

# Today's Session Summary

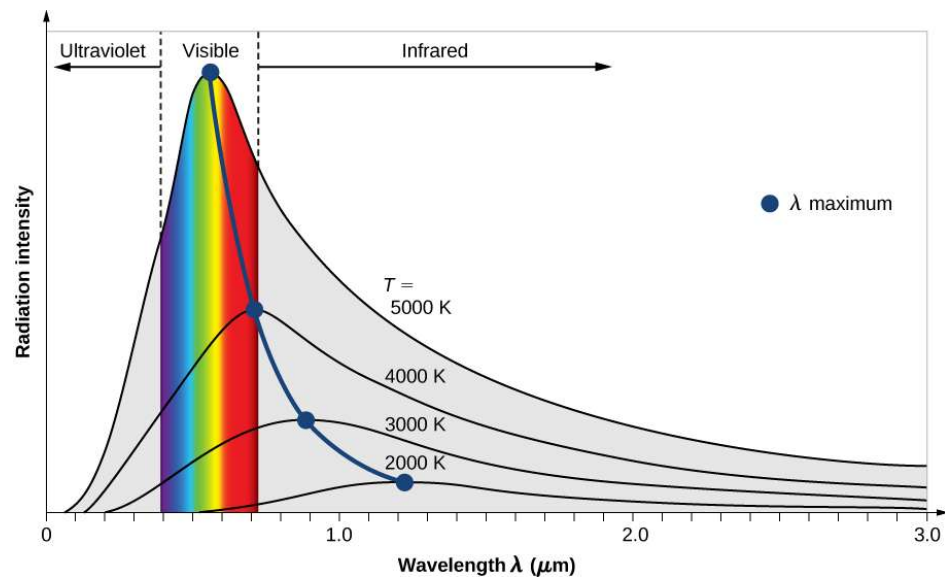
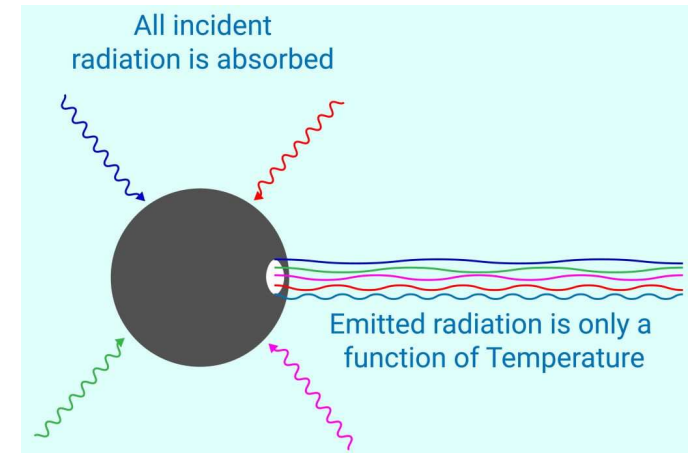
- Radiation
- Solar Panels
- Space systems cooling
- Cooling fin model
- Cell control volume

# Radiation

Black Body – Boltzman Law

$$P = \dot{E} = A \varepsilon \sigma (T^4 - T_{\infty}^4)$$

$$\sigma = 5.67 \cdot 10^{-8} \frac{W}{m^2 K^4}$$



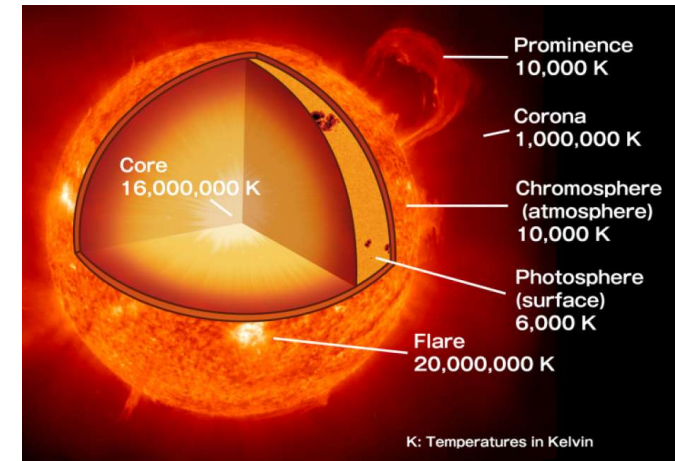
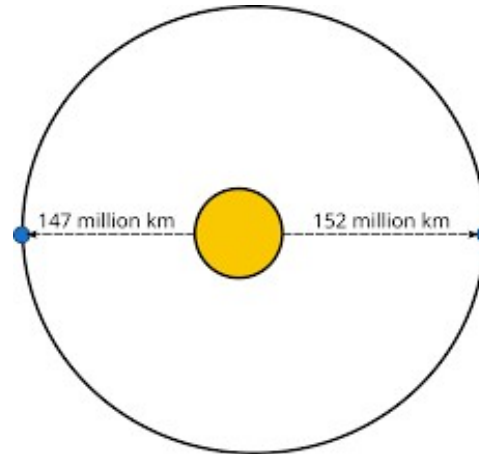
From Equations to Innovation:  
Modeling and Optimization in Engineering

# Radiation

$$P = A \varepsilon \sigma (T^4 - T_{\infty}^4)$$

$$R_{sun} = 6.96 \cdot 10^8 m;$$

$$T_{sun} = 5778 K$$



$$P_{emitted} = 4\pi R_{sun}^2 \varepsilon \sigma (T^4 - T_{\infty}^4) = 4\pi (6.96 \cdot 10^8 m)^2 \cdot 1 \cdot 5.67 \cdot 10^{-8} \frac{W}{m^2 K^4} ((5778 K)^4 - (293 K)^4) = 3.85 \cdot 10^{26} W$$

$$P_{received} = \frac{P_{emitted}}{4\pi d_{sun\_earth}^2} =$$

$$d_{sun\_earth} = 150 \cdot 10^9 m$$

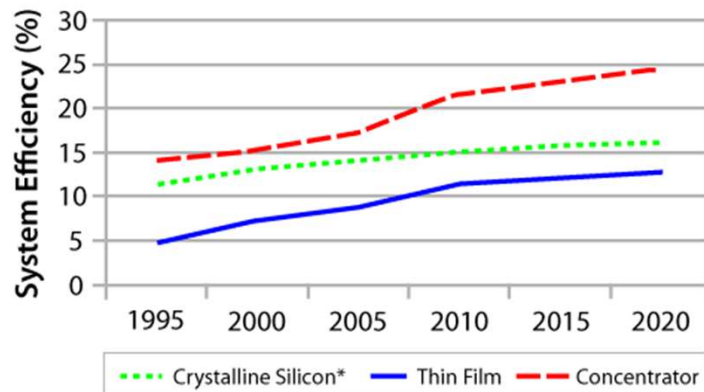
# Solar panel efficiency

Power generated: 100W / 53.99USD

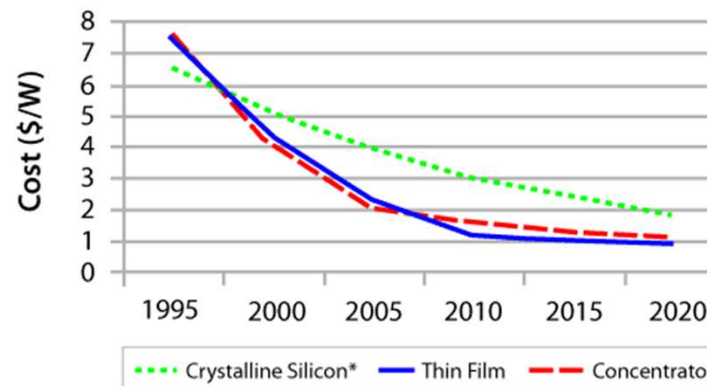
Efficiency?



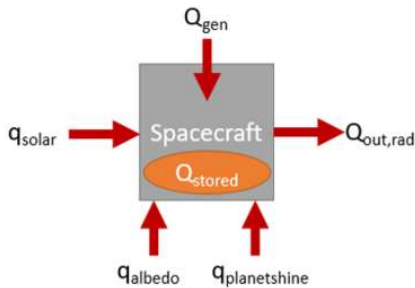
PV System Efficiency



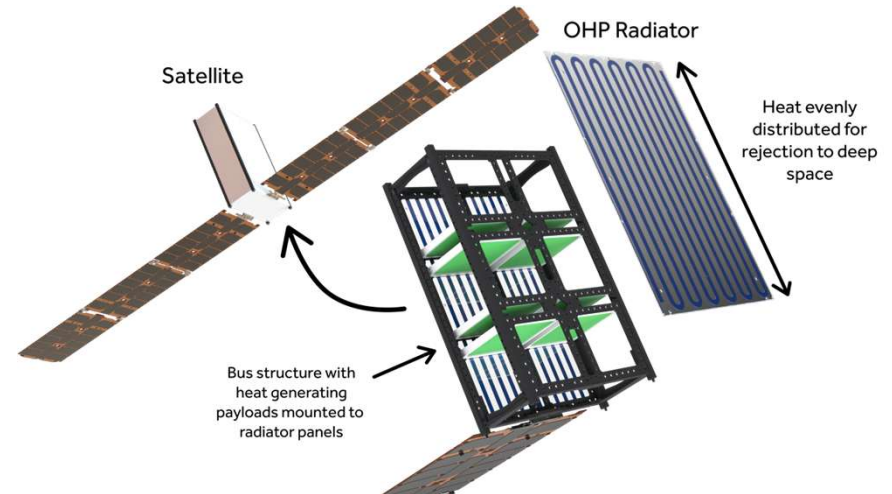
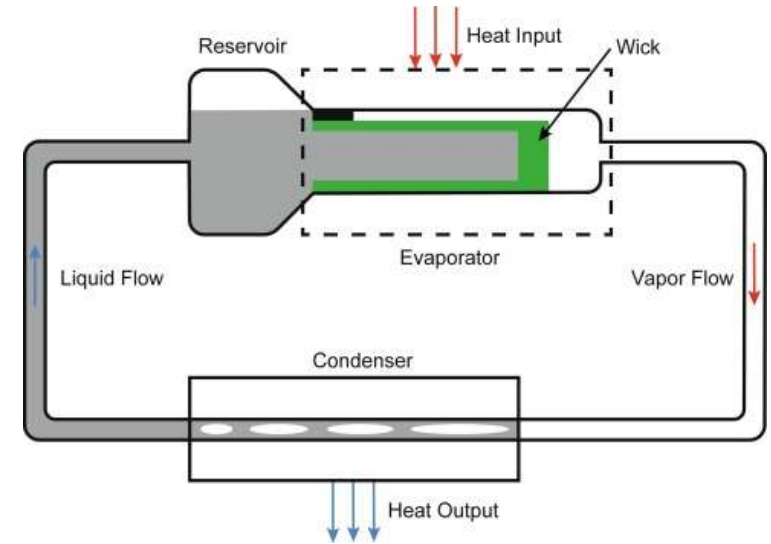
PV System Capital Cost



# Space systems cooling



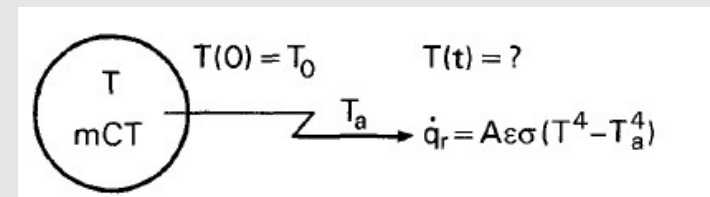
$Q_{gen}$  = Heat generated by spacecraft  
 $q_{solar}$  = Solar heating  
 $q_{albedo}$  = Solar heating reflected by planet  
 $q_{planetshine}$  = Infrared heating from planet  
 $Q_{out,rad}$  = Heat emitted via radiation  
 $Q_{stored}$  = Heat stored by the spacecraft



# Practice

Sphere cooling

Determine Temperature evolution



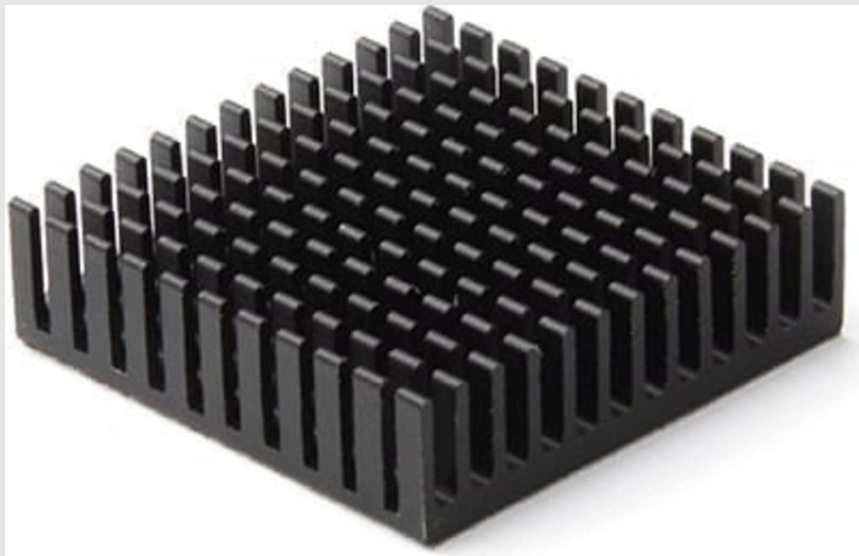
$$A\epsilon\sigma (T^4 - T_{\infty}^4) = \dot{Q}$$

$$mC\dot{T} = \dot{Q}$$

## Practice

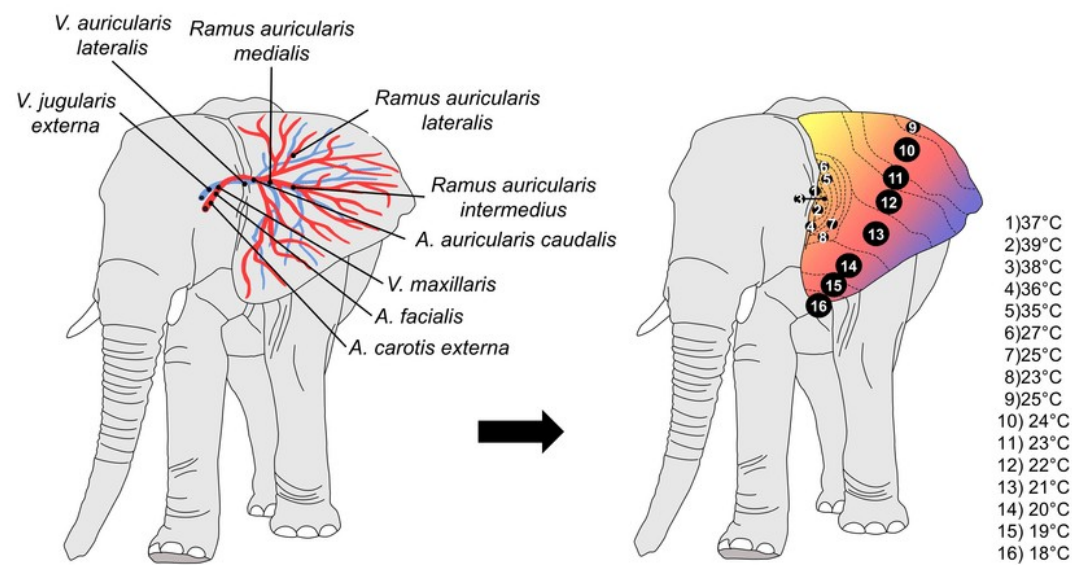
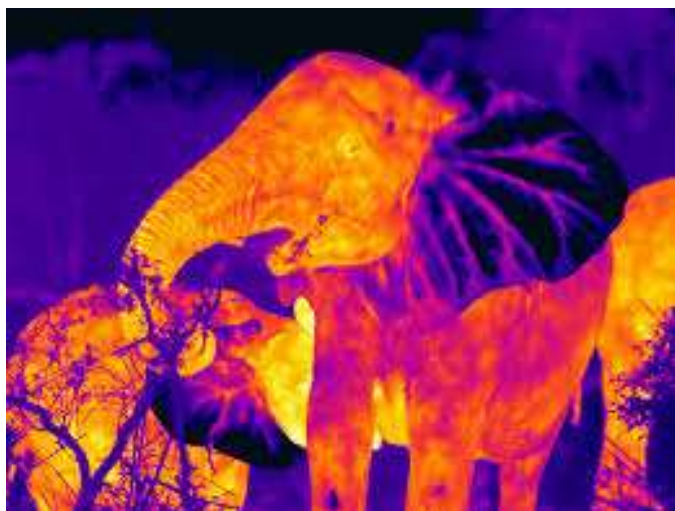
Develop model to evaluate a heat sink thermal behavior.

Analyze heat sink power dissipation capability for a limit temperature of 60C with an environment temperature range from -20C to 45C.



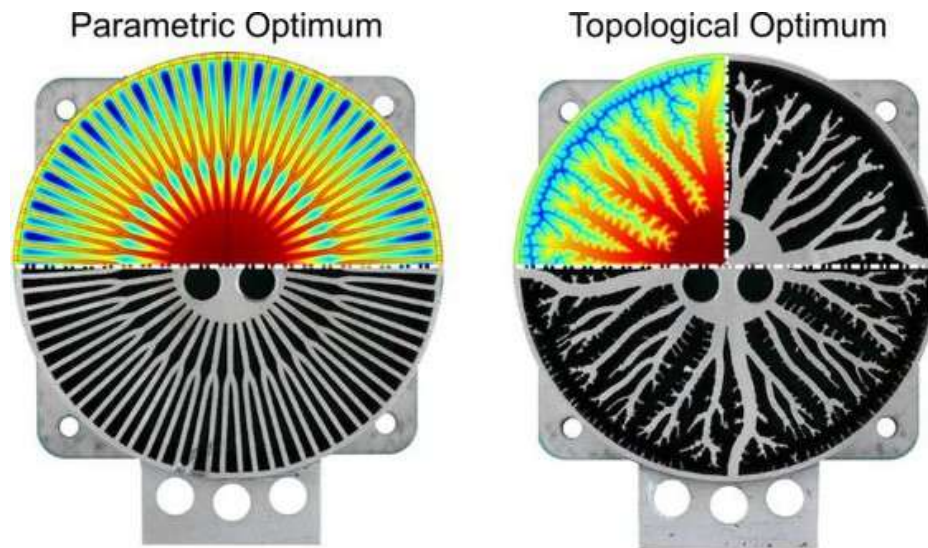
143 Fins. Aluminium Heatsink Cooling Module  
Fins: 2.5(L) x 1mm(W) x 10mm(H)  
Module: 40mm(L) x 40mm(W) x 11mm(H)

# Cooling fin model

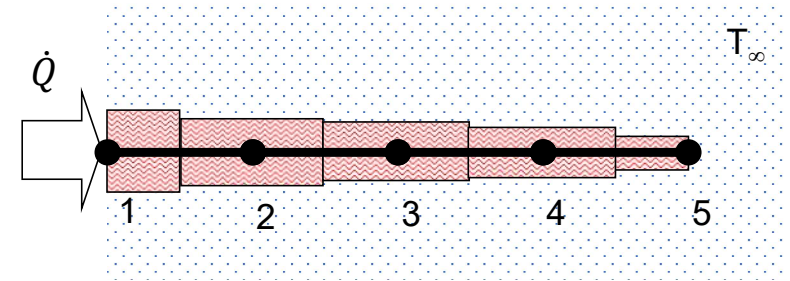
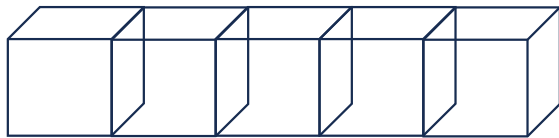




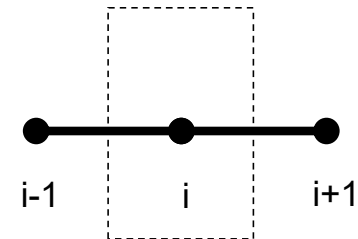
# Cooling fin model



# Cooling fin model



Cell Control Volume

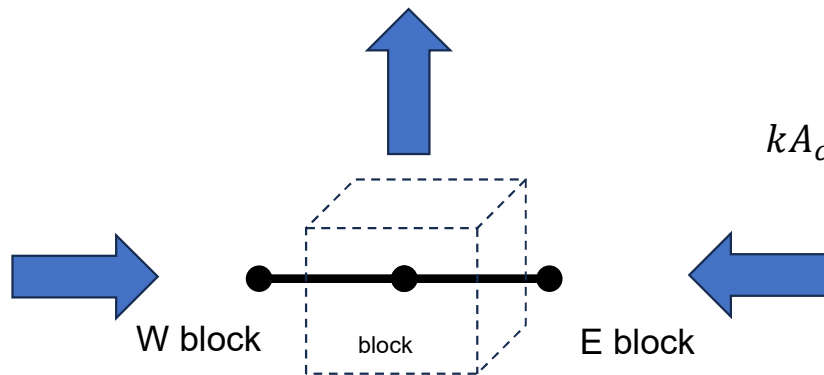


$$m_{block} C \dot{T}_{block} = \dot{Q}$$

# Cell control volume

Heat Balance

$$hA_{convection}(T_{block} - T_{\infty}) = \dot{Q}_{convected}$$



$$kA_{conduction} \frac{T_{E\ block} - T_{block}}{Distance} = \dot{Q}_{E\ conducted}$$

$$kA_{conduction} \frac{T_{W\ block} - T_{block}}{Distance} = \dot{Q}_{W\ conducted}$$

Time variation

$$m_{block} C \dot{T}_{block} = \dot{Q}$$

$$kA_{conduction} \frac{T_{W\ block} - T_{block}}{Distance} + kA_{conduction} \frac{T_{E\ block} - T_{block}}{Distance} + hA_{convection}(T_{block} - T_{\infty}) = m_{block} C \dot{T}_{block}$$

# End Session 19