Research Log

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June 30, 2016

March 30, 2016	Established research log after 3 hours of learning new LaTeX

April 2, 2016	Added some additional comments to the **Process**

April 3, 2016 — Have been reading [Shum2007] [1].

Question for Kamangar: regarding [Shum2007] [1] about difference between:
- **Camera Plane** : Cooridinates u,v
- **Focal Plane** : Cooridinates s,t

April 11, 2016 — Reviewing blog articles located at:
- `https://erget.wordpress.com/2014/02/01/calibrating-a-stereo-camera-with-opencv/`
- `https://erget.wordpress.com/2014/02/28/calibrating-a-stereo-pair-with-python/`
- `https://erget.wordpress.com/2014/03/13/building-an-interactive-gui-with-opencv/`
- `https://erget.wordpress.com/2014/04/27/producing-3d-point-clouds-with-a-stereo-camera-in-opencv/`

for process to get webcam up and running. Previous issues related to fine-tuning *block matching* parameters. Need to review sources at list at bottom of `http://docs.opencv.org/2.4/modules/calib3d/doc/camera_calibration_and_3d_reconstruction.html` to understand.

April 19, 2016 — Made adjustments to python for image acquisition scripts (from blogs mentioned on April 11, 2016.)

NOTE: Consider creating rig with glue to keep stereo camera placement / direction constant.

April 19, 2016 — **UPDATE:** Error with `calibrate_cameras` python code causing linux machine to crash. If can't be resolved switch over to MacBook.

NOTE: Package should be setup by calling `$ python setup.py install`.

April 19, 2016 — **UPDATE:** Crash due to recursive shell call and was fixed. OpenCV not detecting all chessboard corners. Will try a new board.

April 20, 2016 — Did small amount of work on **Change of Reference** section in the paper. Added a section to the intro containing a map of commonly used symbols and notation.

April 29, 2016	Read following sections of [Chen1993] [2]: • Abstract • Introduction • Visibility Morphing **SUMMARY:** Explicit Geometry is ignored (i.e. surface mesh and 3d-points). Geometry is kept in 2-d. Whereas Image Morphing interpolates between *pixel intensity values in fixed locations* the method in this article interpolates between *pixel locations with (relatively) fixed intensity values*. **Question:** Sections read mention that pixel positions are stored in 3d (3-tuple) data structure. I'm not sure I understand this correctly, since 1. This would effectively make this structure a point cloud (but no mention of it in the paper). 2. There is no mention of special "depth-based" hardware or cameras (Far as I know this is upposed to be a regular image).

April 30, 2016	Checked understanding of *epipolar constraint* through reading of [Hartley2004] [3] and its derivation of $$'\mathbf{x}^T \cdot \mathbf{E} \cdot \mathbf{x} = '\mathbf{x}^T \cdot [\mathbf{t}]_\times \cdot \mathbf{R} \cdot \mathbf{x}$$ $$= '\mathbf{x}^T \cdot 'l$$ and creation of MatLab code verifying this. I may have been mistaken about relation of **Fundamental Matrix** and **Essential Matrix**. My current understanding is the *Fundamental Matrix* describes point/epipolar line correspondance for images under **scale invariant** conditions (i.e. point correspondance and Fundamental matrix does not change when one image (or both images) are scaled (uniformly or omni-directionally). *Essential Matrix* describes point/epipolar line correspondance for images under **normalized** conditions (i.e. unit-length is set equal to focal-length, and projection center is set at $(0, 0, 1)$.

May 2, 2016	Additional wording to Stereo-vision section. I am unsure of best order to present ideas related to *multi-view* geometry.

May 18, 2016	Reviewed [Chen1993] [2] Section 2. Consider reviewing follow relevant articles: • Disparity [Gosh89] • Optical Flow [Nage86] • Look-up tables [Wolb89] • 3d scenes [Pogg91] Working on MatLab code to pick correspondig points in stereo-images, and calculate pixel offset vectors.

May 19, 2016	Read Section 2.3 of [Chen1993] [2]. View interpolation is limited by: • **Penumbra**: pixels visible in one source image *but not both* • **Umbra**, pixels visible in neither source image, and *invisible* in destination image. • **Holes**, pixels visible in neither source image, but *visible* in destination image. Calculatred formula for *pre-displaced* quad-pixel calculation using a bi-linear interpolation as: $$\mathbf{P}(u,v) = \mathbf{P}(0,0)\cdot(1-u)\cdot(1-v) + \mathbf{P}(1,0)\cdot u\cdot(1-v) + \mathbf{P}(0,1)\cdot(1-u)\cdot v + \mathbf{P}(1,1)\cdot u\cdot v$$

May 20, 2016	Derived formula for *uv* calculation using *geometry matrix*, *blending matrix* and *basis vectors* of $\mathbf{u} = [u\ 1]^T$ and $\mathbf{v} = [v\ 1]^T$

$$x_{uv} = \begin{bmatrix} u & 1 \end{bmatrix} \begin{bmatrix} -1 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} x_{00} & x_{01} \\ x_{10} & x_{11} \end{bmatrix} \begin{bmatrix} -1 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} v \\ 1 \end{bmatrix}$$

$$y_{uv} = \begin{bmatrix} u & 1 \end{bmatrix} \begin{bmatrix} -1 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} y_{00} & y_{01} \\ y_{10} & y_{11} \end{bmatrix} \begin{bmatrix} -1 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} v \\ 1 \end{bmatrix}$$

Question for Kamangar: Is there a way given x and y to solve for u and v?

May 22, 2016	Added more to thesis document.

Worked on singular-value of previous blending equation. where:

$$\begin{bmatrix} x_{uv} & 0 \\ 0 & y_{uv} \end{bmatrix} = \begin{bmatrix} \mathbf{u} & \mathbf{0} \\ \mathbf{0} & \mathbf{u} \end{bmatrix}^T \begin{bmatrix} \mathbf{M} & \mathbf{0} \\ \mathbf{0} & \mathbf{M} \end{bmatrix}^T \begin{bmatrix} \mathbf{X} & \mathbf{0} \\ \mathbf{0} & \mathbf{Y} \end{bmatrix} \begin{bmatrix} \mathbf{M} & \mathbf{0} \\ \mathbf{0} & \mathbf{M} \end{bmatrix} \begin{bmatrix} \mathbf{v} & \mathbf{0} \\ \mathbf{0} & \mathbf{v} \end{bmatrix}$$

where

$$\mathbf{u} = \begin{bmatrix} u \\ 1 \end{bmatrix}, \mathbf{v} = \begin{bmatrix} v \\ 1 \end{bmatrix}, \mathbf{X} = \begin{bmatrix} x_{00} & x_{01} \\ x_{10} & x_{11} \end{bmatrix}, \mathbf{Y} = \begin{bmatrix} y_{00} & y_{01} \\ y_{10} & y_{11} \end{bmatrix}, \text{ and } \mathbf{M} = \begin{bmatrix} -1 & 1 \\ 1 & 0 \end{bmatrix}$$

May 23, 2016	Read [Chen1993] [2] section 2.4 on *Block Compression*.

SUMMARY: Blocks are established established by *threshold* where each block contains pixels that are *offset by no more than the threshold*, allowing all pixels to be offset at once.

Question for Kamangar: Doesn't this assume that all pixels in the block have a uniform offset?

Working on MatLab program to perform pixel offsets of corresponding points (i.e. assign corresponding points to pixels in MatLab by non automatic methods)

May 24, 2016	Read following sections from [Chen1993] [2]:

- Implementations (3)
  - Preprocessing (3.1)
  - Interactive Interpolation (3.2)
  - Examples (3.3)
- Applications (4)
  - Virtual Reality (4.1)
  - Motion Blur (4.2)

Question for Kamangar: With regards to Section 3.1 and Section 1, why is a graph structure needed? Why is it a lattice?

Question for Kamangar: With regards to Section 4.1, I don't understand the concepts of *temporal anti-aliasing* and *super-sampling*?

Made additional changes / added material to thesis document.

May 25, 2016	Was using figures from `http://www.robots.ox.ac.uk/~vgg/hzbook/hzbook2/HZfigures.html` as test images, which may not be best source as there white borders, appear to be up-sampled, and do not contain (extrinsic) calibration info. Consider using images located at `http://vision.middlebury.edu/stereo/data/scenes2014/` that contain meta-info including (intrinsic) calibration info.

May 29, 2016	Finished [Chen1993] [2]. Not sure if remaining article is of consequence.

Finished MatLab program for *animating / hand-drawing* (See wording in [Chen1993] [2]) offset vectors. Program performs offsets in 2-dimensional space. Conisder adding automatic *feature correspondance* and *z-buffer* information from depth map images avaiable on MiddleBury database. |
| May 30, 2016 | Point-correspondances do not follow even pattern as indicated in [Chen1993] [2]: *Bi-linear coordinates* and *quad partitionions*; May be better to use *Barycentric coordinates triangle partitions*.

Read on MatLab `tform`, `maketform`, and `Delaunay` triangles for purpose of image partitions. |
| June 1, 2016 | Read and finished [Park2003] [4].

SUMMARY: Multiple sections including *point correspondance* and *interpolation*. **Point correspondance**: Breaks images into rectangular partitions. Gets maximum horizontal and vertical pixel gradients using *Sobel operator* in each partition. The maximum gradient in each partition is thresholded to disregard homogeneous and textured regions. **Interpolation**: The images are partitioned with *Delaunay triangulation* using the point correspondances as triangle vertices.

Question for Kamangar: Article published seems to be vastly different depending on source (See `Park2003` folder). ScienceDirect version has more math and detail (maybe too much since it details what a *Sobel filter* is). Why would critical information, including algorithm steps and details, be ommited? |
| June 2, 2016 | Reviewing PDF at `https://staff.fnwi.uva.nl/l.dorst/hz/chap11_13.pdf` for information on *tri-focal tensor*. Don't understand *practical* calculation of *fundamental matrix* from *Singular Value Decomposition* and *Linear Least Squares* (i.e. don't understand LLS calculation from SVD). |
| June 3, 2016 | Working on implementing *triangle patch transform* in MatLap (using previously mentioned `delaunay`, `tform`, and `maketform` functions) needed for [Chen1993] [2] and [Park2003] [4]. |
| June 4, 2016 | Continuting work on getting triangular patches transformed in MatLab. Will use `affine2d` and `imwarp` instead of `maketform` and `imtransform`.

Spent several hours on a false start trying to implement line drawing on pixel data, in order to implment polygon seperation. Finally found MatLab's `roipoly` function which does what I need. |
| June 5, 2016 | Almost done with MatLab triangle interpolation program. Hoping to have something to show Kamangar in the next few days.

Was reading up on image-segmentation as a way to improve feature detection through masking. Came accross references to **spectral clustering** which I still don't understand after data mining class. Was reading tutorial at `http://classes.engr.oregonstate.edu/eecs/spring2012/cs534/notes/Spectral.pdf` for starters. |

June 8, 2016	Finalized most recent changes to MatLab program. It performs interpolation (between *source* and *destination* images of triangular patches defined by Delaunay triangularization of point correspondances from stereo images (See `Wood_Kamangar/StatusReports/StatusReport_00/Images`). Delaunay triangularization is performed on the source image only then extended to the corresponding points in the destination image so the arrangement of Delaunay triangles remains the same between images.

Summary of results is as follows:

• Triangles confined to one disparity region (See statue head in `image_source.png`, `image_destination.png`, and `truedisp.row3.col3.pgm`) show few artifacts and minimal blurring.

• Triangles crossing disparity regions or containing pixels occluded in the source or destination images (see camcorder tripod and lamp stand) have visibly more artifacts.

Started reading first page (*Abstract* and *Introduction* sections) of [Sharstein2002] [5]. |
| June 9, 2016 | Continuing to read [Scharstein2002] [5].

SUMMARY: Disparity can be defined by two ideas:

• *Human Vision* : Difference in location of features in the left and right eye.

• *Computer Vision* : Inverse depth. Can be treated as a 3-dimensional projective transformation (collineation or homographyv)of 3-d space (X,Y,Z).

Define flowing terms:

• **Disparity Map**: $d(x, y)$

• **Disparity Space**: (x, y, d)

• **Correspondance**: Pixel (x, y) in reference image r and corresponding pixel (x', y') in matching image m given by $x' = x + sd(x, y)$ and $y' = y$ (assuming horizontal displacement *only*), where $s = \pm 1$ is chose do d is always positive.

• **Disparity Space Image**: Any function or image defined over continous or dispartiy space. |
| June 11, 2016 | Continuing to read [Scharstein2002] [5]:

SUMMARY: Algorithms can be ordered in 4 common subsets:

1. Matching cost computation;

2. Cost (support) aggregation;

3. Disparity computation / optimization;

4. Disparity refinement;

Two main types of agorithms:

• **Local**: Including *Squared Intensity Differences* and *Absolute intensity differences*.

• **Global** Includeing *Energy minimizatio*.

Continuing to read up on *Spectral Clustering* and *Laplacian embedding* for uses in image segmentation. |

June 14, 2016	Working on implementing [Park2003] [4] in MatLab.
	Also working on implementing Spectral Clustering (for images) in MatLab. Started working on `fnDistance.m` to calculate pixel distances (*Distance Matrix*) for vectorized (row major and column major) images, needed for segmentation through spectral clustering.
June 16, 2016	Added some additional text regarding the *epipolar constraint* to the thesis document.
June 17, 2016	Finished implmenting and testing `fnDistance.m` for distance matrix. Next finished working on and testing `fnSimilarity.m` implementing a *Similarity Matrix* for spectral clustering.
June 18, 2016	Wrote small amount additional text on *epipolar contstraint*, and verified understanding through MatLab functions.
June 20, 2016	Holding off on reading any more of [Scharstein2002] [5](*Have completed up to end of page 5*): May be too advanced for me and of little use; Compares methods, but does not go into enough detail about how to implement them. Instead reading [Scharstein1999] [6] which may be more my level.
	Started reading in *Correspondance problem* section of [Scharstein1999] [6]. **SUMMARY:** Matching can be done via *Fearure based correspondacne* and *Area based correspondance*.
	Feature based correpondance finds locally unique or identifiable pixels (i.e. Corners or edge gradients), matchingbetween images occurs between these reduced set of points. Advantages are only a few points are necessary. Disadvantages are that disparity calculations are confined to these points, so interpoint disparity have to be calculated through interpolation and may not be accurate.
	Area based correspondance occurrs over *regions in the image* instead of points used in feature correspondance. Advantages are a denser (and therefore more accurate) disparity map, but require assumptions about local disparity.

June 21, 2016	Continued reading [Scharstein1999] [6].

SUMMARY: 3 general methods are being differentiated:

- **Image Synthesis based on Stereo**: Uses stereo mathods for image creation.
- **Image Interpolation**: Similar to *Image Synthesis based on Stereo*, except mages generated must be on baseline, and baseline must be parallel to image planes.
- **Information from Many Images**: Includes image stitching and panoramic mosaicing.

Other sections involve summaries of various papers and methods published under each of the 3 categories.

Got further clarification on steps for coorespondance matching for *feature-based correspondance.*

1. **Preprocessing**: Color correction between stereo images for conconsistancy, and image warping through rectification so features occur at (approximatley) same horizontal distance reducing search area to the scanline.
2. **Cost Calculation**: Per-pixel cost calculation done as either a *square difference* or *absolute difference.*
3. **Aggregation**: The summing of the cost calculations over the window in question.
4. **Comparison / Calculation**: Window on feature trying to be matched is kept fixed.Window in corresponding image is moved along the scanline for a comparison of potential window aggregates. Correspondance with minimum aggregate (in difference of costs) is selected as the corresponding point in the image being scanned.
5. **Sup-pixel Calculation**: Not yet read. Could be smoothing.

Read up to section 2.2.5 *Disparity Selection* (PDF page 49, Numbered page 35). Stopped to read up on using Dynamic Programming to increase consistancy of stereo points and disparity, including following sourcess:

- `http://www.robots.ox.ac.uk/~az/lectures/opt/lect2.pdf`
- `http://www.cs.umd.edu/~djacobs/CMSC426/PS7.pdf`

June 22, 2016	Continued reading [Sharstein1999] [6]. I'm still unclear about the process (and use of) *Sub-Pixel Disparity Computation* mentioned in section 2.2.6.

I moved onto Chapter 3 (View Synthesis) and have been reading on *three-view rectification.* Read all of Section 3.1 (*Geometry*) (up to but not including PDF page 60, Numbered page 47).

SUMMARY: A new image I_3 is synthesisized from images I_1 and I_2, by estabishing reference frame containing camera centers $\mathbf{C_3}$, $\mathbf{C_1}$, and $\mathbf{C_2}$ respectively. The unit-length is established as the difference between camera centers $\mathbf{C_1}$ and $\mathbf{C_2}$. The positions are set along the x-axis such that $\mathbf{C_1} = [0,0,0]^\top$ and $\mathbf{C_2} = [1,0,0]^\top$. The xy-plane is oriented such that it contains $\mathbf{C_3} = [a,b,0]^\top$ (for some constants a and b).Images I_1 and I_2 are *horizontally rectified* (such that pixel-features occur at the same vertical position), through an *affine warp* to images I_1' and I_2' which occur in the xy-plane at $z = 1$. The synthetic image I_3 is produced from the horizontally rectified image I_3' which also occurs in the $z = 1$ plane.

Question for Kamangar: How can the homography matrix $\mathbf{H}_i = [\mathbf{R}_i|\mathbf{S}_i|\mathbf{O}_i - \mathbf{C}_i]$ be calculated if the vectors $\mathbf{R}_i$, $\mathbf{S}_i$, and $\mathbf{O}_i$ are unknown. How can they be determined from available information?

June 24, 2016	Added additional material to thesis document for *Epipolar constraint* section.

June 25, 2016	Added additional text to thesis document in *Epipolar constraint* and *Fundamental matrix* sections.

Reading up on on *homographies* and *rectification* for [Scharstein1999] [6] and for derivation of *Fundamental matrix* for thesis document.

June 26, 2016	Started reading Chapter 2 of [Hartley2004] [3] for information regarding *Homographices*.

Worked on graphics regarding *Epipolar constraint* for inclusion in thesis document.

June 27, 2016	Continued reading Chapter 2 of [Hartley2004] [3] containing information on *Homographies* for purpose(s) of deriving *Fundamental matrix* formula as well as understanding *Horizontal rectification* used for matching features along scanlines of images.

SUMMARY: Transformations of points in the image plane can be grouped into the following categories:

- **Isometries** (Denoted by $\mathbf{H}_E$): Transfomrations in $\mathbb{P}_2$ including *translation* and *rotation* (including composites of the two) that peserve *Euclidean*-distance. Tranformations are of the form

$$\begin{bmatrix} \epsilon\cos(\theta) & -\sin(\theta) & t_x \\ \epsilon\sin(\theta) & \cos(\theta) & t_y \\ 0 & 0 & 1 \end{bmatrix}$$

  where $\epsilon = \pm 1$. Angles are preserved if $\epsilon = 1$, else if $\epsilon = -1$ angles are reversed (reflection accross an axis).

- **Similarity** (Denoted by $\mathbf{H}_S$): Transformations include *translation*, *rotation*, and *scaling*. Matrices are of the form

$$\begin{bmatrix} s\cos(\theta) & -s\sin(\theta) & t_x \\ s\sin(\theta) & s\cos(\theta) & t_y \\ 0 & 0 & 1 \end{bmatrix}$$

  where s is the scaling factor. While *distances* are not preserved, the *ratio of distances* and *angles* are preserved.

- **Affine** (Denoted by $\mathbf{H}_A$): Transformations include all linear transformations of *translation*, *rotation*, *scaling*, and *shearing*. Matrices are of the form

$$\begin{bmatrix} a_{11} & a_{12} & t_x \\ a_{21} & a_{22} & t_y \\ 0 & 0 & 1 \end{bmatrix}$$

- **Projective** (Denoted by $\mathbf{H}_P$): Transformations in $\mathbb{P}_2$ that are linear transformations in $\mathbb{R}_3$. Matrices are of the form

$$\begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & h_{33} \end{bmatrix}$$

Continuing to read [Hartley2004] [3] for *affine rectification*. Chapters of [Hartley2004] [3] include:

- **Chapter 2: Projective Geometry**:
  - **Section 2.1: Planar Geometry**:
  - **Section 2.2: The 2D projective plane**:

    Lines in $\mathbb{R}^2$ are detailed by $\mathbf{l} = [a, b, c]^\mathsf{T}$ and points as $\mathbf{x} = [x, y, 1]^\mathsf{T}$ such that $\mathbf{l}^\mathsf{T} \cdot \mathbf{x} = a \cdot x + b \cdot y + 1 = 0$. Coordinates $\mathbf{x} = [x, y, 0]^\mathsf{T}$ with a 0 instead of 1 in the last place represent a *point at infinity* since they are the only points where $a \cdot x + b \cdot y + c \cdot 0 = a \cdot x + b \cdot y + c' \cdot 0$ for the two *parallel* lines of $\mathbf{l} = [a, b, c]^\mathsf{T}$ and $\mathbf{l}' = [a, b, c']^\mathsf{T}$

    Cross product of points $\mathbf{x}$ and $\mathbf{x}'$ result in line $\mathbf{l}$ joining the two points (i.e. $\mathbf{x} \times \mathbf{x}' = \mathbf{l}$). Cross product of lines $\mathbf{l}$ and $\mathbf{l}'$ result in point $\mathbf{x}$ where intersection of two lines (i.e. $\mathbf{l} \times \mathbf{l}' = \mathbf{x}$).

    Circles and ovals can be reprsented by a *conic-matrix* of the form

    $$0 = \mathbf{x}^\mathsf{T} \cdot \mathbf{C} \cdot \mathbf{x}$$
    $$= \begin{bmatrix} x & y & 1 \end{bmatrix} \cdot \begin{bmatrix} a & b/2 & d/2 \\ b/2 & c & e/2 \\ d/2 & e/2 & f \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$
    $$= a \cdot x^2 + b \cdot xy + c \cdot y^2 + d \cdot x + e \cdot y + f \cdot 1$$

  - **Section 2.3: Projective transformations**:

    Point $\mathbf{x}$ on an image is mapped to point $\mathbf{x}'$ via a homography $\mathbf{H}$, such that $\mathbf{x}' = \mathbf{H} \cdot \mathbf{x}$. Because a point $\mathbf{x}$ lies on line $\mathbf{l}$ if $\mathbf{l}^\mathsf{T} \cdot \mathbf{x} = 0$, then because

    $$0 = \mathbf{l}^\mathsf{T} \cdot \mathbf{x}$$
    $$= \mathbf{l}^\mathsf{T} \cdot \mathbf{H}^{-1} \cdot \mathbf{H} \cdot \mathbf{x}$$
    $$= \mathbf{l}^\mathsf{T} \cdot \mathbf{H}^{-1} \cdot \mathbf{x}'$$

    the point $\mathbf{x}'$ lies on the line $\mathbf{l}'$ defined by $\mathbf{l}'^\mathsf{T} = \mathbf{l}^\mathsf{T} \cdot \mathbf{H}^{-1}$, or $\mathbf{l}' = \mathbf{H}^{-\mathsf{T}} \cdot \mathbf{l}$. Therefore a homograhy that gives a *point-mapping* of $\mathbf{x}' = \mathbf{H} \cdot x$ has a corresponding *line-mapping* of $\mathbf{l}' = \mathbf{H}^{-\mathsf{T}} \cdot \mathbf{l}$.

    Similarly, for a homography given by $\mathbf{x}' = \mathbf{H} \cdot \mathbf{x}$, the conic under the homography is given by

    $$0 = \mathbf{x}^\mathsf{T} \cdot \mathbf{C} \cdot \mathbf{x}$$
    $$= (\mathbf{H}^{-1} \cdot \mathbf{x}')^\mathsf{T} \cdot \mathbf{C} \cdot (\mathbf{H}^{-1} \cdot \mathbf{x}')$$
    $$= \mathbf{x}'^\mathsf{T} \cdot \mathbf{H}^{-\mathsf{T}} \cdot \mathbf{C} \cdot \mathbf{H}^{-1} \cdot \mathbf{x}'$$
    $$= \mathbf{x}'^\mathsf{T} \cdot \mathbf{C}' \cdot \mathbf{x}'$$

    where $\mathbf{C}' = \mathbf{H}^{-\mathsf{T}} \cdot \mathbf{C} \cdot \mathbf{H}^{-1}$.

  - **Section 2.4: A hierarchy of transformations**:

    See entry from June 27, 2016.

June 29, 2016   *...Continued*

- **Chapter 6: Camera Models**:
  - **Section 6.1: Finite cameras**:

    Transformation from *world-coordinate* system $\mathbf{x}$ to *camera-coordinate* system $^C\mathbf{x}$ is given by $^C\mathbf{x} = \mathbf{R} \cdot (\mathbf{x} - \mathbf{c})$. Camera in world-space occurs is at $\mathbf{x} = \mathbf{c}$. Camera coordinate system has the camera position at $^c\mathbf{x} = 0$ and includes *image-plane* at $z = 1$ or $z = f$

  - **Section 6.2: The projective camera**:
- **Chapter 9: Epipolar Geometry and the Fundamental Matrix**:
  - **Section 9.1: Epipolar geometry**:
  - **Section 9.2: The fundamental matrix F**:
- **Chapter 11: Computation of the Fundamental Matrix**:
  - **Section 11.1: Basic Equations**:

June 30, 2016   **Question for Kamangar:** On pages 162 and 244, how is the ray back-projected from $\mathbf{x}$ by $\mathbf{P}$ (where $\mathbf{x} = \mathbf{PX}$ and $\mathbf{P} = \mathbf{K}[\mathbf{R}|\mathbf{t}]$) given by the formula $\mathbf{X}(\lambda) = \mathbf{P}^+\mathbf{x} + \lambda\mathbf{C}$? How is the formula derived?

References

[1] Sing Bing Kang Heung-Yeung Shum, Shing-Chow Chan. *Image Based Rendering.* Springer Publishing, 1 edition, 2007. Available online at: `http://link.springer.com/content/pdf/10.1007%2F978-0-387-32668-9.pdf` Pages cited are **Book Page** Numbers. Formula for **PDF Page** Number is (**PDF Page Number = Book Page Number + 17**).

[2] Shenchang Eric Chen and Lance Williams. View interpolation for image synthesis. In *Proceedings of the 20th Annual Conference on Computer Graphics and Interactive Techniques*, SIGGRAPH '93, pages 279–288, New York, NY, USA, 1993. ACM.

[3] R. I. Hartley and A. Zisserman. *Multiple View Geometry in Computer Vision.* Cambridge University Press, ISBN: 0521540518, second edition, 2004.

[4] Joon Hong Park and HyunWook Park. Fast view interpolation of stereo images using image gradient and disparity triangulation. In *Image Processing, 2003. ICIP 2003. Proceedings. 2003 International Conference on*, volume 1, pages I–381–4 vol.1, Sept 2003.

[5] Daniel Scharstein and Richard Szeliski. A taxonomy and evaluation of dense two-frame stereo correspondence algorithms. *Int. J. Comput. Vision*, 47(1-3):7–42, April 2002.

[6] Daniel Scharstein. *View Synthesis Using Stereo Vision.* Springer-Verlag, Berlin, Heidelberg, 1999.