

```
struct Node {
                         shared:
                                                 void init() {
                                                     Head = new Node();
   data_t data;
                            Node* Head;
                            Node* Tail;
                                                     Head->next = null;
   Node* node;
}
                                                     Tail = Head;
                                                 }
void enqueue(data_t val) {
                                                 data_t dequeue() {
   Node* node = new Node();
                                                     while (true) {
   node->data = val;
                                                        Node* head = Head;
   node->next = null;
   while (true) {
       Node* tail = Tail;
                                                        Node* tail = Tail;
                                                        Node* next = head -> next;
                                                        if (Head != head) continue;
       Node* next = tail->next;
                                                         if (head == tail) {
       if (Tail != tail) continue;
       if (next == null) {
                                                            if (next == null) return empty_t;
           if (CAS(tail->next, null, node)) {
                                                            else CAS(Tail, tail, next);
              CAS(Tail, tail, node);
                                                        } else {
           }
                                                            data = head->data;
       } else {
                                                            if (CAS(Head, head, next)) {
           CAS(Tail, tail, next);
       }
                                                                return data;
   }
                                                            }
}
                                                         }
                                                     }
                                                 }
```

queue

lock-free

GC

```
struct Node {
                         shared:
                                                 void init() {
                                                     Head = new Node();
   data_t data;
                            Node* Head;
                            Node* Tail;
                                                     Head->next = null;
   Node* node;
}
                                                     Tail = Head;
                                                 }
void enqueue(data_t val) {
                                                 data_t dequeue() {
   Node* node = new Node();
                                                    while (true) {
   node->data = val;
                                                        Node* head = Head;
   node->next = null;
                                                        protect0(head);
   while (true) {
                                                        if (Head != head) continue;
       Node* tail = Tail;
                                                        Node* tail = Tail;
       protect0(tail);
                                                        Node* next = head->next;
       if (Tail != tail) continue;
                                                        protect1(next);
       Node* next = tail->next;
                                                        if (Head != head) continue;
       if (Tail != tail) continue;
                                                        if (head == tail) {
       if (next == null) {
                                                            if (next == null) return empty_t;
           if (CAS(tail->next, null, node)) {
                                                            else CAS(Tail, tail, next);
              CAS(Tail, tail, node);
                                                        } else {
           }
                                                            data = head -> data;
       } else {
                                                            if (CAS(Head, head, next)) {
                                                                retire(head);
           CAS(Tail, tail, next);
       }
                                                                return data;
   }
                                                            }
}
                                                        }
                                                 }
```

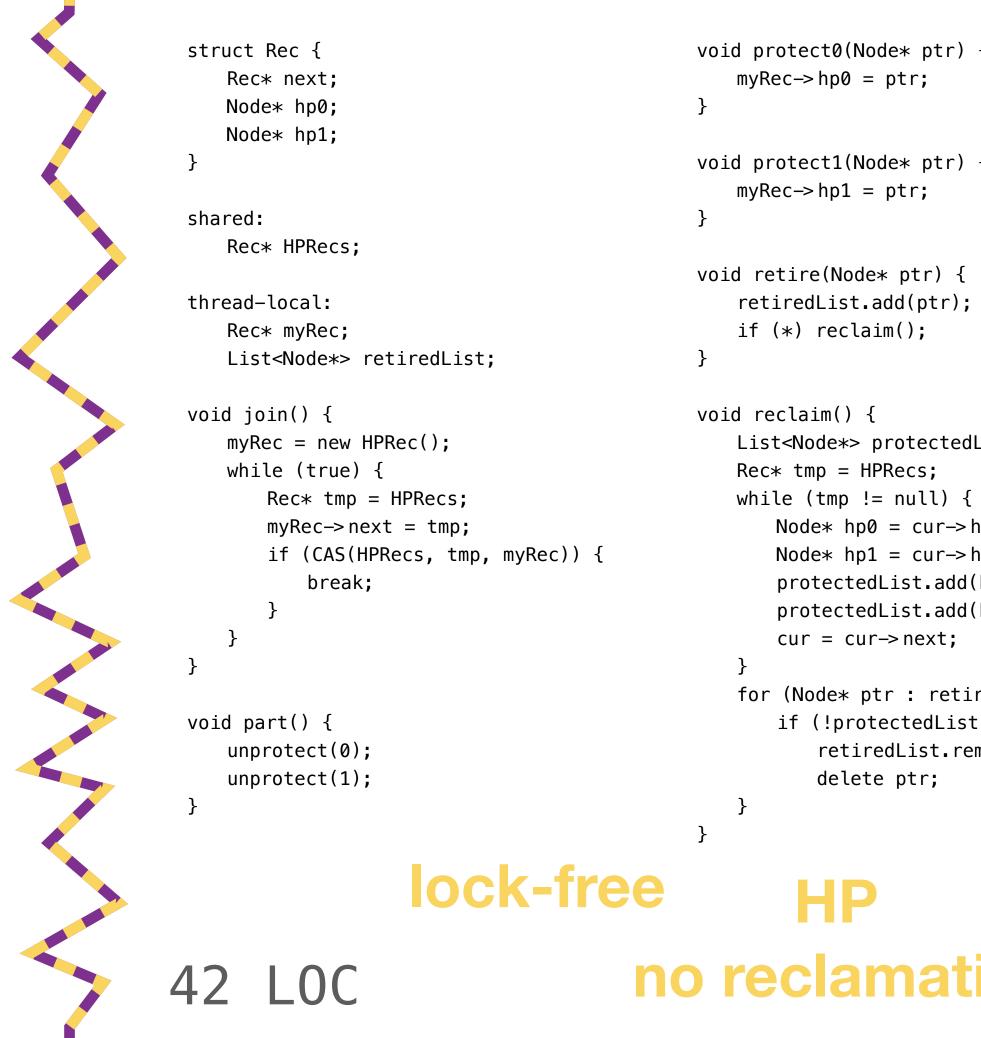
queue

lock-free

SMR

37+6 LOC

Non-blocking Queue (Michael&Scott)



```
void protect0(Node* ptr) {
void protect1(Node* ptr) {
   List<Node*> protectedList;
       Node* hp0 = cur -> hp0;
      Node* hp1 = cur->hp1;
       protectedList.add(hp0);
       protectedList.add(hp1);
   for (Node* ptr : retiredList) {
       if (!protectedList.contains(ptr)) {
          retiredList.remove(ptr);
```

no reclamation



Non-blocking Queue (Michael&Scott)

```
void init() {
struct Node {
                        shared:
   data_t data;
                           Node* Head;
                                                  Head = new Node();
                                                  Head-> next = null;
   Node* node;
                           Node* Tail;
                                                  Tail = Head;
void enqueue(data_t val) {
                                               data_t dequeue() {
   Node* node = new Node():
                                                  while (true) {
   node->data = val;
                                                      Node* head = Head;
                                                     protect0(head);
   node->next = null;
   while (true) {
                                                      if (Head != head) continue;
                                                      Node* tail = Tail;
       Node* tail = Tail;
       protect0(tail);
                                                      Node* next = head->next;
       if (Tail != tail) continue;
                                                      protect1(next);
       Node* next = tail->next;
                                                      if (Head != head) continue;
       if (Tail != tail) continue;
                                                      if (head == tail) {
                                                         if (next == null) return empty_t;
       if (next == null) {
          if (CAS(tail->next, null, node)) {
                                                         else CAS(Tail, tail, next);
              CAS(Tail, tail, node);
                                                      } else {
                                                         data = head -> data;
       } else {
                                                         if (CAS(Head, head, next)) {
          CAS(Tail, tail, next);
                                                             retire(head);
                                                             return data;
      queue
```

lock-free

SMR

37+6 LOC

```
void protect0(Node* ptr) {
struct Rec {
                                                  myRec->hp0 = ptr;
   Rec* next;
   Node* hp0;
   Node* hp1;
                                              void protect1(Node* ptr) {
                                                  myRec \rightarrow hp1 = ptr;
shared:
   Rec* HPRecs;
                                              void retire(Node* ptr) {
                                                  retiredList.add(ptr);
thread-local:
                                                  if (*) reclaim();
   Rec* myRec;
   List<Node*> retiredList;
void join() {
                                              void reclaim() {
   myRec = new HPRec();
                                                  List<Node*> protectedList;
   while (true) {
                                                  Rec* tmp = HPRecs;
       Rec* tmp = HPRecs;
                                                  while (tmp != null) {
       myRec-> next = tmp;
                                                      Node* hp0 = cur -> hp0;
       if (CAS(HPRecs, tmp, myRec)) {
                                                      Node* hp1 = cur->hp1;
           break;
                                                      protectedList.add(hp0);
                                                      protectedList.add(hp1);
                                                      cur = cur->next;
                                                  for (Node* ptr : retiredList) {
void part() {
                                                     if (!protectedList.contains(ptr)) {
   unprotect(0);
                                                         retiredList.remove(ptr);
   unprotect(1);
                                                         delete ptr;
```

no reclamation

lock-free

42 LOC

Verification Challenges

- 1. unbounded shared heap
- 2. unbounded data domain
- 3. unbounded number of threads

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4. fine-grained concurrency