Research Log

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July 25, 2016

| March 30, 2016 | Established research log after 3 hours of learning new \LaTeX | | | | |
|----------------|---|--|--|--|--|
| April 2, 2016 | Added some additional comments to the Process | | | | |
| April 3, 2016 | Have been reading [Shum2007] [1]. | | | | |
| | Question for Kamangar: regarding [Shum2007] [1] about difference between: • Camera Plane : Cooridinates u,v • Focal Plane : Cooridinates s,t | | | | |
| April 11, 2016 | Reviewing blog articles located at: • https://erget.wordpress.com/2014/02/01/ calibrating-a-stereo-camera-with-opencv/ • https://erget.wordpress.com/2014/02/28/ calibrating-a-stereo-pair-with-python/ • https://erget.wordpress.com/2014/03/13/ building-an-interactive-gui-with-opencv/ • https://erget.wordpress.com/2014/04/27/ producing-3d-point-clouds-with-a-stereo-camera-in-opencv/ for process to get webcam up and running. Previous issues related to fine-tuning block matching parameters. Need to review sources at list at bottom of http://docs.opencv.org/2.4/modules/calib3d/doc/camera_calibration_and_3d_reconstruction.html to understand. | | | | |
| April 19, 2016 | Made adjustments to python for image acquisition scripts (from blogs mentioned on April 11, 2016.) NOTE: Consider creating rig with glue to keep stereo camera placement / direction constant. | | | | |
| April 19, 2016 | <pre>UPDATE: Error with calibrate_cameras python code causing linux machine to crash. If can't be resolved switch over to MacBook. NOTE: Package should be setup by calling \$ python setup.py install.</pre> | | | | |
| April 19, 2016 | UPDATE: Crash due to recursive shell call and was fixed. OpenCV not detecting all chessboard corners. Will try a new board. | | | | |
| April 20, 2016 | Did small amount of work on Change of Reference section in the paper. Added a section to the intro containing a map of commonly used symbols and notation. | | | | |
| | | | | | |

April 29, 2016

Read following sections of [Chen1993] [2]:

- Abstract
- Introduction
- Visibility Morphing

SUMMARY: Explicit Geometry is ignored (i.e. surface mesh and 3d-points). Geometry is kept in 2-d. Whereas Image Morphing interpolates between *pixel intensity values in fixed locations* the method in this article interpolates between *pixel locations with (relatively) fixed intensity values.* **Question:** Sections read mention that pixel positions are stored in 3d (3-tuple) data structure. I'm not sure I understand this correctly, since

- 1. This would effectively make this structure a point cloud (but no mention of it in the paper).
- 2. There is no mention of special "depth-based" hardware or cameras (Far as I know this is upposed to be a regular image).

April 30, 2016

Checked understanding of epipolar constraint through reading of [Hartley2004] [3] and its derivation of

$$'\mathbf{x}^T \cdot \mathbf{E} \cdot \mathbf{x} = '\mathbf{x}^T \cdot [\mathbf{t}]_{\times} \cdot \mathbf{R} \cdot \mathbf{x}$$

= $'\mathbf{x}^T \cdot 'l$

and creation of MatLab code verifying this.

I may have been mistaken about relation of ${f Fundamental\ Matrix}$ and ${f Essential\ Matrix}$.

My current understanding is the *Fundamental Matrix* describes point/epipolar line correspondance for images under **scale invariant** conditions (i.e. point correspondance and Fundamental matrix does not change when one image (or both images) are scaled (uniformly or omni-directionally).

Essential Matrix describes point/epipolar line correspondance for images under **normalized** conditions (i.e. unit-length is set equal to focal-length, and projection center is set at (0,0,1).

May 2, 2016

Additional wording to Stereo-vision section. I am unsure of best order to present ideas related to multi-view geometry.

May 18, 2016

Reviewed [Chen1993] [2] Section 2. Consider reviewing follow relevant articles:

- Disparity [Gosh89]
- Optical Flow [Nage86]
- Look-up tables [Wolb89]
- 3d scenes [Pogg91]

Working on MatLab code to pick corresponding points in stereo-images, and calculate pixel offset vectors.

May 19, 2016

Read Section 2.3 of [Chen1993] [2]. View interpolation is limited by:

- Penumbra: pixels visible in one source image but not both
- **Umbra**, pixels visible in neither source image, and *invisible* in destination image.
- Holes, pixels visible in neither source image, but *visible* in destination image.

Calculatred formula for pre-displaced quad-pixel calculation using a bi-linear interpolation as:

$$\mathbf{P}(u,v) = \mathbf{P}(0,0) \cdot (1-u) \cdot (1-v) + \mathbf{P}(1,0) \cdot u \cdot (1-v) + \mathbf{P}(0,1) \cdot (1-u) \cdot v + \mathbf{P}(1,1) \cdot u \cdot v$$

May 20, 2016

Derived formula for uv calculation using geometry matrix, blending matrix and basis vectors of $\mathbf{u} = [u \ 1]^T$ and $\mathbf{v} = [v \ 1]^T$

$$x_{uv} = \begin{bmatrix} u & 1 \end{bmatrix} \begin{bmatrix} -1 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} x_{00} & x_{01} \\ x_{10} & x_{11} \end{bmatrix} \begin{bmatrix} -1 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} v \\ 1 \end{bmatrix}$$
$$y_{uv} = \begin{bmatrix} u & 1 \end{bmatrix} \begin{bmatrix} -1 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} y_{00} & y_{01} \\ y_{10} & y_{11} \end{bmatrix} \begin{bmatrix} -1 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} v \\ 1 \end{bmatrix}$$

Question for Kamangar: Is there a way given x and y to solve for u and v?

May 22, 2016

Added more to thesis document.

Worked on singular-value of previous blending equation. where:

$$\begin{bmatrix} x_{uv} & 0 \\ 0 & y_{uv} \end{bmatrix} = \begin{bmatrix} \mathbf{u} & \mathbf{0} \\ \mathbf{0} & \mathbf{u} \end{bmatrix}^T \begin{bmatrix} \mathbf{M} & \mathbf{0} \\ \mathbf{0} & \mathbf{M} \end{bmatrix}^T \begin{bmatrix} \mathbf{X} & \mathbf{0} \\ \mathbf{0} & \mathbf{Y} \end{bmatrix} \begin{bmatrix} \mathbf{M} & \mathbf{0} \\ \mathbf{0} & \mathbf{M} \end{bmatrix} \begin{bmatrix} \mathbf{v} & \mathbf{0} \\ \mathbf{0} & \mathbf{v} \end{bmatrix}$$

where

$$\mathbf{u} = \begin{bmatrix} u \\ 1 \end{bmatrix}, \ \mathbf{v} = \begin{bmatrix} v \\ 1 \end{bmatrix}, \ \mathbf{X} = \begin{bmatrix} x_{00} & x_{01} \\ x_{10} & x_{11} \end{bmatrix}, \ \mathbf{Y} = \begin{bmatrix} y_{00} & y_{01} \\ y_{10} & y_{11} \end{bmatrix}, \ \text{and} \ \mathbf{M} = \begin{bmatrix} -1 & 1 \\ 1 & 0 \end{bmatrix}$$

May 23, 2016

Read [Chen1993] [2] section 2.4 on Block Compression.

SUMMARY: Blocks are established established by *threshold* where each block contains pixels that are *offset by no more than the threshold*, allowing all pixels to be offset at once.

Question for Kamangar: Doesn't this assume that all pixels in the block have a uniform offset?

Working on MatLab program to perform pixel offsets of corresponding points (i.e. assign corresponding points to pixels in MatLab by non automatic methods)

May 24, 2016

Read following sections from [Chen1993] [2]:

- Implementations (3)
 - Preprocessing (3.1)
 - Interactive Interpolation (3.2)
 - Examples (3.3)
- Applications (4)
 - Virtual Reality (4.1)
 - Motion Blur (4.2)

Question for Kamangar: With regards to Section 3.1 and Section 1, why is a graph structure needed? Why is it a lattice?

Question for Kamangar: With regards to Section 4.1, I don't understand the concepts of *temporal anti-aliasing* and *super-sampling*?

Made additional changes / added material to thesis document.

May 25, 2016

Was using figures from http://www.robots.ox.ac.uk/~vgg/hzbook/hzbook2/HZfigures.html as test images, which may not be best source as there white borders, appear to be up-sampled, and do not contain (extrinsic) calibration info. Consider using images located at http://vision.middlebury.edu/stereo/data/scenes2014/ that contain meta-info including (intrinsic) calibration info.

| May 29, 2016 | Finished [Chen1993] [2]. Not sure if remaining article is of consequence. | | | |
|--------------|--|--|--|--|
| | Finished MatLab program for animating / hand-drawing (See wording in [Chen1993] [2]) offset vectors. Program performs offsets in 2-dimensional space Conisder adding automatic feature correspondance and z-buffer information from depth map images available on MiddleBury database. | | | |
| May 30, 2016 | Point-correspondances do not follow even pattern as indicated in [Chen1993] [2] Bi-linear coordinates and quad partitionions; May be better to use Barycentri coordinates triangle partitions. | | | |
| | Read on MatLab tform, maketform, and Delaunay triangles for purpose of image partitions. | | | |
| June 1, 2016 | Read and finished [Park2003] [4]. | | | |
| | SUMMARY: Multiple sections including <i>point correspondance</i> and <i>interpolation</i> . Point correspondance : Breaks images into rectangular partitions Gets maximum horizontal and vertical pixel gradients using <i>Sobel operato</i> in each partition. The maximum gradient in each partition is thresholded to disregard homogeneous and textured regions. Interpolation : The images are partitioned with <i>Delaunay triangulation</i> using the point correspondances a triangle vertices. | | | |
| | Question for Kamangar: Article published seems to be vastly different depending on source (See Park2003 folder). ScienceDirect version has more mathand detail (maybe too much since it details what a <i>Sobel filter</i> is). Why would critical information, including algorithm steps and details, be ommitted? | | | |
| June 2, 2016 | Reviewing PDF at https://staff.fnwi.uva.nl/l.dorst/hz/chap11_13 pdf for information on tri-focal tensor. Don't understand practical calculation of fundamental matrix from Singular Value Decomposition and Linear Leas Squares (i.e. don't understand LLS calculation from SVD). | | | |
| June 3, 2016 | Working on implementing triangle patch transform in MatLap (using priously mentioned delaunay, tform, and maketform functions) needed [Chen1993] [2] and [Park2003] [4]. | | | |
| June 4, 2016 | Continuting work on getting triangular patches transformed in MatLab. Wi use affine2d and imwarp instead of maketform and imtransform. | | | |
| | Spent several hours on a false start trying to implement line drawing of pixel data, in order to implement polygon seperation. Finally found MatLab' roipoly function which does what I need. | | | |
| June 5, 2016 | Almost done with MatLab triangle interpolation program. Hoping to have something to show Kamangar in the next few days. | | | |
| | Was reading up on image-segmentation as a way to improve feature detection through masking. Came across references to spectral clustering which I still don't understand after data mining class. Was reading tutorial at http://classes.engr.oregonstate.edu/eecs/spring2012/cs534 notes/Spectral.pdf for starters. | | | |

June 8, 2016

Finalized most recent changes to MatLab program. It performs interpolation (between *source* and *destination* images of triangular patches defined by Delaunay triangularization of point correspondances from stereo images (See Wood_Kamangar/StatusReports/StatusReport_00/Images). Delaunay triangularization is performed on the source image only then extended to the corresponding points in the destination image so the arrangement of Delaunay triangles remains the same between images.

Summary of results is as follows:

- Triangles confined to one disparity region (See statue head in image_source.png, image_destination.png, and truedisp.row3.col3.pgm) show few artifacts and minimal blurring.
- Triangles crossing disparity regions or containing pixels occluded in the source or destination images (see camcorder tripod and lamp stand) have visibly more artifacts.

Started reading first page (Abstract and Introduction sections) of [Sharstein2002] [5].

June 9, 2016

Continuing to read [Scharstein 2002] [5].

SUMMARY: Disparity can be defined by two ideas:

- ullet Human Vision: Difference in location of features in the left and right eye.
- \bullet Computer Vision: Inverse depth. Can be treated as a 3-dimensional projective transformation (collineation or homographyv) of 3-d space (X,Y,Z).

Define fllowing terms:

- Disparity Map: d(x,y)
- Disparity Space: (x, y, d)
- Correspondance: Pixel (x, y) in reference image r and corresponding pixel (x', y') in matching image m given by x' = x + sd(x, y) and y' = y (assuming horizontal displacement only), where $s = \pm 1$ is chose do d is always positive.
- **Disparity Space Image**: Any function or image defined over continous or dispartiy space.

June 11, 2016

Continuing to read [Scharstein 2002] [5]:

SUMMARY: Algorithms can be ordered in 4 common subsets:

- 1. Matching cost computation;
- 2. Cost (support) aggregation;
- 3. Disparity computation / optimization;
- 4. Disparity refinement;

Two main types of agorithms:

- Local: Including Squared Intensity Differences and Absolute intensity differences.
- Global Includeing Energy minimizatio.

Continuing to read up on $Spectral\ Clustering\$ and $Laplacian\ embedding\$ for uses in image segmentation.

| June 14, 2016 | Working on implementing [Park2003] [4] in MatLab. |
|---------------|--|
| | Also working on implementing Spectral Clustering (for images) in MatLab. Started working on fnDistance.m to calculate pixel distances (<i>Distance Matrix</i>) for vectorized (row major and column major) images, needed for segmentation through spectral clustering. |
| June 16, 2016 | Added some additional text regarding the $\it epipolar constraint$ to the thesis document. |
| June 17, 2016 | Finished implmenting and testing fnDistance.m for distance matrix. Next finished working on and testing fnSimilarity.m implementing a <i>Similarity Matrix</i> for spectral clustering. |
| June 18, 2016 | Wrote small amount additional text on $\it epipolar\ contstraint$, and verified understanding through MatLab functions. |
| June 20, 2016 | Holding off on reading any more of [Scharstein2002] [5](Have completed up to end of page 5): May be too advanced for me and of little use; Compares methods, but does not go into enough detail about how to implement them. Instead reading [Scharstein1999] [6] which may be more my level. |
| | Started reading in <i>Correspondance problem</i> section of [Scharstein1999] [6]. SUMMARY: Matching can be done via <i>Fearure based correspondance</i> and <i>Area based correspondance</i> . |
| | Feature based correpondance finds locally unique or identifiable pixels (i.e. Corners or edge gradients), matchingbetween images occurrs between these reduced set of points. Advantages are only a few points are necessary. Disadvantages are that disparity calculations are confined to these points, so interpoint disparity have to be calculated through interpolation and may not be accurate. |
| | Area based correspondance occurrs over regions in the image instead of points used in feature correspondance. Advantages are a denser (and therefore more accurate) disparity map, but require assumptions about local disparity. |

SUMMARY: 3 general methods are being differentiated:

- Image Synthesis based on Stereo: Uses stereo mathods for image creation.
- Image Interpolation: Similar to *Image Synthesis based on Stereo*, except mages generated must be on baseline, and baseline must be parallel to image planes.
- Information from Many Images: Includes image stitching and panoramic mosaicing.

Other sections involve summaries of various papers and methods published under each of the 3 categories.

Got further clarification on steps for coorespondance matching for feature-based correspondance.

- 1. **Preprocessing**: Color correction between stereo images for conconsitancy, and image warping through rectification so features occur at (approximatley) same horizontal distance reducing search area to the scanline.
- 2. **Cost Calculation**: Per-pixel cost calculation done as either a *square* difference or absolute difference.
- 3. **Aggregation**: The summing of the cost calculations over the window in question.
- 4. **Comparison / Calculation**: Window on feature trying to be matched is kept fixed. Window in corresponding image is moved along the scanline for a comparison of potential window aggregates. Correspondance with minimum aggregate (in difference of costs) is selected as the corresponding point in the image being scanned.
- 5. Sup-pixel Calculation: Not yet read. Could be smoothing.

Read up to section 2.2.5 Disparity Selection (PDF page 49, Numbered page 35). Stopped to read up on using Dynamic Programming to increase consistancy of stereo points and disparity, including following sourceses:

- http://www.robots.ox.ac.uk/~az/lectures/opt/lect2.pdf
- http://www.cs.umd.edu/~djacobs/CMSC426/PS7.pdf

June 22, 2016 Continued reading [Sharstein1999] [6]. I'm still unclear about the process (and use of) Sub-Pixel Disparity Computation mentioned in section 2.2.6.

I moved onto Chapter 3 (View Synthesis) and have been reading on *three-view rectification*. Read all of Section 3.1 (*Geometry*) (up to but not including PDF page 60, Numbered page 47).

SUMMARY: A new image I_3 is synthesisized from images I_1 and I_2 , by establishing reference frame containing camera centers $\mathbf{C_3}$, $\mathbf{C_1}$, and $\mathbf{C_2}$ respectively. The unit-length is established as the difference between camera centers $\mathbf{C_1}$ and $\mathbf{C_2}$. The positions are set along the x-axis such that $\mathbf{C_1} = [0,0,0]^{\top}$ and $\mathbf{C_2} = [1,0,0]^{\top}$. The xy-plane is oriented such that it contains $\mathbf{C_3} = [a,b,0]^{\top}$ (for some constants a and b).Images I_1 and I_2 are horizontally rectified (such that pixel-features occur at the same vertical position), through an affine warp to images I_1' and I_2' which occur in the xy-plane at z = 1. The synthetic image I_3 is produced from the horizontally rectified image I_3' which also occurs in the z = 1 plane.

Question for Kamangar: How can the homography matrix $\mathbf{H}_i = [\mathbf{R}_i | \mathbf{S}_i | \mathbf{O}_i - \mathbf{C}_i]$ be calculated if the vectors \mathbf{R}_i , \mathbf{S}_i , and \mathbf{O}_i are unknown. How can they be determined from available information?

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| June $24, 2016$ | Added additional | l material to t | hesis documer | t for $Epipa$ | olar constraint section. |
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| June $25, 2016$ | Added additional text to thesis document in Epipolar constraint and Funda- |
|-----------------|--|
| | mental matrix sections. |

Reading up on on homographies and rectification for [Scharstein1999] [6] and for derivation of Fundamental matrix for thesis document.

June 26, 2016 Started reading Chapter 2 of [Hartley2004] [3] for information regarding Homographices.

Worked on graphics regarding $Epipolar\ constraint$ for inclusion in thesis document.

June 27, 2016 Continued reading Chapter 2 of [Hartley2004] [3] containing information on Homographies for purpose(s) of deriving Fundamental matrix formula as well as understanding Horizontal rectification used for matching features along scanlines of images.

SUMMARY: Transformations of points in the image plane can be grouped into the following categories:

• Isometries (Denoted by \mathbf{H}_E): Transformations in \mathbb{P}_2 including translation and rotation (including composites of the two) that peserve Euclidean-distance. Transformations are of the form

$$\begin{bmatrix} \epsilon \cos(\theta) & -\sin(\theta) & t_x \\ \epsilon \sin(\theta) & \cos(\theta) & t_y \\ 0 & 0 & 1 \end{bmatrix}$$

where $\epsilon = \pm 1$. Angles are preserved if $\epsilon = 1$, else if $\epsilon = -1$ angles are reversed (reflection across an axis).

• Similarity (Denoted by \mathbf{H}_S): Transformations include translation, rotation, and scaling. Matrices are of the form

$$\begin{bmatrix} s\cos(\theta) & -s\sin(\theta) & t_x \\ s\sin(\theta) & s\cos(\theta) & t_y \\ 0 & 0 & 1 \end{bmatrix}$$

where s is the scaling factor. While distances are not preserved, the ratio of distances and angles are preserved.

• Affine (Denoted by \mathbf{H}_A): Transformations include all linear transformations of translation, rotation, scaling, and shearing. Matrices are of the form

$$\begin{bmatrix} a_{11} & a_{12} & t_x \\ a_{21} & a_{22} & t_y \\ 0 & 0 & 1 \end{bmatrix}$$

• **Projective** (Denoted by \mathbf{H}_P): Transformations in \mathbb{P}_2 that are linear transformations in \mathbb{R}_3 . Matrices are of the form

$$\begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & h_{33} \end{bmatrix}$$

- Chapter 2: Projective Geometry:
 - Section 2.1: Planar Geometry:
 - Section 2.2: The 2D projective plane:

Lines in \mathbb{R}^2 are detailed by $\mathbf{l} = [a,b,c]^\intercal$ and points as $\mathbf{x} = [x,y,1]^\intercal$ such that $\mathbf{l}^\intercal \cdot \mathbf{x} = a \cdot x + b \cdot y + 1 = 0$. Coordinates $\mathbf{x} = [x,y,0]^\intercal$ with a 0 instead of 1 in the last place represent a *point at infinity* since they are the only points where $a \cdot x + b \cdot y + c \cdot 0 = a \cdot x + b \cdot y + c' \cdot 0$ for the two *parallel* lines of $\mathbf{l} = [a,b,c]^\intercal$ and $\mathbf{l}' = [a,b,c']^\intercal$

Cross product of points \mathbf{x} and \mathbf{x}' result in line l joining the two points (i.e. $\mathbf{x} \times \mathbf{x}' = l$). Cross product of lines l and l' result in point \mathbf{x} where intersection of two lines (i.e. $l \times l' = \mathbf{x}$).

Circles and ovals can be reprsented by a conic-matrix of the form

$$\begin{split} 0 &= \mathbf{x}^\intercal \cdot \mathbf{C} \cdot \mathbf{x} \\ &= \left[\begin{array}{ccc} x & y & 1 \end{array} \right] \cdot \left[\begin{array}{ccc} a & b/2 & d/2 \\ b/2 & c & e/2 \\ d/2 & e/2 & f \end{array} \right] \cdot \left[\begin{array}{c} x \\ y \\ 1 \end{array} \right] \\ &= a \cdot x^2 + b \cdot xy + c \cdot y^2 + d \cdot x + e \cdot y + f \cdot 1 \end{split}$$

- Section 2.3: Projective transformations:

Point \mathbf{x} on an image is mapped to point \mathbf{x}' via a homography \mathbf{H} , such that $\mathbf{x}' = \mathbf{H} \cdot \mathbf{x}$. Because a point \mathbf{x} lies on line \mathbf{l} if $\mathbf{l}^{\intercal} \cdot \mathbf{x} = 0$, then because

$$0 = \mathbf{l}^{\mathsf{T}} \cdot \mathbf{x}$$
$$= \mathbf{l}^{\mathsf{T}} \cdot \mathbf{H}^{-1} \cdot \mathbf{H} \cdot \mathbf{x}$$
$$= \mathbf{l}^{\mathsf{T}} \cdot \mathbf{H}^{-1} \cdot \mathbf{x}'$$

the point \mathbf{x}' lies on the line \mathbf{l}' defined by $\mathbf{l}'^{\mathsf{T}} = \mathbf{l}^{\mathsf{T}} \cdot \mathbf{H}^{-1}$, or $\mathbf{l}' = \mathbf{H}^{-\mathsf{T}} \cdot \mathbf{l}$. Therefore a homography that gives a *point-mapping* of $\mathbf{x}' = \mathbf{H} \cdot x$ has a corresponding *line-mapping* of $\mathbf{l}' = \mathbf{H}^{-\mathsf{T}} \cdot \mathbf{l}$.

Similarly, for a homography given by $\mathbf{x}' = \mathbf{H} \cdot \mathbf{x}$, the conic under the homography is given by

$$0 = \mathbf{x}^{\mathsf{T}} \cdot \mathbf{C} \cdot \mathbf{x}$$

$$= (\mathbf{H}^{-1} \cdot \mathbf{x}')^{\mathsf{T}} \cdot \mathbf{C} \cdot (\mathbf{H}^{-1} \cdot \mathbf{x}')$$

$$= \mathbf{x}'^{\mathsf{T}} \cdot \mathbf{H}^{-\mathsf{T}} \cdot \mathbf{C} \cdot \mathbf{H}^{-1} \cdot \mathbf{x}'$$

$$= \mathbf{x}'^{\mathsf{T}} \cdot \mathbf{C}' \cdot \mathbf{x}'$$

where $\mathbf{C}' = \mathbf{H}^{-\intercal} \cdot \mathbf{C} \cdot \mathbf{H}^{-1}$.

- Section 2.4: A hierarchy of transformations:

See entry from June 27, 2016.

• Chapter 6: Camera Models:

– Section 6.1: Finite cameras:

Transformation from world-coordinate system \mathbf{x} to cameracoordinate system $^C\mathbf{x}$ is given by $^C\mathbf{x} = \mathbf{R} \cdot (\mathbf{x} - \mathbf{c})$. The Camera in world-space occurs at $\mathbf{x} = \mathbf{c}$. Camera-space has the camera located at $^C\mathbf{x} = 0$ and includes an image-plane at z = f. All rays intersect the image plane at z = f and converge on the origin $^C\mathbf{x} = 0$ which is known as the camera center. This results in points $^C\mathbf{x}$ in camera space being projected to points $\tilde{\mathbf{y}}$ in the image plane by means of the projection matrix \mathbf{P} such that

$$\mathbf{P} \cdot {}^{C}\tilde{\mathbf{x}} = \begin{bmatrix} f & 0 & 0 & 0 \\ 0 & f & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} {}^{C}x_1 \\ {}^{C}x_2 \\ {}^{C}x_3 \\ 1 \end{bmatrix} = \begin{bmatrix} f \cdot {}^{C}x_1 \\ f \cdot {}^{C}x_2 \\ {}^{C}x_3 \end{bmatrix}$$
$$= {}^{C}x_3 \cdot \begin{bmatrix} f \cdot {}^{C}x_1/{}^{C}x_3 \\ f \cdot {}^{C}x_2/{}^{C}x_3 \\ 1 \end{bmatrix} = {}^{C}x_3 \cdot \tilde{\mathbf{y}}$$

This results in points containing infinitley large values of x_3 being mapped to the same principal point of $\mathbf{y}=0$ in the image plane. This assumes the principal point is always located in the image plane at $\mathbf{y}=0$. Projecting point $\tilde{\mathbf{x}}$ to the image plane with arbitrary principal point $\mathbf{p}=[p_x,p_y]$ requires modifying the projection matrix to include camera-specific parameters. The camera calibration matrix \mathbf{K} is given as

$$\mathbf{P} \cdot {}^{C}\tilde{\mathbf{x}} = \begin{bmatrix} f & 0 & p_{x} & 0 \\ 0 & f & p_{y} & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} {}^{C}x_{1} \\ {}^{C}x_{2} \\ {}^{C}x_{3} \\ 1 \end{bmatrix} = \begin{bmatrix} f \cdot {}^{C}x_{1} + p_{x} \cdot {}^{C}x_{3} \\ f \cdot {}^{C}x_{2} + p_{y} \cdot {}^{C}x_{3} \end{bmatrix}$$
$$= {}^{C}x_{3} \cdot \begin{bmatrix} f \cdot {}^{C}x_{1}/{}^{C}x_{3} + p_{x} \\ f \cdot {}^{C}x_{2}/{}^{C}x_{3} + p_{y} \end{bmatrix} = {}^{C}x_{3} \cdot \tilde{\mathbf{y}}$$

June 30, 2016 Question for Kamangar: On pages 162 and 244, how is the ray back-projected from \mathbf{x} by \mathbf{P} (where $\mathbf{x} = \mathbf{P}\mathbf{X}$ and $\mathbf{P} = \mathbf{K}[\mathbf{R}|\mathbf{t}]$) given by the formula $\mathbf{X}(\lambda) = \mathbf{P}^+\mathbf{x} + \lambda\mathbf{C}$? How is the formula derived?

July 1, 2016 Added section called **Points and Lines in the Image Plane** in the **Background** section.

Continued adding text to **Background** section of Thesis Document, in *Epipolar Geometry* and *Intrinsic Calibration Matrix* sections.

July 11, 2016 Trying to consolidate knowledge (and explain in thesis document) behind the pinhole camera model. Specifically the concept of *focal-length* as it relates to *similarity of triangles*.

 $\label{eq:July 12} \text{July 12, 2016} \qquad \text{Started reading [Martin 2008] [7]}.$

July 5, 2016

July 13, 2016

Reading [Fusiello1999] [8]. Running throuh MatLab code at http://www.diegm.uniud.it/fusiello/demo/rect/ to understand algorithm. [Fusiello1999] [8] gives more insight into rectification discussed on June 22, 2016:

SUMMARY: Rectification of stereo images warps each image so that points are (vertically) aligned with their conjugate epipolar lines, and so that the collection of epipolar lines (in each image) are parallel. This aids in the use of Dynamic Programming for searching of corresponding points along each scan-line of the rectified image.

Normally, when the *camera centers* do not lie in *focal planes*¹, the *epipolar lines* intersect at the *epipole*. When the *camera center* of image A is located in the *focal plane* of image B, the *epipolar lines* in image B will be parallel. Similarly, when the *camera center* of image B is located in the *focal plane* of image A, the *epipolar lines* in image A will be parallel.

Rectification consists of transforming the cameras in each image such that the *camera centers* are co-planar

Question for Kamangar: My current understanding is this: Rectification of images is used to search along scanlines for point correspondances. In order to do Rectification, point correspondances are required. Doesn't this present a problem? It seems to be a chicken and the egg type problem.

July 15, 2016

Finished reading [Fusiello2000] [?]. Aside from details of algorithm and errors in experimental resuls, no more useful information gained since summarizing on July 13, 2016.

Since implementation is already done in MatLab, I'm porting methodology to Python using OpenCV and OpenGL in *final demonstration*.

Resumed reading of [Martin2008] [7].

July 17, 2016

Spent a couple of hours working on demonstration code in OpenGL and OpenCV.

July 18, 2016

Spending day working on thesis document. Sections worked on include:

- Intrinsic Calibration Matrix
- Fundamental Matrix

July 19, 2016

Continuing to add material to thesis document, including:

- Extrinsi Calibration Matrix
- Fundamental Matrix

Going back to reread first parts of Chapter 6 from [Hartley2004] [3], as I need clarification on some aspects of the *calibration matrix*. Namely, I *still* do not understand how $\mathbf{X}(\lambda) = \mathbf{P}^+\mathbf{x} + \lambda \mathbf{C}$ represents the equation of a ray passing through *optical center* \mathbf{C} in *world space*, with *projection matrix* \mathbf{P} .

July 20, 2016

Added material on fundamental matrix calculation from data to thesis document. Reading additional material from [Hartley2004] [3] on fundamenta matrix theoretical calculation.

¹May cause confusion depending on understanding of the terms focal plane and retinal plane. [Fusiello1999] [8] refers to focal plane as the plane containing the optical center and parallel to the image plane. The image plane is also referred to as the retinal plane. [Hartley2004] [?, Hartley2004] efers to focal plane as being synonymous with the image plane, but the retinal plane is the plane containing the optical center and parallel to the image plane. Here we are using the definition from [Fusiello1999] [8].

July 21, 2016 Continuing to read [Martin2008] [7]. See questions below.

Question for Kamangar: I don't understand the difference between *forward mapping* and *backward mapping*.

I'm a bit confused about most of the material being discussed in [Martin2008] [7]. Will read [Karathanasis1996] [9] for background on disparity estimation using dynamic programming.

UPDATE: My question on July 13, 2016 may have been worded wrong: The dynamic programming is used for estimating disparity, which in turn is used for point correspondance. The dynamic programming is not used DIRECTLY, in calcuating point correspondance.

Orignal question still holds though:

Question for Kamangar: I understand ALL of the following to be TRUE, which one needs to be FALSE (or my understanding revised):

- Point correspondence is needed to compute rectifying homographies.
- Rectifying homography is needed to compute disparities.
- Disparity is needed to compute point correspondence.

July 22, 2016 Started reading [Karathanasis1996] [9], no new information from first few sections.

July 25, 2016 Started woring on implmentation of disparity estimation using dynamic programming in MatLab. The generic method (summary below) seems to be a little different than method described in [Karathanasis1996] [9].

SUMMARY: A left image and right image each contain many *scanlines*, each at the same vertical position. Though each image's scanline is 1-dimensional, each point in the scanline is a square matrix of *normalized* pixel values. The point i in the left scanline is m, :

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