

Thesis or Article

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# Chapter 1

## Introduction

Through the development of applications such as augmented and virtual reality, object / scene reconstruction and visual effects, the process of generating images from an arbitrary vantage point can be found in a variety of applications. In this Thesis (or Article) I will discuss various methods for Image Creation from an arbitrary vantage point, which can be accomplished by two main methodologies of Geometric Construction and Image Synthesis. While both methods use stereo correspondance of multiple images, they differ in the way information is stored and used.

Geometric Construction (GC) contains information about the real-world spatial properties (Coordinates in space, Color), thus viewing results are non-constrained in vantage point. Image Synthesis (IS) relies on image properties (pixel displacement) and is thus viewing results are limited in the possible vantage points.

## Symbols and Notation

Symbol	Description
$\mathbf{v}$	Vectors in <i>lowercase</i> bold
$\mathbf{M}$	Matrices in <i>uppercase</i> bold
$\mathbf{u}$	Image coordinate
$\tilde{\mathbf{u}}$	Image coordinate (expressed <i>homogeneously</i> )
$\mathbf{x}$	Spatial coordinate
$\tilde{\mathbf{x}}$	Spatial coordinate (expressed <i>homogeneously</i> )
${}^A\mathbf{x}$	Spatial coordinate in reference frame $A$
${}^A\tilde{\mathbf{x}}$	Spatial coordinate (expressed <i>homogeneously</i> ) in reference frame $A$
${}^C_B\tilde{\mathbf{M}}$	Change from of reference frame $B$ to reference frame $C$
$s$	Normalizing factor applied to <i>homogeneous</i> vector so last element becomes equal to 1
${}^D\mathbb{S}$	Spatial reference frame $D$
$[\mathbf{x}]_{\times}$	Skew-symmetric matrix version of vector $\mathbf{x}$ used as <i>left</i> -operand in the <i>cross</i> -product such that $[\mathbf{x}]_{\times} \cdot \mathbf{y} = \mathbf{x} \times \mathbf{y}$
$l$	Epipolar line

## Chapter 2

# Background

Ordinarily, real-world data contains 3-dimensions. Because standard images only include 2-dimensional data, information regarding depth is lost (i.e. it is often difficult to judge distance from a single image without visual cues). *Stereovision* attempts to resolved this by finding the same point in both *stereoscopic* images (known as a *corresponding point*), and recovering the depth information. An elementary example of this occurs in stereoscopic images with relatively low distance between cameras (i.e they are right next to each other). Objects that are *farther* away from the observer occur closer together in the stereo images, whereas objects *closer* to the camera appear appear farther apart in the stereo-images.

### Change of Reference

Each view from a pair of stereo-images encompasses its own *frame of reference* (i.e. the directions of *forward* or *backward* are unique to image and may differ considerably depending on camera displacement). This requires expressing points from different frames of reference (traditionally referred to *left* and *right*) in a single reference frame. As such it is necessary to be able to express coordinates in a given reference frame in any other reference frame.

Coordinates given in  ${}^A\mathbf{x}$  can be expressed in  ${}^B\mathbf{x}$  by the geometric transformation:

$${}^B\mathbf{x} = {}^B_A\mathbf{R} \cdot {}^A\mathbf{x} + {}^B_A\mathbf{t}$$

or

$$\begin{aligned} {}^B\tilde{\mathbf{x}} &= \left[ \begin{array}{c|c} {}^B_A\mathbf{R} & {}^B_A\mathbf{t} \\ \hline 0 & 1 \end{array} \right] \cdot {}^A\tilde{\mathbf{x}} \\ &= {}^B_A\mathbf{M} \cdot {}^A\tilde{\mathbf{x}} \end{aligned}$$

where  ${}^B_A\mathbf{M}$  is also the geometric transformation necessary to transform  ${}^B\mathbf{S}$  into  ${}^A\mathbf{S}$ .

Withough calculating any new quantities, rearranging allows us to express coordinates in  ${}^B\mathbf{x}$  in the  ${}^A\mathbf{x}$  reference frame as:

$${}^B_A\mathbf{R}^\top \cdot ({}^B\mathbf{x} - {}^B_A\mathbf{t}) = {}^A\mathbf{x}$$

and similarly transforms  ${}^A\mathbf{S}$  into  ${}^B\mathbf{S}$ .

## Epipolar constraint

### Essential Matrix

When coordinates from a reference frame are expressed as *normalized image coordinates* the range of possible NIC values in the corresponding image are given by the *epipolar* constraint

### Intrinsic Calibration Matrix

### Essential Matrix

## Chapter 3

# Point Interpolation

Pixels from image  $a$  and image  $b$  can be used to create a new images. This is done by interpolating the pixel positions ( $\mathbf{p}_a$  and  $\mathbf{p}_b$ ) of corresponding points between frames. Because not all pixels are established as corresponding points, pixel correspondances *between* corresponding points are calculated through bi-linear interpolation.

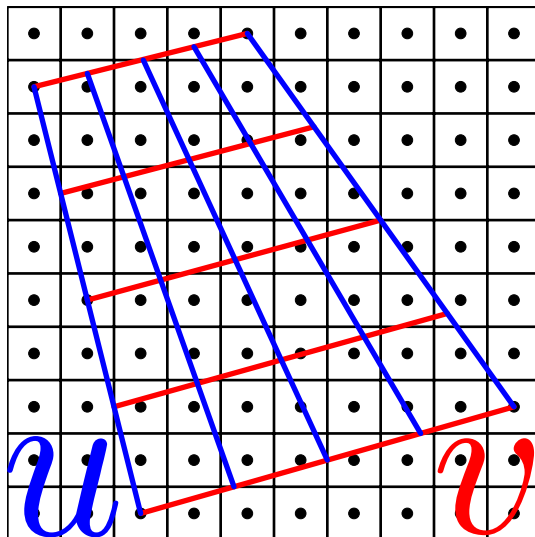


Figure 3.1: Bi-Linear Point Correspondance

# Chapter 4

## Process

The system in question contains 3 main components

### 1. Image Acquisition System

- Webcam / Kinect set-up
- If Webcam should also contain Image-Processing module for:
  - Feature Identification
  - Point-correspondance
  - Sub-Pixel interpolation

### 2. Point Cloud Processing

- Should take inputs
- Should produce point-clouds as one of the output
- (Possible) Options for Surface Reconstruction include:
  - Calculation of surface Normal through PCA
  - Mesh construction through Delaunay triangulation
  - Parametrization of Bezier surface through linear-least squares.