

Today's Session Summary

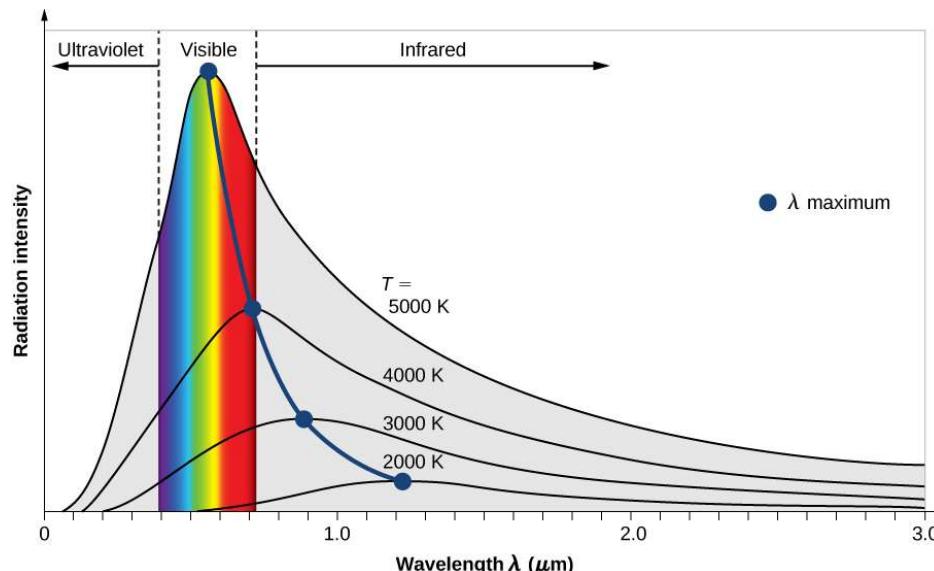
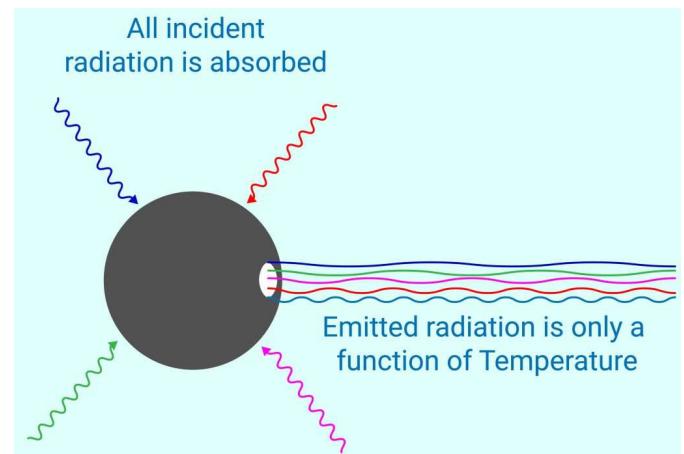
- Radiation
- Solar Panels
- Space systems cooling
- Cooling fin model
- Cell control volume

Radiation

Black Body – Boltzman Law

$$P = \dot{E} = A\epsilon\sigma (T^4 - T_\infty^4)$$

$$\sigma = 5.67 \cdot 10^{-8} \frac{W}{m^2 K^4}$$



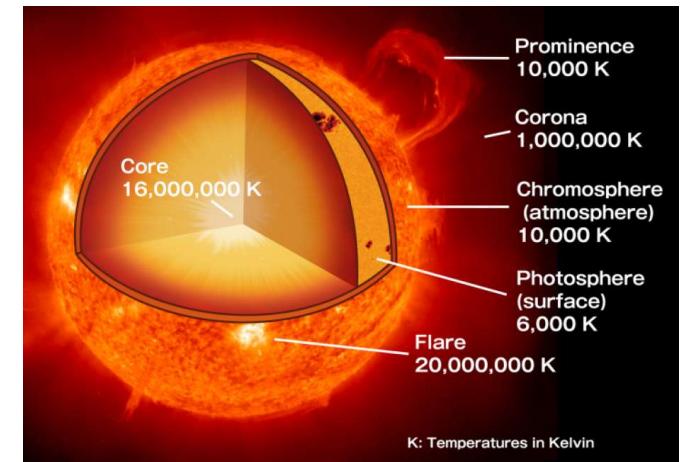
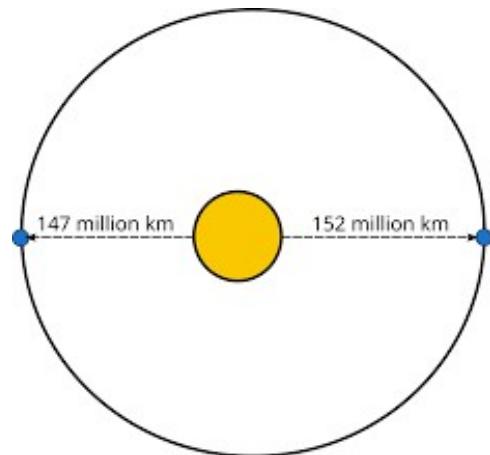
From Equations to Innovation:
Modeling and Optimization in Engineering

Radiation

$$P = A \varepsilon \sigma (T^4 - T_\infty^4)$$

$$R_{\text{sun}} = 6.96 \cdot 10^8 \text{ m};$$

$$T_{\text{sun}} = 5778 \text{ K}$$



$$P_{\text{emitted}} = 4\pi R_{\text{sun}}^2 \varepsilon \sigma (T^4 - T_\infty^4) = 4\pi (6.96 \cdot 10^8 \text{ m})^2 1.567 \cdot 10^{-8} \frac{\text{W}}{\text{m}^2 \text{K}^4} ((5778 \text{ K})^4 - (293 \text{ K})^4) = 3.85 \cdot 10^{26} \text{ W}$$

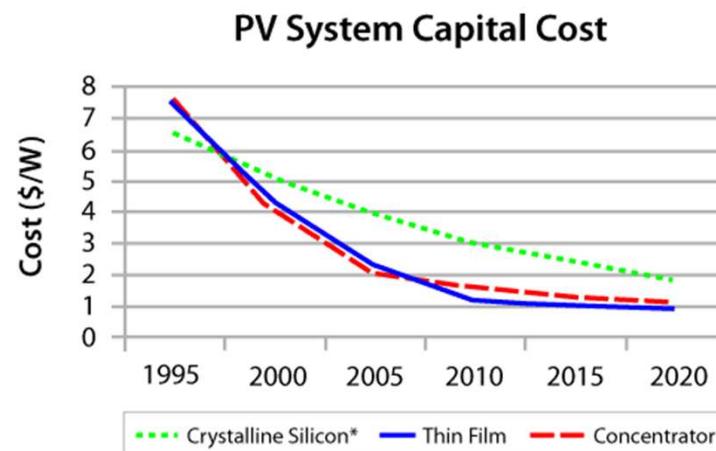
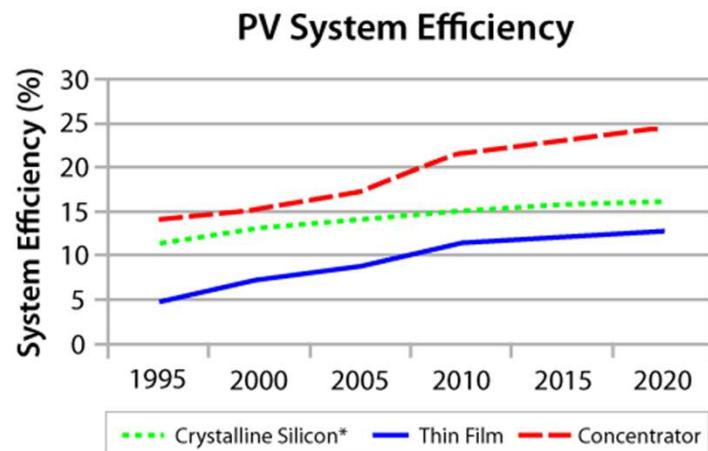
$$P_{\text{received}} = \frac{P_{\text{emitted}}}{4\pi d_{\text{sun_earth}}^2} =$$

$$d_{\text{sun earth}} = 150 \cdot 10^9 \text{ m}$$

Solar panel efficiency

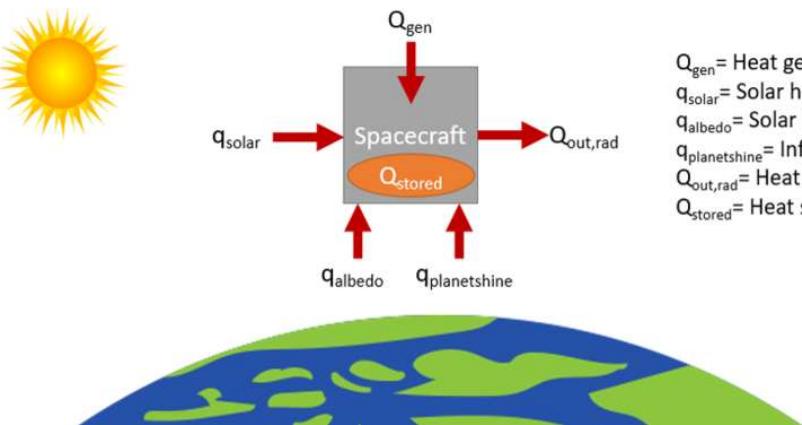
Power generated: 100W / 53.99USD

Efficiency?

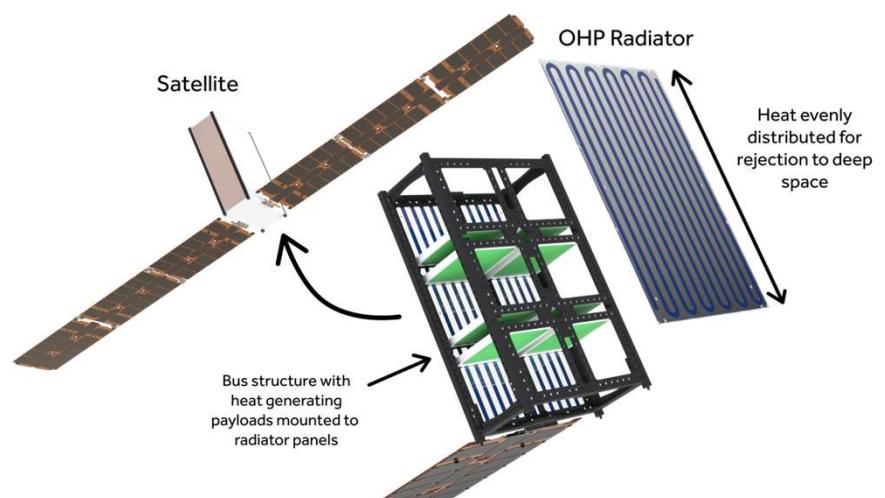
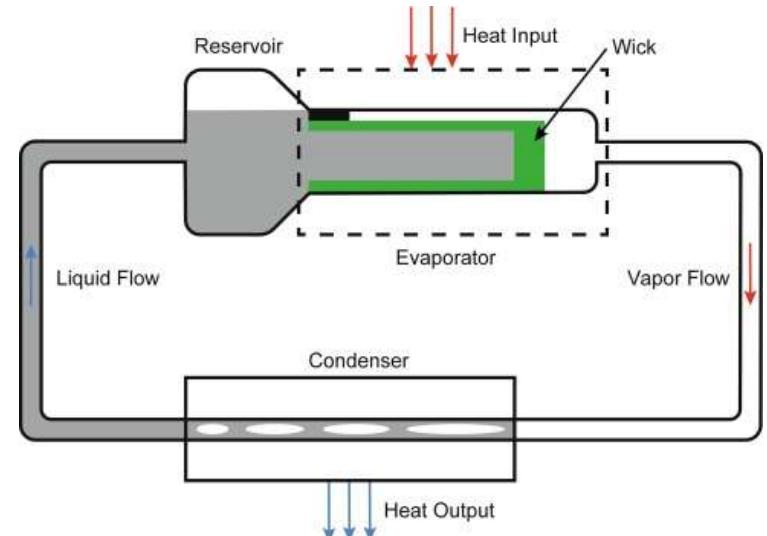


From Equations to Innovation:
Modeling and Optimization in Engineering

Space systems cooling



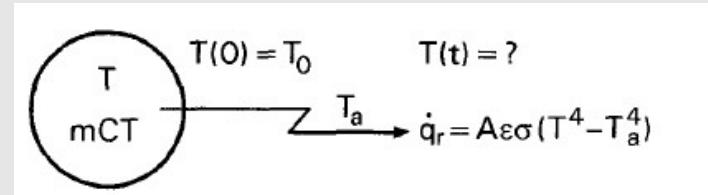
Q_{gen} = Heat generated by spacecraft
 q_{solar} = Solar heating
 q_{albedo} = Solar heating reflected by planet
 $q_{\text{planetshine}}$ = Infrared heating from planet
 $Q_{\text{out,rad}}$ = Heat emitted via radiation
 Q_{stored} = Heat stored by the spacecraft



Practice

Sphere cooling

Determine Temperature evolution



$$A\varepsilon\sigma (T^4 - T_\infty^4) = \dot{Q}$$

$$mC\dot{T} = \dot{Q}$$

Practice

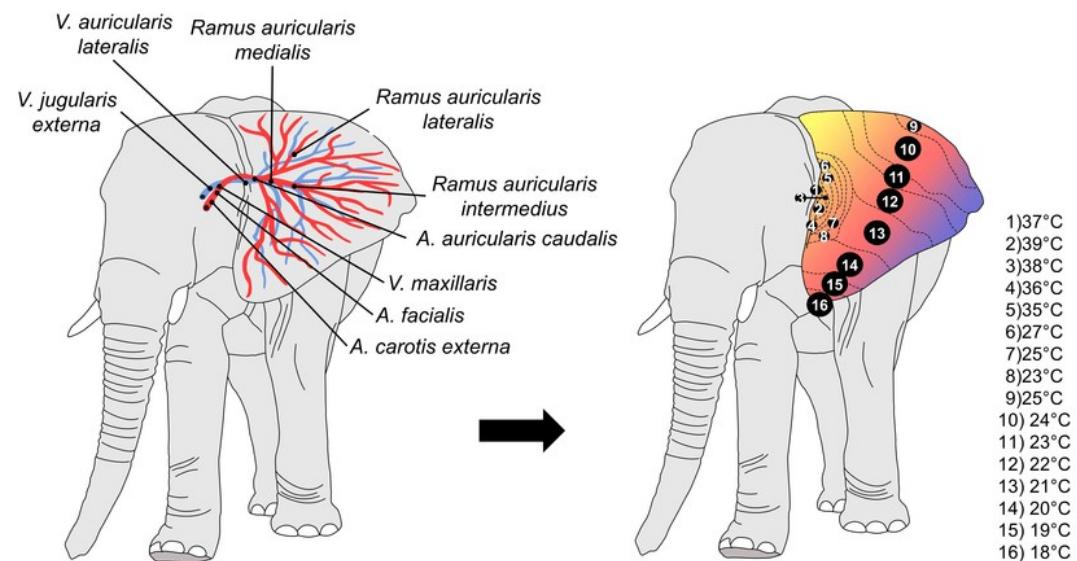
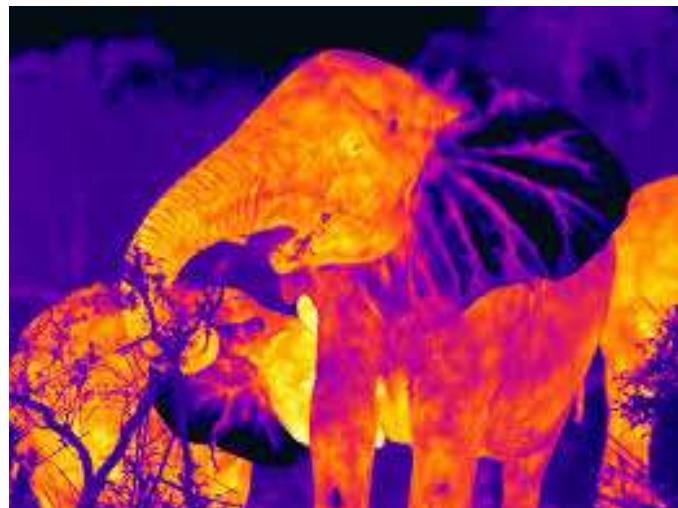
Develop model to evaluate a heat sink thermal behavior.

Analyze heat sink power dissipation capability for a limit temperature of 60C with an environment temperature range from -20C to 45C.

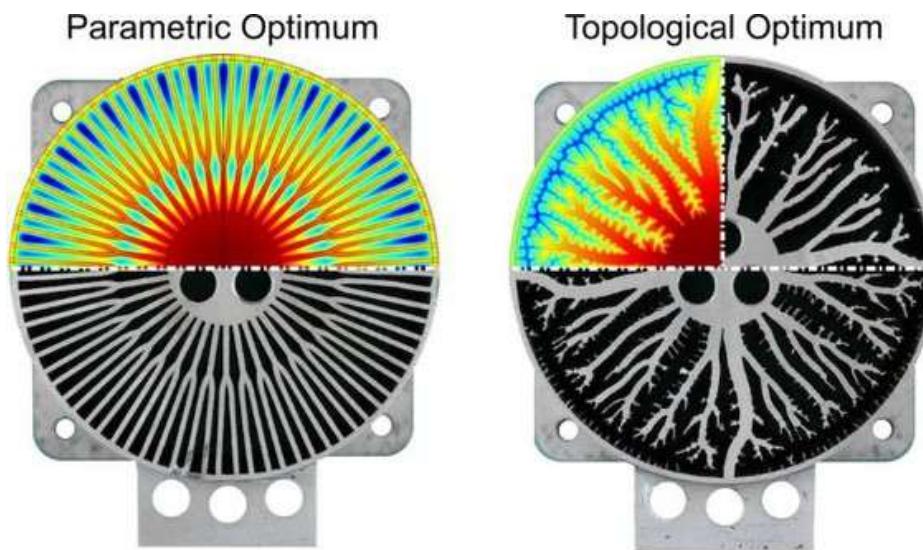


143 Fins. Aluminium Heatsink Cooling Module
Fins: 2.5(L) x 1mm(W) x 10mm(H)
Module: 40mm(L) x 40mm(W) x 11mm(H)

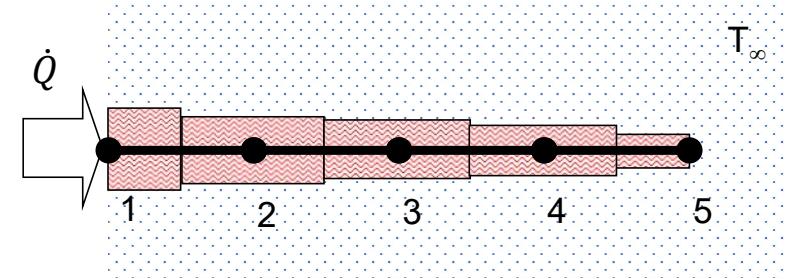
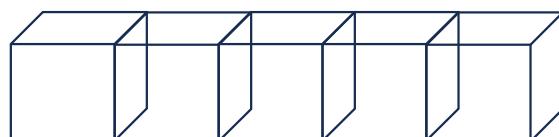
Cooling fin model



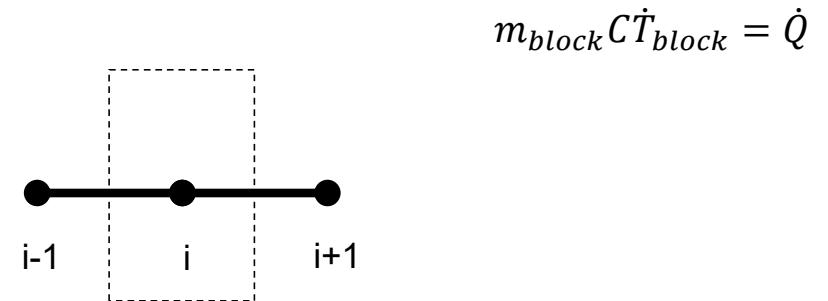
Cooling fin model



Cooling fin model



Cell Control Volume

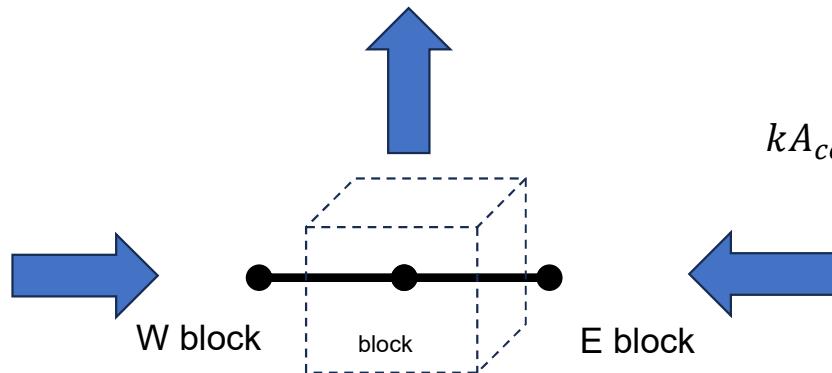


$$m_{block} C \dot{T}_{block} = \dot{Q}$$

Cell control volume

Heat Balance

$$hA_{convection}(T_{block} - T_{\infty}) = \dot{Q}_{convected}$$



$$kA_{conduction} \frac{T_{E\ block} - T_{block}}{Distance} = \dot{Q}_{E\ conducted}$$

$$kA_{conduction} \frac{T_{W\ block} - T_{block}}{Distance} = \dot{Q}_{W\ conducted}$$

Time variation

$$m_{block}C\dot{T}_{block} = \dot{Q}$$

$$kA_{conduction} \frac{T_{W\ block} - T_{block}}{Distance} + kA_{conduction} \frac{T_{E\ block} - T_{block}}{Distance} + hA_{convection}(T_{block} - T_{\infty}) = m_{block}C\dot{T}_{block}$$

End Session 19