Climate Data Visualization -

Atmospheric CO_2 Concentration / Temperature / Precipitation

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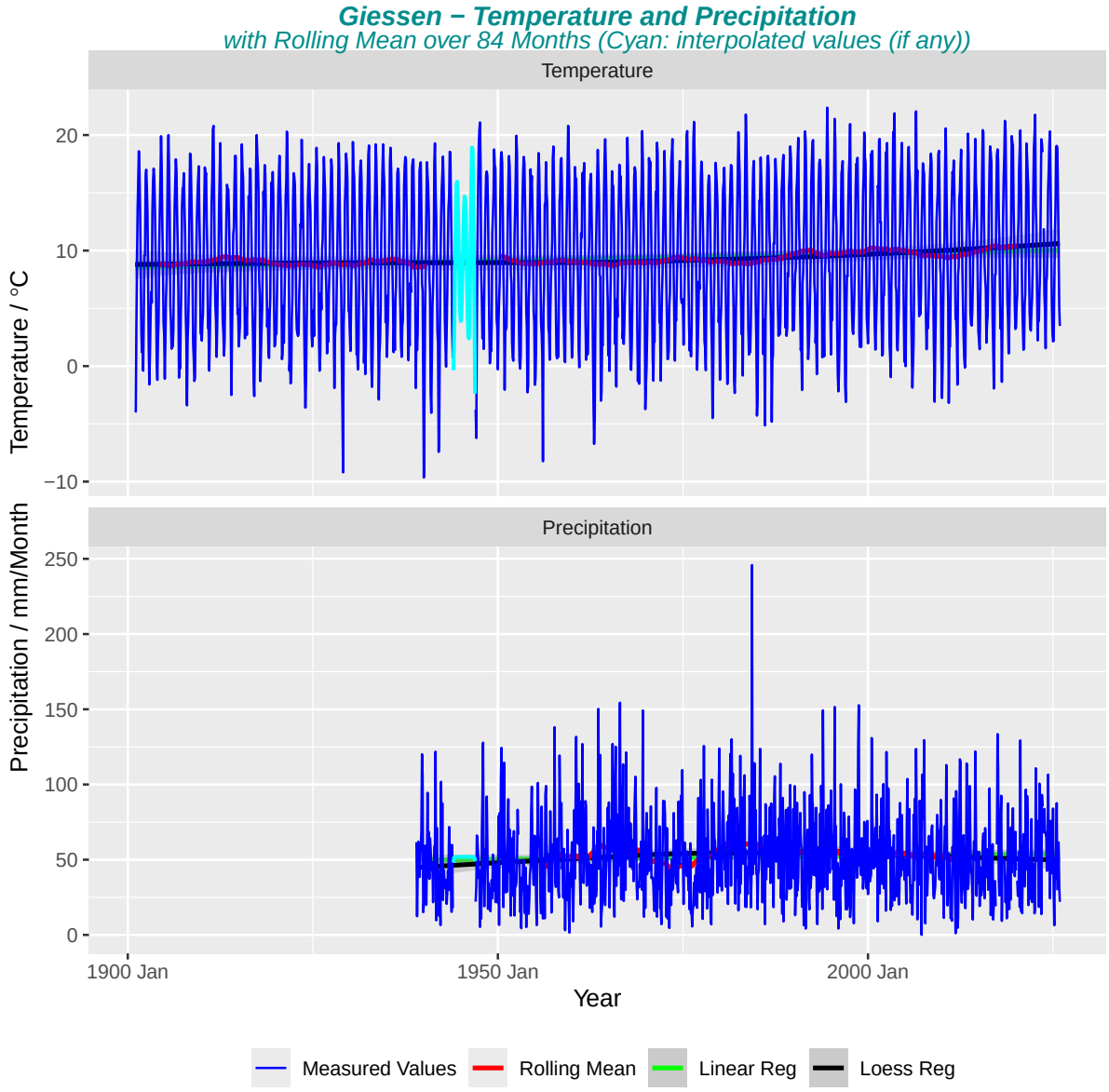
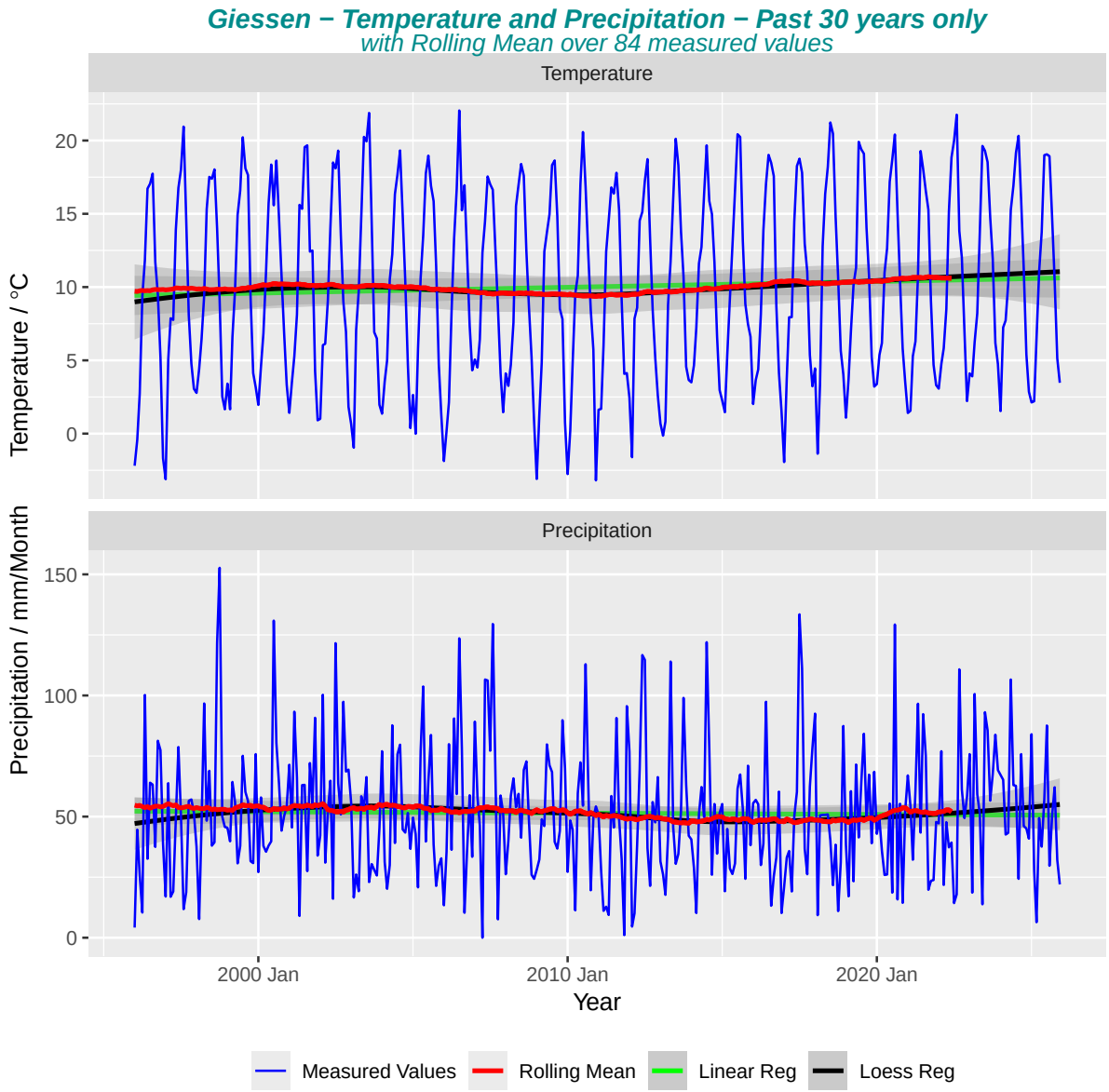
2026-01-08

Contents

1 Giessen - Visualization of Temperature, Precipitation Data 1901 - 2025

1.1 Monthly Time Plots with Rolling Mean



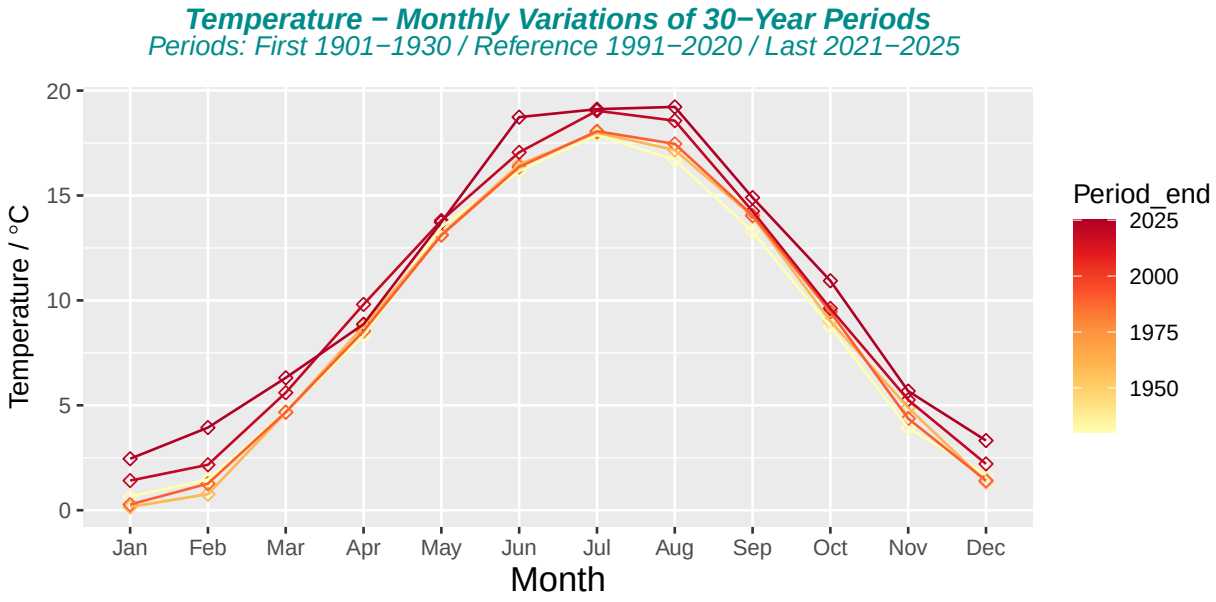


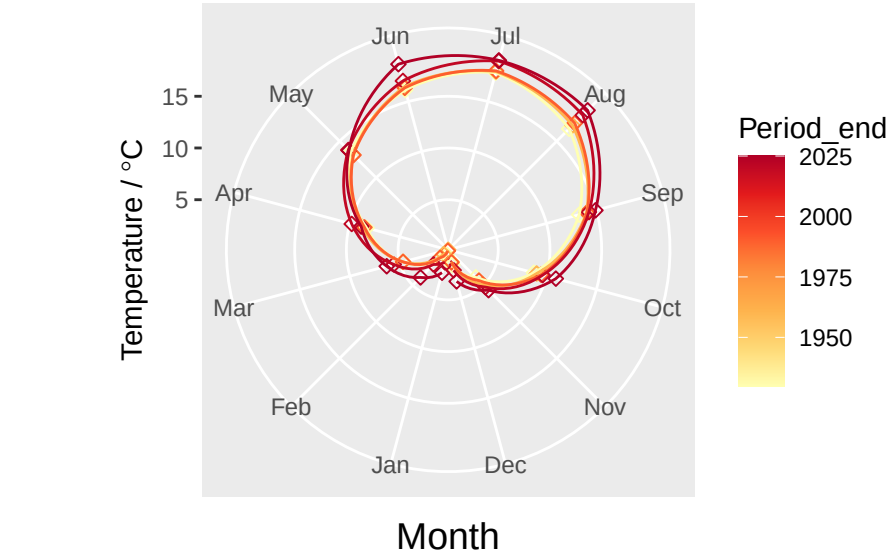
1.2 Annual seasonal plots with monthly breakdown

The seasonal charts show the monthly seasonal patterns, where available.

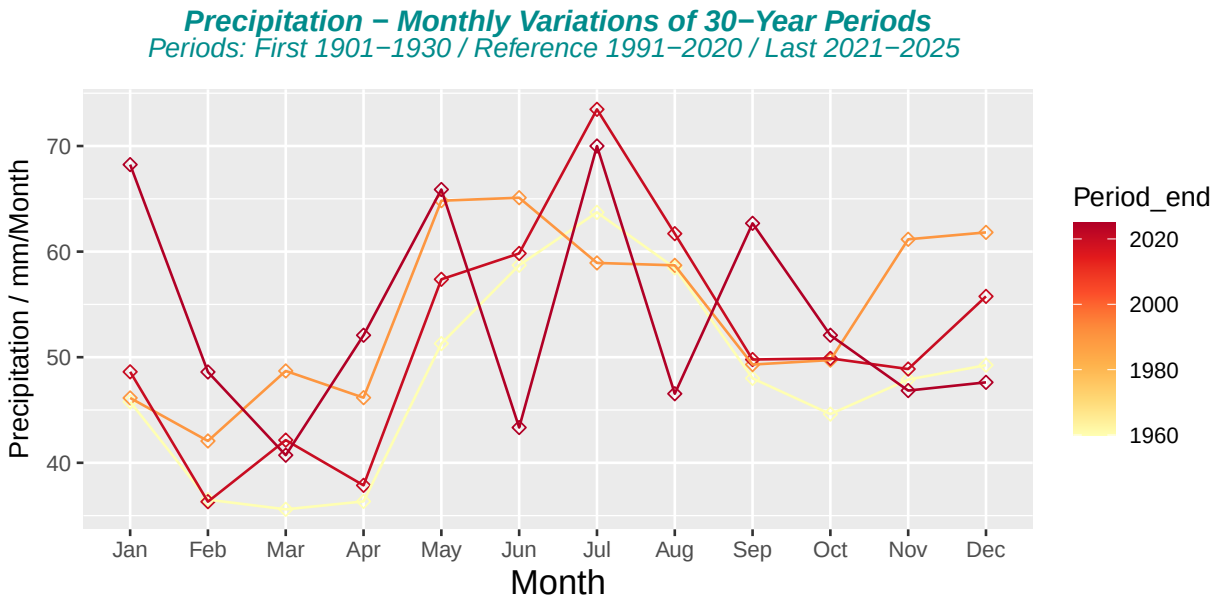

Monthly Data with Local Polynomial Regression Fitting
Giessen 1901 − 2025
Temperature
Precipitation
Temperature / °C
Precipitation / mm/Month
20
10
0
−10
250
200
150
100
50
0
1900 Jan
1950 Jan
2000 Jan
Year
Month
Jan
Feb
Mar
Apr
May
Jun
Jul
Aug
Sep
Oct
Nov
Dec

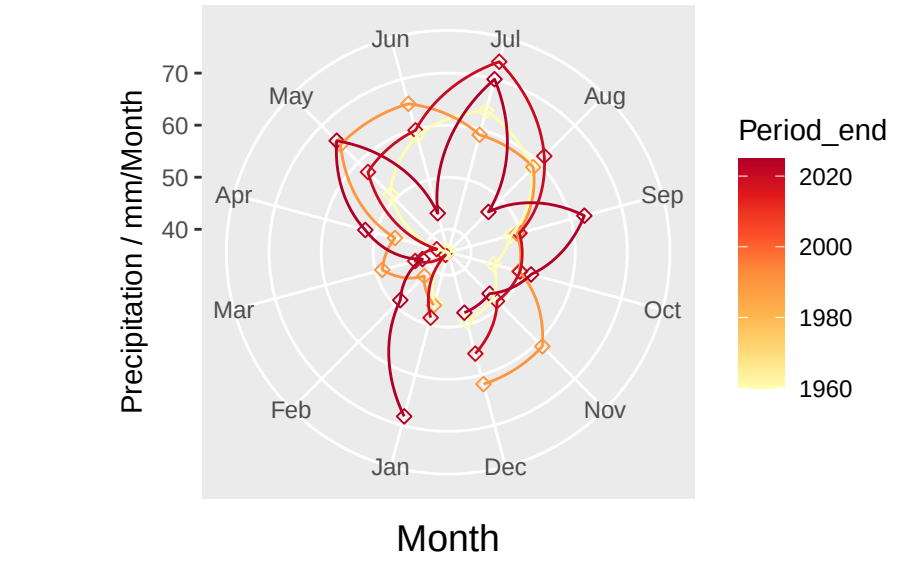
1.2.1 30-year period plots with monthly breakdown - Cartesian and Polar Coordinates





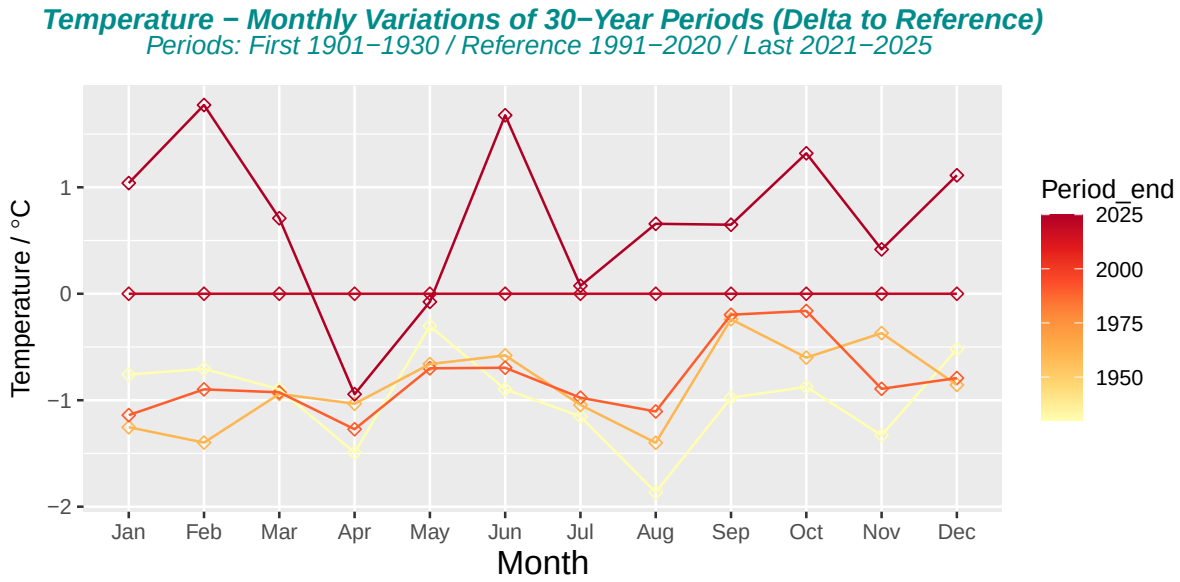

```
#>
#> _
```

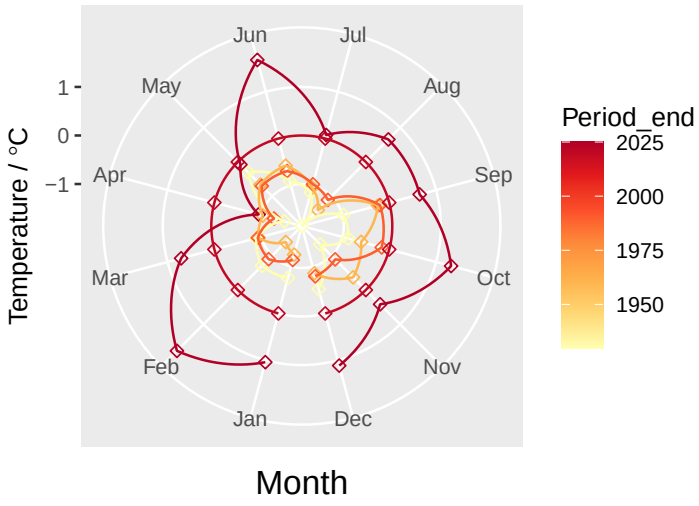

Precipitation − Monthly Variations of 30−Year Periods
Periods: First 1901−1930 / Reference 1991−2020 / Last 2021−2025
Precipitation / mm/Month
70
60
50
40
Jan
Feb
Mar
Apr
May
Jun
Jul
Aug
Sep
Oct
Nov
Dec
Month
Period_end
2020
2000
1980
1960


Precipitation − Monthly Variations of 30−Year Periods
Periods: First 1901−1930 / Reference 1991−2020 / Last 2021−2025
Precipitation / mm/Month
70
60
50
40
Jun
Jul
May
Aug
Apr
Sep
Mar
Oct
Feb
Nov
Jan
Dec
Month
Period_end
2020
2000
1980
1960

```
#>
#> _
```

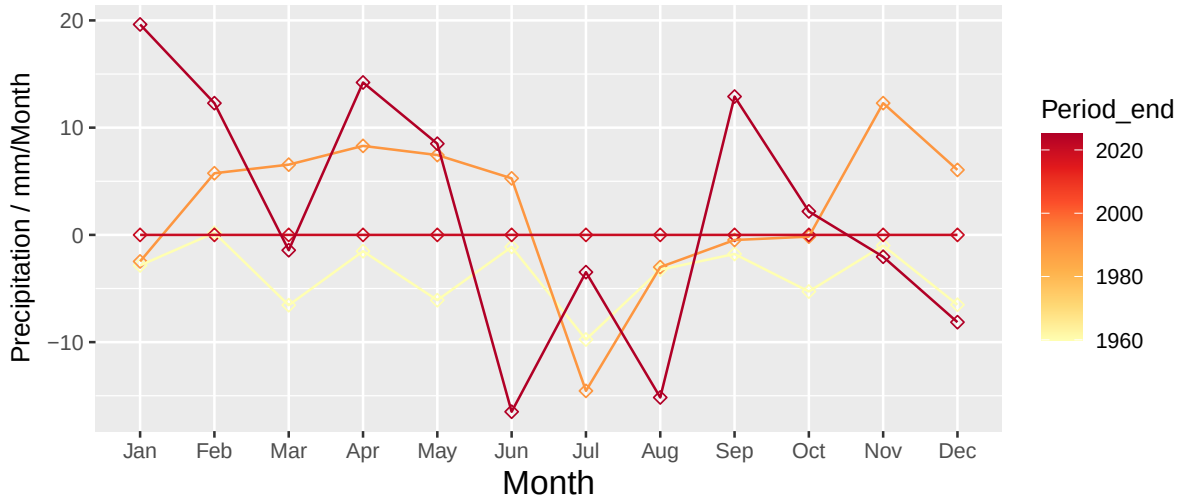
1.2.2 Plot Monthly Delta to Reference Period - Cartesian and Polar Coordinates





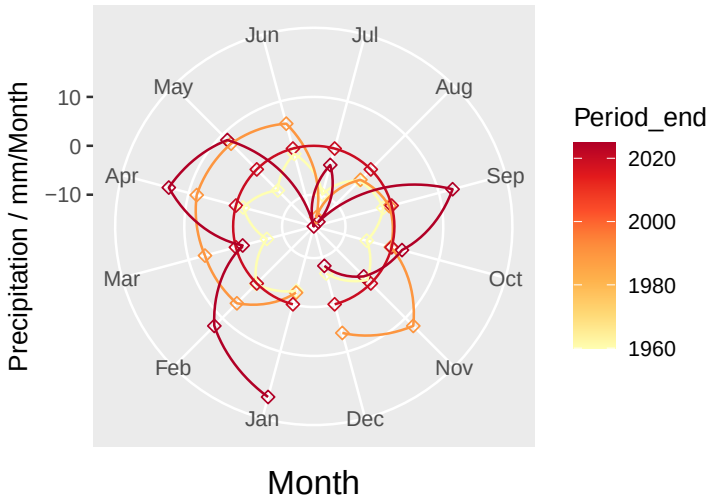
Precipitation − Monthly Variations of 30−Year Periods (Delta to Reference)

Periods: First 1901−1930 / Reference 1991−2020 / Last 2021−2025

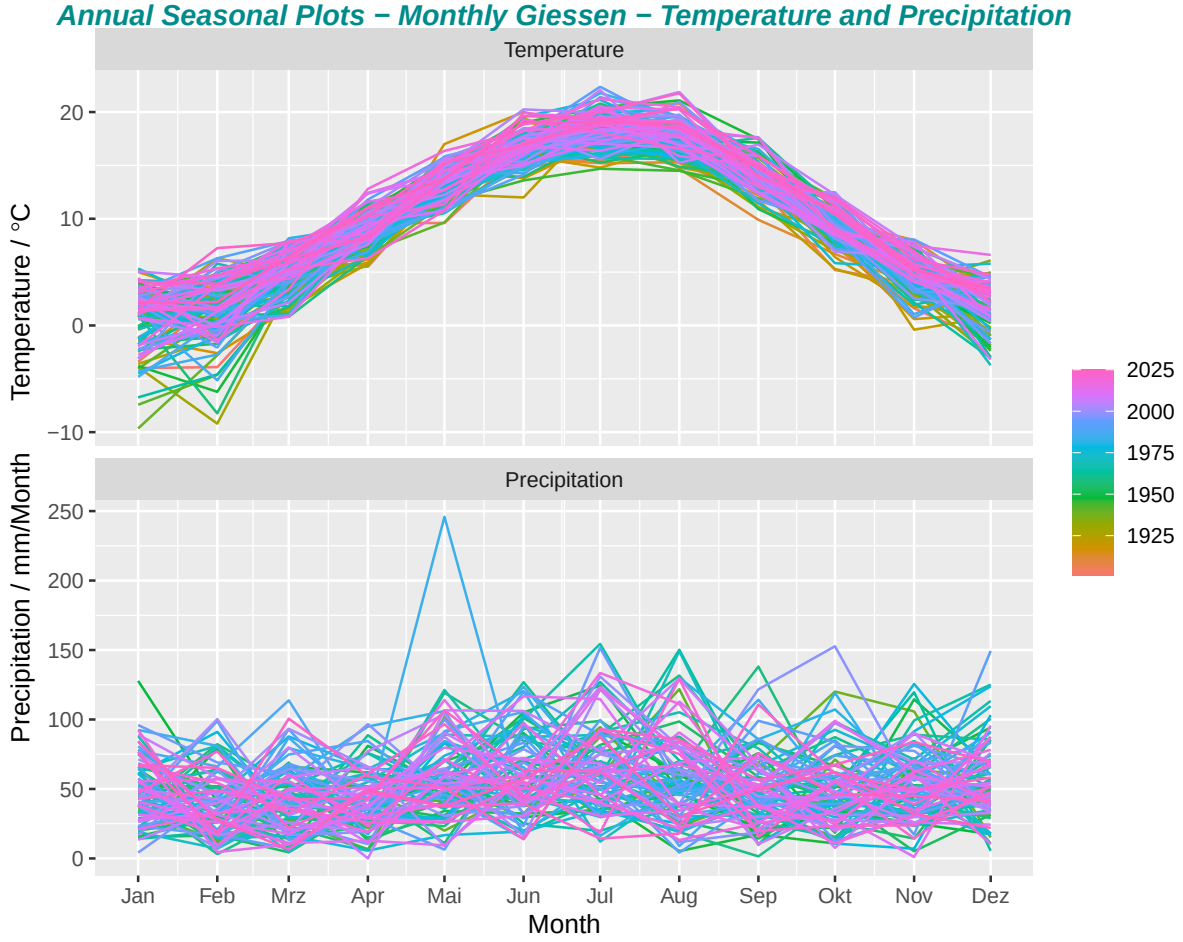


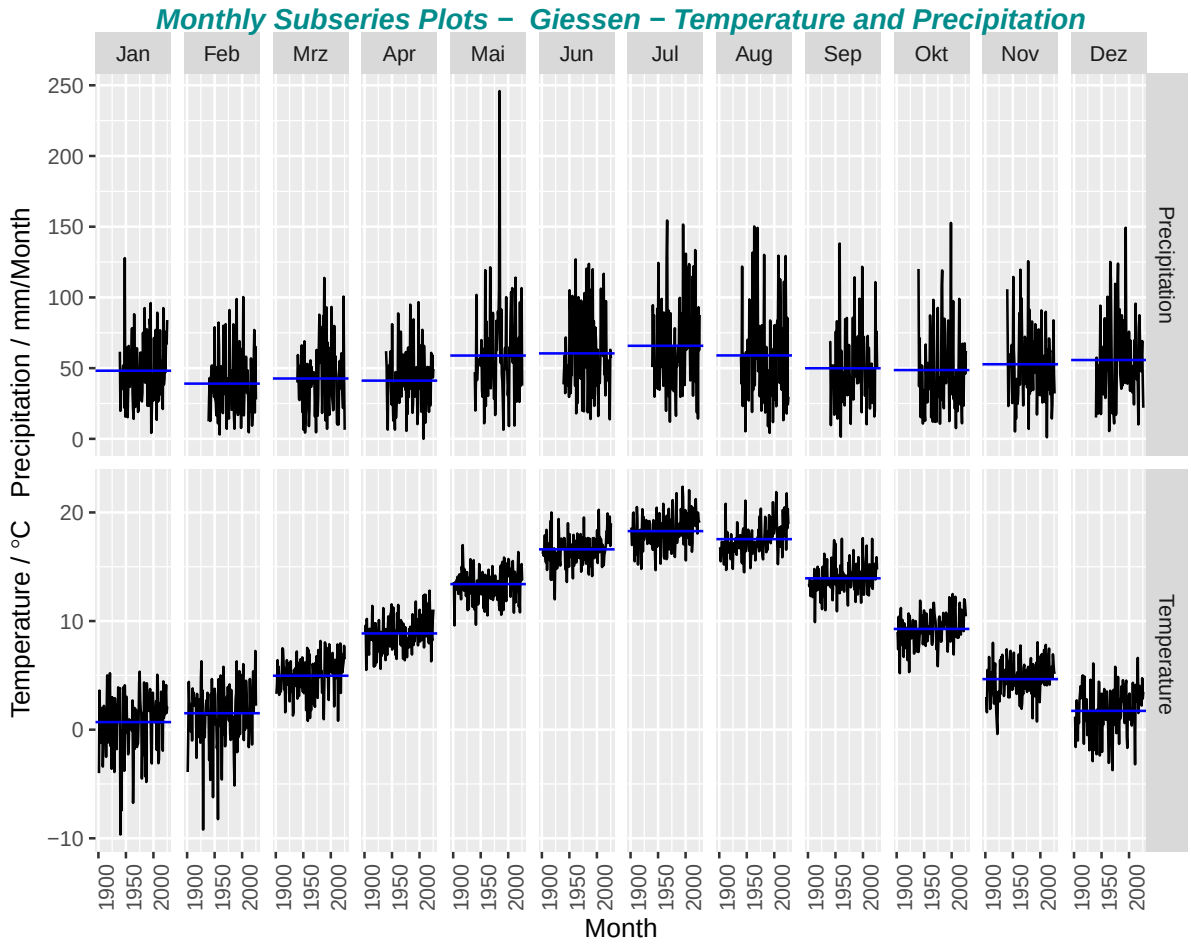
Precipitation − Monthly Variations of 30−Year Periods (Delta to Reference)

Periods: First 1901−1930 / Reference 1991−2020 / Last 2021−2025



Annual Seasonal Plots − Monthly Giessen − Temperature and Precipitation

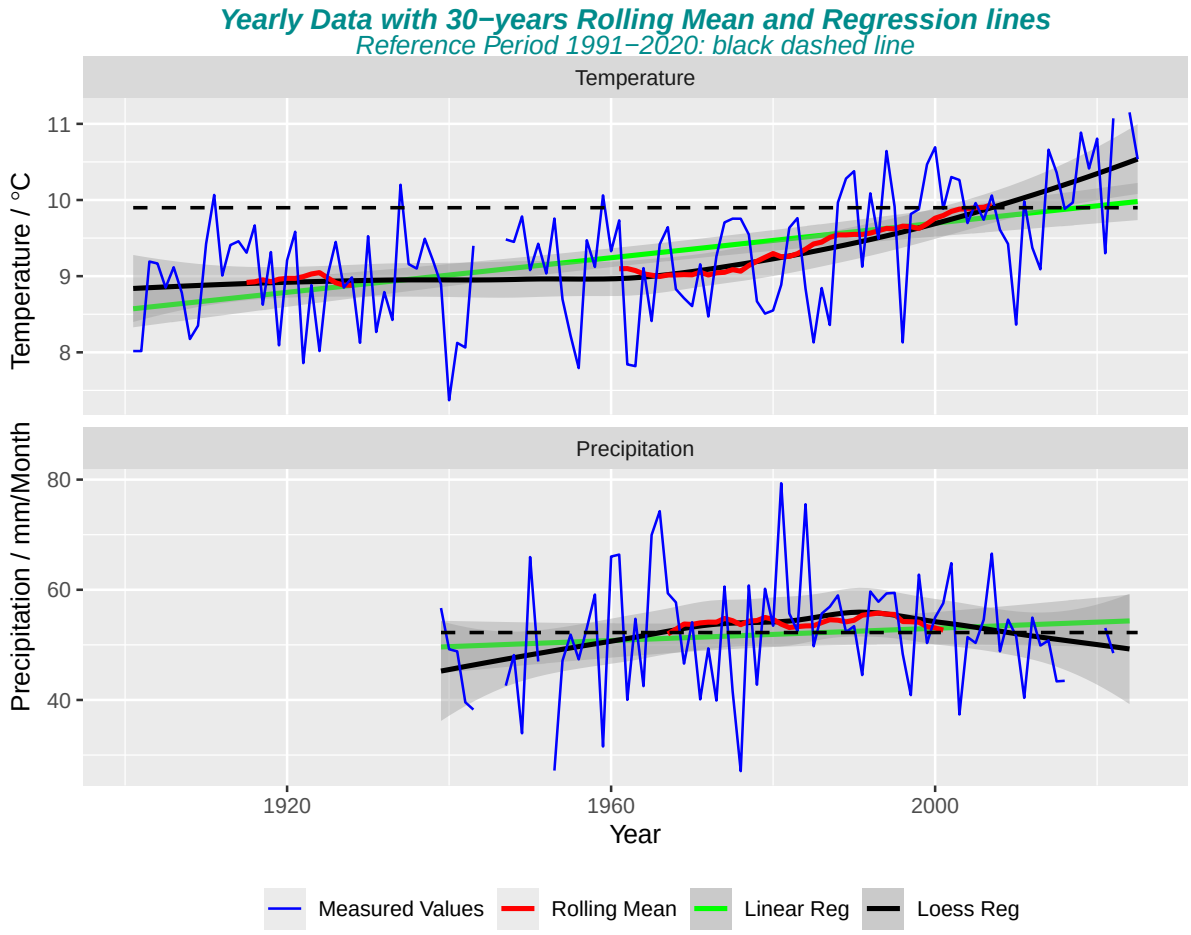




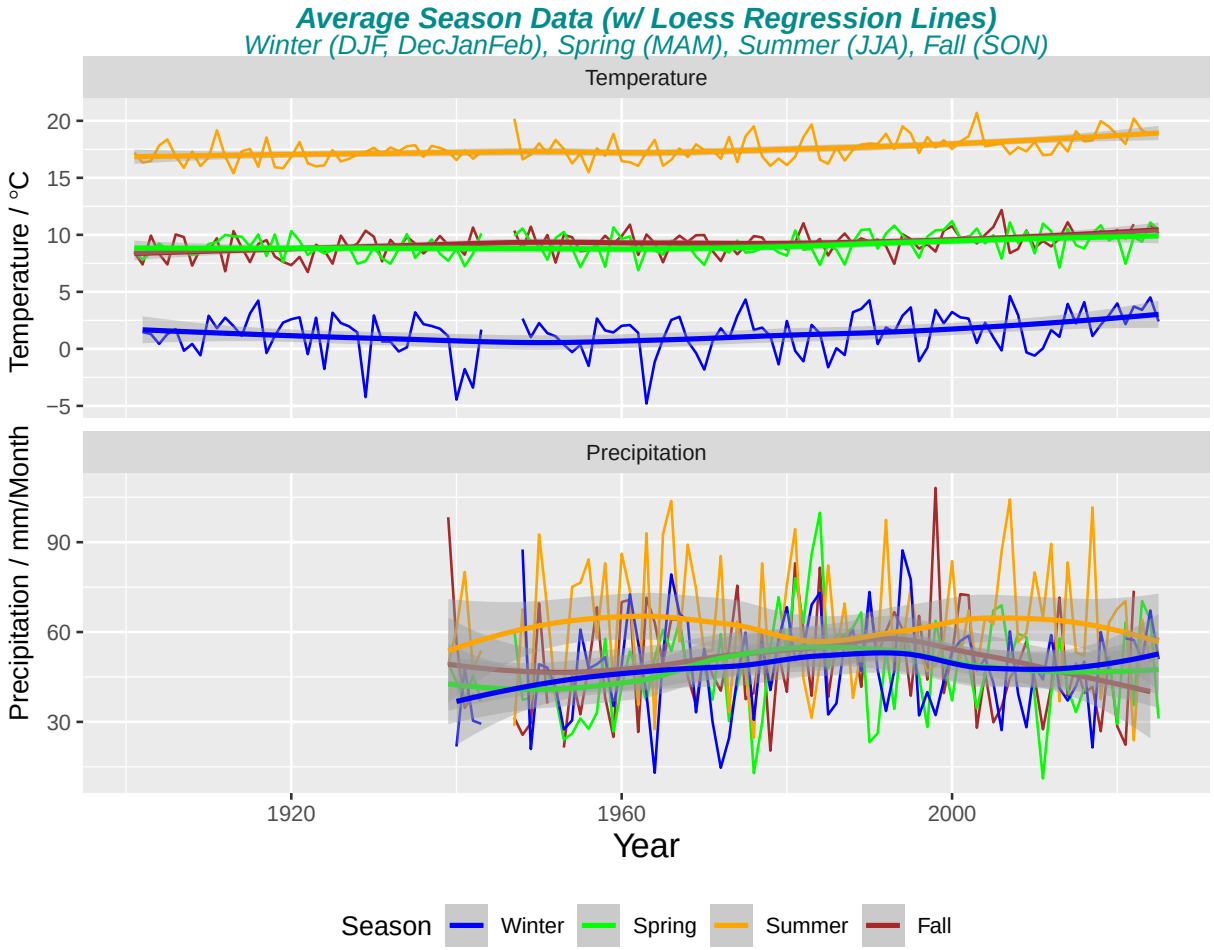
The blue horizontal lines within the seasonal subseries plot indicate the means for each month.

1.3 Annual Giessen - Temperature and Precipitation

1.3.1 Annual Time Plot of Temperature, Precipitation



1.3.2 Annual Seasonal Plot of Temperature, Precipitation



2 Trend and Seasonal Analysis

2.1 Time Series Decomposition - Trend and Seasonal Components

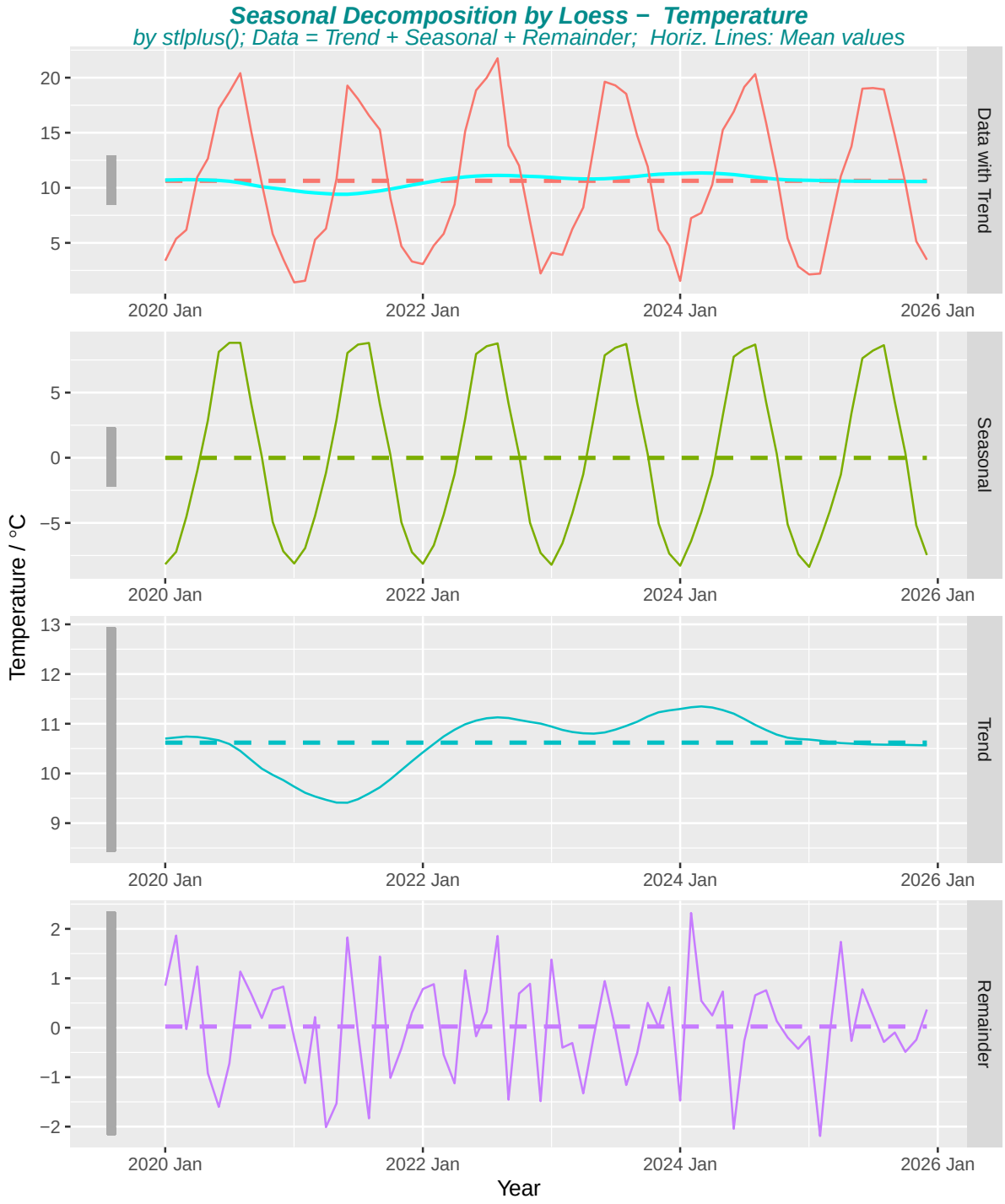
An *additive model* would be used when the variations around the trend do not vary with the level of the time series whereas a *multiplicative model* would be appropriate if the trend is proportional to the level of the time series.

Time series using an

- additive model: $y_t = T_t + C_t + S_t + \epsilon_t$
- multiplicative model: $y_t = T_t * C_t * S_t * \epsilon_t$

Trend / Cycle / Seasonal / Noise component
Cyclical components is often grouped into the Trend component

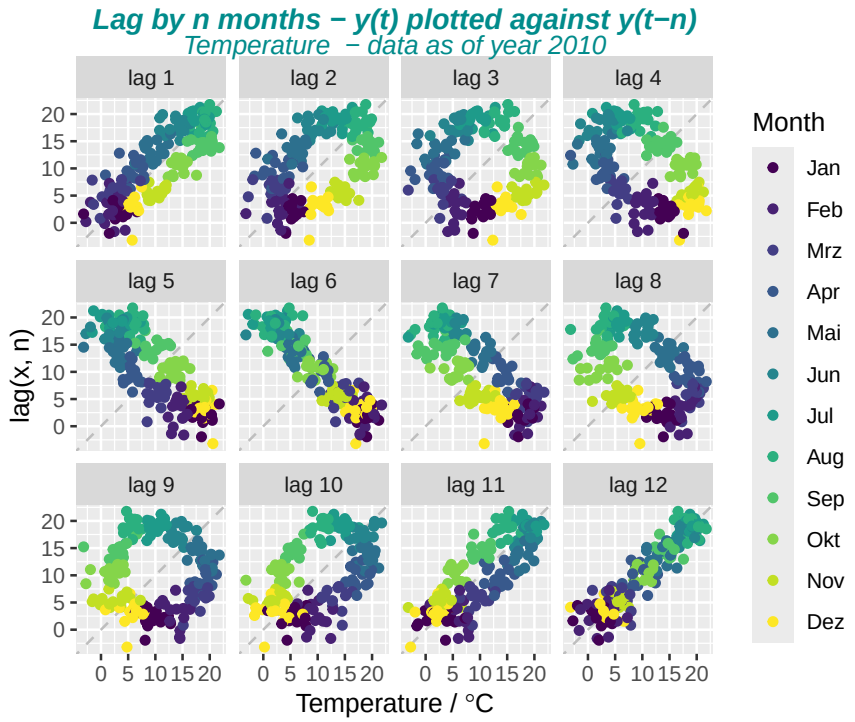
For *Seasonal decomposition of time series by Loess (stlplus)* uses in general an additive error model, it only provides facilities for additive decompositions. It is possible to obtain a multiplicative decomposition by first taking logs of the data.

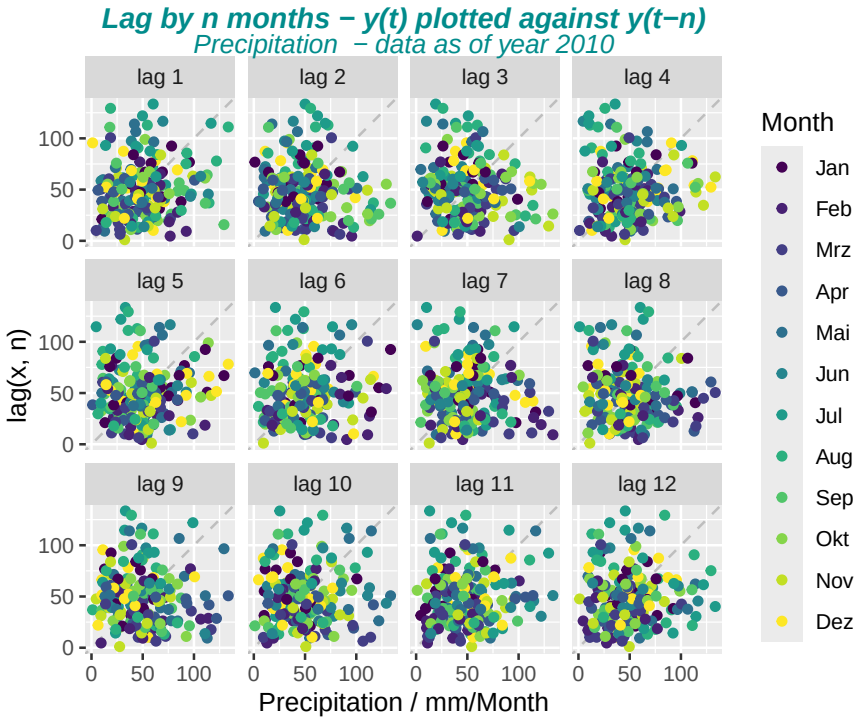


2.2 Periodicities - Season Frequency

2.2.1 Lag Plot - Differences

Lagged scatterplots, where the horizontal axis shows lagged ($k = 1, .., 12$) values of the time series. Each graph shows y_t plotted against y_{t-k} for different values of k. For seasonal data the relationship is strongly positive at a lag $k = 12$, reflecting the strong seasonality of the data. The strongly negative relationship is evident in the case oflag $k = 6$.


Lag by n months − y(t) plotted against y(t−n)
Temperature − data as of year 2010
lag 1
lag 2
lag 3
lag 4
lag 5
lag 6
lag 7
lag 8
lag 9
lag 10
lag 11
lag 12
lag(x, n)
Temperature / °C
Month
Jan
Feb
Mrz
Apr
Mai
Jun
Jul
Aug
Sep
Okt
Nov
Dez


Lag by n months − y(t) plotted against y(t−n)
Precipitation − data as of year 2010
lag 1
lag 2
lag 3
lag 4
lag 5
lag 6
lag 7
lag 8
lag 9
lag 10
lag 11
lag 12
lag(x, n)
Precipitation / mm/Month
Month
Jan
Feb
Mrz
Apr
Mai
Jun
Jul
Aug
Sep
Okt
Nov
Dez

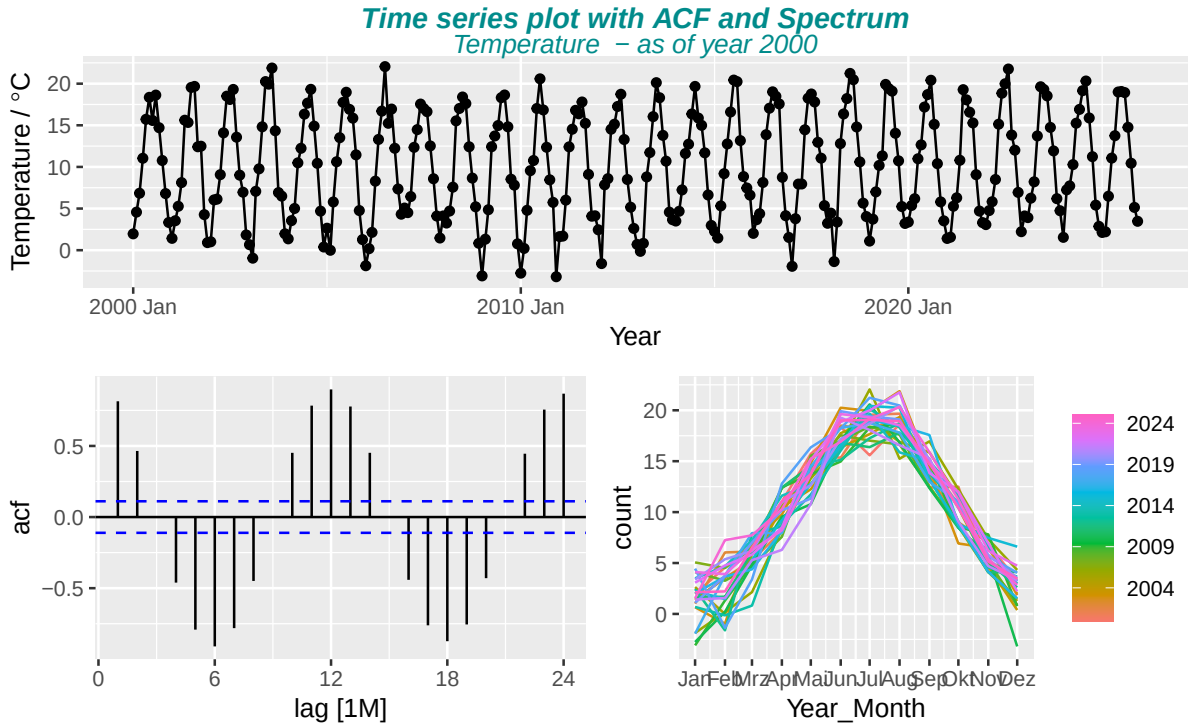
2.2.2 Periodogram - Spectral Density Estimation of a Time Series

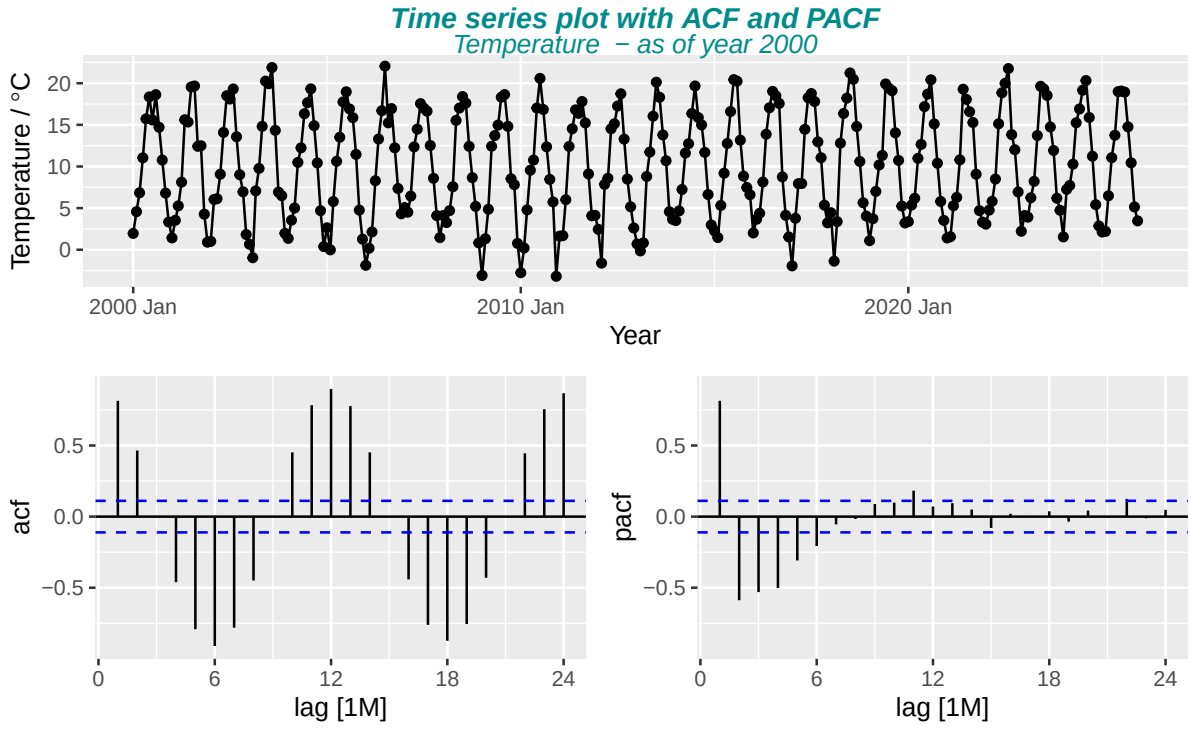
The spectral density characterizes the frequency content of the signal. One purpose of estimating the spectral density is to detect any periodicities in the data, by observing peaks at the frequencies corresponding to these periodicities.

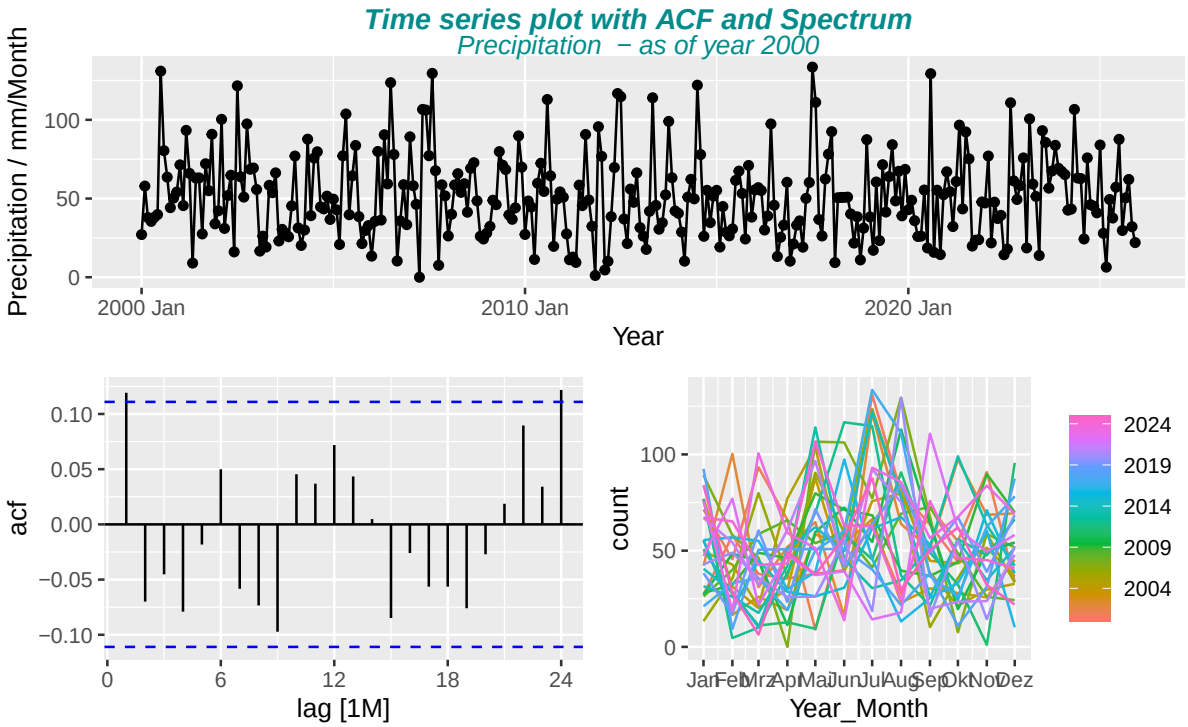
At frequency $\lambda = 1/12$ there is a significant peak => This pattern repeats every full frequency = every 12 months / every year

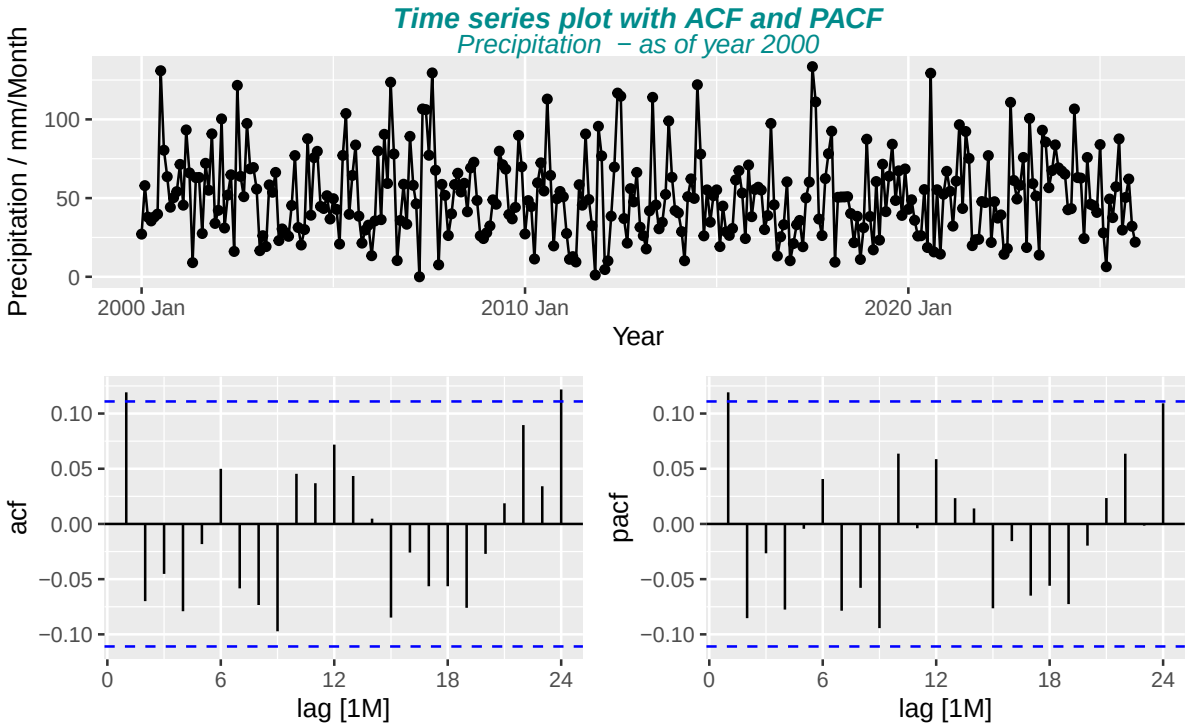
The remaining peaks are random and therefore cannot be assigned significantly.

Note: The blue dashed lines in the (P)ACF plots ((Partial) Autocorrelation Function) indicate white noise series limits. In that case 95% of the spikes lie within the dashed lines.






Time series plot with ACF and Spectrum
Precipitation − as of year 2000
Precipitation / mm/Month
100
50
0
2000 Jan
2010 Jan
2020 Jan
Year
acf
0.10
0.05
0.00
−0.05
−0.10
0
6
12
18
24
lag [1M]
count
100
50
0
Jan Feb Mrz Apr Mai Jun Jul Aug Sep Okt Nov Dez
Year_Month
2024
2019
2014
2009
2004


Time series plot with ACF and PACF
Precipitation − as of year 2000
Precipitation / mm/Month
100
50
0
2000 Jan
2010 Jan
2020 Jan
Year
acf
0.10
0.05
0.00
−0.05
−0.10
0
6
12
18
24
lag [1M]
pacf
0.10
0.05
0.00
−0.05
−0.10
0
6
12
18
24
lag [1M]

3 Forecasting - Estimate/Train the model

3.1 Forecasting with ETS and ARIMA model

Exponen**T**ial **S**moothing (**ETS**) and **A**uto**R**egressive **I**ntegrated **M**oving **A**verage Forecasting Models **ARIMA** models are the two most widely used approaches to time series forecasting, and provide complementary approaches to the problem.

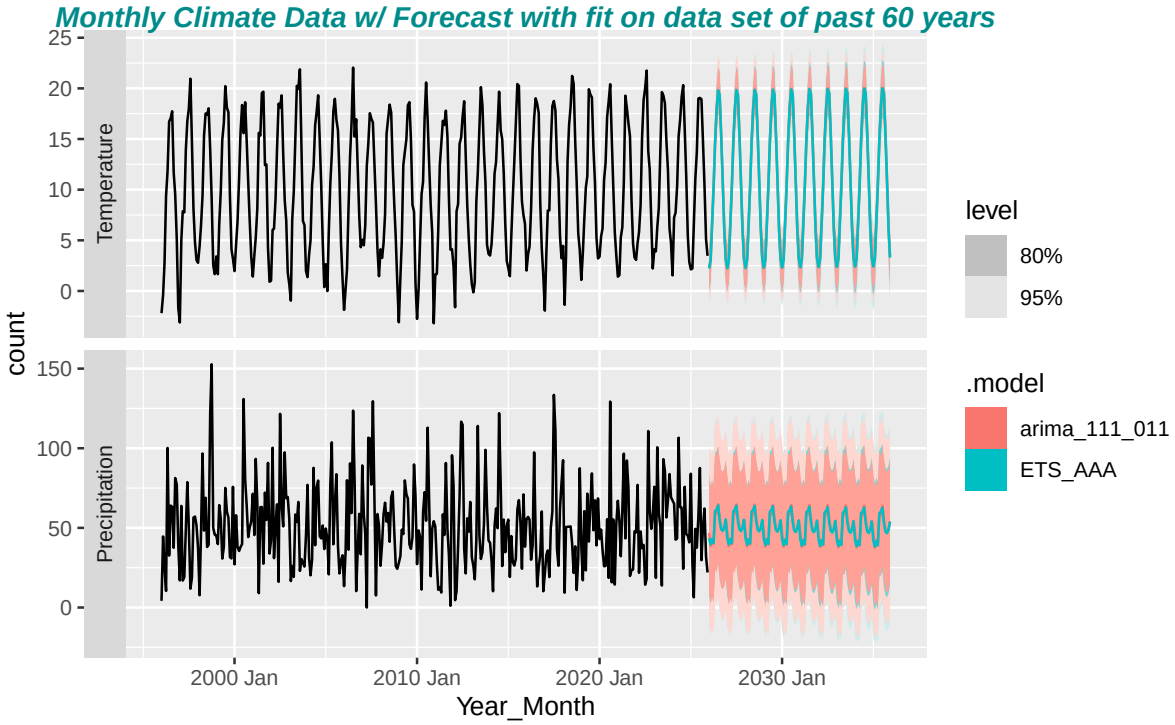
Forecasts produced using **ETS** methods are weighted averages of past observations, with the weights decaying exponentially as the observations get older.

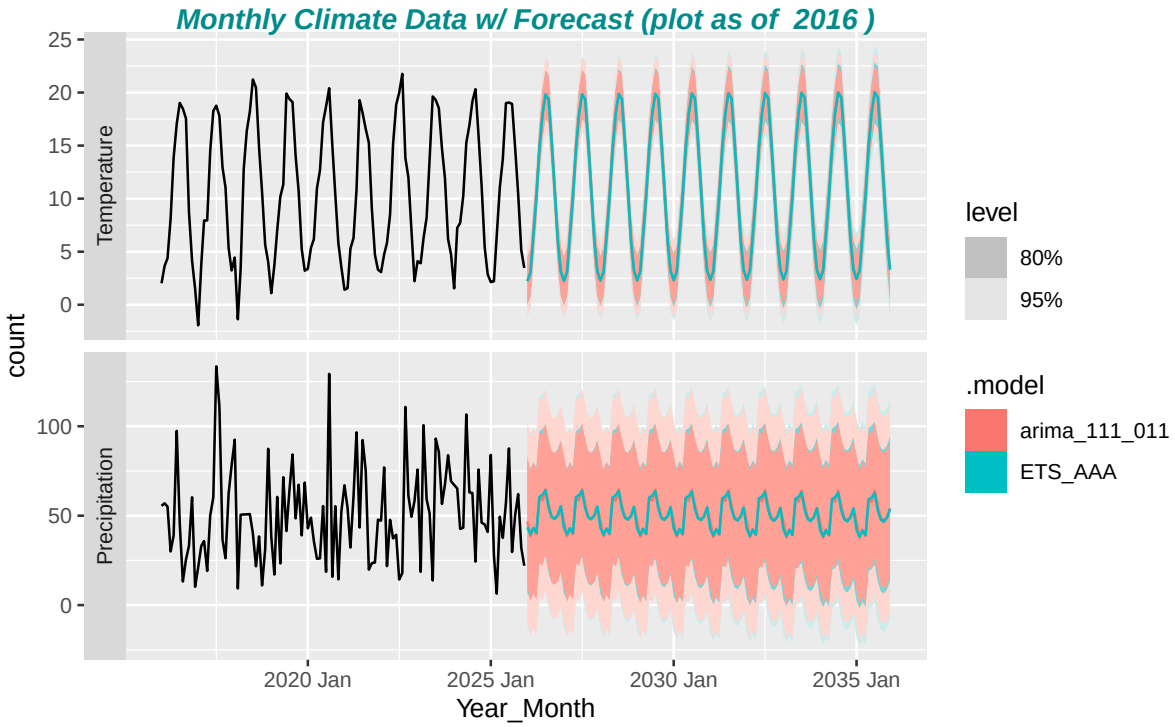
Here a $ETS(A, A|A)$ **model** with additive ("A") *Error term*, *Trend term* and *Seasonal term* was chosen.

While exponential smoothing models are based on a description of the trend and seasonality in the data, **ARIMA** models aim to describe the autocorrelations in the data.

Here a $ARIMA(111)(011)_{12}$ **model** with autoregressive, differencing, and moving average terms of (111) in the ordinary and 011 in the seasonal term with a seasonal period 12 (12 months/year)

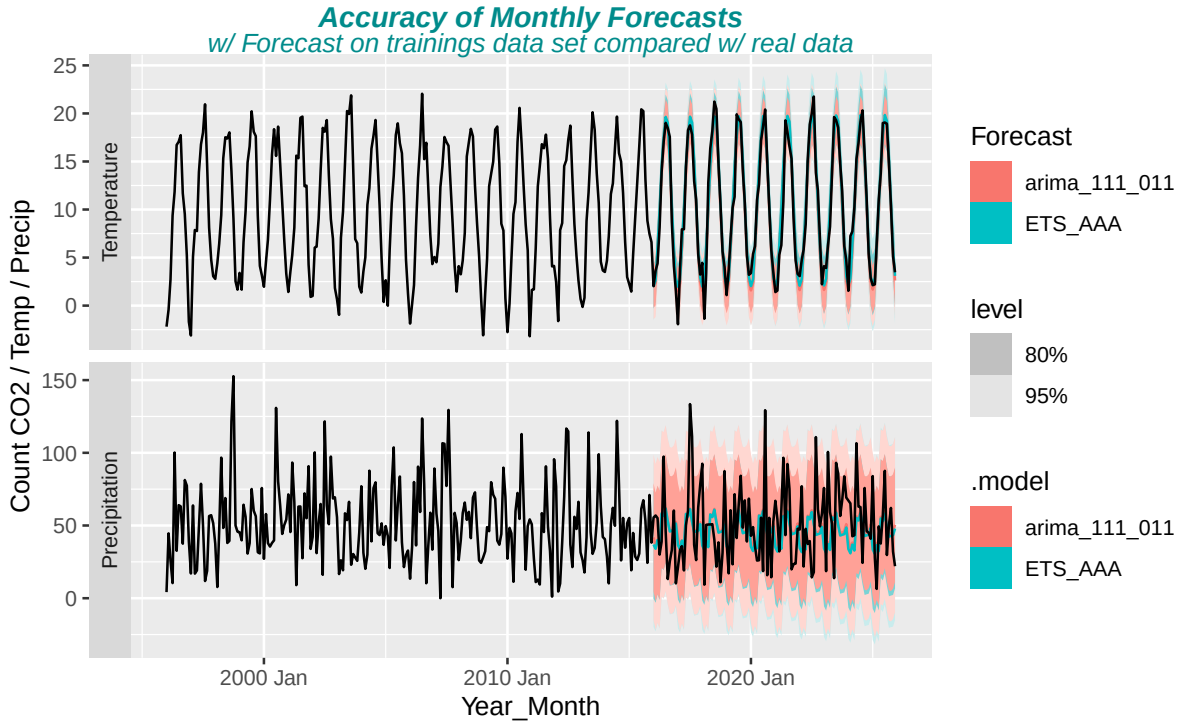
```
#> # A mable: 2 x 4
#> # Key:     City, Measure [2]
#>   City    Measure            ETS_AAA              arima_111_011
#>   <chr>   <fct>              <model>                    <model>
#> 1 Giessen Temperature   <ETS(A,A,A)> <ARIMA(1,1,1)(0,1,1)[12]>
#> 2 Giessen Precipitation <ETS(A,A,A)> <ARIMA(1,1,1)(0,1,1)[12]>
```




Monthly Climate Data w/ Forecast (plot as of 2016)
count
Temperature
Precipitation
25
20
15
10
5
0
100
50
0
2020 Jan
2025 Jan
2030 Jan
2035 Jan
Year_Month
level
80%
95%
.model
arima_111_011
ETS_AAA

3.2 Forecast Accuracy Evaluation

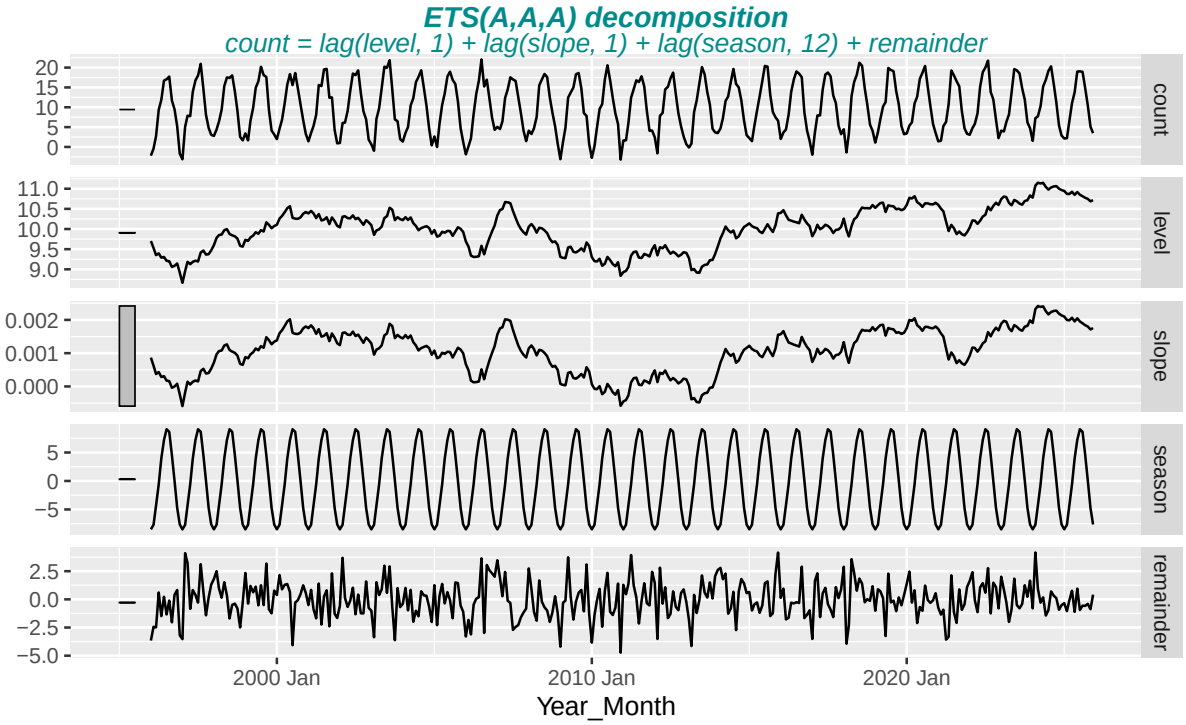
- Forecast Accuracy Evaluation w/ training data “data_train” & test data “data_test”
  - “data” : complete dataset includes the forecasted (future) data range on top of data_train
  - “data_train” = “data” - forecast_range (“data_test”)
    - data used to train the model (~80% of “data)
  - “data_test” = “data” - “data_train”
    - ~ 20% of “data”
  - e.g. for last_year = 2025:
    - data_train is selected from 1966 - 2015
    - data_test is selected from 2016 - 2025



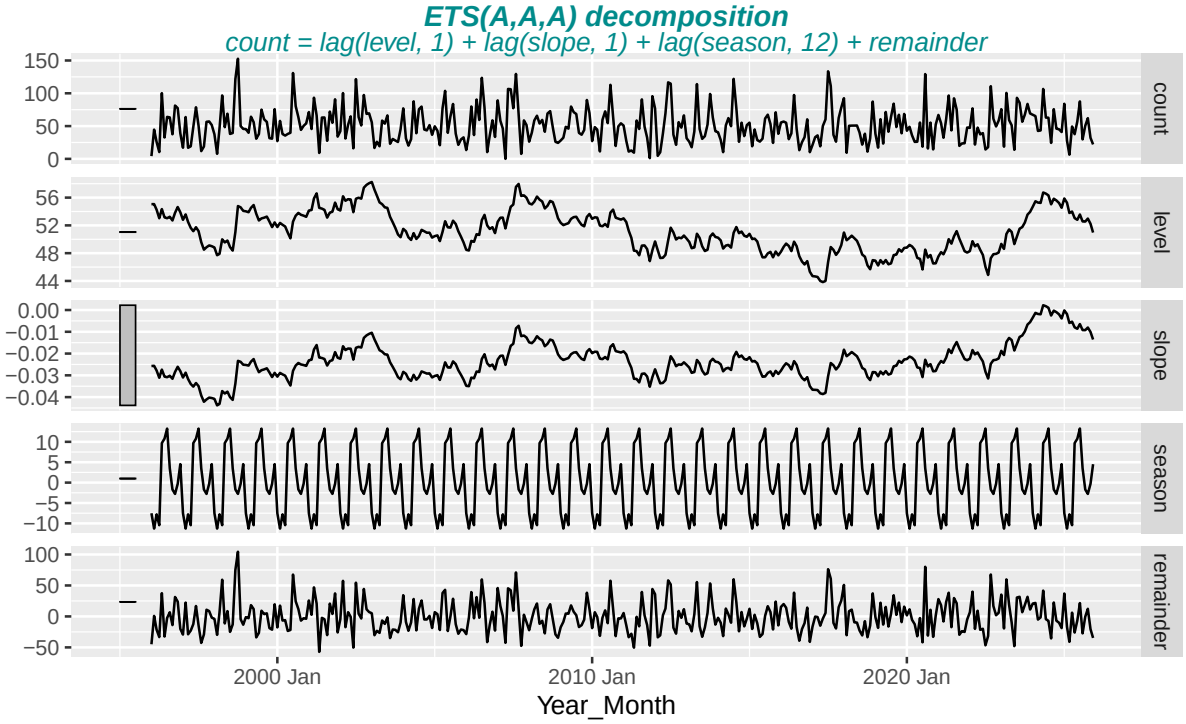
3.2.1 components(fit_ets) - plot of the decomposition of the fitted ETS model

- Note: compare Time series decomposition, for ETS model is valid:
  - count = lag(level, 1) + lag(slope, 1) + lag(season, 12) + remainder

```
#> [1] "Temperature"
```

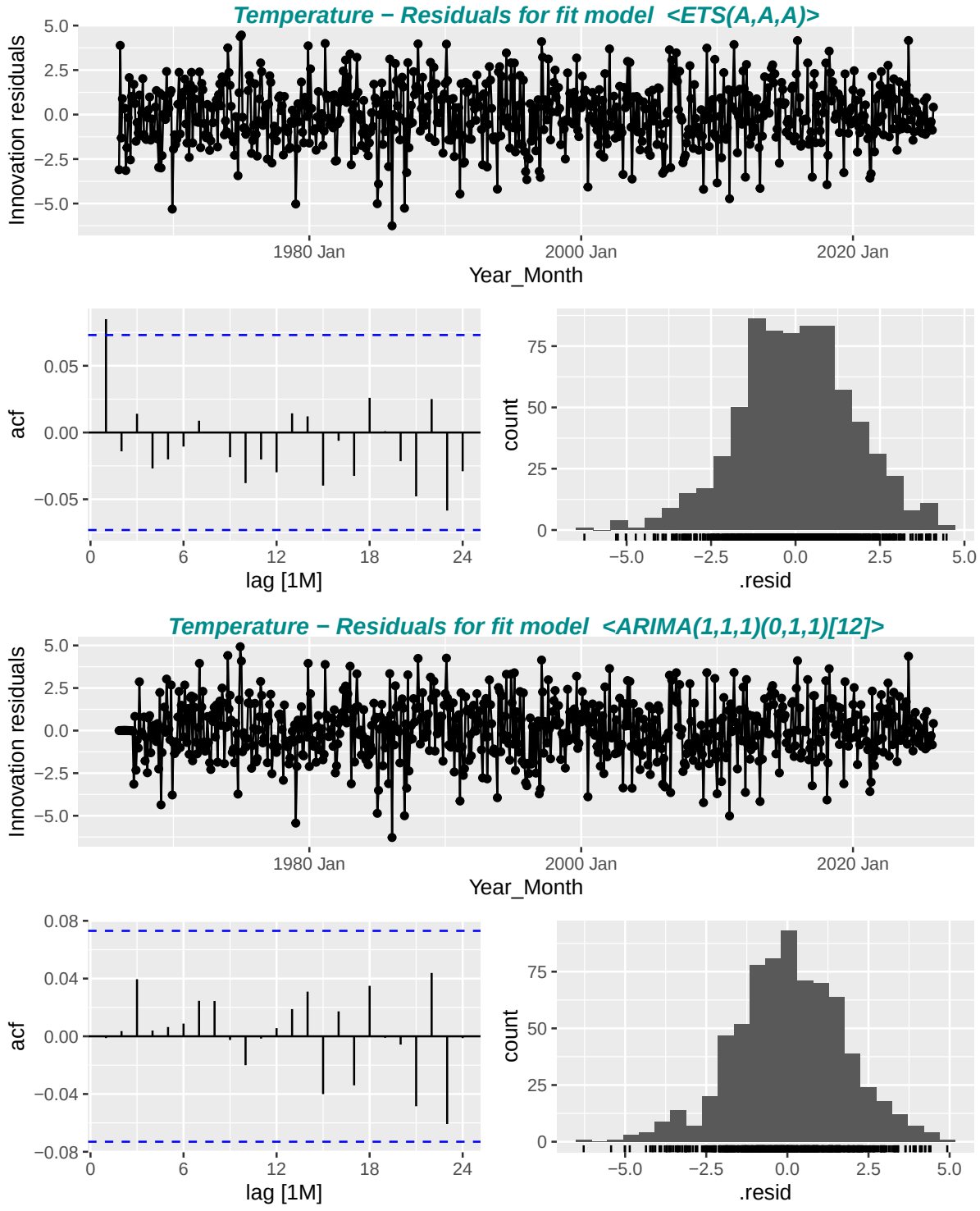


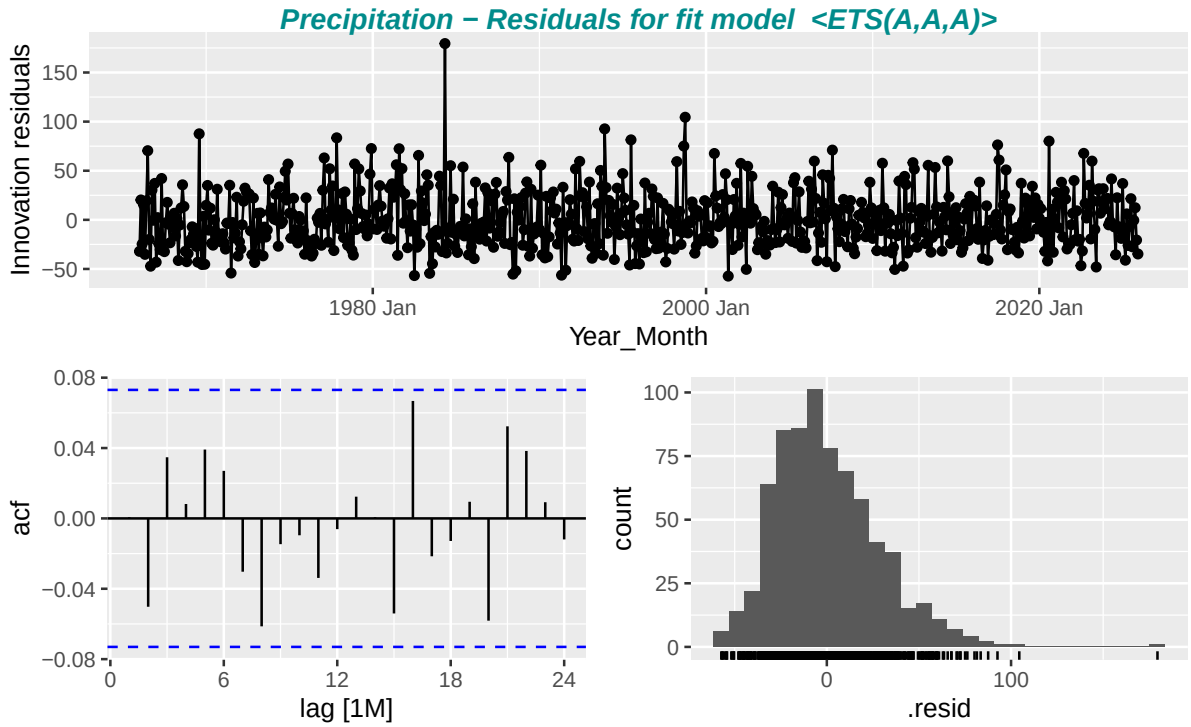

```
#> [1] "Precipitation"
```

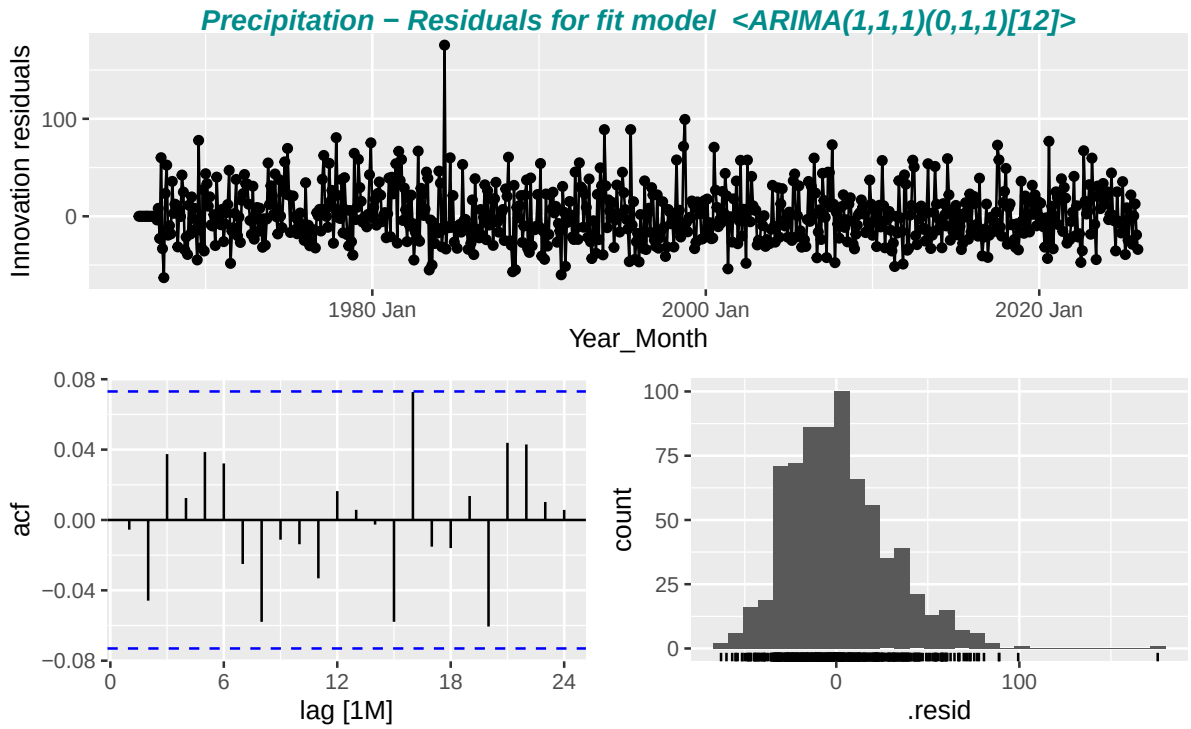


3.2.2 gg_tsresiduals(fit) - plot of innovation residuals, acf and histogram

- gg_tsresiduals(fit) (Ch 7.3 Evaluating the regression model)
  - TS of innovation residuals, acf plot, histogram of residuals | PACF (plot_type='partial')
  - innovation residuals should have constant variance ("homoscedasticity")
  - histogram of the innovation residuals: should be normally distributed




Precipitation − Residuals for fit model <ETS(A,A,A)>
Innovation residuals
150
100
50
0
−50
1980 Jan
2000 Jan
2020 Jan
Year_Month
acf
0.08
0.04
0.00
−0.04
−0.08
0
6
12
18
24
lag [1M]
count
100
75
50
25
0
0
100
.resid


Precipitation − Residuals for fit model <ARIMA(1,1,1)(0,1,1)[12]>
Innovation residuals
100
0
1980 Jan
2000 Jan
2020 Jan
Year_Month
acf
0.08
0.04
0.00
−0.04
−0.08
0
6
12
18
24
lag [1M]
count
100
75
50
25
0
0
100
.resid

4 Forecast Tables

4.1 Yearly mean values of past time periods

Table 1: Mean values for the given time periods; Units: Temperature (degree C), Precipitation (mm/Month), CO2 (ppm)

Period_Time	Temperature	Precipitation
1901-1930	8.9	NA
1931-1960	9.0	48.0
1961-1990	9.1	54.4
1991-2020	9.9	51.8
2021-2025	10.6	53.7

4.2 Yearly mean forecast values for the next 25 years

Table 2: Mean Yearly ARIMA and ETS Forecast values (next 25 years); Units: Temperature (degree C), Precipitation (mm/Month), CO2 (ppm)

City	Measure	Year	ETS_AAA	arima_111_011
Giessen	Temperature	2026	10.73	10.76
Giessen	Temperature	2030	10.81	10.87
Giessen	Temperature	2035	10.92	11.00
Giessen	Temperature	2040	11.02	11.13
Giessen	Temperature	2045	11.13	11.27
Giessen	Temperature	2050	11.23	11.40
Giessen	Precipitation	2026	50.88	50.92
Giessen	Precipitation	2030	50.23	50.53
Giessen	Precipitation	2035	49.42	50.00
Giessen	Precipitation	2040	48.60	49.47
Giessen	Precipitation	2045	47.79	48.94
Giessen	Precipitation	2050	46.98	48.41

Table 3: Forecast increase/decrease over the next 25 years; Units: Temperature (degree C), Precipitation (mm/Month), CO2 (ppm)

Measure	Year.x	Year.y	ETS.x	ARIMA.x	ETS.y	ARIMA.y	Delta_ETS	Delta_ARIMA
Temperature	2026	2050	10.73	10.76	11.23	11.40	0.51	0.64
Precipitation	2026	2050	50.88	50.92	46.98	48.41	-3.90	-2.51

Table 4: Forecast increase/decrease over the next 25 years; Units: Temperature (degree C), Precipitation (mm/Month), CO2 (ppm)

Measure	Month	Year.x	Year.y	Mean.x_ETS	Mean.x_ARIMA	Mean.y_ETS	Mean.y_ARIMA	Delta_ETS	Delta_ARIMA
Temperature	Jan	2026	2050	2.22	2.26	2.73	2.86	0.51	0.61
Temperature	Feb	2026	2050	3.03	3.10	3.54	3.74	0.51	0.64
Temperature	Mar	2026	2050	6.41	6.47	6.92	7.12	0.51	0.64
Temperature	Apr	2026	2050	10.15	10.22	10.65	10.86	0.51	0.64
Temperature	May	2026	2050	14.66	14.66	15.17	15.31	0.51	0.64
Temperature	Jun	2026	2050	17.93	17.98	18.44	18.62	0.51	0.64
Temperature	Jul	2026	2050	19.82	19.81	20.32	20.45	0.51	0.64

Measure	Month	Year.x	Year.y	Mean.x_ETS	Mean.x_ARIMA	Mean.y_ETS	Mean.y_ARIMA	Delta_ETS	Delta_ARIMA
Temperature	Aug	2026	2050	19.37	19.33	19.87	19.97	0.51	0.64
Temperature	Sep	2026	2050	15.26	15.29	15.76	15.93	0.51	0.64
Temperature	Oct	2026	2050	10.80	10.80	11.30	11.45	0.51	0.64
Temperature	Nov	2026	2050	6.00	6.02	6.51	6.67	0.51	0.64
Temperature	Dec	2026	2050	3.10	3.20	3.61	3.84	0.51	0.64
Precipitation	Jan	2026	2050	43.46	46.76	39.56	44.56	-3.90	-2.20
Precipitation	Feb	2026	2050	39.66	38.62	35.76	36.08	-3.90	-2.54
Precipitation	Mar	2026	2050	43.14	43.16	39.24	40.61	-3.90	-2.54
Precipitation	Apr	2026	2050	40.47	39.74	36.57	37.19	-3.90	-2.54
Precipitation	May	2026	2050	60.59	60.25	56.69	57.71	-3.90	-2.54
Precipitation	Jun	2026	2050	61.65	58.70	57.75	56.15	-3.90	-2.54
Precipitation	Jul	2026	2050	64.14	64.83	60.24	62.29	-3.90	-2.54
Precipitation	Aug	2026	2050	54.40	56.36	50.50	53.81	-3.90	-2.54
Precipitation	Sep	2026	2050	49.15	49.33	45.25	46.79	-3.90	-2.54
Precipitation	Oct	2026	2050	48.06	48.58	44.15	46.03	-3.90	-2.54
Precipitation	Nov	2026	2050	50.51	49.69	46.61	47.15	-3.90	-2.54
Precipitation	Dec	2026	2050	55.32	55.07	51.42	52.53	-3.90	-2.54

5 Backup

5.1 Giessen - Average Yearly and Seasonal Data

Table 5: Annual paste("Temperature /", degree * C) (first and last 10 years)

City	Measure	Year	Winter_avg	Spring_avg	Summer_avg	Fall_avg	Year_avg
Giessen	Temperature	1901	NA	8.6	17.2	8.5	8.0
Giessen	Temperature	1902	1.5	7.8	16.3	7.4	8.0
Giessen	Temperature	1903	1.3	8.5	16.5	9.9	9.2
Giessen	Temperature	1904	0.4	9.2	17.8	8.3	9.2
Giessen	Temperature	1905	1.3	8.7	18.4	7.4	8.8
Giessen	Temperature	1906	1.7	8.6	16.9	10.0	9.1
Giessen	Temperature	1907	-0.2	8.5	15.9	9.8	8.8
Giessen	Temperature	1908	0.4	8.2	17.3	7.3	8.2
Giessen	Temperature	1909	-0.6	8.4	16.0	8.8	8.3
Giessen	Temperature	1910	2.9	9.2	16.8	8.6	9.4
Giessen	Temperature	2016	4.1	8.8	18.2	10.2	9.9
Giessen	Temperature	2017	1.1	10.1	18.3	9.8	10.0
Giessen	Temperature	2018	2.1	10.8	20.0	10.3	10.9
Giessen	Temperature	2019	3.0	9.5	19.5	10.0	10.4
Giessen	Temperature	2020	4.0	9.9	18.8	10.4	10.8
Giessen	Temperature	2021	2.2	7.5	18.0	9.7	9.3
Giessen	Temperature	2022	3.7	9.8	20.2	10.9	11.1
Giessen	Temperature	2023	3.4	9.4	19.2	NA	NA
Giessen	Temperature	2024	4.5	11.1	18.8	10.8	11.2
Giessen	Temperature	2025	2.4	10.4	19.0	10.1	10.5

Table 6: Annual Precipitation / mm/Month (first and last 10 years)

City	Measure	Year	Winter_avg	Spring_avg	Summer_avg	Fall_avg	Year_avg
Giessen	Precipitation	1939	NA	49.7	49.0	98.3	56.7
Giessen	Precipitation	1940	21.8	43.4	60.9	56.6	49.2
Giessen	Precipitation	1941	48.1	37.0	80.1	34.7	48.8
Giessen	Precipitation	1942	30.4	45.5	47.7	39.0	39.6
Giessen	Precipitation	1943	29.4	37.1	53.8	37.1	38.2
Giessen	Precipitation	1944	NA	NA	NA	NA	NA
Giessen	Precipitation	1945	NA	NA	NA	NA	NA
Giessen	Precipitation	1946	NA	NA	NA	NA	NA
Giessen	Precipitation	1947	NA	60.5	28.7	31.4	42.6
Giessen	Precipitation	1948	87.6	37.4	67.5	25.7	48.1
Giessen	Precipitation	2016	50.2	41.3	52.1	39.6	43.5
Giessen	Precipitation	2017	21.5	NA	101.6	41.8	NA
Giessen	Precipitation	2018	60.0	NA	37.6	26.9	NA
Giessen	Precipitation	2019	47.6	51.8	63.2	51.6	52.0
Giessen	Precipitation	2020	NA	29.3	67.8	28.5	NA
Giessen	Precipitation	2021	57.9	63.2	70.3	22.4	53.1
Giessen	Precipitation	2022	57.3	35.6	23.8	73.8	48.5
Giessen	Precipitation	2023	50.9	70.4	64.2	NA	NA
Giessen	Precipitation	2024	67.2	64.2	50.0	55.7	56.9
Giessen	Precipitation	2025	50.9	31.1	58.2	NA	NA

Table 7: Monthly Means over all Years (Temperature / degree C and Monthly Precipitation / mm)

City	Month	Temperature	Precipitation
Giessen	Jan	0.7	48.2
Giessen	Feb	1.5	39.1
Giessen	Mar	5.0	42.7
Giessen	Apr	8.9	41.2
Giessen	May	13.4	58.9
Giessen	Jun	16.6	60.4
Giessen	Jul	18.3	65.8
Giessen	Aug	17.5	59.0
Giessen	Sep	13.9	49.9
Giessen	Oct	9.3	48.6
Giessen	Nov	4.7	52.7
Giessen	Dec	1.7	55.7

5.2 Giessen - Head and tail of data

```
#> # A tsibble: 6 x 5 [1M]
#> # Key:       City, Measure [1]
#> # Groups:    City, Measure [1]
#>   City    Measure     Year_Month Period_Time count
#>   <chr>   <fct>            <mth> <chr>       <dbl>
#> 1 Giessen Temperature   1901 Jan 1901-1930   -4
#> 2 Giessen Temperature   1901 Feb 1901-1930   -3.9
#> 3 Giessen Temperature   1901 Mrz 1901-1930    3.3
#> 4 Giessen Temperature   2025 Okt 2021-2025   10.4
#> 5 Giessen Temperature   2025 Nov 2021-2025    5.14
#> 6 Giessen Temperature   2025 Dez 2021-2025    3.47
#> # A tsibble: 6 x 5 [1M]
#> # Key:       City, Measure [1]
#> # Groups:    City, Measure [1]
#>   City    Measure       Year_Month Period_Time count
#>   <chr>   <fct>              <mth> <chr>       <dbl>
#> 1 Giessen Precipitation   1939 Jan 1931-1960    61.6
#> 2 Giessen Precipitation   1939 Feb 1931-1960    12.4
#> 3 Giessen Precipitation   1939 Mrz 1931-1960    39.9
#> 4 Giessen Precipitation   2025 Okt 2021-2025    62.1
#> 5 Giessen Precipitation   2025 Nov 2021-2025    32.1
#> 6 Giessen Precipitation   2025 Dez 2021-2025    22
```

5.3 Data Sources

5.3.1 Temperatures and Precipitation

- Basel / Davos: **Federal Office of Meteorology and Climatology MeteoSwiss**
  - https://www.meteoswiss.admin.ch/home/climate/swiss-climate-in-detail/homogeneous-data-series-since-1864.html
- Cottbus/ Giessen/ Hohenpeissenberg/ Mannheim/ Potsdam: **DWD Archiv Monats- und Tageswerte**
  - https://www.dwd.de/DE/leistungen/klimadatendeutschland/klarchivtagmonat.html
  - *Monatswerte historisch und aktuell*
  - File: produkt_klima_monat_xy.txt
    - column MO_TT (Temperature; Monatsmittel der Lufttemperatur in 2m Höhe in °C and MO_RR (Precipitation; Monatssumme der Niederschlagshoehe in mm))
- England **Met Office - National Meteorological Service for the UK**
  - https://www.metoffice.gov.uk/hadobs/hadcet/data/download.html
  - Monthly_HadCET_mean.txt, 1659 to date

5.3.2 CO2 Concentrations

- **National Oceanic & Atmospheric Administration - Earth System Research Laboratory**
  - *NOAA ESRL* https://www.esrl.noaa.gov/gmd/ccgg/trends/global.html
  - Data file: ***Mauna Loa CO2*** monthly mean data
  - https://www.esrl.noaa.gov/gmd/ccgg/trends/data.html

5.4 R code

- Source code (maybe not yet the latest version) and output files are stored on GitHub repository https://github.com/WoVollmer/R-TimesSeriesAnalysis/tree/master/Climate
- Partially based on *c't Magazin* articles by *Andreas Krause*:
  - #3/2014 p.188 http://www.ct.de/1403188 & #6/2014 p.180 http://www.ct.de/1406180
- *Forecasting: Principles and Practice (3rd ed)* https://otexts.com/fpp3
  - Rob J Hyndman and George Athanasopoulos; Monash University, Australia