/leistungen/klimadatendeutschland/klarchivtagmonat.html

 $(Monatswerte\ historisch\ und\ aktuell,\ column\ MO_TT\ (Temperature;\ Monatsmittel\ der\ Lufttemperatur\ in\ 2m\ H\"{o}he\ in\ ^{\circ}C\ and\ MO_RR\ (Precipitation;\ Monatssumme\ der\ Niederschlagshoehe\ in\ mm))$

• England Met Office - National Meteorological Service for the UK

 $https://www.metoffice.gov.uk/hadobs/hadcet/data/download.html\ Monthly_HadCET_mean.txt,\ 1659\ to\ date$

3.2.2 CO2 Concentrations

National Oceanic & Atmospheric Administration - Earth System Research Laboratory

 $NOAA\ ESRL\ https://www.esrl.noaa.gov/gmd/ccgg/trends/global.html$

Data file: Mauna Loa CO2 monthly mean data

https://www.esrl.noaa.gov/gmd/ccgg/trends/data.html

3.3 R code

Partially based on c 't Magazin articles by Andreas Krause: #3/2014 p.188 <code>http://www.ct.de/1403188</code> & #6/2014 p.180 <code>http://www.ct.de/1406180</code>