$$\sum_{k=1}^{m} \frac{\left| n - x_k \right| \left(1 + \left| n - x_k \right| \right)}{2} = \mathcal{J}(n)$$

$$\sum_{k=1}^{m} \frac{\left| n - x_k \right|}{2} + \frac{\left(n - x_k \right)^2}{2} = \mathcal{J}(n)$$

$$\int_{k=1}^{\infty} \frac{sgn(n-x_k)}{2} = mn - x_{sum} + \frac{1}{2} \sum_{k=1}^{m} sgn(n-x_k)$$

$$0 = mn - x_{sam} + \frac{1}{2} \sum sgn(n - xk)$$

$$x_{sum} - \frac{1}{2} \sum_{k=1}^{M} sgn(n - xk) = n$$

mean $-\frac{1}{2m}\sum_{k=1}^{m} sgn(n-x_k) = n$

$$n \in \left[\text{ mean } -\frac{1}{2}, \text{ mean } + \frac{1}{2} \right]$$