



# From hardness assumptions to energy-secure protocols: A systematic survey of Euclidean lattice-based cryptography

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## ABSTRACT

The fast development of quantum computing poses major challenges for classical cryptographic techniques, hence post-quantum cryptography is needed. Emphasizing their fit for securing energy-critical infrastructure, this work methodically reviews lattice-based cryptographic systems. Theoretically strong and practically relevant fundamental lattices including the Shortest Vector Problem (SVP), Learning with Errors (LWE), and Module-LWE are investigated in limited environments including smart grids and IoT devices. Examined are important advancements in hardware implementations, algorithmic optimizations, and cryptanalysis with an eye toward programs including Falcon, Dilithium, and CRYSTALS-Kyber. Over systems including Vehicle-to-Grid (V2G) networks and Supervisory Control and Data Acquisition (SCADA) systems, lattice-based cryptography's efficacy and deployability are shown. The review ends with a discussion of future research paths to support long-term quantum-safe infrastructure security and newly arising theoretical hazards.

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